

# Accelerators-II

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Joel Emer, Vivienne Sze, Hyoukjun Kwon, Felix Kao

# Outline

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- Recap
- Dataflows for 1D Convolution
- Getting more realistic
- Advanced Dataflows

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# Recap

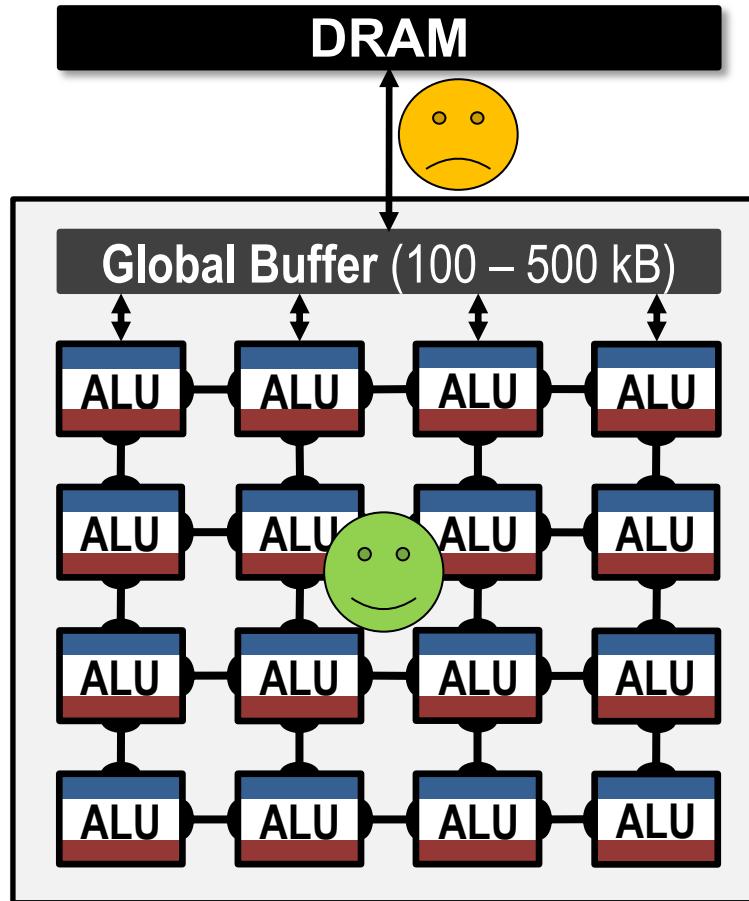
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- Why domain-specific accelerators?
  - High Throughput requirements (workload constraint)
  - Energy costs of Data Movement (technology constraint)
- Why do accelerators help?
  - custom datapaths for the operator(s) of interest (e.g., matrix multiplication)
  - remove control overheads that Turing-complete engines (e.g., CPUs) have such as instruction fetch/decode, speculation, caches, ..

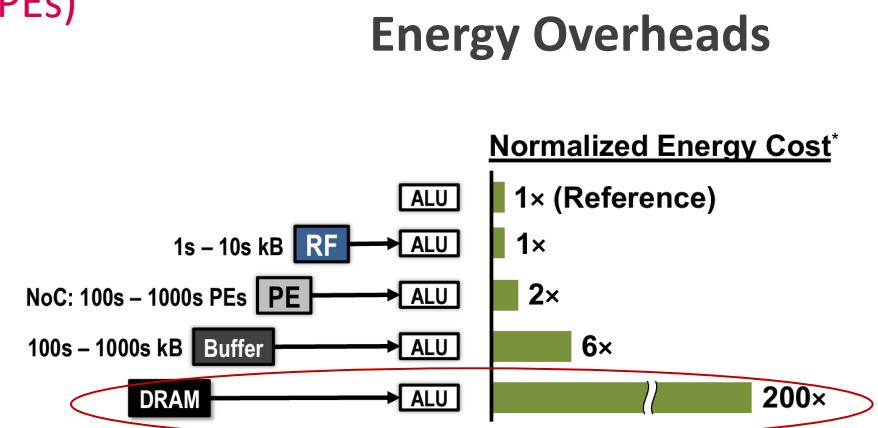
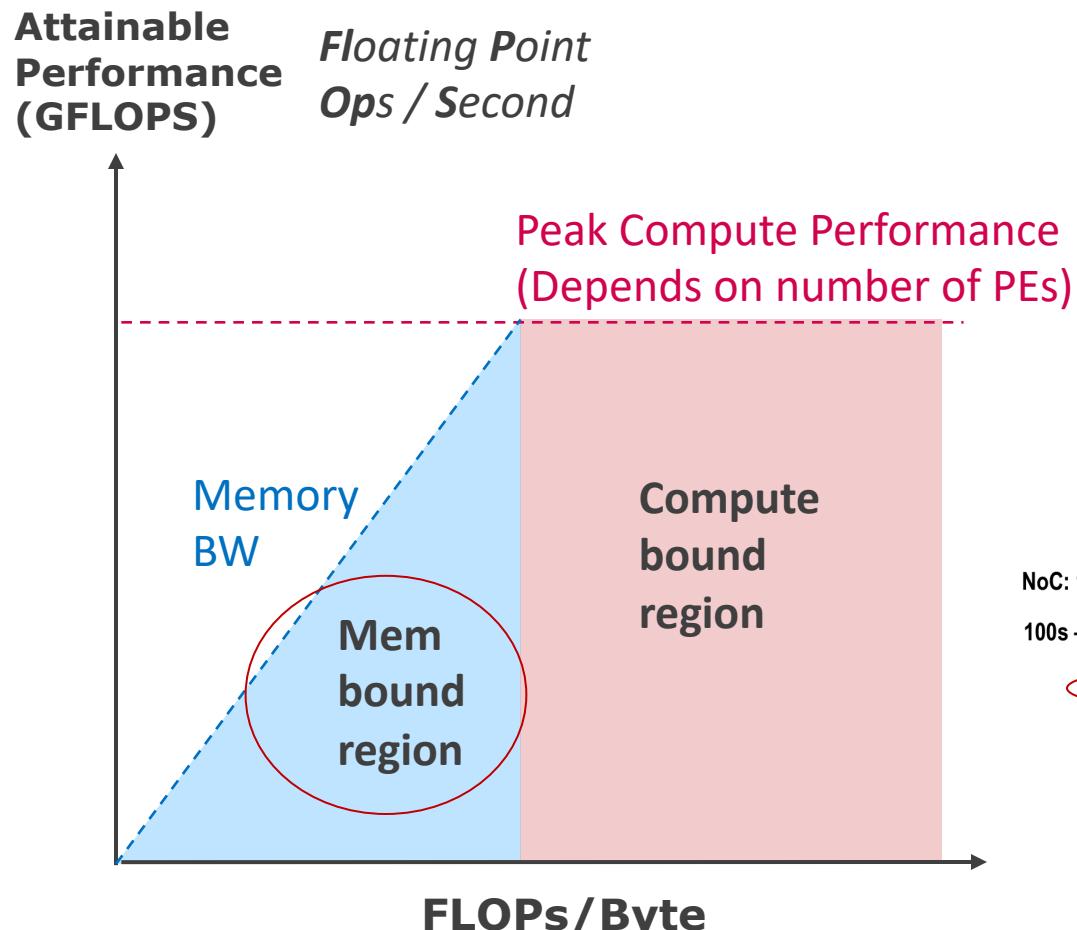
# Accelerators

Off-Chip  
Memory

Custom  
Datapath



# Why does this matter?



# How to reduce BW requirement?

---

| VGG16 conv 3_2   |              |
|------------------|--------------|
| Multiply Add Ops | 1.85 Billion |
| Weights          | 590 K        |
| Inputs           | 803 K        |
| Outputs          | 803 K        |

Data  
Reuse

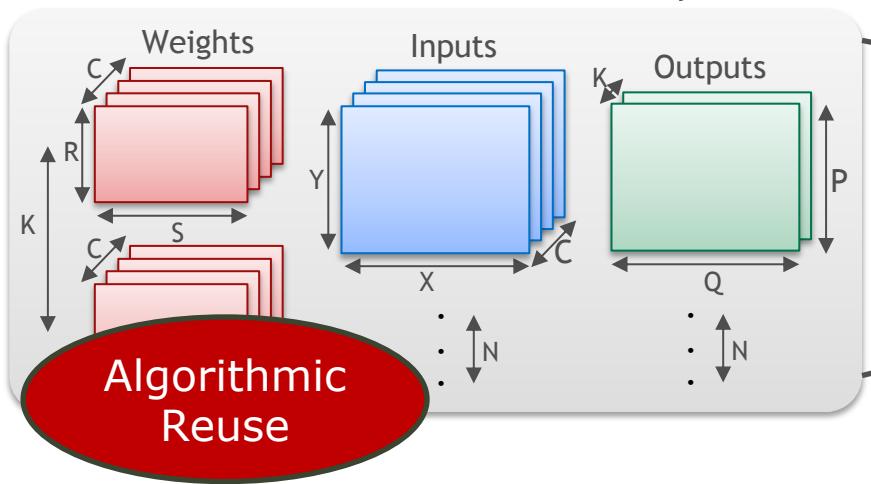
## How to exploit reuse? “Dataflow”

i.e., fine-grained schedule of computations within DNN accelerators

- Computation Order
- Parallelization Strategy

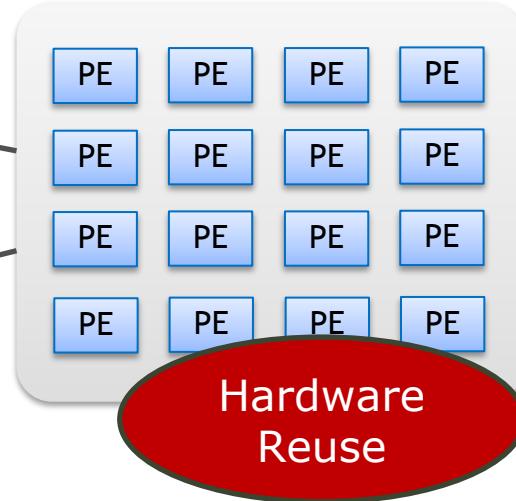
# Dataflow Implication: Algorithm Reuse → HW Reuse

7-dimensional network layer

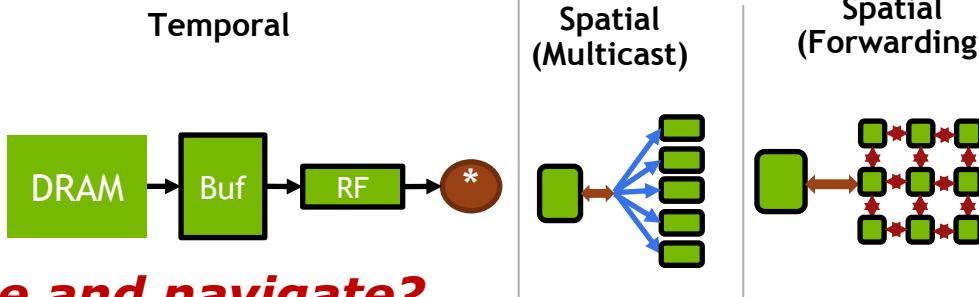


- **7D Computation Space**
  - $R * S * X * Y * C * K * N$
- **4D Operand/Result Data Spaces -**
  - Weights -  $R * S * C * K$
  - Inputs -  $X * Y * C * N$
  - Outputs -  $P * Q * K * N$

2D hardware array



- **HW Design-space**
  - Number of PEs
  - Memory Hierarchy (Sizes and Bandwidths)
  - Interconnect Bandwidth
- **HW Reuse Structures**



**How to describe and navigate?**

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- Advanced Dataflows

# Output Stationary (OS) Dataflow



## Computation

```
for(int x = 0; x < X'; x++)
    for(int s = 0; s < S; s++)
        Output[x] += Weight[s] * Input[x+s]
```

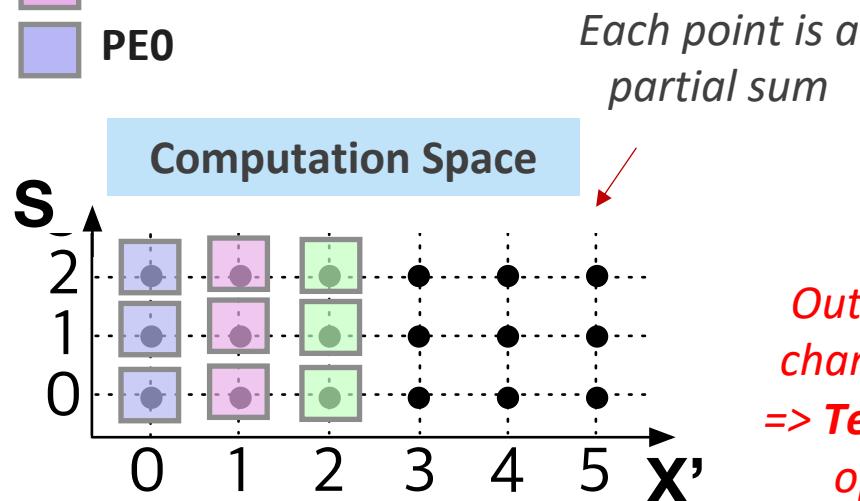


**Data**  
PartialSum[X'][S] needs to access:  

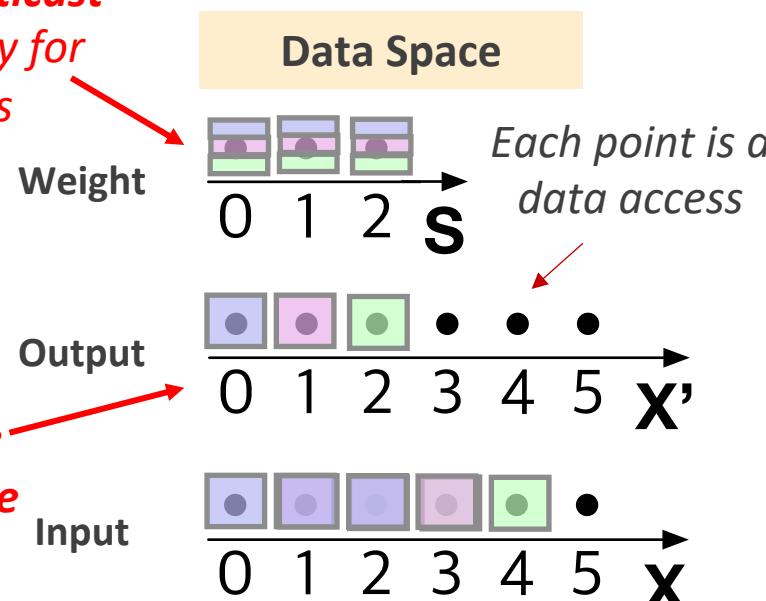
- Weight[s]
- Output[x']
- Input[x'+s]

