

Todo list

These might need to be replaced with variants for Reals/Integers	3
Do we want to have the length of our vectors as a type argument?	3
define criteria for what a well-formed expression language should provide	3
Quantities discussion – remaining untyped	3
modulo, remainder, etc.	4
discuss vectors in general	5
oddity: topology appears as a constructor arg and signature arg but can desync – can we just remove the constructor arg?	5
addressed in “misc” section	5

0.1 Syntax

0.1.1 Current

An idealized version of the current syntax.

Type	τ	::=	Integer	\mathbb{Z}	Integer numbers
			Real	\mathbb{R}	Real numbers
			String	<i>String</i>	Text
			Bool	\mathbb{B}	Truth values (true/false)*
			Vector(τ, n)	$[\tau]_n$	Vectors (single element type, fixed length)*
			Tuple($\tau_1 \dots \tau_n$)	$\tau_1 \times \tau_2 \times \dots \times \tau_n$	Alternative vectors/tuples (fixed len+diff typed e
Literal	l	::=	Integer[n]	n	Integer number
			Real[r]	r	Real number
			String[s]	<i>“s”</i>	Text
			Bool[b]	b	Boolean value
			Vector($l_1 \dots l_n$)	$\langle l_1, \dots, l_n \rangle$	Vectors*
			Tuple($l_1 \dots l_n$)	(l_1, \dots, l_n)	Tuples*
UnaryOp	\ominus	::=	Not	\neg	Logical negation
			Neg	$-$	Numeric negation
			...		omitted for brevity
BinaryOp	\oplus	::=	Sub	$-$	Subtraction
			Pow	$-$	Powers
			...		omitted for brevity
AssocBinOp	\otimes	::=	Add	$+$	Addition
			Mul	\times	Multiplication
			...		omitted for brevity
UID	u	::=	UID(s)	UID ‘‘s’’	UIDs
Expr	e	::=	Literal(l)	l	Literal values
			Vector($e_1 \dots e_n$)	$\langle e_1, \dots, e_n \rangle$	Vectors
			Var(u)	u	Variable (QuantityDict Chunk)
			FuncCall($f, e_1 \dots e_n$)	$f(e_1 \dots e_n)$	“Complete” function application
			UnaryOp(\ominus, e)	$\ominus e$	Unary operations
			BinaryOp(\oplus, e_1, e_2)	$e_1 \oplus e_2$	Binary operations
			AssocOp($\otimes, e_1 \dots e_n$)	$e_1 \otimes \dots \otimes e_n$	Associative binary operations
			Case($e_{1c} e_{1e} \dots e_{nc} e_{ne}$)	<i>if</i> e_{1c} <i>then</i> e_{2e} <i>elif</i> e_{2c} ...	If-then-else-if-then-else (Switch-like)
			BigAsBinOp(\otimes, e_1, e_2)	$\bigotimes_{i=e_1}^{e_2} i$	Apply a “big” op to a discrete range
			IsInRlItrvl(u, e_1, e_2)	$u \in [e_1, e_2]$	Variable in range

*: does not currently appear in the code at the moment, but would be needed/desired

0.2 Typing Rules

0.2.1 Literal

1. Integers:

$$\frac{i : \text{Integer}}{\text{Integer}[i] : \text{Literal Integer}} \quad (1)$$

2. Strings (Text):

$$\frac{s : \text{String}}{\text{Str}[s] : \text{Literal String}} \quad (2)$$

3. Real numbers:

$$\frac{d : \text{Double}}{\text{Dbl}[d] : \text{Literal Real}} \quad (3)$$

4. Whole numbered reals ($\mathbb{Z} \subset \mathbb{R}$):

$$\frac{d : \text{Integer}}{\text{ExactDbl}[d] : \text{Literal Real}} \quad (4)$$

5. Percentages:

$$\frac{n : \text{Integer} \quad d : \text{Integer}}{\text{Perc}[n, d] : \text{Literal Real}} \quad (5)$$

0.2.2 Miscellaneous

Sorts Legend **Numerics(T)** : any numeric type
NumericsWithNegation(T) : any signed numeric type

Vectors

As of right now, Drasil/GOOL only supports lists and arrays as “code types”, which would be the representations used for representing “vectors” in Drasil.

For now, the below type rules define vectors with Haskell lists. We can choose to create our own type with the length of the vector as a parameter – likely going “too far into Haskell”.

Functions

Presently, functions are defined through “QDefinitions”, where a list of UUIDs used in an expression are marked as the parameters of the function. Function “calls”/applications are captured in “Expr” (the expression language) by providing a list of input expressions and a list of named inputs (expressions) – $f(x, y, z, a = "b")$.

