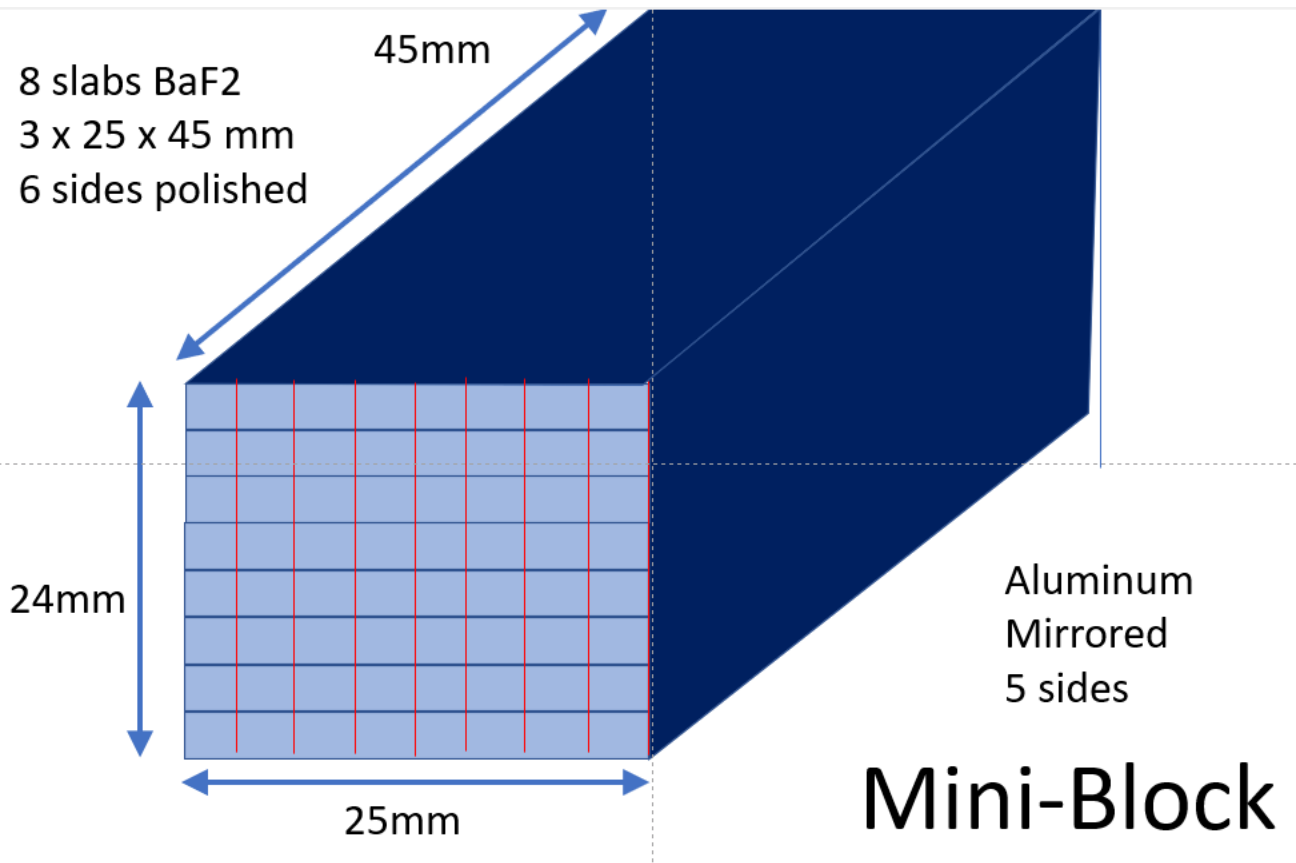


Specular Infinity Mirror Optics Model Validation Python/GitHub/Google Colab

Bill Worstell

PicoRad Imaging

10/10/2023



Isomorphism: There is a 1-to-1 map from a ray starting at a point within the miniblock then reflecting off mirrors (or by total internal reflection) -> a virtual ray traveling in a straight line through a double layer of 2D virtual lattices

$[x, y, z, t, \Theta, \Phi] \mid [dX, DX, dy, DY, dz, DZ, nx, ny, \eta x, \eta y] \rightarrow$ detected $[X, Y, T]$ and multiple reflection survival probability