- PE2
- PE1
- PE0

## Time = 0



*Spatial multicast opportunity for weights*



*Output does not change over time => Temporal reuse opportunity*

# Describing OS dataflow



```
int i[X];      # Input activations
int w[S];      # Filter weights
int o[X'];     # Output activations

for (x = 0; x < X'; x++) {
    for (s = 0; s < S; s++) {
        o[x] += i[x+s]*w[s];
}
```

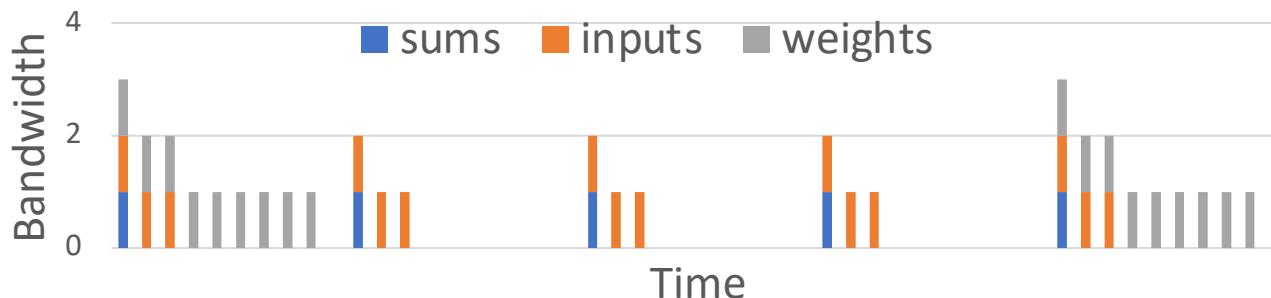
How often does the datapath change the weight and input?  
Output?

Every cycle  
Every S cycles: “Output stationary”

# What do we mean by “stationary”?

**The datatype (and dimension) that changes most slowly**

Sums: 1/10, Inputs: 3/10, Weights: 9/40



- Imprecise analogy: think of data transfers as a wave with “amplitude” and “period”
  - The stationary datatype has the **longest** period (locally held tile changes most slowly)
    - Note: like waves, may have harmful “interference” (bursts)
    - intermediate staging buffers reduce both bandwidth and energy
- Often corresponds to datatype that is “done with” earliest without further reloads
- **Note:** the “stationary” name is meant to give intuition, not to be a complete specification of all the behavior of a dataflow

# “Done with” vs “Needs Reload”

---

```
int i[X];      # Input activations
int w[S];      # Filter weights
int o[X'];     # Output activations

for (x = 0; x < X'; x++) {
    for (s = 0; s < S; s++) {
        o[x] += i[x+s]*w[s];
    }
}
```

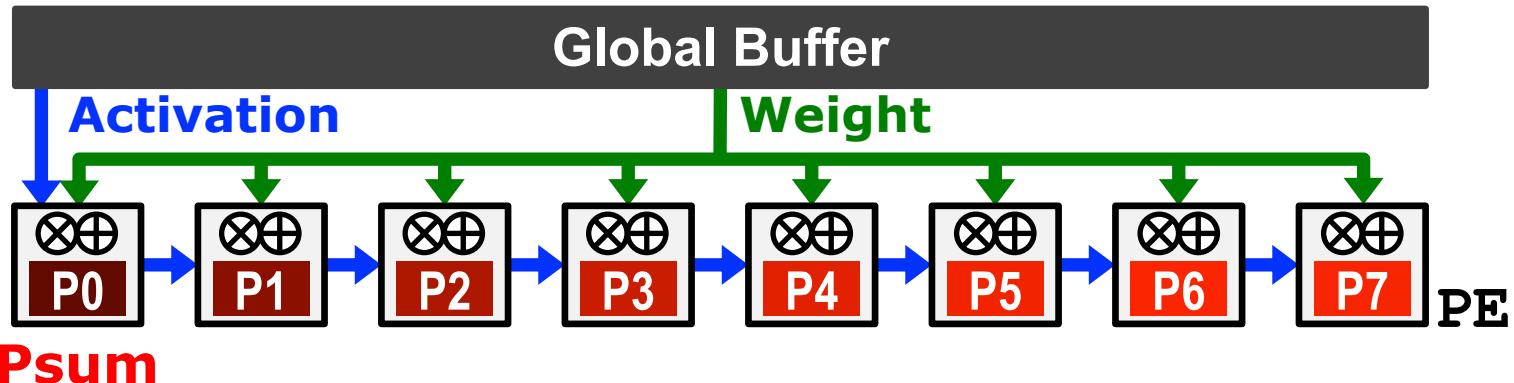
How many times  
will  $x == 2$ ?

How many times  
will  $x+s == 2$ ?

How many times  
will  $s == 2$ ?

- Temporal distance between re-occurrence dictates buffer size to avoid re-load
- How do you know if a buffer that size is worth it?

# OS Dataflow Implementation



- **Minimize partial sum** R/W energy consumption
  - maximize local accumulation
- **Broadcast/Multicast filter weights and reuse activations spatially** across the PE array

# Weight Stationary (WS) Dataflow



## Computation

```
for(int s = 0; s < S; s++)
    for(int x = 0; x < X'; x++)
        Output[x] += Weight[s] * Input[x+s]
```



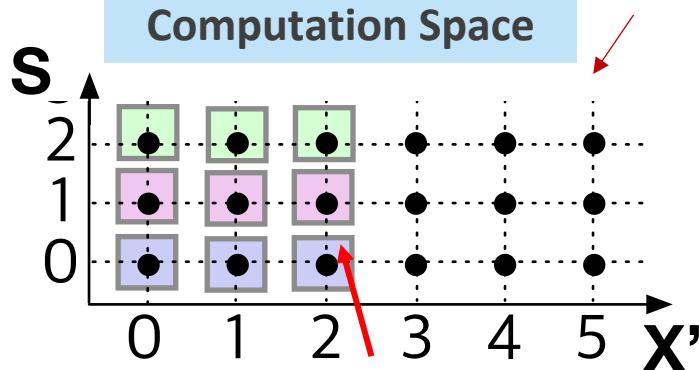
## Data

PartialSum[X'][S] needs to access:

- Weight[s]
- Output[x']
- Input[x'+s]

## Time = 0

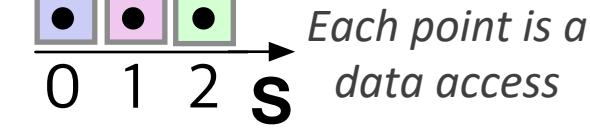
PE2  
PE1  
PE0



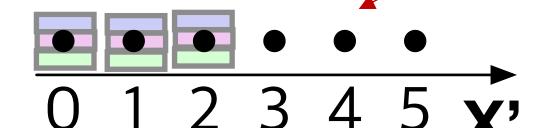
Each point is a partial sum

Weight does not change over time  
=> Temporal reuse opportunity

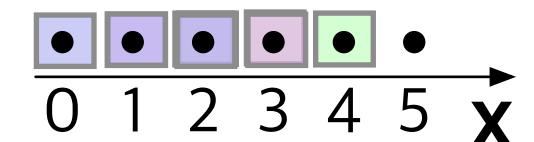
Weight



Output



Input



Need Spatial reduction for output

# Describing WS Dataflow



## Computation

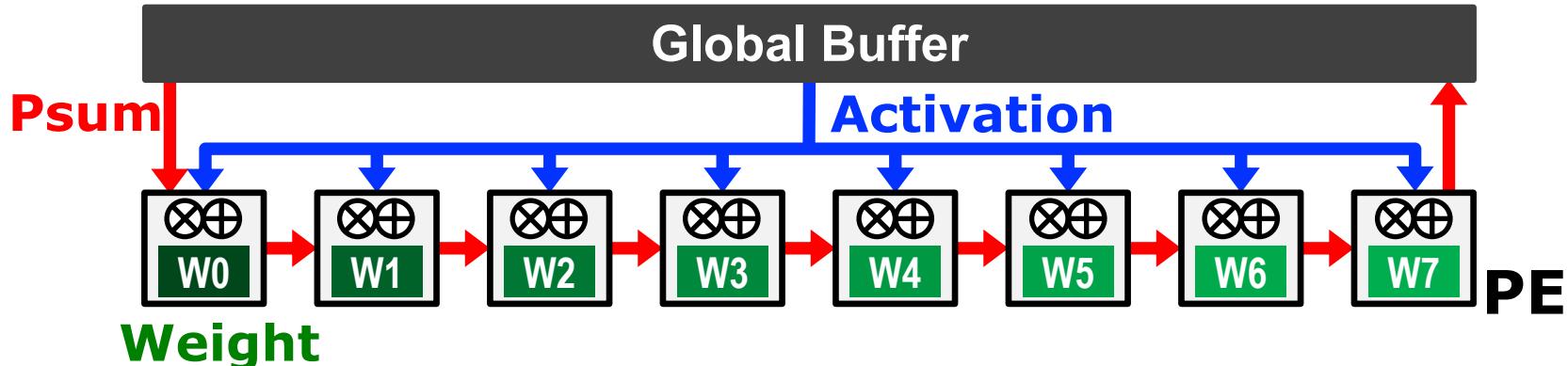
```
int i[X];      # Input activations
int w[S];      # Filter weights
int o[X'];     # Output activations

for (s = 0; s < S; s++) {
    for (x = 0; x < X'; x++) {
        o[x] += i[x+s]*w[s];
    }
}
```

What about the loop nest makes it weight stationary?

*outermost loop is S rank*

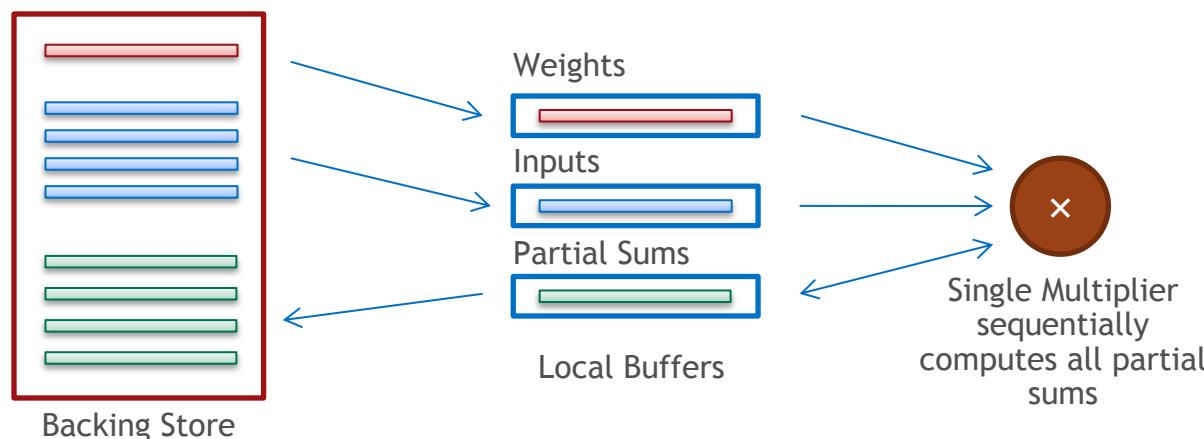
# WS Dataflow Implementation



- **Minimize weight** read energy consumption
  - maximize convolutional and filter reuse of weights
- **Broadcast activations** and **accumulate psums spatially** across the PE array.

