CS-4053 Recommender System

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Lecture 3: Content-based Recommender System

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Content-based Recommendations: Preamble

- The basic idea of a content-based recommender system is to match user with items that are similar to what they rated highly in the past
- The similarity is not on the basis of rating correlations across users
- The attributes of the items are used to find similarity

Content-based Recommendations: Preamble

- These type of recommendation systems can work well in cases where personalized recommendations are needed
 - Movie recommendations e.g. a user liking a movie of a certain director more
 - Websites or blogs *e.g.* recommending similar news or article to the user to the one he is querying or interested in

Content-based Recommendations: Preamble

- What exactly do we mean by content?
- □ Content are explicit attributes or characteristics of the item e.g. for a movie:
 - ☐ Genre: Action / Superhero
 - Actor: Robert Downey Jr.
 - **☐ Year**: 2019
- □ It can also be textual content (title, description, table of content, etc.)
 - Several techniques to compute the distance between two textual documents
 - Can use NLP techniques to extract content features
- Can be extracted from the signal itself (audio, image)

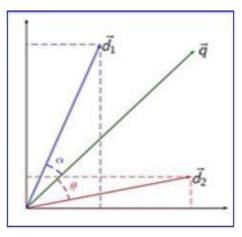
Content-based Recommender System

- Formally, a **content-based recommender systems** try to match users to items that are *similar* to what they have liked in the past
- This *similarity* is not necessarily based on rating correlations across users but on the basis of the attributes of the objects liked by the user

Vector Space Model

- In a vector space model, each item is saved as a vector of its attributes (features) in n-dimensional space
- The angle between two vectors give similarity between the contents of these items
- Each user is saved as a user profile vector and the similarity is calculated the same way

Vector Space Model



User profile and Item feature vectors in 2-D vector space

Content-based Filtering: Approach

- Content-based systems are common for recommending text-based products e.g. news articles, wiki pages
- A lazy approach is to recommend an item containing content that is most similar to that present in user's highly rated items
 - Also called lazy approach
- ☐ More novel approaches involve training a classifier (decision trees, neural networks etc.) to predict a rating given a set of features as input

Content-based Filtering: Approach

☐ Input

- ☐ A vector containing attributes for each unrated (unseen) item
- ☐ A user profile vector expressing their taste using already rated items

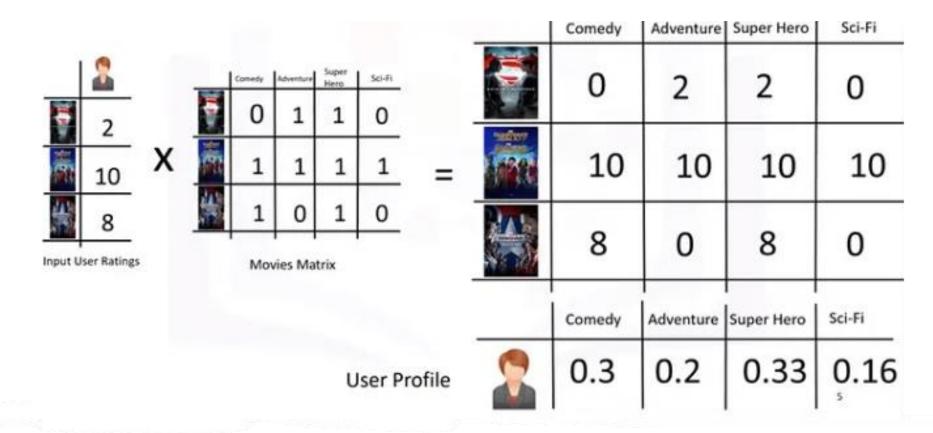
☐ Output

- A weighted matrix depicting user's measure of *liking* of each attribute for all items
- ☐ A recommendation vector containing predicted ratings for unseen items

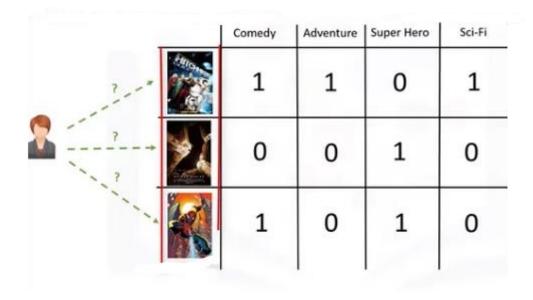
We have an input of user ratings for a set of movies and their attributes



☐ We first create a user profile based on already rated items (and attributes)



Which one of the yet unrated movies should we be recommending?