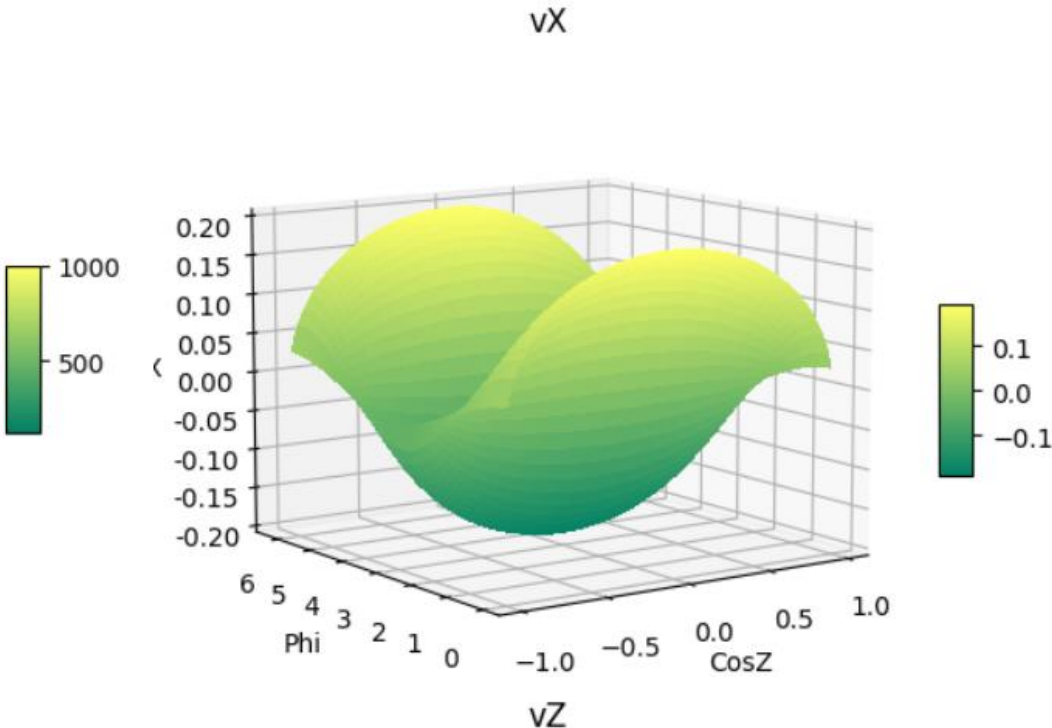
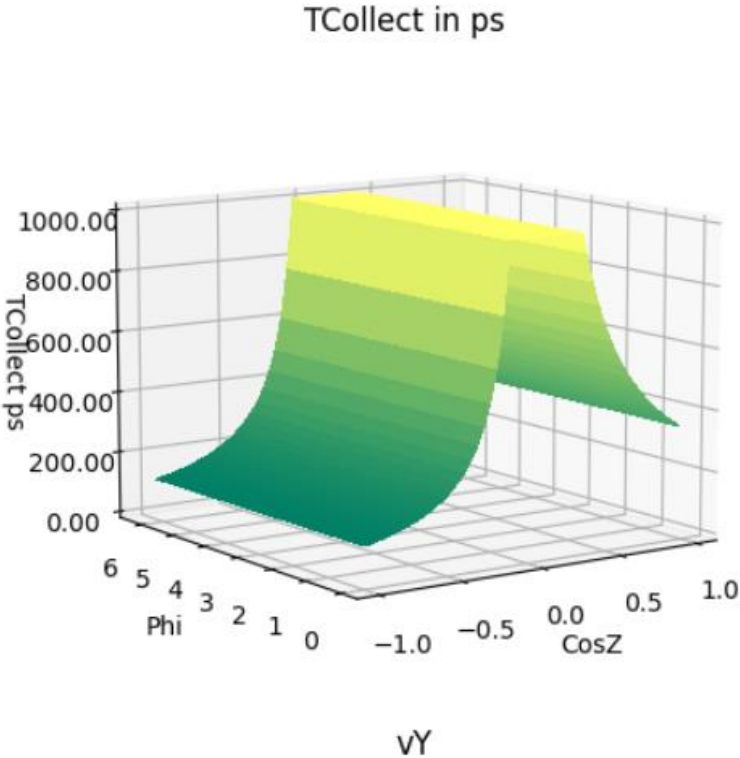
X-reflection: $[vx, vy, vz] \rightarrow [-vx, vy, vz]$

Y-reflection: $[vx, vy, vz] \rightarrow [vx, -vy, vz]$

Z-reflection: $[vx, vy, vz] \rightarrow [vx, vy, -vz]$

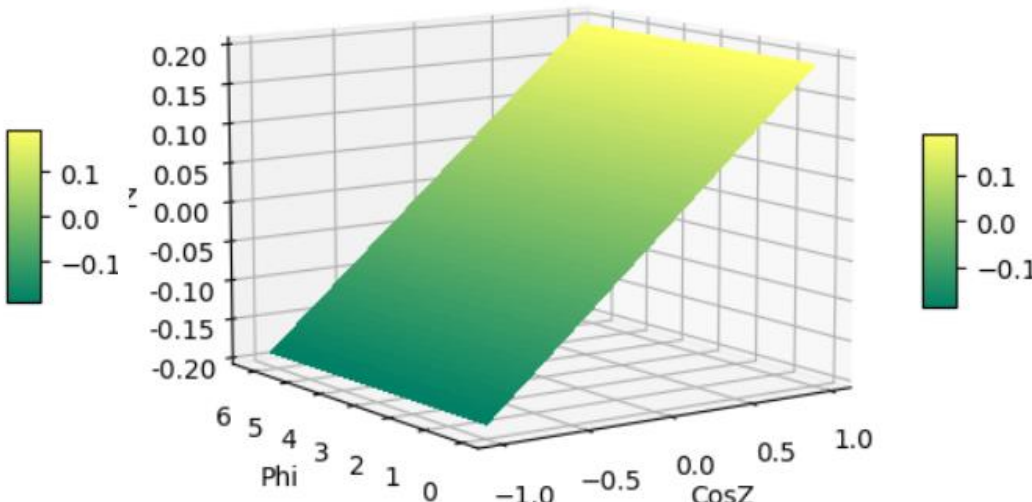
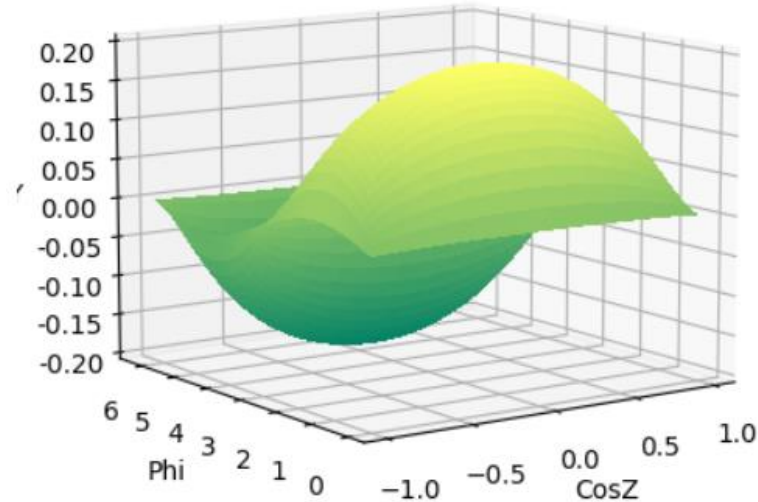
2-D Infinite Mirror at each pixel, and for Miniblock

$[\Theta, \Phi, n] \rightarrow [vX, vY, vZ]$



https://colab.research.google.com/github/BillWorstell/BaF2_LAPPD/blob/main/SimpleOpticsPhotons.ipynb