# Simple Model for Mapping Dataflows to HW

$$\text{Weights } S * \text{Inputs } X = \text{Outputs } X' = X \cdot \text{ceil}(S/2)$$



| Common metric                                | Weights | Inputs | Outputs / Partial Sums |
|--|---------|--------|------------------------|
| Alg. Min. accesses to backing store (MINALG) | $S$     | $X$    | $X'$                   |
| Maximum operand uses (MAXOP)                 | $SX'$   | $SX'$  | $SX'$                  |

# 1D Convolution Summary

| <b>Hardware Structure</b>                    | <b>Per Data Type</b> | <b>OS Dataflow Implication</b> | <b>WS Dataflow Implication</b> |
|--|----------------------|--------------------------------|--------------------------------|
| <b>Bandwidth to MAC</b>                      | Weight Fetch Rate    | Every Cycle                    | Every S Cycles                 |
|  | Input Fetch Rate     | Every Cycle                    | Every Cycle                    |
|  | Output Fetch Rate    | Every S Cycles                 | Every Cycle                    |
| <b>Local Buffer Sizes for Temporal Reuse</b> | Weight Buffer Size   | S                              | 1                              |
|  | Input Buffer Size    | S                              | $X'$                           |
|  | Output Buffer Size   | 1                              | $X'$                           |
| <b>Total Local Buffer Accesses</b>           | Weight Buffer        | $X'$                           | $SX'$                          |
|  | Input Buffer         | $X'$                           | S                              |
|  | Output Buffer        | $SX'$                          | S                              |

*Why is product always  $SX'$ ?*

Total computations same

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  - Multi-layer Buffering
  - Multiple PEs
  - Full Convolution
- Advanced Dataflows

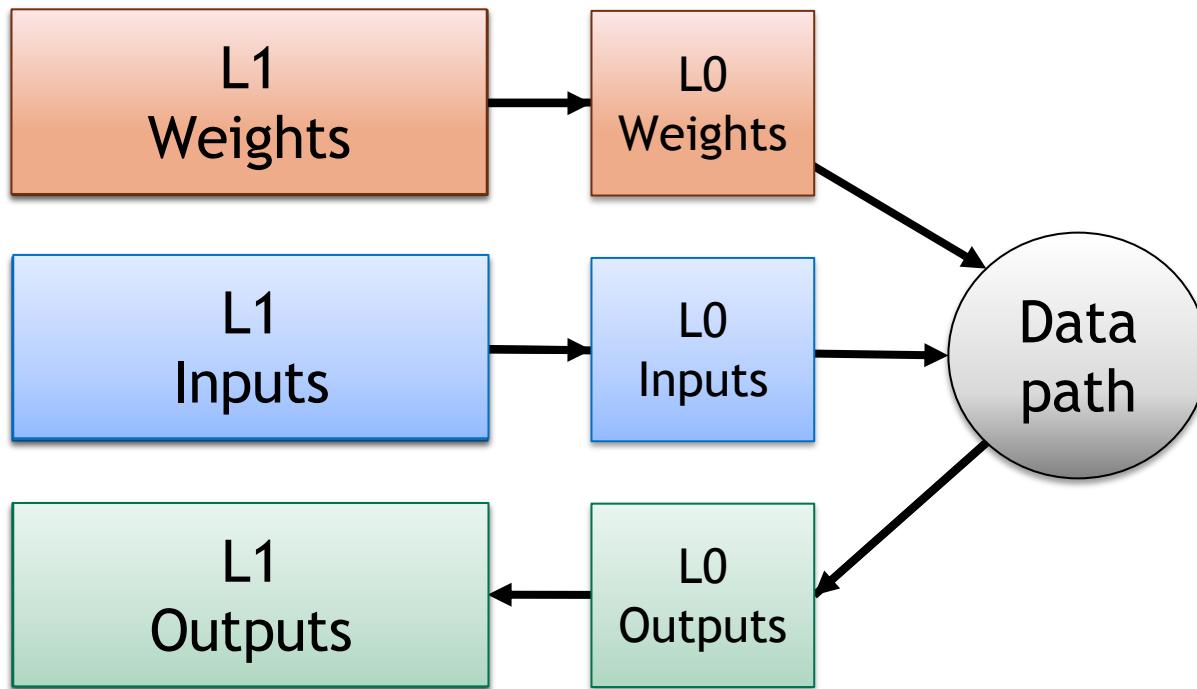
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# Multi-layer Buffering

---



How will this be reflected  
in the loop nest?

New 'level' of loops

# 1D Convolution – “Tiled”

|   |        |   |                              |
|---|--------|---|------------------------------|
| Weights   | Inputs | = | Outputs                      |
|  | *      |   |                              |
| S   | X      |   | $X' = X - \lceil X/2 \rceil$ |

```
int i[X];      # Input activations
int w[S];      # Filter Weights
int o[X'];     # Output activations

// Level 1
for (x1 = 0; x1 < X'1; x1++) {
    for (s1 = 0; s1 < S1; s1++) {
        // Level 0
        for (x0 = 0; x0 < X'0; x0++) {
            for (s0 = 0; s0 < S0; s0++) {
                x = x1 * X'0 + x0;
                s = r1 * R0 + r0;
                o[x] += i[x+s] * w[s];
            }
        }
    }
}
```

Note  $X'$  and  $S$  are factored so:  
 $X'0 * X'1 = X'$   
 $S0 * S1 = S$

# Buffer sizes

```
// Level 1
for (x1 = 0; x1 < X'1; x1++) {
    for (s1 = 0; s1 < S1; s1++) {
        // Level 0
        for (x0 = 0; x0 < X'0; x0++) {
            for (s0 = 0; s0 < S0; s0++) {
                o[x1*X'0+x0] += i[x1*X'0+x0 + s1*S0+s0] * w[s1*S0+s0];
            }
        }
    }
}
```

Constant over each level 1 iteration

- Level 0 buffer size is volume needed in each Level 1 iteration.
- Level 1 buffer size is volume needed to be preserved and re-delivered in future (usually successive) Level 1 iterations.
- A **legal mapping** will fit into the hardware's buffer sizes

# Buffer sizes

```
// Level 1
for (x1 = 0; x1 < X'1; x1++) {
    for (s1 = 0; s1 < S1; s1++) {
        // Level 0
        for (x0 = 0; x0 < X'0; x0++) {
            for (s0 = 0; s0 < S0; s0++) {
                o[x1*X'0+x0] += i[x1*X'0+x0 + s1*S0+s0] * w[s1*S0+s0];
            }
        }
    }
}
```

Constant over each level 1 iteration

|         | Level 0   | Level 1 |
|---------|-----------|---------|
| Weights | $S_0$     | $S$     |
| Inputs  | $X'0+S_0$ | $S$     |
| Outputs | $X'0$     | 1       |

# Energy Costs

```
// Level 1
for (x1 = 0; x1 < X'1; x1++) {
    for (s1 = 0; s1 < S1; s1++) {
        // Level 0
        for (x0 = 0; x0 < X'0; x0++) {
            for (s0 = 0; s0 < S0; s0++) {
                o[x1*X'0+x0] += i[x1*X'0+x0 + s1*S0+s0] * w[s1*S0+s0];
            }
        }
    }
}
```

Constant over each level 1 iteration

Energy of a buffer access is a function of the size of the buffer

Each buffer level's energy is proportional the number of accesses at that level

For level 0 that is all the operands to the Datapath

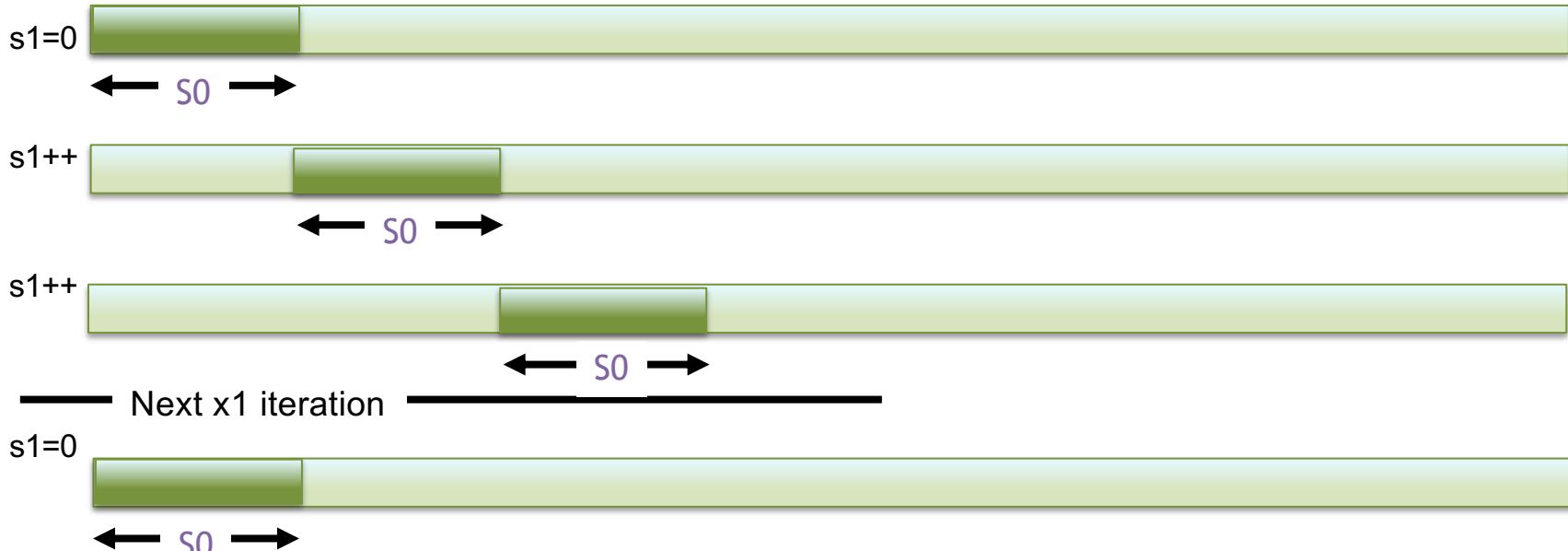
For level  $L>0$  there are three components:

- Data arriving from level  $L+1$
- Data that needs to be transferred to level  $L-1$
- Data that is returned from level  $L-1$

# Mapping – Weight Access Costs

```
// Level 1
for (x1 = 0; x1 < X'1; x1++) {
    for (s1 = 0; s1 < S1; s1++) {
        // Level 0
        for (x0 = 0; x0 < X'0; x0++) {
            for (s0 = 0; s0 < S0; s0++) {
                o[x1*X'0+x0] += i[x1*X'0+x0 + s1*S0+s0] * w[s1*S'0+s0];
            }
        }
    }
}
```

Weights



# Mapping – Weight Access Costs

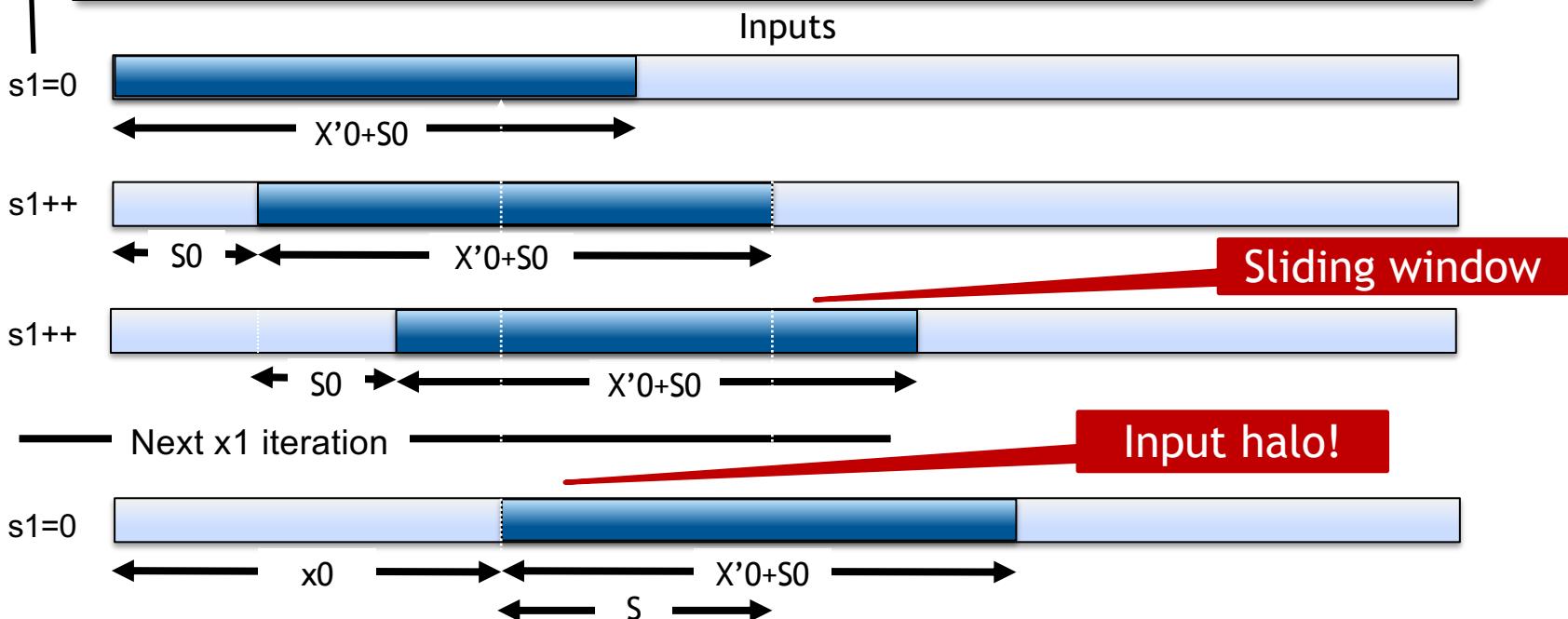
---

- Level 0 reads
  - Per level 1 iteration ->  $X'0*S0$  weight reads
  - Times  $X'1*S1$  level 1 iterations
  - Total reads =  $(X'0*S0)*(X'1*S1) = (X'0*X'1)*(S0*S1) = SX'$  reads
- Level 1 to 0 transfers
  - Per level 1 iteration ->  $S0$  weights transferred
  - Times same number of level 1 iterations =  $X'1 * S1$
  - Total transfers ->  $S0*(X'1*S1) = X'1*(S0*S1) = SX'1$