☐ We can recommend the movie that gives us the maximum weighted average



☐ Maximum weighted average can also be expressed as raw predicted rating



Content-based Filtering: Exercise

Task: Find Cosine similarity between user profile and movie matrix and compare with previous results.

- Let us assume that a user clicks and reads a blog on a website
- ☐ The objective is to recommend **two** similar blogs to the user
- We can calculate the **TF** (term frequency) and **IDF** (inverse document frequency) of the blogs in order to find their relative importance based on how similar they are to the current blog

- Term Frequency (**TF)** is simply the number of times a term (feature) appears in the document (item)
- We generally use transformed **TF** in order to de-emphasize the effect of frequency on relevance of the term. Hence:

$$TF_{tk,dj} = \frac{freq(tk)}{max(ti,dj)}$$

☐ Inverse Document Frequency (IDF) helps us find the overall relevance of a term

$$IDF_{tk} = log_{10} \frac{N}{n_k}$$

Let us assume that **Blog 1** is being read by the user and contains the given three terms with their frequencies

| Blog | Business | Invention | Hospital |
|--------|----------|-----------|----------|
| Blog 1 | 31 | 27 | 0 |

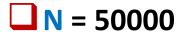
☐ The given table contains retrieved blog along with information for all other blogs (from which two are to be recommended)

| Blog | Business | Invention | Hospital | |
|--------|----------|-----------|----------|--|
| Blog 1 | 31 | 27 | 0 | |
| Blog 2 | 29 | 61 | 3 | |
| Blog 3 | 52 | 99 | 6 | |
| Blog 4 | 10 | 29 | 5 | |
| Blog 5 | 13 | 41 | 7 | |

Assume that the corpus contains 50000 documents (blogs) on the website and 2500 of them contain the term Business, 1200 contain Invention and 800 contain Hospital

The given table contains retrieved blog along with information for all other blogs (from which two are to be recommended)

| Blog | Business | Invention | Hospital |
|------------|----------|-----------|----------|
| Blog 1 | 31 | 27 | 0 |
| Blog 2 | 29 | 61 | 3 |
| Blog 3 | 52 | 99 | 6 |
| Blog 4 | 10 | 29 | 5 |
| Blog 5 | 13 | 41 | 7 |
| Doc. Freq. | 2500 | 1200 | 800 |



 \square We first calculate TF for each attribute of every blog e.g.

$$TF_{Business, Blog2} = \frac{freq(Business, Blog2)}{max(freq(any other term, Blog2))} = \frac{29}{61} = 0.47$$

| Blog | Business | Invention | Hospital | |
|------------|----------|-----------|----------|--|
| Blog 1 | 31 | 27 | 0 | |
| Blog 2 | 0.47 | 61 | 3 | |
| Blog 3 | 52 | 99 | 6 | |
| Blog 4 | 10 | 29 | 5 | |
| Blog 5 | 13 | 41 | 7 | |
| Doc. Freq. | 2500 | 1200 | 800 | |

☐ We calculate TF for all other attributes in the same manner

$$TF_{Business,Blog2} = \frac{freq(Business,Blog2)}{\max(freq_i,Blog2)} = \frac{29}{61} = 0.47$$

| Blog | Business Invention | | Hospital |
|------------|--------------------|------|----------|
| Blog 1 | 1.14 0.87 | | 0 |
| Blog 2 | 0.47 | 2.10 | 0.04 |
| Blog 3 | 0.52 | 1.90 | 0.06 |
| Blog 4 | 0.34 | 2.9 | 0.17 |
| Blog 5 | 0.31 | 3.15 | 0.17 |
| Doc. Freq. | 2500 | 1200 | 800 |