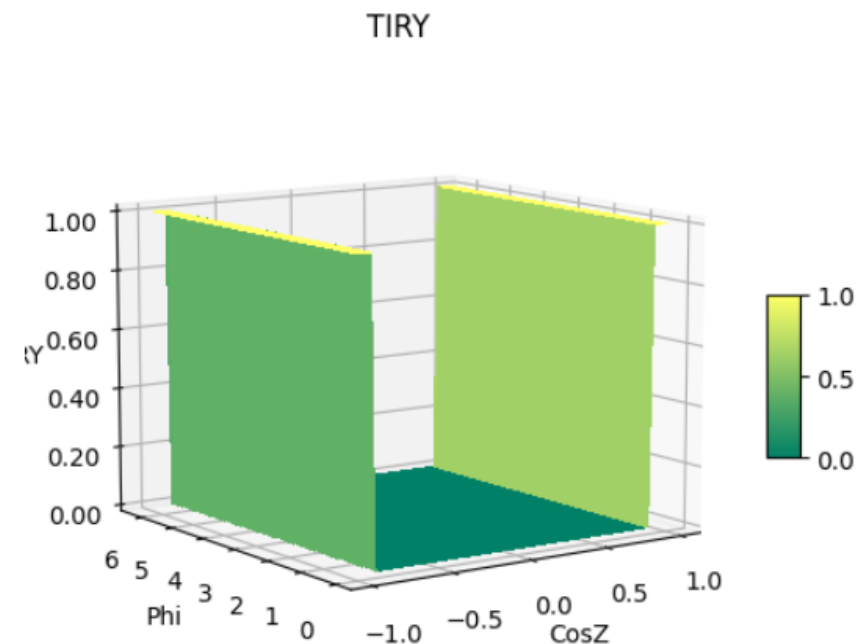
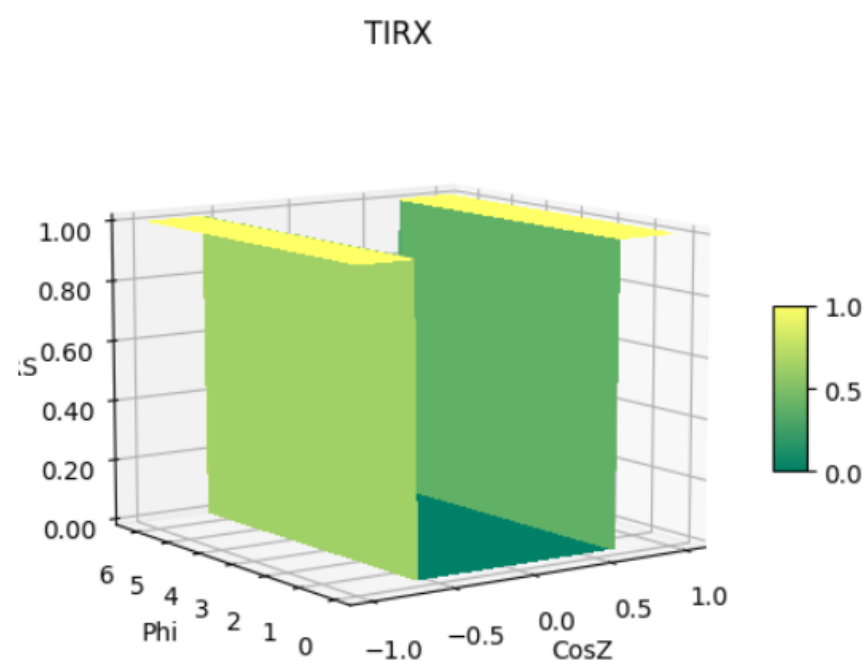
$[z, t, vZ] | [DZ] \rightarrow [T]$



```

# Index of refraction for
optical barriers
# (Air and LIOB=Laser
Induced Optical Barrier)
IndexX=1.0
IndexY=1.40
# Index of refraction for
fast and slow component
IndexFastBaF2=1.55
IndexSlowBaF2=1.50
# Reflectivity of mirrored
surfaces
ReflectX=0.90
ReflectY=0.90
ReflectZ=0.90

```



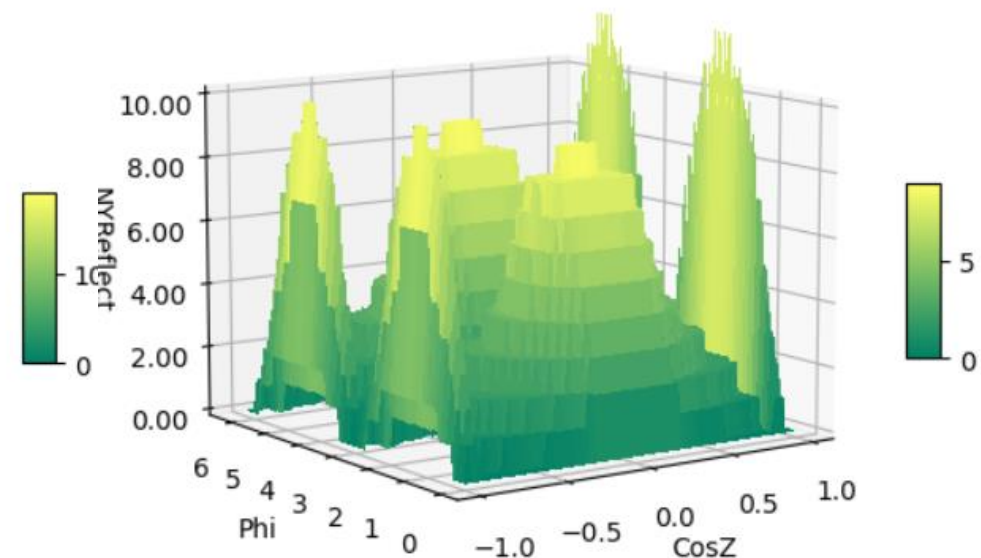
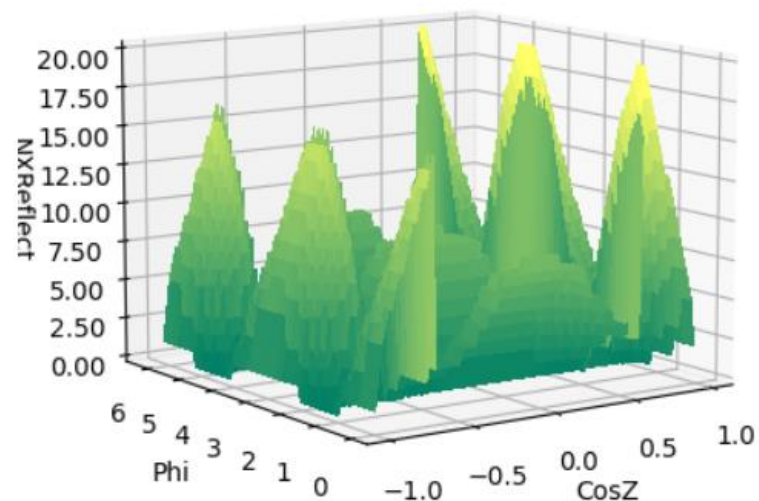
NXReflect X= 1.5 Y=1.0 Z=17.5 DZ=45.0