Disjoint/partitioned reuse pattern

# Mapping – Input Access Costs

```
// Level 1
for (x1 = 0; x1 < X'1; x1++) {
    for (s1 = 0; s1 < S1; s1++) {
        // Level 0
        for (x0 = 0; x0 < X'0; x0++) {
            for (s0 = 0; s0 < S0; s0++) {
                o[x1*X'0+x0] += i[x1*X'0+x0 + s1*S0+s0] * w[s1*S0+s0];
            }
        }
    }
}
```



# Mapping – Input Access Costs

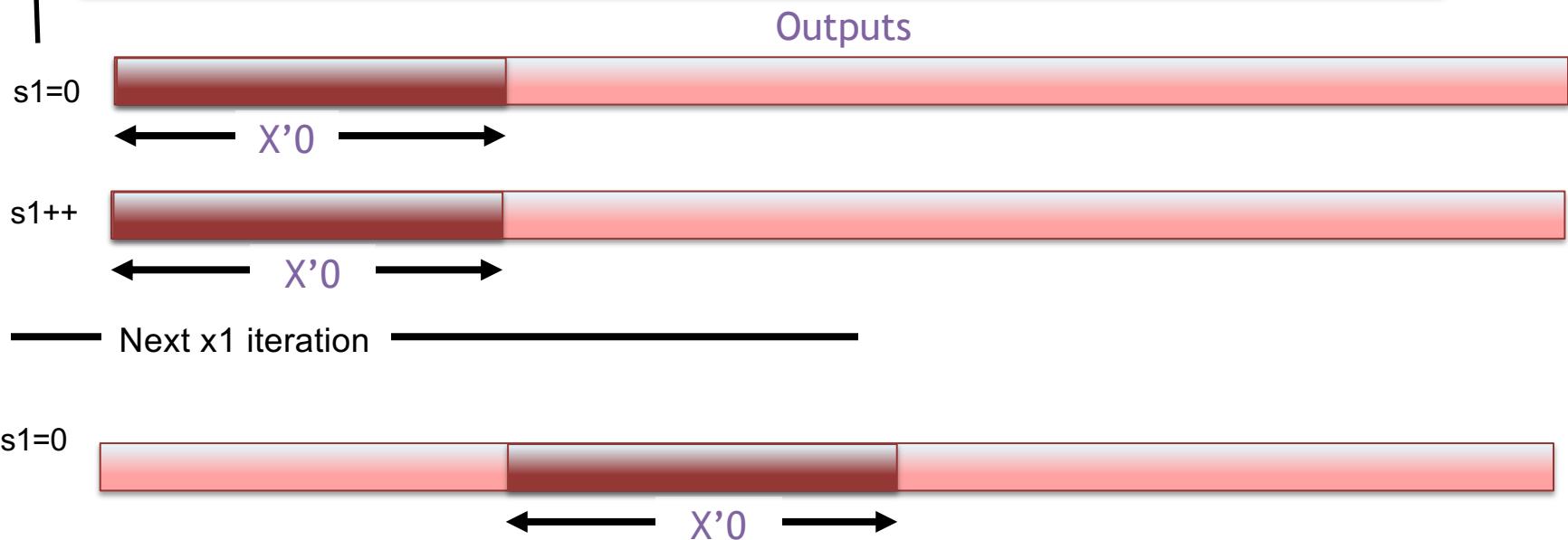
---

- Level 0 reads
  - Per level 1 iteration ->  $X'0+S0$  inputs reads
  - Times  $X'1*S1$  level 1 iterations
  - Total reads =  $X'1*S1*(X'0+S0) = ((X'1*X'0)*S1)+(X'1*(S1*S0))$   
=  $X'*S1+X'1*S$  reads
- 
- Level 1 to 0 transfers
  - For  $s=0$ ,  $X'0+S0$  inputs transferred
  - For each of the following  $S1-1$  iterations another  $S0$  inputs transferred
  - So total per  $x1$  iteration is:  $X'0+S0*S1 = X'0+S$  inputs
  - Times number of  $x1$  iterations =  $X'1$
  - So total transfers =  $X'1*(X'0+S) = (X'1*X'0)+X'1*S = X'+X'1*S$

Sliding window/partitioned reuse pattern

# Mapping – Output Access Costs

```
// Level 1
for (x1 = 0; x1 < X'1; x1++) {
    for (s1 = 0; s1 < S1; s1++) {
        // Level 0
        for (x0 = 0; x0 < X'0; x0++) {
            for (s0 = 0; s0 < S0; s0++) {
                o[x1*X'0+x0] += i[x1*X'0+x0 + s1*S0+s0] * w[s1*S0+s0];
```



# Mapping – Output Access Costs

---

- Level 0 writes
  - Due to level 0 being ‘output stationary’ only  $X'0$  writes per level 1 iteration
  - Times  $X'1 * S1$  level 1 iterations
  - Total writes =  $X'0 * (X'1 * S1) = (X'0 * X'1) * S1 = X' * S1$  writes
- 
- Level 0 to 1 transfers
  - After each  $S1$  iterations a completed partial sum for  $X'0$  outputs are transferred
  - There are  $X'1$  chunks of  $S1$  iterations
  - So total is  $X'1 * X'0 = X'$  transfers

# Mapping Data Cost Summary

```
// Level 1
for (x1 = 0; x1 < X'1; x1++) {
    for (s1 = 0; s1 < S1; s1++) {
        // Level 0
        for (x0 = 0; x0 < X'0; x0++) {
            for (s0 = 0; s0 < S0; s0++) {
                o[x1*X'0+x0] += i[x1*X'0+x0 + s1*S0+s0]* w[s1*S0+s0];
            }
        }
    }
}
```

|               | Level 0          | Level 1 to 0 transfers |
|---------------|------------------|------------------------|
| Weight Reads  | SX'              | SX'1                   |
| Input Reads   | X' * S1+ X'1 * S | X'+X'1*S               |
| Output Reads  | N/A              | N/A                    |
| Output Writes | X' * S1          | X'                     |

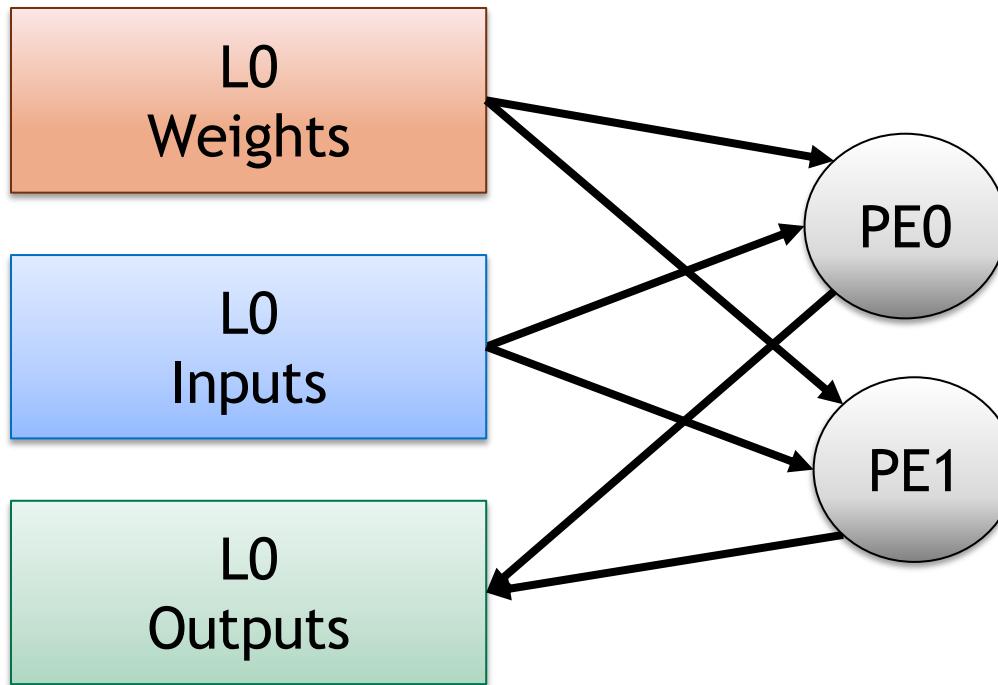
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# Spatial PEs

---



How will this be reflected  
in the loop nest?      New 'level' of loops

# 1D Convolution – Partition Outputs



```
int i[X];         # Input activations
int w[S];         # Filter Weights
int o[X'];        # Output activations

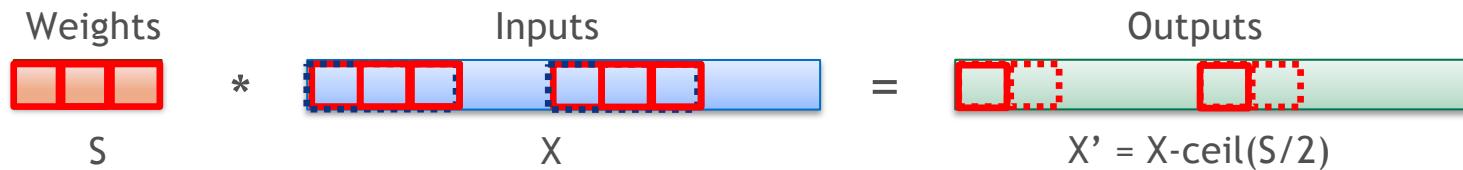
// Level 1
parallel-for (x1 = 0; x1 < X'1; x1++) {
- parallel-for (s1 = 0; s1 < S1; s1++) {
    // Level 0
    for (x0 = 0; x0 < X'0; x0++) {
        for (s0 = 0; s0 < S0; s0++) {
            o[x1*X'0+x0] += i[x1*X'0+x0 + s1*S0+s0]
                        * w[s1*S0+s0];
        }
    }
}
```

Note:  
 $X'0*X'1 = X'$   
 $S0*S1 = S$

X'1 = 2

S1 = 1 => s1 = 0

# 1D Convolution – Partition Outputs

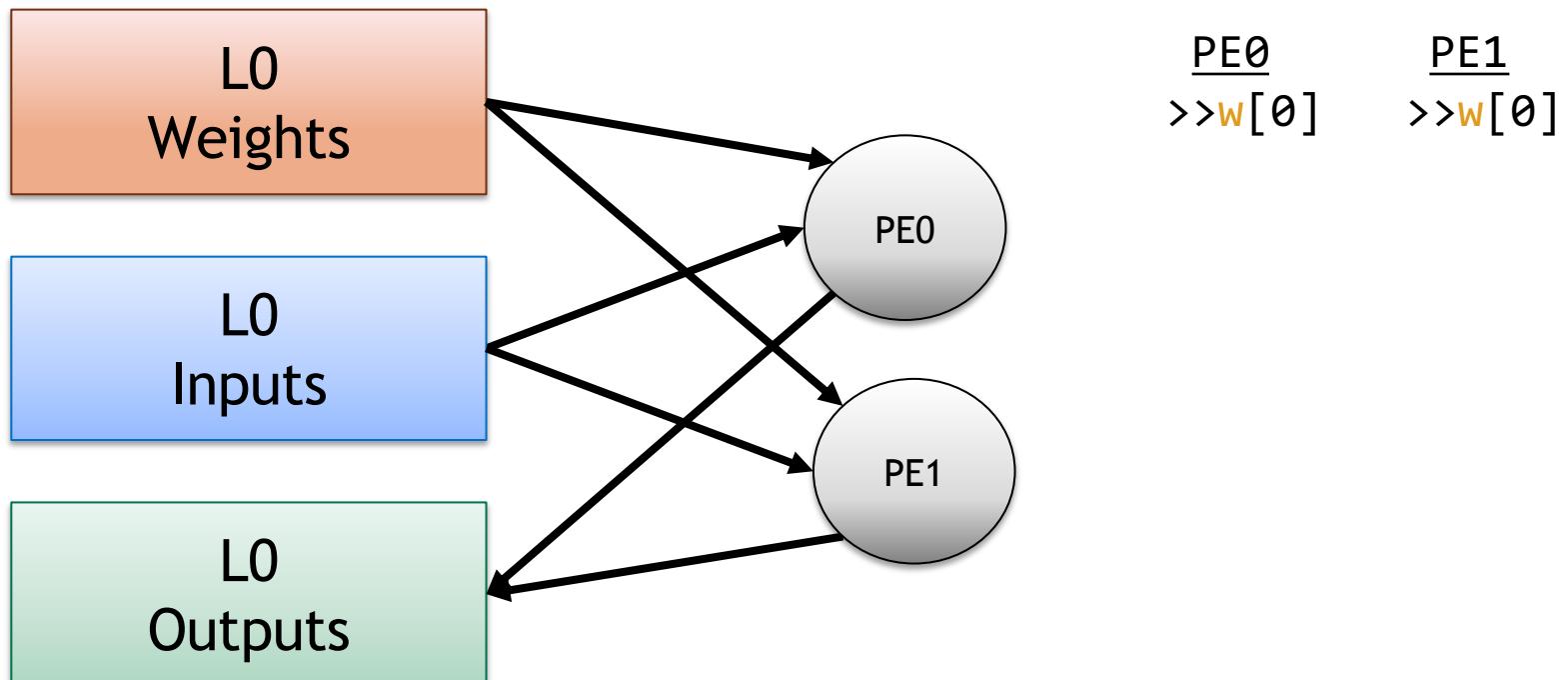


```
int i[X];      # Input activations
int w[S];      # Filter Weights
int o[X'];     # Output activations

// Level 1
parallel-for (x1 = 0; x1 < 2; x1++) {
// Level 0
    for (x0 = 0; x0 < X'0; x0++) {
        for (s0 = 0; s0 < S0; s0++) {
            o[x1*X'0+x0] += i[x1*X'0+x0 + s1*S0+s0]
                            * w[s1*S0+s0];
    }
}
```

# Spatial PEs

---



Implementation opportunity?

