



**A** System maintenance is scheduled for Wednesday, August 29, 2018 from 14:30-15:30 UTC. Courses might not be available during this time.

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## 4.2.2 Transposing a Partitioned Matrix

# 4.2.2 Transposing a Partitioned Matrix

## Important

Around 1:20 in the below video, the slide that shows the transposed matrix is completely wrong (the indices of the blocks are wrong...) Here is how it should be:

Let  $A \in \mathbb{R}^{m \times n}$  be partitioned as follows:

$$A = \left( \begin{array}{c|c|c|c} A_{0,0} & A_{0,1} & \cdots & A_{0,N-1} \\ \hline A_{1,0} & A_{1,1} & \cdots & A_{1,N-1} \\ \hline \vdots & \vdots & & \vdots \\ \hline A_{M-1,0} & A_{M-1,1} & \cdots & A_{M-1,N-1} \end{array} \right),$$

where  $A_{i,j} \in \mathbb{R}^{m_i \times n_j}$ . Then

$$A^T = \left( \begin{array}{c|c|c|c} A_{0,0}^T & A_{1,0}^T & \cdots & A_{M-1,0}^T \\ \hline A_{0,1}^T & A_{1,1}^T & \cdots & A_{M-1,1}^T \\ \hline \vdots & \vdots & & \vdots \\ \hline A_{0,N-1}^T & A_{1,N-1}^T & \cdots & A_{M-1,N-1}^T \end{array} \right).$$

Similarly, later, in "special cases",

**Each submatrix is a scalar.** If

$$A = \left( \begin{array}{c|c|c|c} \alpha_{0,0} & \alpha_{0,1} & \cdots & \alpha_{0,N-1} \\ \hline \alpha_{1,0} & \alpha_{1,1} & \cdots & \alpha_{1,N-1} \\ \hline \vdots & \vdots & & \vdots \\ \hline \alpha_{M-1,0} & \alpha_{M-1,1} & \cdots & \alpha_{M-1,N-1} \end{array} \right)$$

then

$$A^T = \left( \begin{array}{c|c|c|c} \alpha_{0,0}^T & \alpha_{1,0}^T & \cdots & \alpha_{M-1,0}^T \\ \hline \alpha_{0,1}^T & \alpha_{1,1}^T & \cdots & \alpha_{M-1,1}^T \\ \hline \vdots & \vdots & & \vdots \\ \hline \alpha_{0,N-1}^T & \alpha_{1,N-1}^T & \cdots & \alpha_{M-1,N-1}^T \end{array} \right) = \left( \begin{array}{cccc} \alpha_{0,0} & \alpha_{1,0} & \cdots & \alpha_{M-1,0} \\ \alpha_{0,1} & \alpha_{1,1} & \cdots & \alpha_{M-1,1} \\ \vdots & \vdots & & \vdots \\ \alpha_{0,N-1} & \alpha_{1,N-1} & \cdots & \alpha_{M-1,N-1} \end{array} \right).$$

The more I look at it, the more I notice how much I messed up the indices in this particular video... I hate indices...

Best to read the "Related Reading" for this unit...

[Start of transcript. Skip to the end.](#)

✕

## Homework 4.2.2.1

1/1 point (graded)

Show, step-by-step, how to transpose:  $\left( \begin{array}{ccc|c} 1 & -1 & 3 & 2 \\ 2 & -2 & 1 & 0 \\ 0 & -4 & 3 & 2 \end{array} \right)$

Steps:

$$1. \left( \begin{array}{cc|c} \begin{pmatrix} 1 & 2 \\ -1 & -2 \\ 3 & 1 \end{pmatrix} & \begin{pmatrix} 0 \\ -4 \\ 3 \end{pmatrix} \\ \hline (2 \ 0) & (2) \end{array} \right) = \left( \begin{array}{cc|c} 1 & 2 & 0 \\ -1 & -2 & -4 \\ 3 & 1 & 3 \\ \hline 2 & 0 & 2 \end{array} \right)$$

$$2. \left( \begin{array}{ccc|c} \begin{pmatrix} 1 & -1 & 3 \\ 2 & -2 & 1 \end{pmatrix} & \begin{pmatrix} 2 \\ 0 \end{pmatrix} \\ \hline (0 \ -4 \ 3) & (2) \end{array} \right)^T$$

$$3. \left( \begin{array}{ccc|ccc} \begin{pmatrix} 1 & -1 & 3 \\ 2 & -2 & 1 \end{pmatrix}^T & & & (0 & -4 & 3)^T \\ \hline \begin{pmatrix} 2 \\ 0 \end{pmatrix}^T & & & & & (2)^T \end{array} \right)$$

List the correct order of the steps taken above. (Answer Format: x,x,x where x is a step number)

2,3,1



Submit

## Homework 4.2.2.2

6/6 points (graded)

$$(\mathbf{3})^T = (\mathbf{3})$$

TRUE



$$\begin{pmatrix} 3 \\ 1 \\ 1 \\ 8 \end{pmatrix}^T = \begin{pmatrix} 8 \\ 1 \\ 1 \\ 3 \end{pmatrix}$$

FALSE



$$\left( \begin{array}{c|c|c|c} 3 & 1 & 1 & 8 \end{array} \right)^T = \begin{pmatrix} 3 \\ 1 \\ 1 \\ 8 \end{pmatrix}$$

TRUE



$$\left( \begin{array}{c|c|c|c} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \\ 9 & 10 & 11 & 12 \end{array} \right)^T = \left( \begin{array}{c|c|c|c} 1 & 2 & 3 & 4 \\ \hline 5 & 6 & 7 & 8 \\ \hline 9 & 10 & 11 & 12 \end{array} \right)$$

FALSE



$$\left( \begin{array}{c|c|c} 1 & 5 & 9 \\ 2 & 6 & 10 \\ 3 & 7 & 11 \\ 4 & 8 & 12 \end{array} \right)^T = \left( \begin{array}{ccc|c} 1 & 2 & 3 & 4 \\ \hline 5 & 6 & 7 & 8 \\ \hline 9 & 10 & 11 & 12 \end{array} \right)$$



$$\left( \left( \begin{array}{c|c|c} 1 & 2 & 3 & 4 \\ \hline 5 & 6 & 7 & 8 \\ \hline 9 & 10 & 11 & 12 \end{array} \right)^T \right)^T = \left( \begin{array}{c|c|c} 1 & 2 & 3 & 4 \\ \hline 5 & 6 & 7 & 8 \\ \hline 9 & 10 & 11 & 12 \end{array} \right)$$