NYReflect X= 1.5 Y=1.0 Z=17.5 DZ=45.0

```

#Constant Geometry
Parameters
DZ = 45. #mm
DetectNX = 8
dX = 3.0 #mm
DX = DetectNX * dX
DetectNY = 12;
dY = 2.0; #mm
DY = DetectNY * dY

```

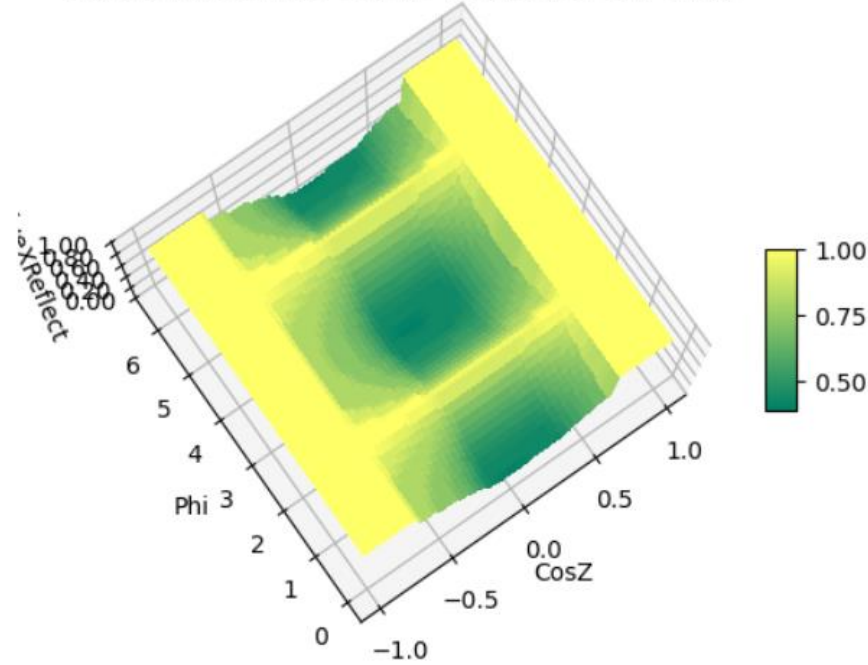


$[x, y, z, t, \Theta, \Phi]$
 $[dX, DX, dy, DY, dz, DZ,$
 $nx, ny, \eta x, \eta y]$ ->
collected T and
multiple reflection
survival probability

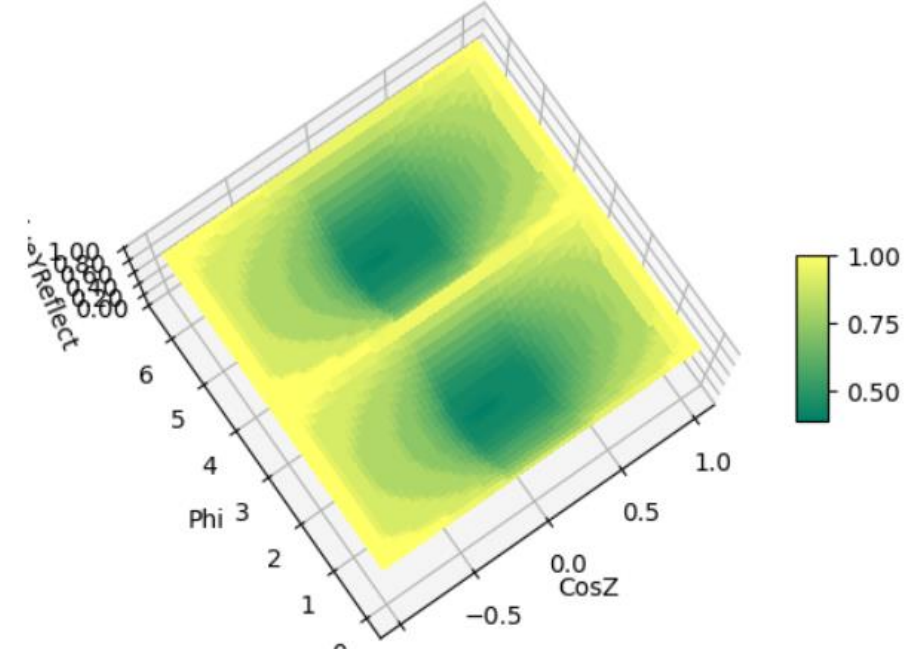
TCollect to be later convolved
with emission time
distribution and detector
timing jitter distribution
when randomly sampling
(fast parallel in PyTorch)

SimpleOpticsPhotons.ipynb

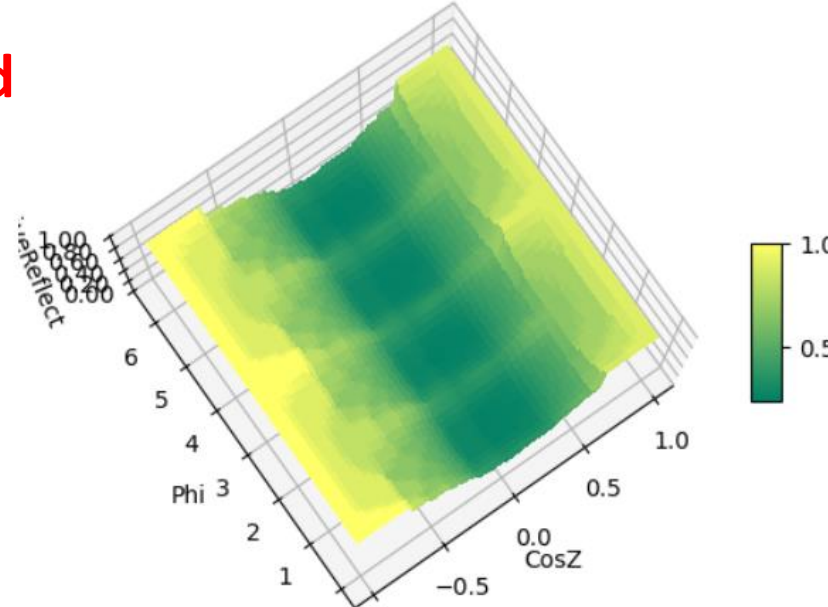
SurviveXReflect X= 1.5 Y=5.0 Z=7.5 DZ=45.0