Yes, single fetch and multicast

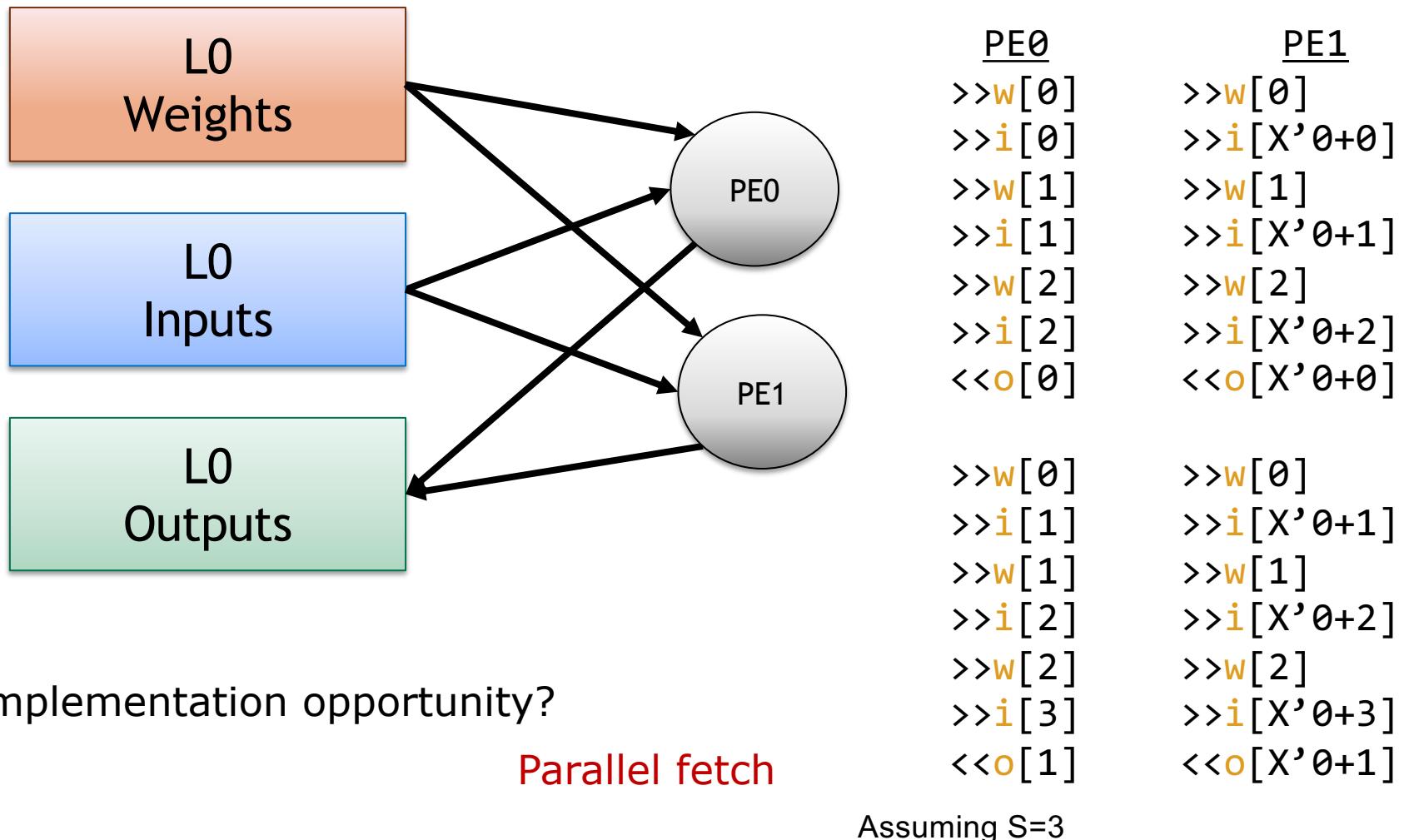
# 1D Convolution – Partition Outputs

```
// Level 1
parallel-for (x1 = 0; x1 < 2; x1++) {
    // Level 0
    for (x0 = 0; x0 < X'0; x0++) {
        for (s0 = 0; s0 < S0; s0++) {
            o[x1*X'0+x0] += i[x1*X'0+x0 + s1*S0+s0]
                * w[s1*S0+s0];
        }
    }
}
```

How do we recognize multicast opportunities?

Indices independent of spatial index

# Spatial PEs: Partitioned Outputs



# 1D Convolution – Partition Weights

$$\begin{array}{c} \text{Weights} \\ \boxed{S} \end{array} * \begin{array}{c} \text{Inputs} \\ \boxed{X} \end{array} = \begin{array}{c} \text{Outputs} \\ \boxed{X' = X \cdot \text{ceil}(S/2)} \end{array}$$

```
int i[X];      # Input activations
int w[S];      # Filter Weights
int o[X'];     # Output activations
```

```
// Level 1
parallel-for (s1 = 0; s1 < 2; s1++) {
    // Level 0
    for (x0 = 0; x0 < X'0; x0++) {
        for (s0 = 0; s0 < S0; s0++) {
            o[x1*X'0+x0] += i[x1*X'0+x0 + s1*S0+s0]
                * w[s1*S0+s0];
        }
    }
}
```

Note:  
 $X'0*X'1 = X'$   
 $S0*S1 = S$

# 1D Convolution – Partition Weights

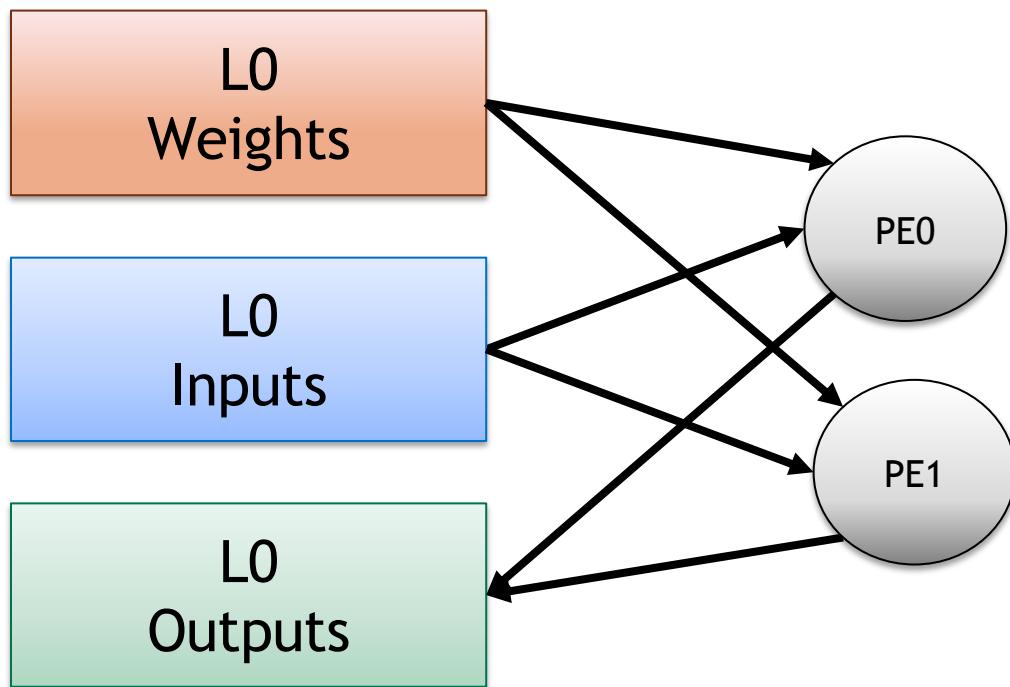
```
// Level 1
parallel-for (s1 = 0; s1 < 2; s1++) {
    // Level 0
    for (x0 = 0; x0 < X'0; x0++) {
        for (s0 = 0; s0 < S0; s0++) {
            o[x1*x'0+x0] -= i[x1*X'0+x0 + s1*s0+s0]
                * w[s1*s0+s0];
    }
}
```

How do we handle same index for output **Spatial reduction** in multiple PEs?

Other multicast opportunities?

No

# Spatial PEs: Partitioned Weights



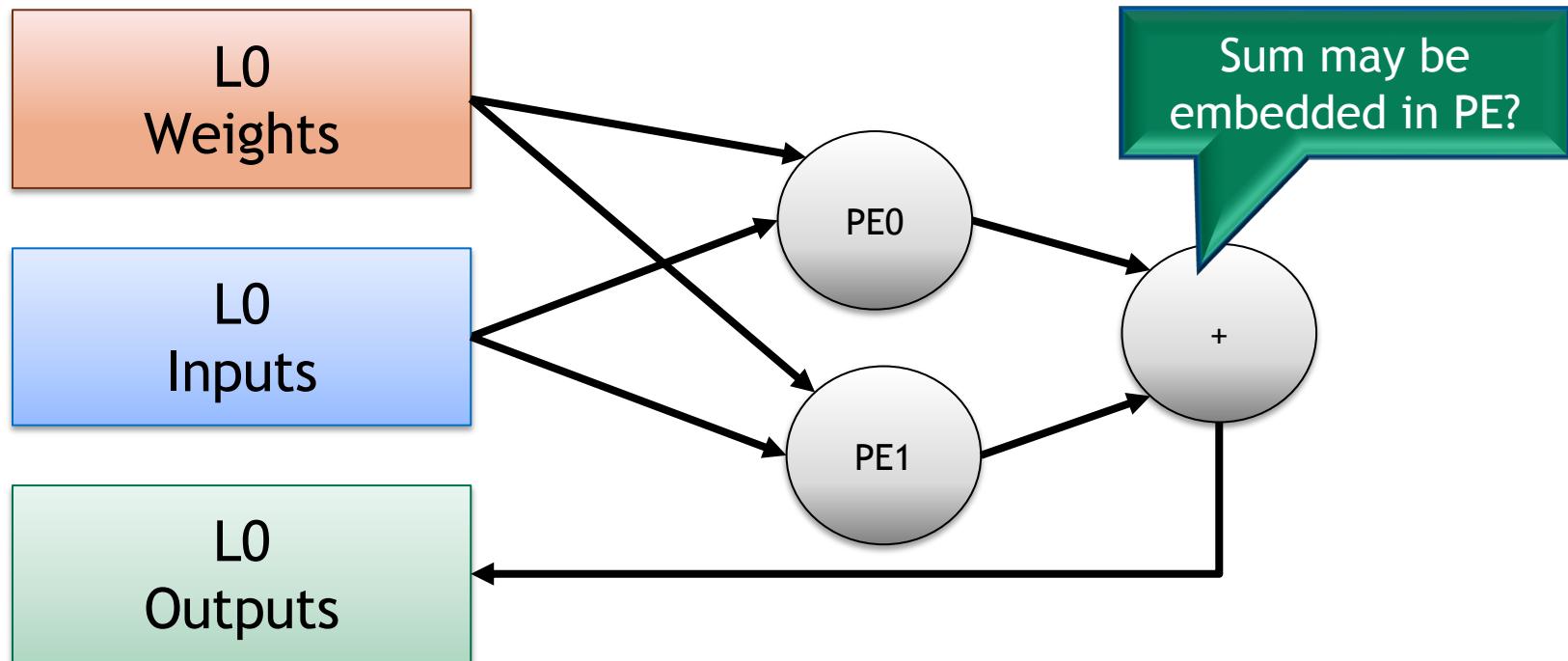
Spatial sum needed?

Yes

| <u>PE0</u> | <u>PE1</u>     |
|------------|----------------|
| $\gg w[0]$ | $\gg w[S_0+0]$ |
| $\gg i[0]$ | $\gg i[S_0+0]$ |
| $\gg w[1]$ | $\gg w[S_0+1]$ |
| $\gg i[1]$ | $\gg i[S_0+1]$ |
| $\gg w[2]$ | $\gg w[S_0+2]$ |
| $\gg i[2]$ | $\gg i[S_0+2]$ |
| $\ll o[0]$ | $\ll o[0]$     |
| $\gg w[0]$ | $\gg w[S_0+1]$ |
| $\gg i[1]$ | $\gg i[S_0+1]$ |
| $\gg w[1]$ | $\gg w[S_0+2]$ |
| $\gg i[2]$ | $\gg i[S_0+2]$ |
| $\gg w[2]$ | $\gg w[S_0+3]$ |
| $\gg i[3]$ | $\gg i[S_0+3]$ |
| $\ll o[1]$ | $\ll o[1]$     |

Assuming S=3

# Spatial PEs with Spatial Summation



What if hardware cannot do a spatial sum?