☐ We also need to calculate **IDF** for each attribute e.g.

$$IDF_{Business} = log_{10} \left(\frac{50000}{2500} \right) = 1.30$$

| Blog | Business | Invention | Hospital | |
|------------|-----------|-----------|----------|--|
| Blog 1 | 1.14 0.87 | | 0 | |
| Blog 2 | 0.47 | 2.10 | 0.04 | |
| Blog 3 | 0.52 | 1.90 | 0.06 | |
| Blog 4 | 0.34 | 2.9 | 0.17 | |
| Blog 5 | 0.31 | 3.15 | 0.17 | |
| Doc. Freq. | 2500 | 1200 | 800 | |
| IDF | 1.30 | 1.61 | 1.79 | |

Let us calculate the TF-IDF weights for each term in every blog e.g. $TF-IDF_{tk,dj} = TF-IDF_{Business,Blog2} = 0.47 * 1.30 = \textbf{0.61}$

| Blog | Business Invention | | Hospital |
|------------|--------------------|------|----------|
| Blog 1 | 1.14 | 0.87 | 0 |
| Blog 2 | 0.61 | 2.10 | 0.04 |
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Let us calculate the TF-IDF weights for each term in every blog e.g. $TF-IDF_{tk,dj} = TF-IDF_{Business,Blog2} = 0.47 * 1.30 = \textbf{0.61}$

| Blog | Business Invention | | Hospital |
|------------|--------------------|---------------|----------|
| Blog 1 | 1.48 | 1.40 | 0 |
| Blog 2 | 0.61 | 3.38 | 0.07 |
| Blog 3 | 0.67 | 3.05 | 0.10 |
| Blog 4 | 0.44 | 4.66 | 0.30 |
| Blog 5 | 0.40 | 0.40 5.07 0.3 | |
| Doc. Freq. | 2500 | 1200 | 800 |
| IDF | 1.30 | 1.61 | 1.79 |

Let us first find the length of each vector and then use it calculate the normalized TF-IDF weights e.g.

$$Length_{Blog1} = \sqrt{1.48^2 + 1.40^2 + 0^2} = 2.03$$

| Blog | Business | Invention | Hospital | Magnitude |
|------------|----------|-----------|----------|-----------|
| Blog 1 | 1.48 | 1.40 | 0 | 2.03 |
| Blog 2 | 0.61 | 3.38 | 0.07 | 3.43 |
| Blog 3 | 0.67 | 3.05 | 0.10 | 3.12 |
| Blog 4 | 0.44 | 4.66 | 0.30 | 4.69 |
| Blog 5 | 0.40 | 5.07 | 0.30 | 5.09 |
| Doc. Freq. | 2500 | 1200 | 800 | |
| IDF | 1.30 | 1.61 | 1.79 | |

Let us first find the length of each vector and then use it calculate the normalized TF-IDF weights e.g.

$$w_{Business_{,}Blog1} = \frac{TF-IDF_{Business_{,}Blog1}}{Length_{Blog1}} = 0.73$$

| Blog | Business | Invention | Hospital | Magnitude |
|------------|----------|-----------|----------|-----------|
| Blog 1 | 0.73 | 0.68 | 0 | 2.03 |
| Blog 2 | 0.17 | 0.98 | 0.02 | 3.43 |
| Blog 3 | 0.21 | 0.97 | 0.03 | 3.12 |
| Blog 4 | 0.09 | 0.99 | 0.06 | 4.69 |
| Blog 5 | 0.07 | 0.99 | 0.05 | 5.09 |
| Doc. Freq. | 2500 | 1200 | 800 | |
| IDF | 1.30 | 1.61 | 1.79 | |