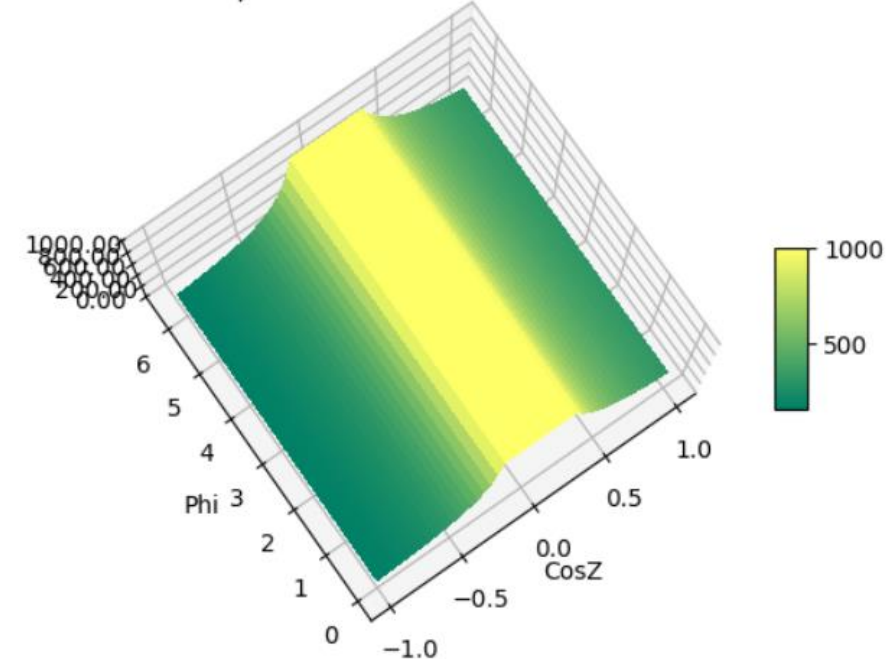
SurviveYReflect X= 1.5 Y=5.0 Z=7.5 DZ=45.0



SurviveReflect X= 1.5 Y=5.0 Z=7.5 DZ=45.0



TCollect ps X= 1.5 Y=5.0 Z=7.5 DZ=45.0

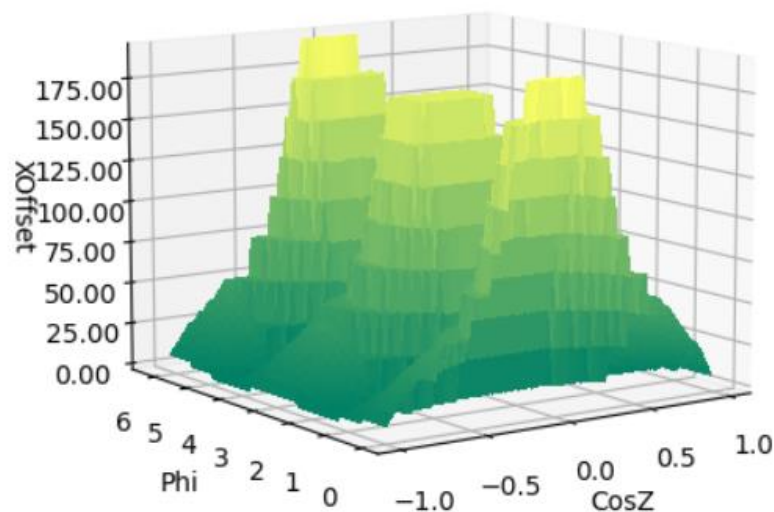


$[x, y, z, t, \Theta, \Phi]$
| $[dX, DX, dy, DY, dz,$
 $DZ, nx, ny, \eta x, \eta y]$ -
> detected $[X, Y]$

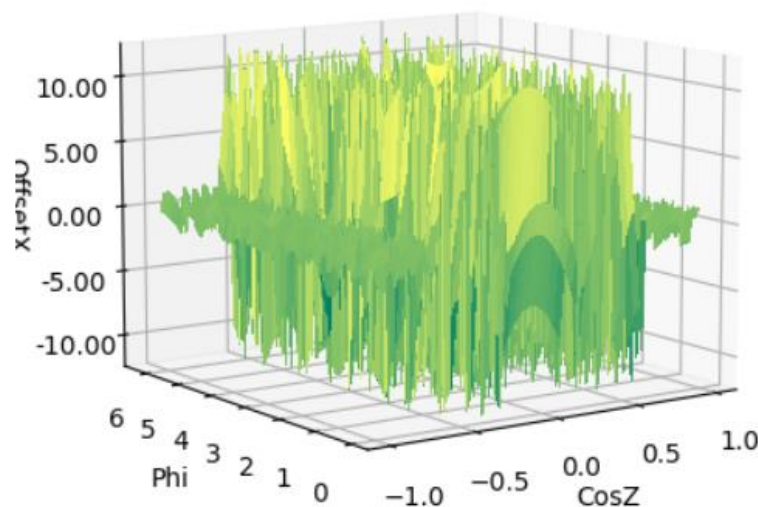
Find detection point
in virtual detector
within a reflected
virtual unit cell, then
map back onto real
detection point
within a real unit cell

