

# Vector equation of line

$$\vec{r}(t) = \vec{r}_0 + t\vec{v}$$

↙ direction  
↘ initial position

12.5

- ③ Find vector & parametric equations of line through  $(2, 2.4, 3.5)$  and parallel to  $3\hat{i} + 2\hat{j} - \hat{k}$

$$\vec{r}_0 = \langle 2, 2.4, 3.5 \rangle$$

$$\vec{v} = \langle 3, 2, -1 \rangle$$

$$\vec{r}(t) = \langle 2, 2.4, 3.5 \rangle + t \langle 3, 2, -1 \rangle$$

$$= \langle \underbrace{2+3t}_x, \underbrace{2.4+2t}_y, \underbrace{3.5-t}_z \rangle$$

parametric:

$$x = 2 + 3t$$

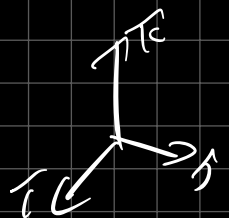
$$y = 2.4 + 2t$$

$$z = 3.5 - t$$

Symmetric:  $\frac{x-2}{3} = \frac{y-2.4}{2} = \frac{z-3.5}{-1}$

(10) line through  $(2, 1, 0)$   $\perp$  to  
 $\hat{i} + \hat{j}$  &  $\hat{j} + \hat{k}$ .

$$\vec{r}_0 = \langle 2, 1, 0 \rangle$$



$$\begin{aligned} \vec{v} &= (\hat{i} + \hat{j}) \times (\hat{j} + \hat{k}) = \hat{k} - \hat{j} + \hat{i} \\ &= \hat{i} - \hat{j} + \hat{k} \end{aligned}$$

$$\vec{r}(t) = \langle 2, 1, 0 \rangle + t \langle 1, -1, 1 \rangle = \langle 1, -1, 1 \rangle$$

$$= \langle 2+t, 1-t, t \rangle$$

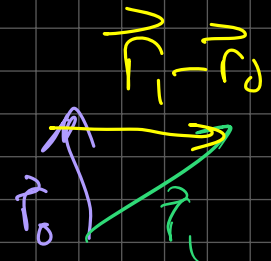
Q: if  $t$  is restricted, what happens?  
 $a \leq t \leq b \rightarrow$  segment.

(17)  $(6, -1, 9)$  ,  $(7, 6, 0)$

Find vector equation of line segment connecting these points.

$$\vec{r}_0 = \langle 6, -1, 9 \rangle$$

$$\vec{r}_1 = \langle 7, 6, 0 \rangle$$



$$\vec{r}(t) = \vec{r}_0 + t(\vec{r}_1 - \vec{r}_0)$$

$$\underline{\underline{0 \leq t \leq 1}}$$

$$= (1-t)\vec{r}_0 + t\vec{r}_1$$

$$= \langle 6, -1, 9 \rangle + t \langle 1, 7, -9 \rangle$$

$$= \langle 6+t, -1+7t, 9-9t \rangle \quad \text{subst.}$$

(24) Find equation of plane through  
 $(5, 3, 5)$  with normal vector  $2\hat{i} + \hat{j} - \hat{k}$

point  $(x_0, y_0, z_0) \rightarrow \vec{r}_0 = \langle x_0, y_0, z_0 \rangle$  end  
 on plane  
 $\vec{r} = \langle x, y, z \rangle$

$\vec{r} - \vec{r}_0$  vector in the plane

$\vec{n} = \langle a, b, c \rangle =$  normal vector

$$\vec{n} \cdot (\vec{r} - \vec{r}_0) = 0 \quad \text{Vector eqn of plane}$$

Scalar  
eqn

$$a(x - x_0) + b(y - y_0) + c(z - z_0) = 0$$

Standard:

$$ax + by + cz = d.$$

Point:  $(5, 3, 5)$

normal vector  $2\hat{i} + \hat{j} - \hat{k}$   
 $a=2, b=1, c=-1$

$$2(x-5) + 1(y-3) + (-1)(z-5) = 0$$

Standard form:

$$2x + y - z = 8$$

(3)  $\begin{pmatrix} (0, 1, 1) \\ (1, 0, 1) \\ (1, 1, 0) \end{pmatrix}$   $\vec{u}$

find plane containing  
these points

use  
Point

$$\vec{u} = \langle 1, -1, 0 \rangle$$

$$\vec{v} = \langle 1, 0, -1 \rangle$$

$$\vec{u} \times \vec{v} = \langle 1, 1, 1 \rangle$$

$$a=1 \\ b=1 \\ c=1$$

plane:

$$1(x-0) + 1(y-1) + 1(z-1) = 0$$

$$x + y - 1 + z - 1 = 0$$

$$x + y + z = 2$$

(40) plane passes through intersection of

$$x - z = 1$$

$$y + 2z = 3$$

$$z = x - 1$$
$$z = \frac{y - 3}{-2}$$

$$\perp \quad \begin{matrix} \nearrow \\ \nwarrow \end{matrix} \quad x + y - 2z = 1$$

