

This homework is done by Tianwei Mo.

1.

- a)  $256*256*100$
- b)  $40*80*2400$
- c)  $32*300*512*512$

2.

- a)  $K_1$  and  $k_2$  are in  $[0, 1]$
- b)  $5*4$
- c) The largest positive  $Z[I, j]$  appears when  $X[I, j]$  and  $X[i+1, j]$  are the biggest and  $X[I, j+1]$  and  $X[i+1, j+1]$  are the smallest. That is  $3 + 3 = 6$  when  $I = [1, 2, 3, 4]$  and  $j = 3$ .
- d) The largest negative  $Z[I, j]$  appears when  $X[I, j]$  and  $X[i+1, j]$  are the smallest and  $X[I, j+1]$  and  $X[i+1, j+1]$  are the biggest. That is  $-3 + -3 = -6$  when  $I = [1, 2, 3, 4]$  and  $j = 0$ .
- e)  $Z[I, j] = 0$  when  $I, j = [0, 1], [0, 2], [1, 1], [1, 2]$

3.

- a)  $Z$  has shape  $[46, 62, 20]$ .  $U$  has the same shape as  $Z$ .
- b) The number of input channels is  $[48, 64, 10]$ . The number of output channels is  $[46, 62, 20]$
- c) For each  $z$ , there are  $k_1+k_2+n$  multiplications. The total number is  $(3+3+10)*46*62*20=912640$
- d)  $3*3*10*20+20=1820$

4.

- a)  $Dj/dz = dj/du * du/dz = dj/du * (\exp(-z)/(1+\exp(-z))^2)$
- b)  $Dj/dw = dj/dz * dz/dw = dj/dz * \sum_{k_1} \sum_{k_2} \sum_n X[i, j_1 + k_1, j_2 + k_2, n]$
- c)  $Dj/dx = dj/dz * dz/dx = dj/dz * \sum_{k_1} \sum_{k_2} \sum_n W[k_1, k_2, n, m]$

5.

- a)  $Y = [1, 3, 0, 1]$
- b)  $Y = [2, 3, 10, 1]$
- c)  $Y[I, j, n] = \max_{m=0,1,\dots,p-1} x[i, sj + m, sn + m], \quad j, n = 0, 1, \dots, \left\lceil \frac{n-1}{s} \right\rceil$