Size of unit cell
depends on total
internal reflect or not

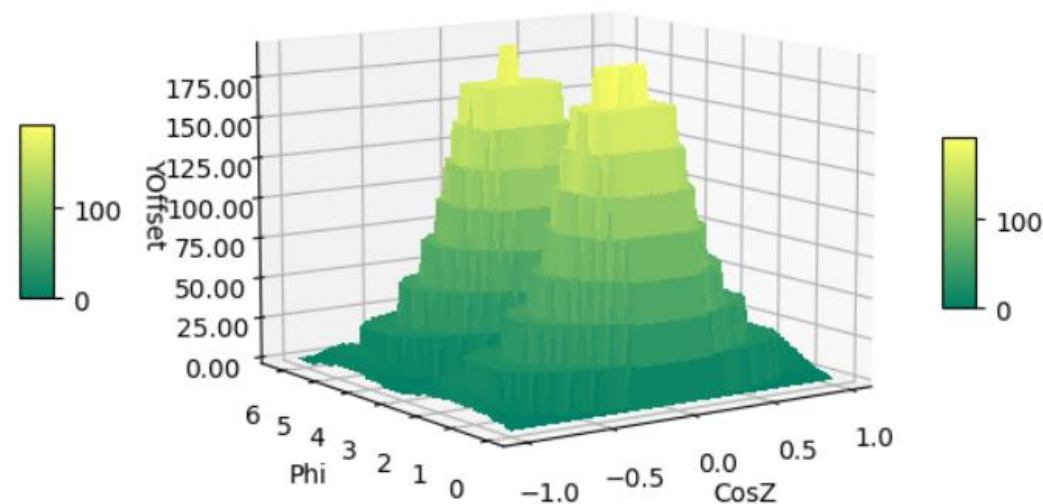
XOffset X= 1.5 Y=1.0 Z=17.5 DZ=45.0



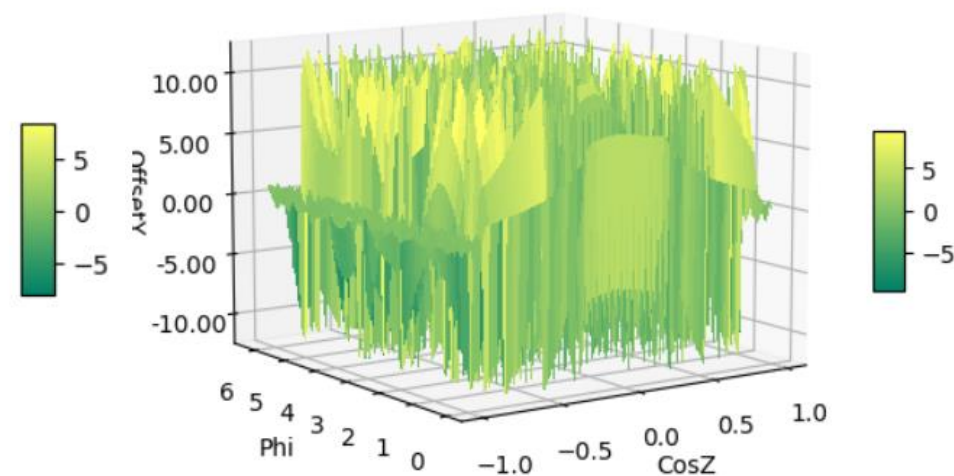
OffsetX X= 1.5 Y=1.0 Z=17.5 DZ=45.0