• Investigate intersection

• find normal vector.  $\langle a, b, c \rangle = \langle 1, 1, -2 \rangle = 0$

let  $z = t \in \mathbb{R}$

$$x = 1 + t$$

$$y = 3 - 2t$$

line.  $\vec{r}(t) = \langle 1+t, 3-2t, t \rangle$

$t=0$  find  $(1, 3, 0)$

$t=1$  find  $(2, 1, 1)$

or any  $t$ .

only need 1 pt.

use  $(1, 3, 0)$

need our vector:  $\langle a, b, c \rangle = \langle 1, 1, -2 \rangle = 0$

$$a + b - 2c = 0$$

need more info!!

Try more later

Create discussion board on  
Brightspace.

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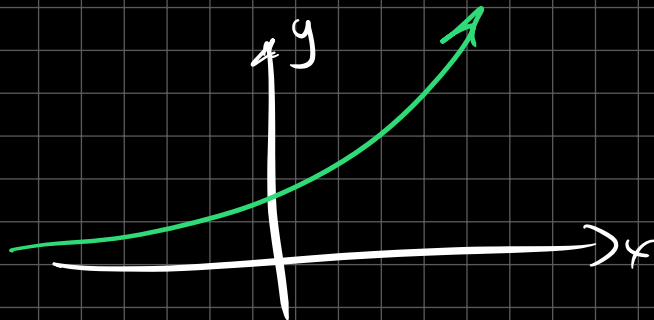
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②

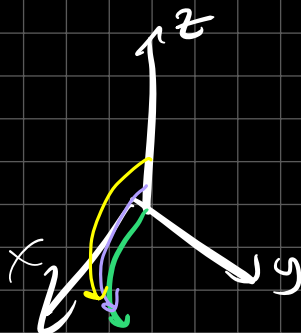
$$y = e^x$$

Sketch a graph.

$\mathbb{R}^2$



$\mathbb{R}^3$



(20)  $x = y^2 - z^2$

fix  $z$   
traces in  $z$ . (level curves)

$z=0$

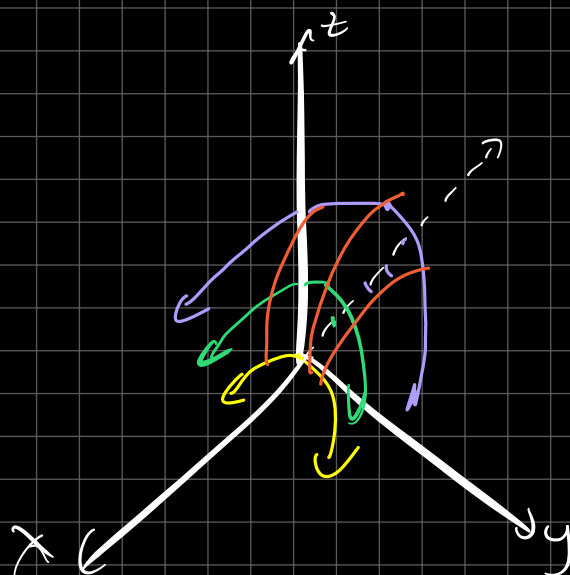
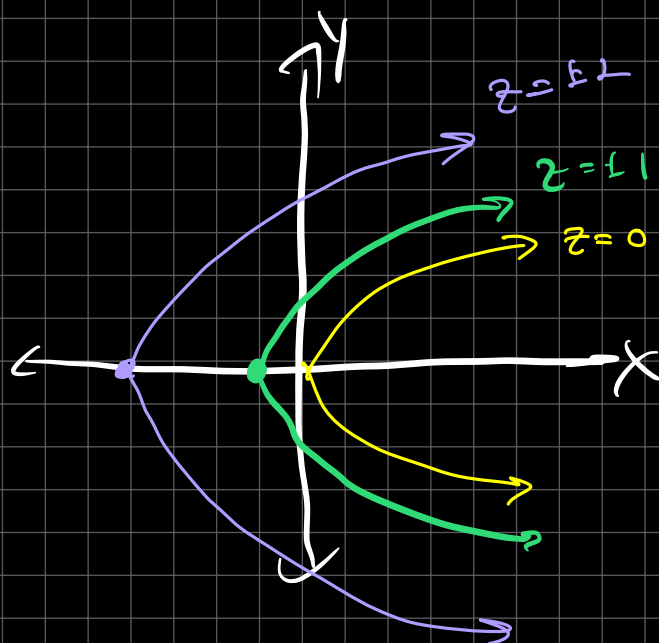
$x = y^2$

$z=\pm 1$

$x = y^2 - 1$

$z=\pm 2$

$x = y^2 - 4$



Traces in  $y$ .  $x = y^2 - z^2$

$y=0$

$x = -z^2$



$$y=1 \quad x=1-z^2$$

$$y=2 \quad x=4-z^2$$