A few solutions:

1. Leave expressions in general untyped in Haskell, and rely on calculating the “space” of an expression dynamically to ensure that expressions are well-formed. If runtime (drasil’s compiling-knowledge-time) type analysis is ever needed, this will prove much easier to use in general.
2. Push the typing rules into Haskell via Generalized Algebraic Data Types (GADTs). Here, a larger question appears regarding functions – how should we handle function creation, application, and typing?
 - (a) Currying and applying arguments (allowing partial function applications): This would work well if we only generated functional languages, but it might prove problematic for GOOL if expressions are left with partial function applications.

Type Rules

1. Completeness:

$$\overline{Complete[] : Completeness} \quad (6)$$

$$\overline{Incomplete[] : Completeness} \quad (7)$$

2. AssocOp:

- (a) Numerics:

$$\frac{x : \text{Numerics}(T)}{Add[] : \text{AssocOp } x} \quad (8)$$

$$\frac{x : \text{Numerics}(T)}{Mul[] : \text{AssocOp } x} \quad (9)$$

- (b) Bool:

$$\overline{And[] : \text{AssocOp } Bool} \quad (10)$$

$$\overline{Or[] : \text{AssocOp } Bool} \quad (11)$$

3. UnaryOp:

- (a) Numerics:

$$\frac{x : \text{NumericsWithNegation}(T)}{Neg[] : \text{UnaryOp } x \ x} \quad (12)$$

$$\frac{x : \text{NumericsWithNegation}(T)}{Abs[] : \text{UnaryOp } x \ x} \quad (13)$$

$$\frac{x : \text{Numerics}(T)}{Exp[] : \text{UnaryOp } x \ Real} \quad (14)$$

For Log, Ln, Sin, Cos, Tan, Sec, Csc, Cot, Arcsin, Arccos, Arctan, and Sqrt, please use the following template, replacing “\$TRG” with the desired operator:

$$\overline{\$TRG[] : \text{UnaryOp } Real \ Real} \quad (15)$$

$$\overline{RtoI[]} : \text{UnaryOp Real Integer} \quad (16)$$

$$\overline{ItoR[]} : \text{UnaryOp Integer Real} \quad (17)$$

$$\overline{Floor[]} : \text{UnaryOp Real Integer} \quad (18)$$

$$\overline{Ceil[]} : \text{UnaryOp Real Integer} \quad (19)$$

$$\overline{Round[]} : \text{UnaryOp Real Integer} \quad (20)$$

$$\overline{Trunc[]} : \text{UnaryOp Real Integer} \quad (21)$$

(b) Vectors:

$$\frac{x : \text{NumericsWithNegation}(T)}{\overline{NegV[]} : \text{UnaryOp [x] [x]}} \quad (22)$$

$$\frac{x : \text{Numerics}(T)}{\overline{Norm[]} : \text{UnaryOp [x] Real}} \quad (23)$$

$$\frac{x : \tau}{\overline{Dim[]} : \text{UnaryOp [x] Integer}} \quad (24)$$

(c) Booleans:

$$\overline{Not[]} : \text{UnaryOp Bool Bool} \quad (25)$$

4. BinaryOp:

(a) Arithmetic:

$$\overline{FracI[]} : \text{BinaryOp Integer Integer Integer} \quad (26)$$

$$\overline{FracR[]} : \text{BinaryOp Real Real Real} \quad (27)$$

(b) Bool:

$$\overline{Impl[]} : \text{BinaryOp Bool Bool Bool} \quad (28)$$

$$\overline{If f[]} : \text{BinaryOp Bool Bool Bool} \quad (29)$$

(c) Equality:

$$\frac{x : \tau}{\overline{Eq[]} : \text{BinaryOp x x Bool}} \quad (30)$$

$$\frac{x : \tau}{\overline{NEq[]} : \text{BinaryOp x x Bool}} \quad (31)$$

(d) Ordering:

$$\frac{x : \text{Numerics}(T)}{\overline{Lt[]} : \text{BinaryOp x x Bool}} \quad (32)$$

$$\frac{x : \text{Numerics}(T)}{\overline{Gt[]} : \text{BinaryOp x x Bool}} \quad (33)$$

$$\frac{x : \text{Numerics}(T)}{\overline{LEq[]} : \text{BinaryOp x x Bool}} \quad (34)$$

$$\frac{x : \text{Numerics}(T)}{\overline{GEq[]} : \text{BinaryOp x x Bool}} \quad (35)$$