Calculate the Cosine Similarity between the weighted user profile (Blog1) and each weighted item profile (all other blogs) to recommend blogs

| Blog | Business | Invention | Hospital | Magnitude |
|------------|----------|-----------|----------|-----------|
| Blog 1 | 0.73 | 0.68 | 0 | 2.03 |
| Blog 2 | 0.17 | 0.98 | 0.02 | 3.43 |
| Blog 3 | 0.21 | 0.97 | 0.03 | 3.12 |
| Blog 4 | 0.09 | 0.99 | 0.06 | 4.69 |
| Blog 5 | 0.07 | 0.99 | 0.05 | 5.09 |
| Doc. Freq. | 2500 | 1200 | 800 | |
| IDF | 1.30 | 1.61 | 1.79 | |

Calculate the Cosine Similarity between the weighted user profile (Blog1) and each weighted item profile (all other blogs) to recommend blogs

$$Cosine_{(Blog1,Blog2)} = \frac{(0.73*0.17) + (0.68*0.98) + (0*0.02)}{\sqrt{0.73^2 + 0.68^2 + 0^2} \cdot \sqrt{0.17^2 + 0.98^2 + 0.02^2}} = 0.79$$

| Blog | Business | Invention | Hospital | Magnitude | Cosine Similarity |
|------------|----------|-----------|----------|-----------|-------------------|
| Blog 1 | 0.73 | 0.68 | 0 | 2.03 | |
| Blog 2 | 0.17 | 0.98 | 0.02 | 3.43 | 0.79 |
| Blog 3 | 0.21 | 0.97 | 0.03 | 3.12 | |
| Blog 4 | 0.09 | 0.99 | 0.06 | 4.69 | |
| Blog 5 | 0.07 | 0.99 | 0.05 | 5.09 | |
| Doc. Freq. | 2500 | 1200 | 800 | | |
| IDF | 1.30 | 1.61 | 1.79 | | |

Calculate the Cosine Similarity between the weighted user profile (Blog1) and each weighted item profile (all other blogs) to recommend blogs

| Blog | Business | Invention | Hospital | Magnitude | Cosine Similarity |
|------------|----------|-----------|----------|-----------|-------------------|
| Blog 1 | 0.73 | 0.68 | 0 | 2.03 | |
| Blog 2 | 0.17 | 0.98 | 0.02 | 3.43 | 0.79 |
| Blog 3 | 0.21 | 0.97 | 0.03 | 3.12 | 0.82 |
| Blog 4 | 0.09 | 0.99 | 0.06 | 4.69 | 0.74 |
| Blog 5 | 0.07 | 0.99 | 0.05 | 5.09 | 0.73 |
| Doc. Freq. | 2500 | 1200 | 800 | | |
| IDF | 1.30 | 1.61 | 1.79 | | |

Based on Cosine Similarities, Blog 2 and Blog 3 will be recommended to the user for reading

| Blog | Business | Invention | Hospital | Magnitude | Cosine Similarity |
|------------|----------|-----------|----------|-----------|-------------------|
| Blog 1 | 0.73 | 0.68 | 0 | 2.03 | |
| Blog 2 | 0.17 | 0.98 | 0.02 | 3.43 | 0.79 |
| Blog 3 | 0.21 | 0.97 | 0.03 | 3.12 | 0.82 |
| Blog 4 | 0.09 | 0.99 | 0.06 | 4.69 | 0.74 |
| Blog 5 | 0.07 | 0.99 | 0.05 | 5.09 | 0.73 |
| Doc. Freq. | 2500 | 1200 | 800 | | |
| IDF | 1.30 | 1.61 | 1.79 | | |

Content-based Filtering: Pros and Cons

Pros

- Scalable in terms of new users
- Highly personalized recommendations
- Partially solves cold start problem i.e. solves for new item
- Recommendations are explainable

Cons

- Not easy to hand-engineer meaningful attributes
- Has little to no serendipity
- Suffers from cold start user problem