YOffset X= 1.5 Y=1.0 Z=17.5 DZ=45.0



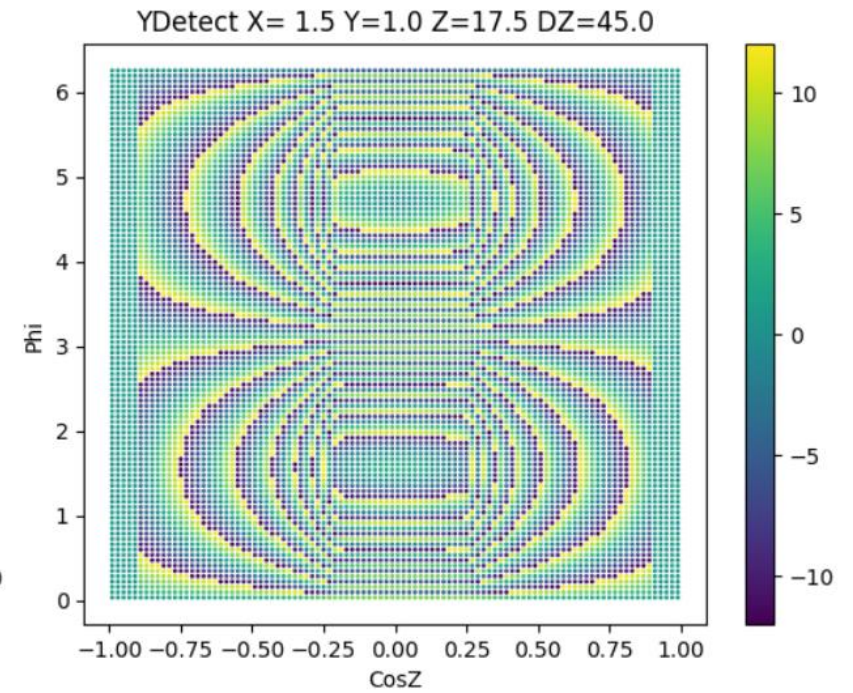
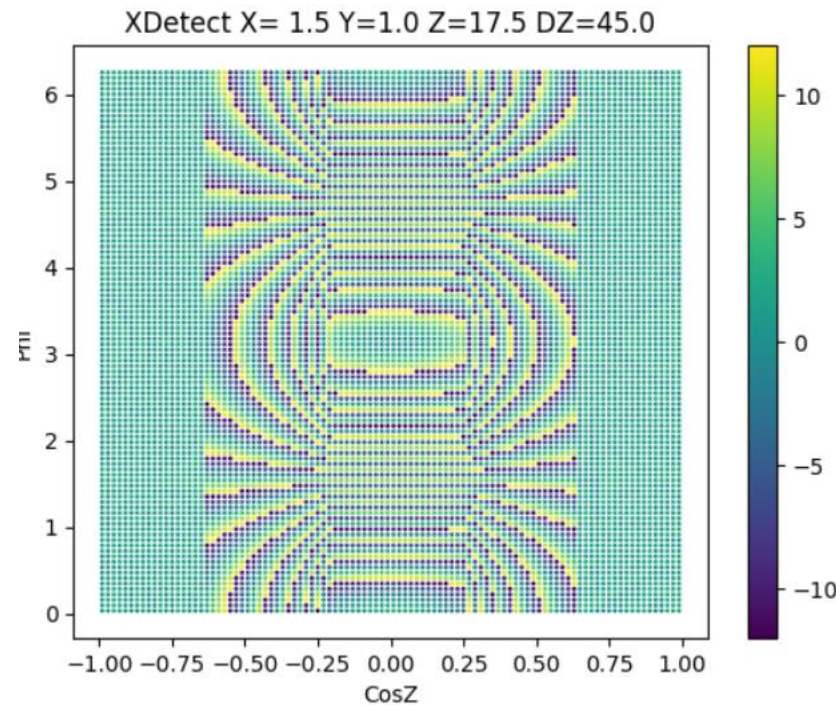
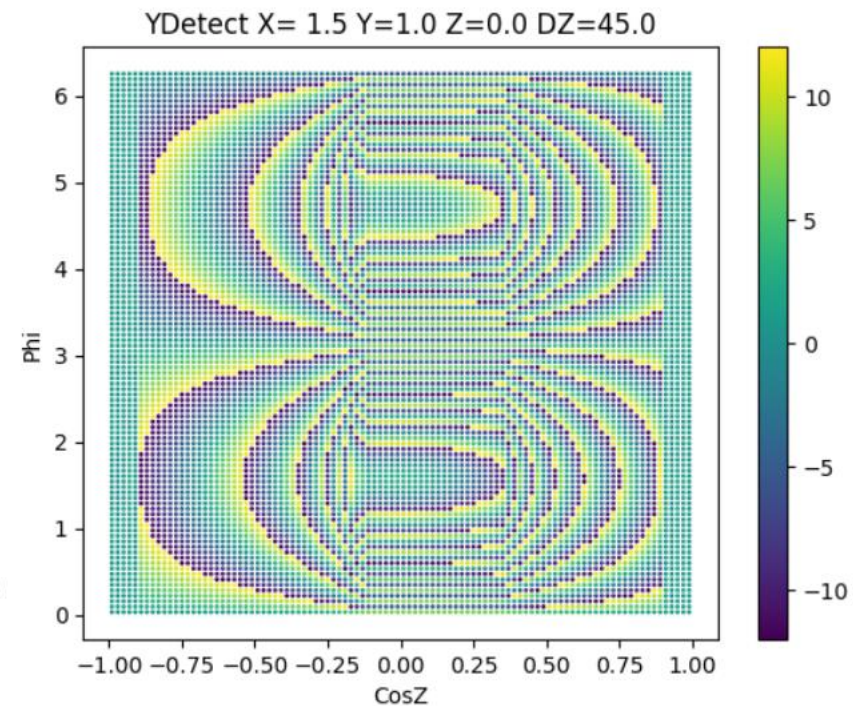
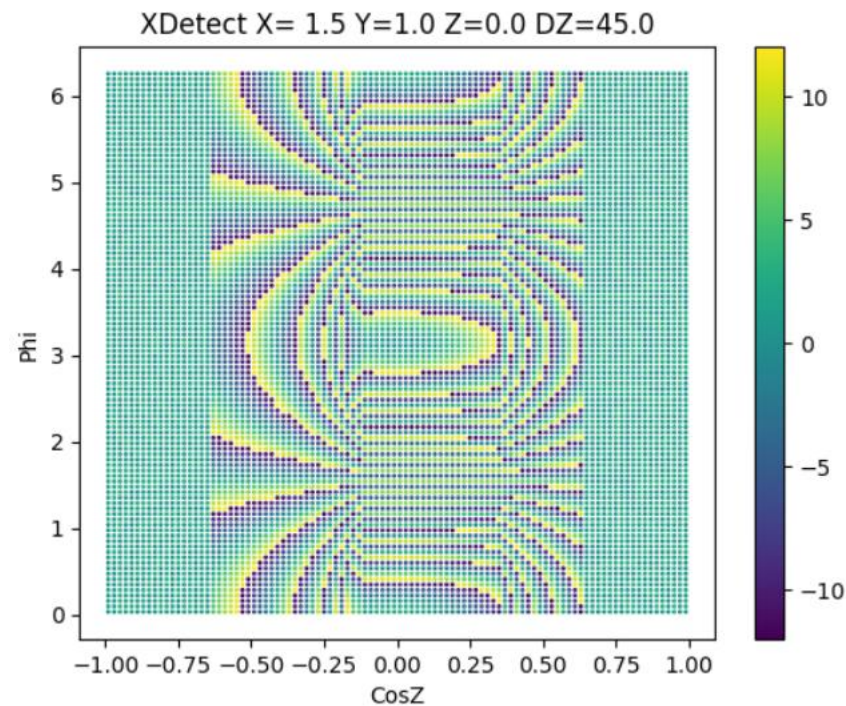
OffsetY X= 1.5 Y=1.0 Z=17.5 DZ=45.0