(e) Indexing:

$$\frac{x : \tau}{\text{Index}[] : \text{BinaryOp } [x] \text{ Integer } x} \quad (36)$$

(f) Vectors:

$$\frac{x : \text{Numerics}(T)}{\text{Cross}[] : \text{BinaryOp } [x] [x] [x]} \quad (37)$$

$$\frac{x : \text{Numerics}(T)}{\text{Dot}[] : \text{BinaryOp } [x] [x] x} \quad (38)$$

$$\frac{x : \text{Numerics}(T)}{\text{Scale}[] : \text{BinaryOp } [x] x [x]} \quad (39)$$

5. RTopology:

$$\frac{}{\text{Discrete}[] : \text{RTopology}} \quad (40)$$

$$\frac{}{\text{Continuous}[] : \text{RTopology}} \quad (41)$$

6. DomainDesc:

$$\frac{\text{top} : \tau_1 \quad \text{bot} : \tau_2 \quad s : \text{Symbol} \quad \text{rtop} : \text{RTopology}}{\text{BoundedDD}[s, \text{rtop}, \text{top}, \text{bot}] : \text{DomainDesc Discrete } \tau_1 \tau_2} \quad (42)$$

$$\frac{\text{topT} : \tau \quad \text{botT} : \tau \quad s : \text{Symbol} \quad \text{rtop} : \text{RTopology}}{\text{AllDD}[s, \text{rtop}] : \text{DomainDesc Continuous topT botT}} \quad (43)$$

7. Inclusive:

$$\frac{}{\text{Inc}[] : \text{Inclusive}} \quad (44)$$

$$\frac{}{\text{Exc}[] : \text{Inclusive}} \quad (45)$$

8. RealInterval:

$$\frac{a : \tau \quad b : \tau \quad \text{top} : (\text{Inclusive}, a) \quad \text{bot} : (\text{Inclusive}, b)}{\text{Bounded}[\text{top}, \text{bot}] : \text{RealInterval } a \ b} \quad (46)$$

$$\frac{a : \tau \quad b : \tau \quad \text{top} : (\text{Inclusive}, a)}{\text{UpTo}[\text{top}] : \text{RealInterval } a \ b} \quad (47)$$

$$\frac{a : \tau \quad b : \tau \quad \text{bot} : (\text{Inclusive}, b)}{\text{UpFrom}[\text{bot}] : \text{RealInterval } a \ b} \quad (48)$$

0.2.3 Expr

1. Literals:

$$\frac{x : \tau \quad l : \text{Literal } x}{\text{Lit}[l] : \text{Expr } x} \quad (49)$$

2. Associative Operations:

$$\frac{x : \tau \quad \text{op} : \text{AssocOp } x \quad \text{args} : [\text{Expr } x]}{\text{Assoc}[\text{op}, \text{args}] : \text{Expr } x} \quad (50)$$

3. Symbols:

$$\frac{x : \tau \quad u : \text{UID}}{C[u] : \text{Expr } x} \quad (51)$$

4. Function Call:

5. Case:

$$\frac{x : \tau \quad c : \text{Completeness} \quad \text{ces} : [(\text{Expr Bool}, \text{Expr } x)]}{\text{Case}[c, \text{ces}] : \text{Expr } x} \quad (52)$$

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6. Matrices:

$$\frac{x : \tau \quad es : [[\text{Expr } x]]}{\text{Matrix}[es] : \text{Expr } x} \quad (53)$$

7. Unary Operations:

$$\frac{x : \tau \quad y : \tau \quad op : \text{UnaryOp } x \ y \quad e : \text{Expr } x}{\text{Unary}[op, e] : \text{Expr } y} \quad (54)$$

8. Binary Operations:

$$\frac{x : \tau \quad y : \tau \quad z : \tau \quad op : \text{BinaryOp } x \ y \ z \quad l : \text{Expr } x \quad r : \text{Expr } y}{\text{Binary}[op, l, r] : \text{Expr } z} \quad (55)$$

9. “Big” Operations:

$$\frac{x : \tau \quad op : \text{AssocOp } x \quad dom : \text{DomainDesc Discrete (Expr } x) \text{ (Expr } x)}{\text{BigOp}[op, dom] : \text{Expr } x} \quad (56)$$

10. “Is in interval” operator:

$$\frac{x : \tau \quad u : \text{UID} \quad itvl : \text{RealInterval (Expr } x) \text{ (Expr } x)}{\text{RealI}[u, itvl] : \text{Expr } x} \quad (57)$$

0.2.4 ModelExpr

1.

$$\frac{B \quad C}{A}$$

0.2.5 CodeExpr

1.

$$\frac{B \quad C}{A}$$