Illegal mapping!

# NoC Support

---

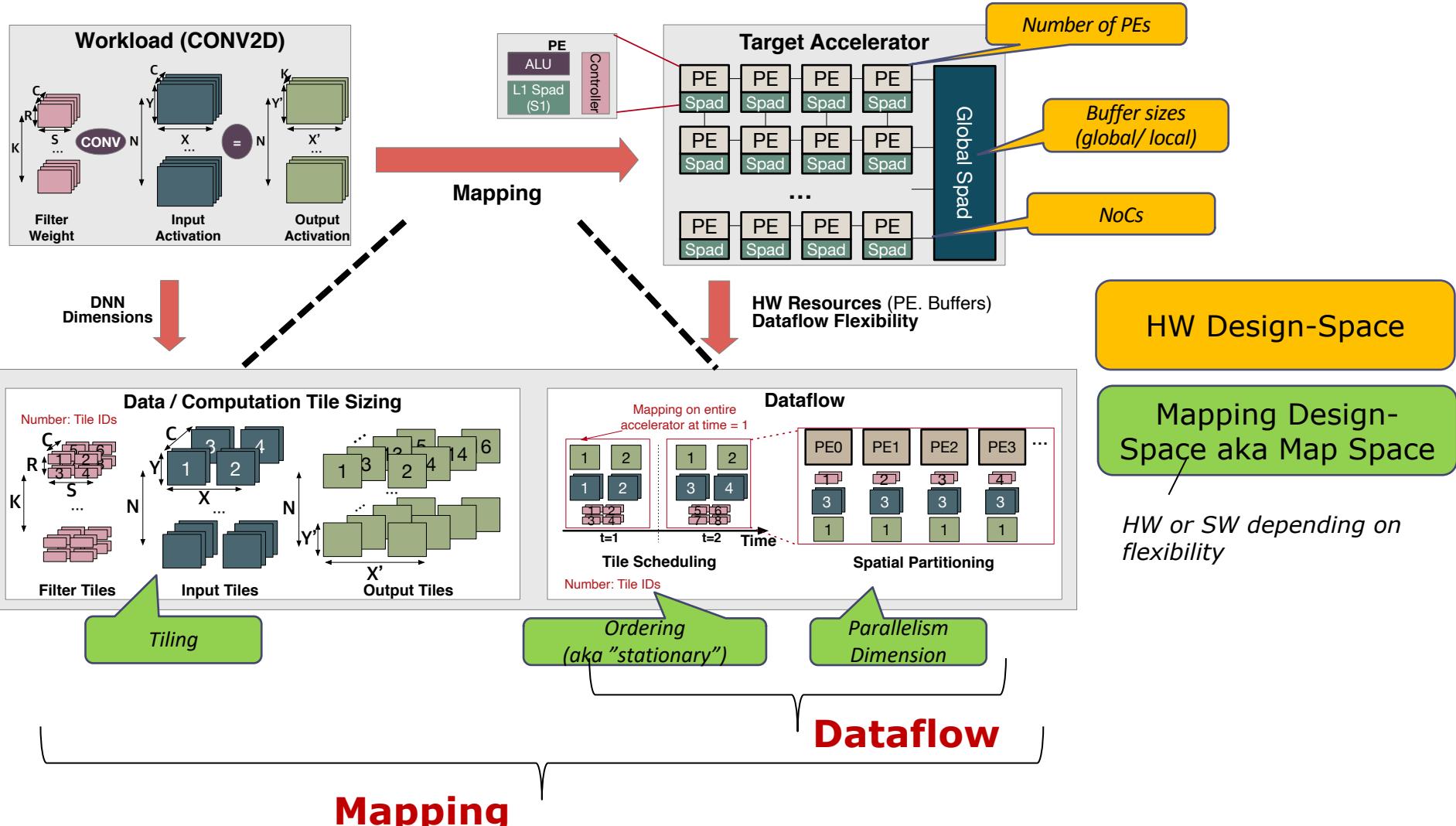
| <b>Hardware Structure</b>                | <b>Per Data Type</b> | <b>Output-partitioned Dataflow Implication</b> | <b>Weight-partitioned Dataflow Implication</b> |
|--|----------------------|--|--|
| <b>Network-on-Chip for Spatial Reuse</b> | Weight Distribution  | Spatial Multicast                              | Unicast  |
|  | Input Distribution   | Unicast/Spatial Multicast                      | Unicast  |
|  | Output Collection    | Temporal Reduction                             | Spatial Reduction                              |

# More Realistic Loop Nest

```
int i[W];      # Input activations
int w[R];      # Filter Weights
int o[E];      # Output activations

// Level 2
for (x2 = 0; x2 < X'2; x2++) {
    for (s2 = 0; s2 < S2; s2++) {
        // Level 1
        parallel-for (x1 = 0; x1 < X'1; x1++) {
            parallel-for (s1 = 0; s1 < S1; s1++) {
                // Level 0
                for (x0 = 0; x0 < X'0; x0++) {
                    for (s0 = 0; s0 < S0; s0++) {
                        ...
                    }
                }
            }
        }
    }
}
```

# Design-space of a DNN Accelerator

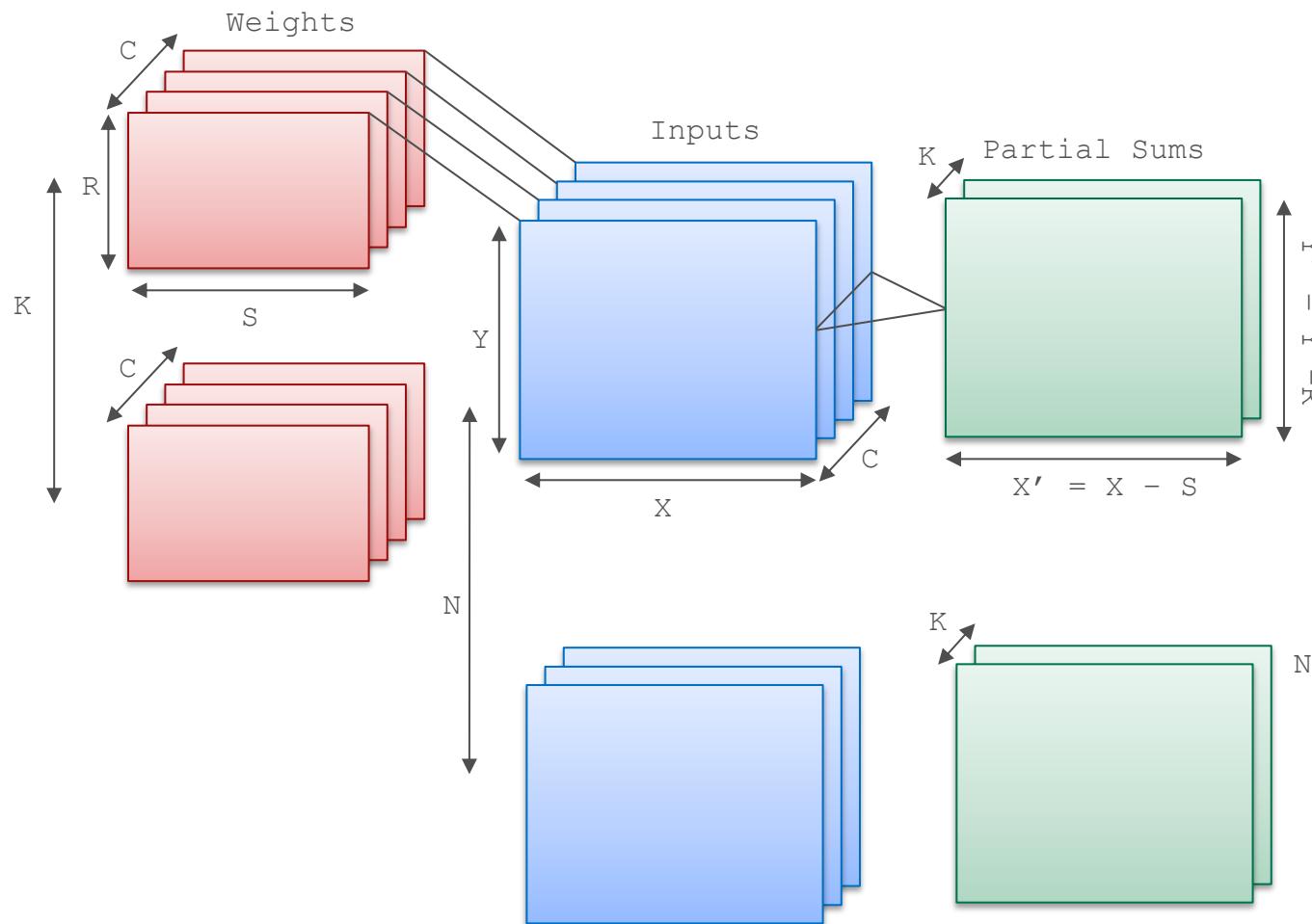


# Outline

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- Recap
- Dataflows for 1D Convolution
- Getting more realistic
  - Multi-layer Buffering
  - Multiple PEs
  - Full Convolution
- Advanced Dataflows

# Mapping a Full Convolution



# Reference Convolution Layer

---

```
int i[C][Y][X];      # Input activation channels
int w[K][C][R][S];  # Filter weights (per channel pair)
int o[K][Y'][X'];   # Output activation channels

for (k = 0; k < K; k++) {
    for (y = 0; y < Y'; y++) {
        for (x = 0; x < X'; x++) {
            for (c = 0; c < C; c++) {
                for (r = 0; r < R; r++) {
                    for (s = 0; s < S; s++) {
                        o[k][y][x] += i[c][y+r][x+s]*w[k][c][r][s];
```



# A Mapping Representation

---

- For each temporal and spatial level:
  - Permutation order of all indices
  - Partitioning of data volume for all indices (factoring)
    - $\forall X \in \text{indices} \left( \prod_{l=0}^{\text{maxlevel}} X_l \right) \geq X_{\text{total}}$
  - Data bypass flag per datatype (for temporal layers)

$$(N_l \ K_l \ C_l \ X'_l \ Y'_l \ R_l \ S_l) \ [I_l, W_l, O_l]$$

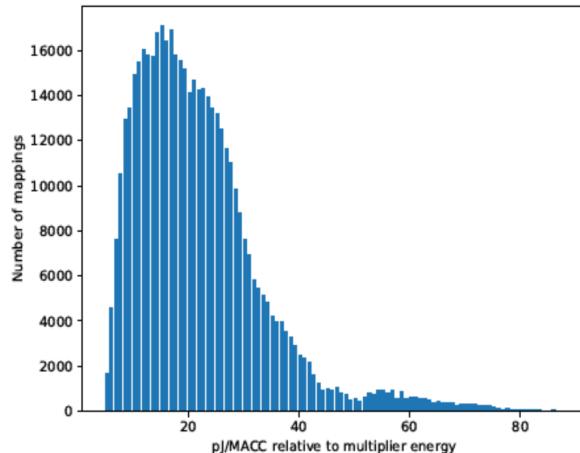
How many permutations per level? (# Indices)!

How many bypass combinations per level?  $2^N$

Total choices per temporal level? (# Indices)! \*  $2^N$  \* factorings

# Impact of Mappings

VGG conv3 2 Layer. Source: Timeloop



480,000 mappings shown

Spread: 19x in energy efficiency

Only 1 is optimal, 9 others within 1%

6,582 mappings have min. DRAM accesses but vary 11x in energy efficiency

1-level par.

**Immense  
Search  
space**

2-level par.

$O(10^{12})$

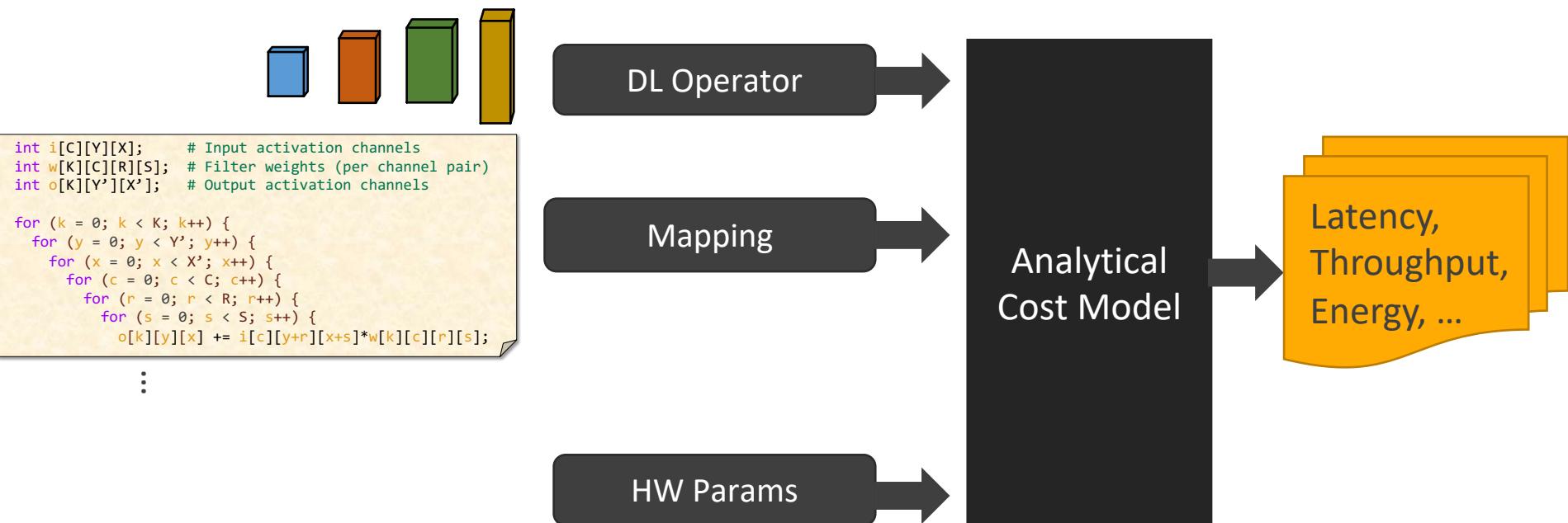
$+ O(10^{24})$

3-level par.

