

1 Typing Rules

1.1 Literal

1. Integers:

$$\frac{i : \text{Integer}}{\text{Integer}[i] : \text{Literal Integer}}$$

2. Strings (Text):

$$\frac{s : \text{String}}{\text{Str}[s] : \text{Literal String}}$$

3. Real numbers:

$$\frac{d : \text{Double}}{\text{DbI}[d] : \text{Literal Real}}$$

4. Whole numbered reals ($\mathbb{Z} \subset \mathbb{R}$):

$$\frac{d : \text{Integer}}{\text{ExactDbI}[d] : \text{Literal Real}}$$

5. Percentages:

$$\frac{n : \text{Integer} \quad d : \text{Integer}}{\text{Perc}[n, d] : \text{Literal Real}}$$

1.2 Miscellaneous

1. Completeness:

$$\frac{}{\text{Complete}[] : \text{Completeness}}$$

$$\frac{}{\text{Incomplete}[] : \text{Completeness}}$$

2. AssocOp:

- (a) Numerics:

$$\frac{x : \text{Numerics}(\tau)}{\text{Add}[] : \text{AssocOp } x}$$

$$\frac{x : \text{Numerics}(\tau)}{\text{Mul}[] : \text{AssocOp } x}$$

- (b) Bool:

$$\frac{}{\text{And}[] : \text{AssocOp Bool}}$$

$$\frac{}{\text{Or}[] : \text{AssocOp Bool}}$$

3. UnaryOp:

(a) Numerics:

$$\frac{x : \text{NumericsWithNegation}(x)}{Neg[] : \text{UnaryOp } x \ x}$$

$$\frac{x : \text{NumericsWithNegation}(x)}{Abs[] : \text{UnaryOp } x \ x}$$

For Log, Ln, Sin, Cos, Tan, Sec, Csc, Cot, Arcsin, Arccos, Arctan, and Sqrt, please use the following template, replacing “\$TRG” with the desired operator:

$$\overline{\$TRG[] : \text{UnaryOp } \text{Real } \text{Real}}$$

(b) Vectors:

$$\frac{x : \text{NumericsWithNegation}(x)}{NegV[] : \text{UnaryOp } [x] \ [x]}$$

$$\frac{x : \text{Numerics}(x)}{Norm[] : \text{UnaryOp } [x] \ \text{Real}}$$

$$\frac{x : \tau}{Dim[] : \text{UnaryOp } [x] \ \text{Integer}}$$

(c) Booleans:

$$\overline{Not[] : \text{UnaryOp } \text{Bool } \text{Bool}}$$

1.3 Expr

1. Literals:

$$\frac{x : \tau \quad l : \text{Literal } x}{Lit[l] : \text{Expr } x}$$

2. Associative Operations:

$$\frac{x : \tau \quad op : \text{AssocOp } x \quad args : [\text{Expr } x]}{Assoc[op, args] : \text{Expr } x}$$

3. Symbols:

$$\frac{x : \tau \quad u : \text{UID}}{C[u] : \text{Expr } x}$$

4. Function Call:

5. Case:

$$\frac{x : \tau \quad c : \text{Completeness} \quad ces : [(\text{Expr } \text{Bool}, \text{Expr } x)]}{Case[c, ces] : \text{Expr } x}$$

6. Matrices:

$$\frac{x : \tau \quad es : [[\text{Expr } x]]}{\text{Matrix}[es] : \text{Expr } x}$$

7. Unary Operations:

$$\frac{x : \tau \quad y : \tau \quad op : \text{UnaryOp } x \ y \quad e : \text{Expr } x}{\text{Unary}[op, e] : \text{Expr } y}$$

8. Binary Operations:

$$\frac{x : \tau \quad y : \tau \quad z : \tau \quad op : \text{BinaryOp } x \ y \ z \quad l : \text{Expr } x \quad r : \text{Expr } y}{\text{Binary}[op, l, r] : \text{Expr } z}$$

9. “Big” Operations:

$$\frac{x : \tau \quad op : \text{AssocOp } x \quad dom : \text{DiscreteDomainDesc } (\text{Expr } x) \ (\text{Expr } x)}{\text{BigOp}[op, dom] : \text{Expr } x}$$

10. “Is in interval” operator:

$$\frac{x : \tau \quad u : \text{UID} \quad itvl : \text{RealInterval } (\text{Expr } x) \ (\text{Expr } x)}{\text{RealI}[u, itvl] : \text{Expr } x}$$

1.4 ModelExpr

1.

$$\frac{B \ C}{A}$$

1.5 CodeExpr

1.

$$\frac{B \ C}{A}$$