$O(10^{36})$

# Exploring Mappings

- Gigantic space of potential loop orders & factorizations
- Cycle-accurate modeling of realistic dimensions and fabric sizes too slow
- Solution: use an analytic modeling



e.g.,: Timeloop (ISPASS 2019),  
MAESTRO (MICRO 2019), ..

# Outline

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- Recap
- Dataflows for 1D Convolution
- Getting more realistic
- Advanced Dataflows
  - Fusion
  - Sparsity

# Outline

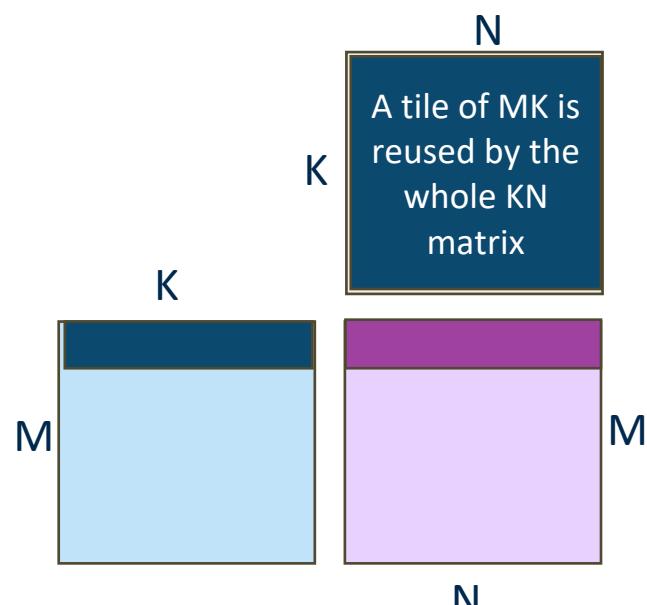
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- Recap
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# Not All GEMMs are Compute Bound

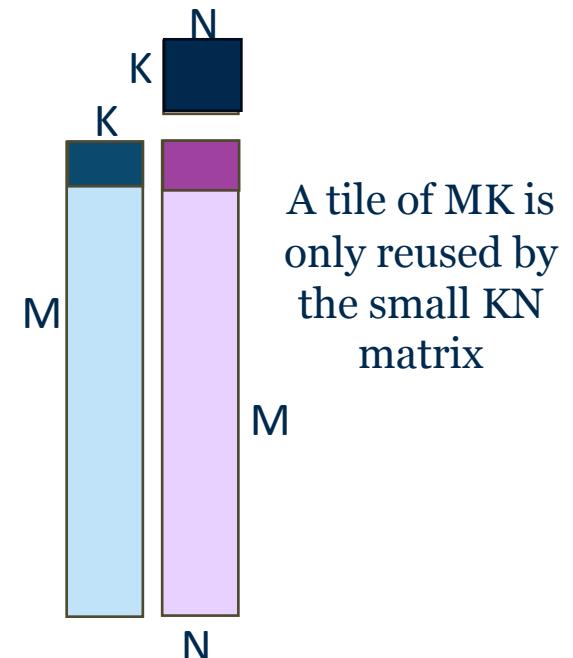
Even in the best case with infinite on-chip storage and large number of PEs.

$$AI_{best\_GEMM} = \frac{M \times K \times N}{M \times K + K \times N + M \times N}$$



Regular GEMM ( $M=1024, K=1024, N=1024$ )

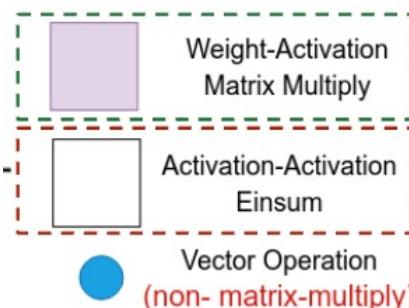
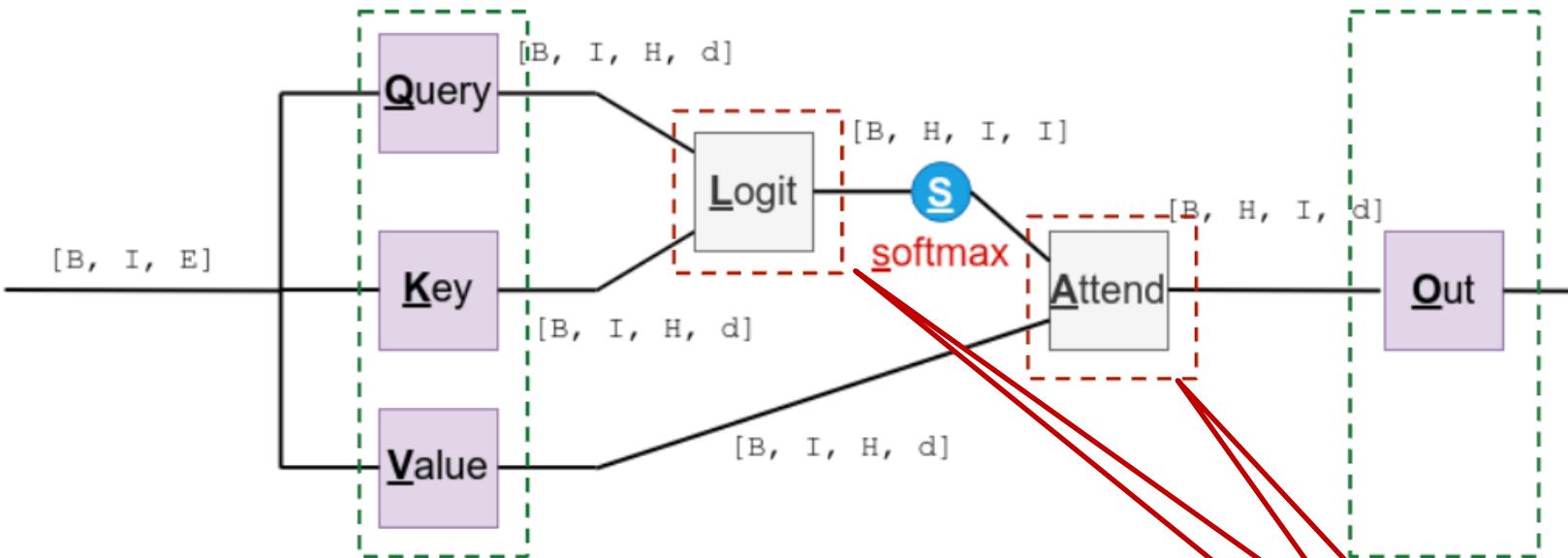
$$AI_{best\_GEMM} = 341.33 \text{ ops/word}$$



Skewed GEMM ( $M=1048576, N=32, K=32$ )

$$AI_{best\_GEMM} = 16 \text{ ops/word}$$

# GEMMs in Attention Layers



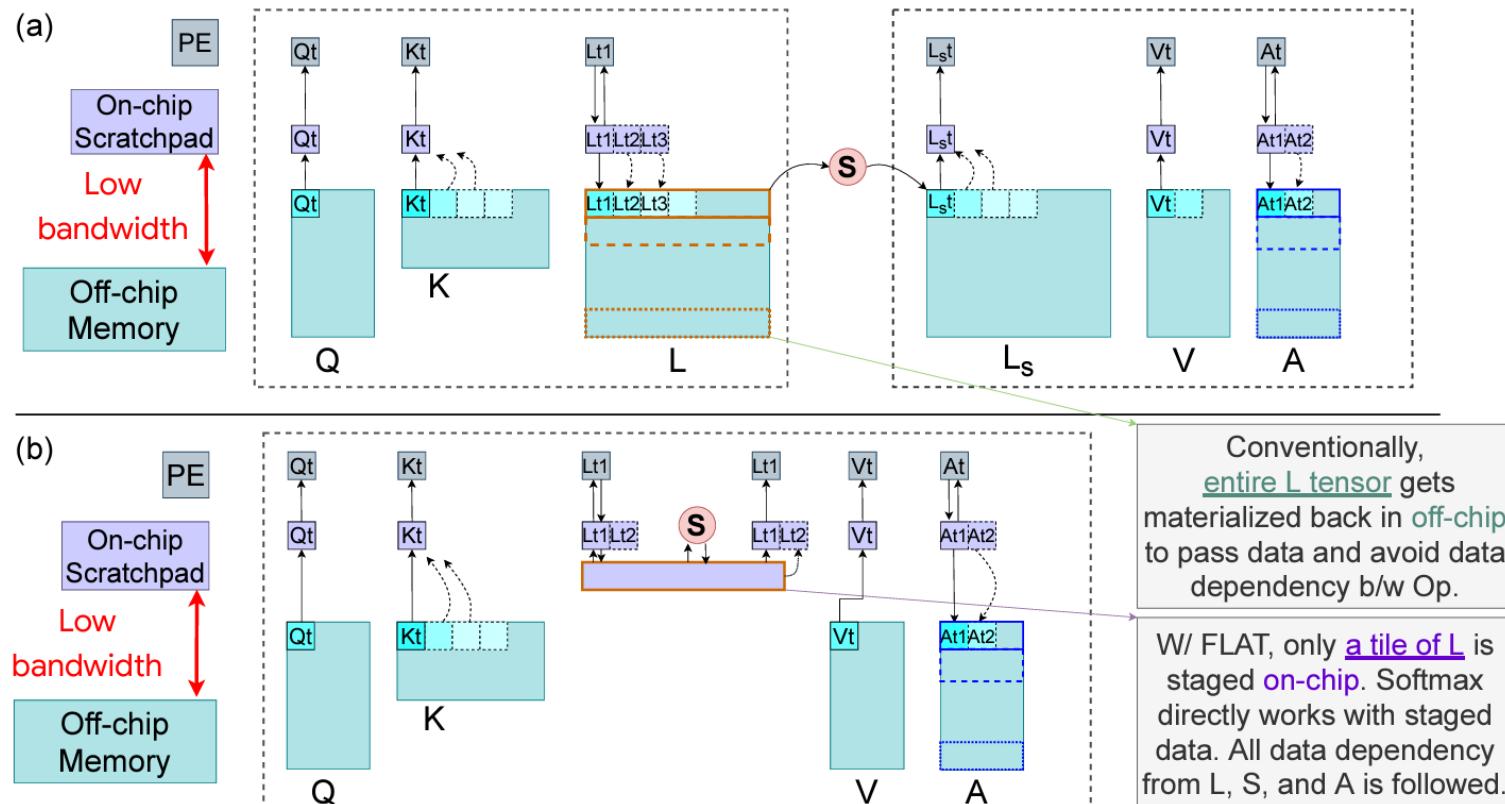
Compute-bound  $\Rightarrow$  Intra-operator dataflow to improve reuse is effective

Memory-bound  $\Rightarrow$  Intra-operator dataflow is not effective

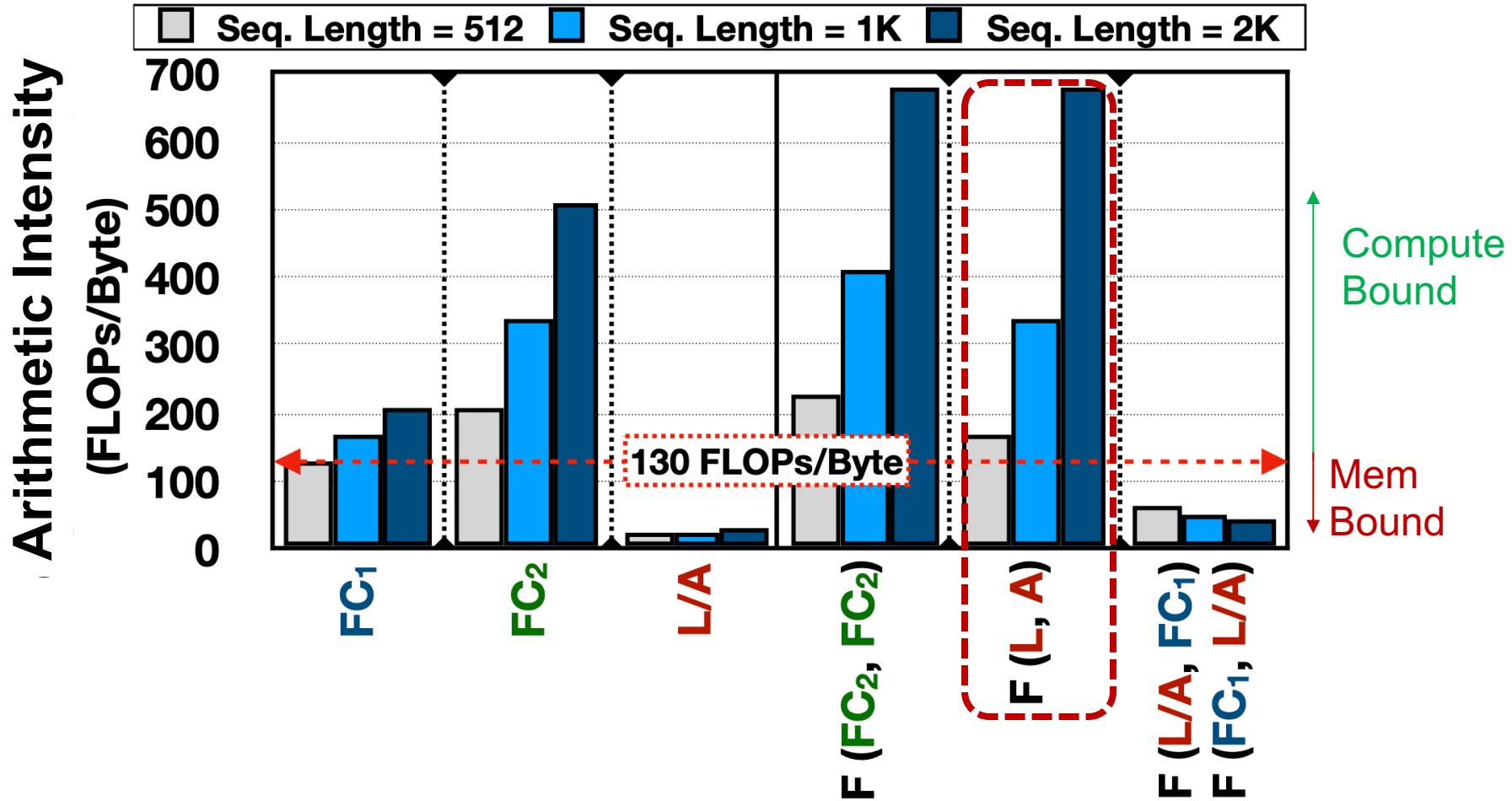
Activation – Activation GEMMs

# Opportunity: Fusion

- Key Intuition: “Reuse” the intermediate output immediately



# Opportunity: Fusion

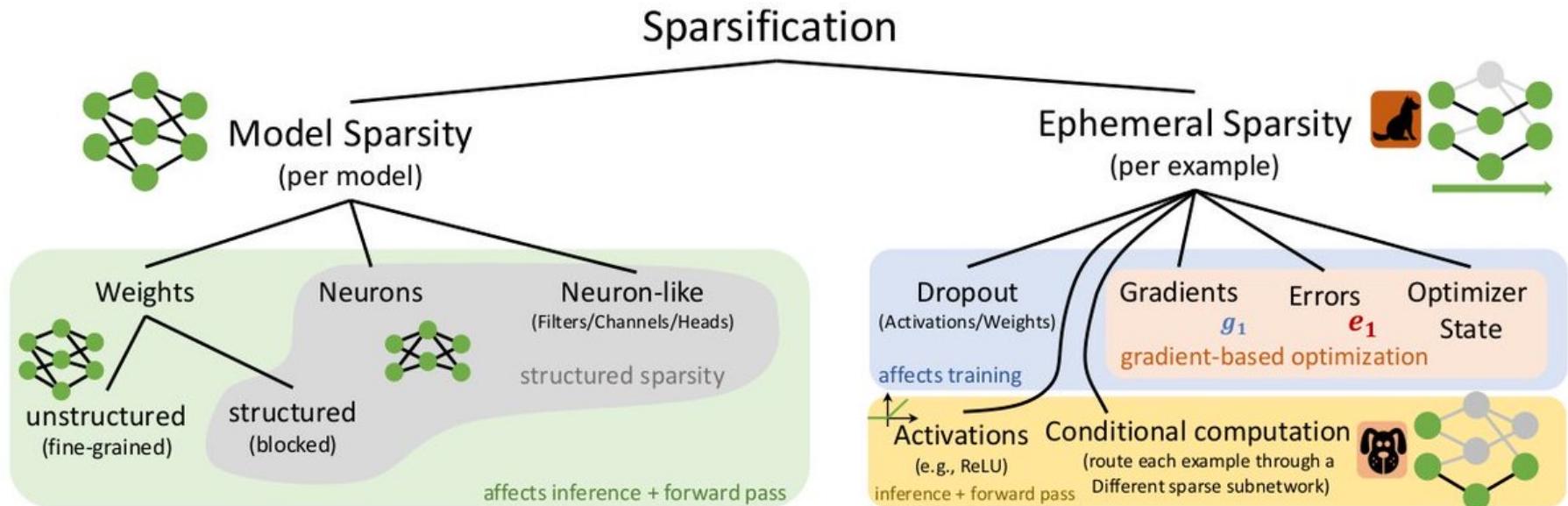


# Outline

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- Recap
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- Getting more realistic
- Advanced Dataflows
  - Fusion
  - Sparsity

# Sparsity in DNNs



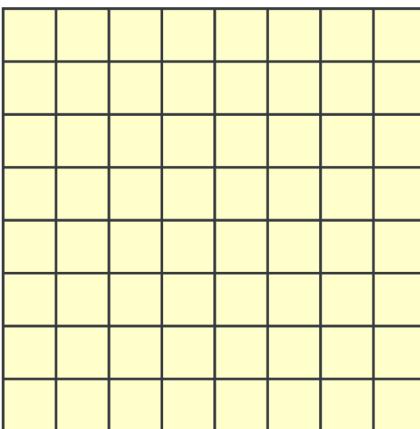
Source: *Sparsity in Deep Learning: Pruning and growth for efficient inference and training in neural networks*

Figure source: <https://htor.inf.ethz.ch/sparsity-in-dl/>

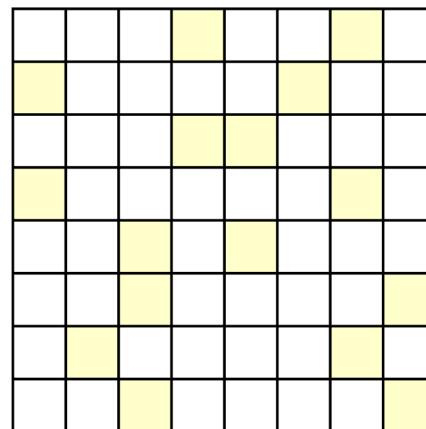
**10-90% sparsity across ML Models today**

# Sparsity Patterns

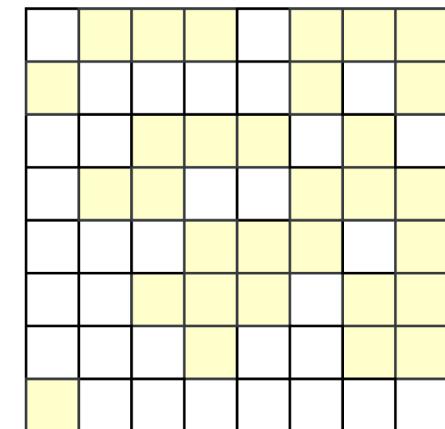
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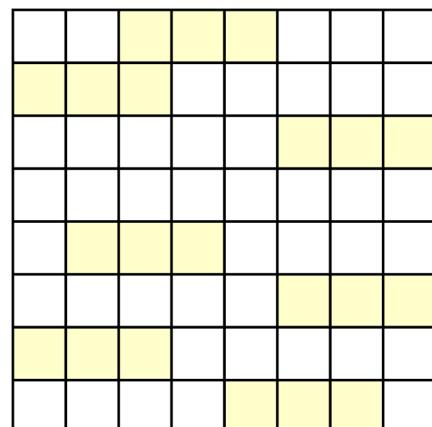
DENSE



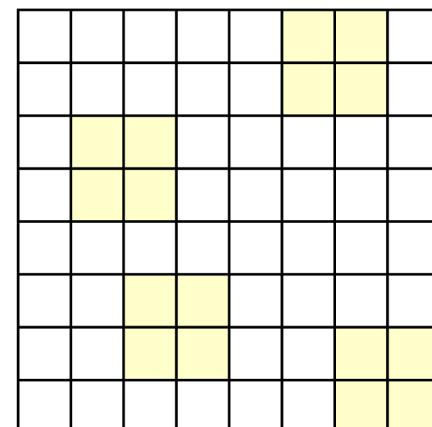
Block Balanced (Eg: N:M)



Unstructured

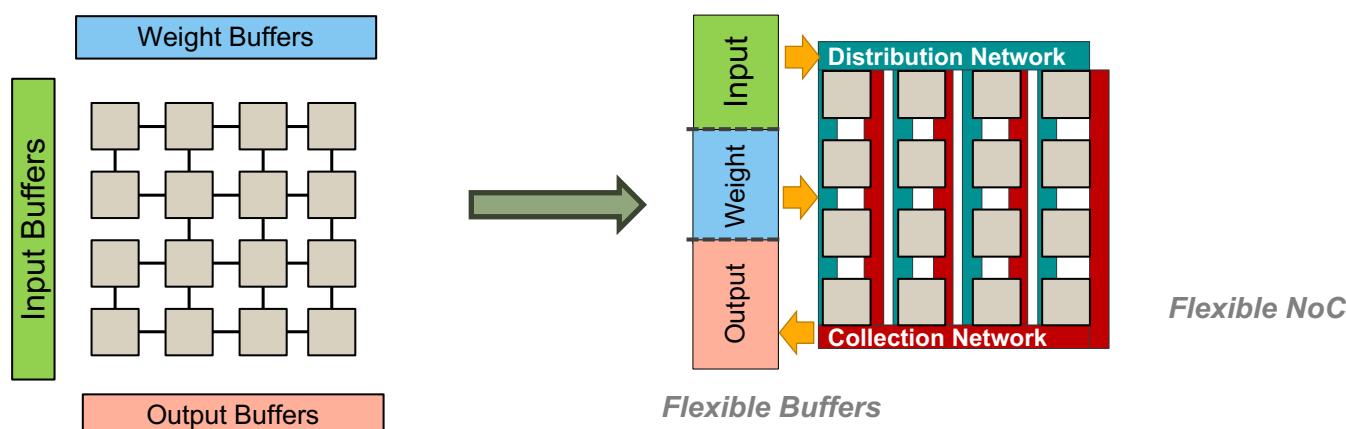
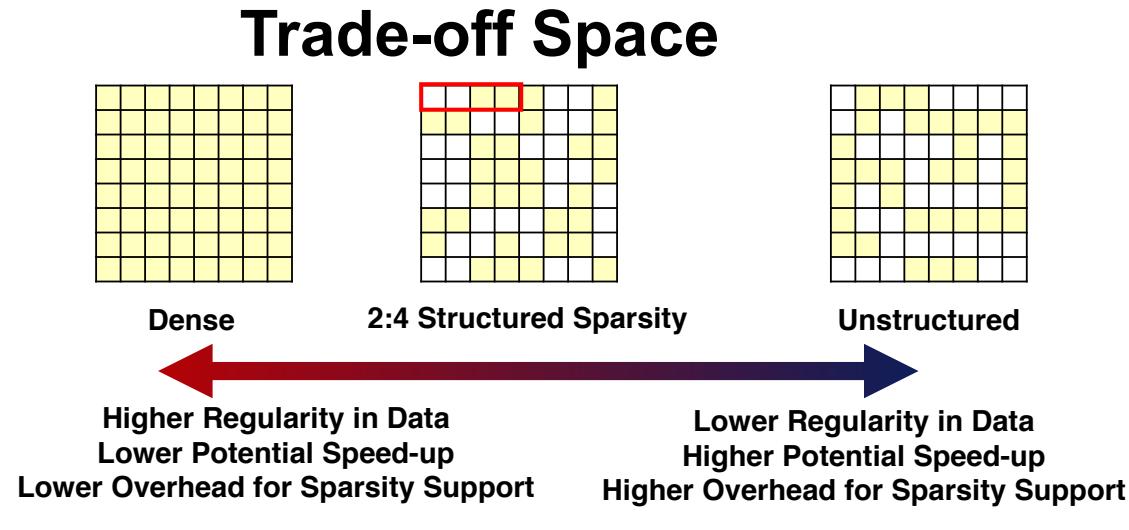


1D Blocks



2D Blocks

# Sparse Accelerators



# Sparse Dataflows

---

$$\begin{array}{c} A_{MK} \\ \hline \begin{array}{|c|c|c|c|} \hline & A_{01} & & \\ \hline A_{10} & & A_{12} & A_{13} \\ \hline \end{array} \end{array} \times \begin{array}{c} B_{KN} \\ \hline \begin{array}{|c|c|c|} \hline & B_{01} & B_{02} \\ \hline B_{10} & & B_{12} \\ \hline B_{20} & & \\ \hline B_{30} & B_{31} & B_{32} \\ \hline \end{array} \end{array} = \begin{array}{c} C_{MN} \\ \hline \begin{array}{|c|c|c|} \hline C_{00} & & C_{02} \\ \hline C_{10} & C_{11} & C_{12} \\ \hline \end{array} \end{array}$$

- Inner Product
- Outer Product
- Gustavson's

**Active area of research!**

*Thank you!*