$[x, y, z, \Theta, \Phi] \rightarrow [dX, DX, dy, DY, dz, DZ, nx, ny, \eta x, \eta y] \rightarrow$
detected $[X, Y]$

Find detection point
in virtual detector
within a reflected
virtual unit cell, then
map back onto real
detection point
within a real unit cell

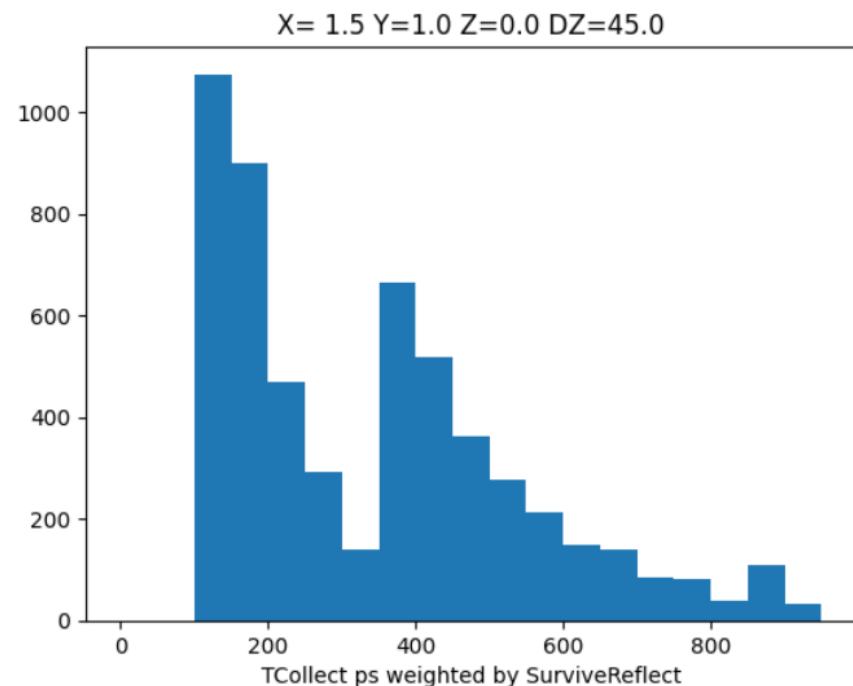
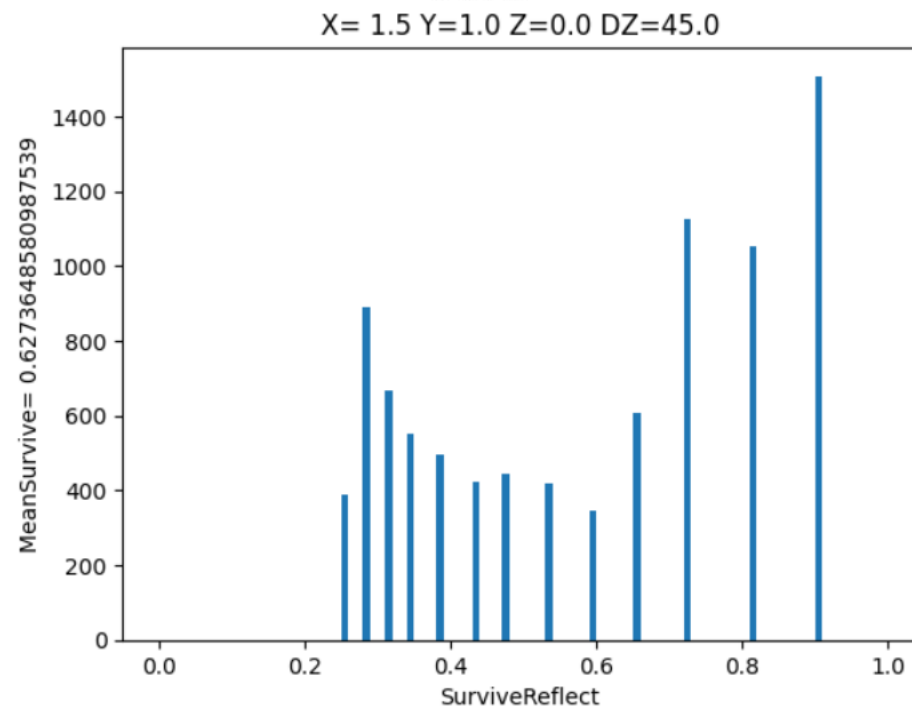
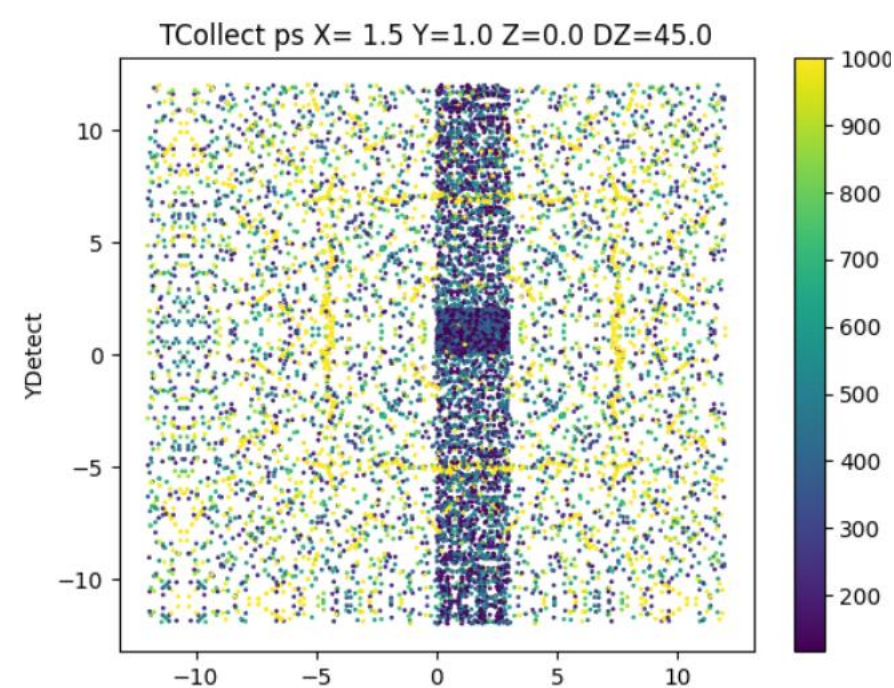
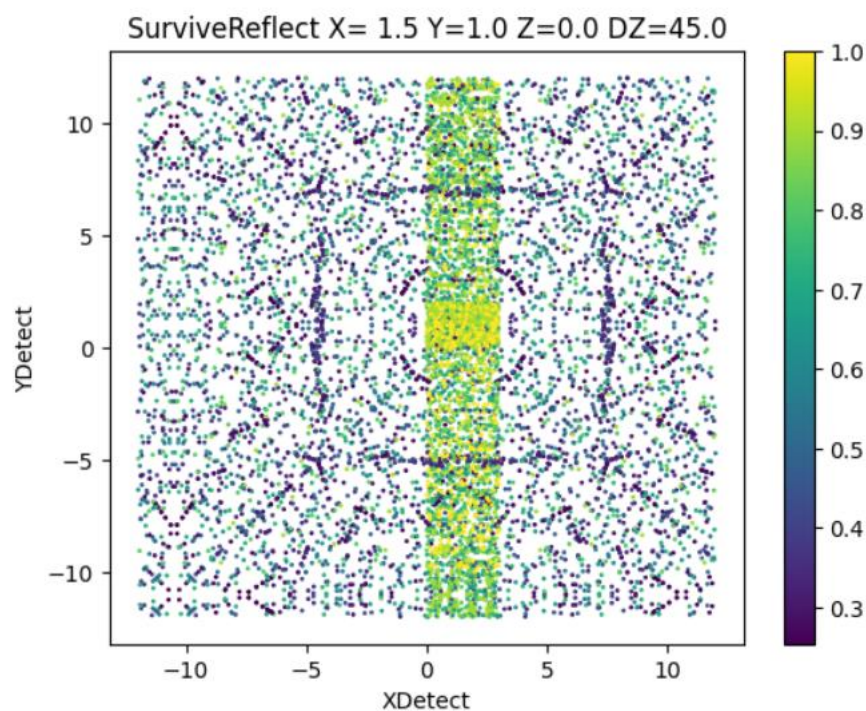
Size of unit cell
depends on total
internal reflect or not



$[x,y,z,t,\Theta,\Phi]$
 $[dX,DX,dy,DY,dz,DZ,$
 $nx,ny,\eta x,\eta y]$ ->
 collected T and
 multiple reflection
 survival probability

$[X,Y]$ distribution
 encodes $[x,y]$

T distribution
 encodes t and Z



Z Scan:

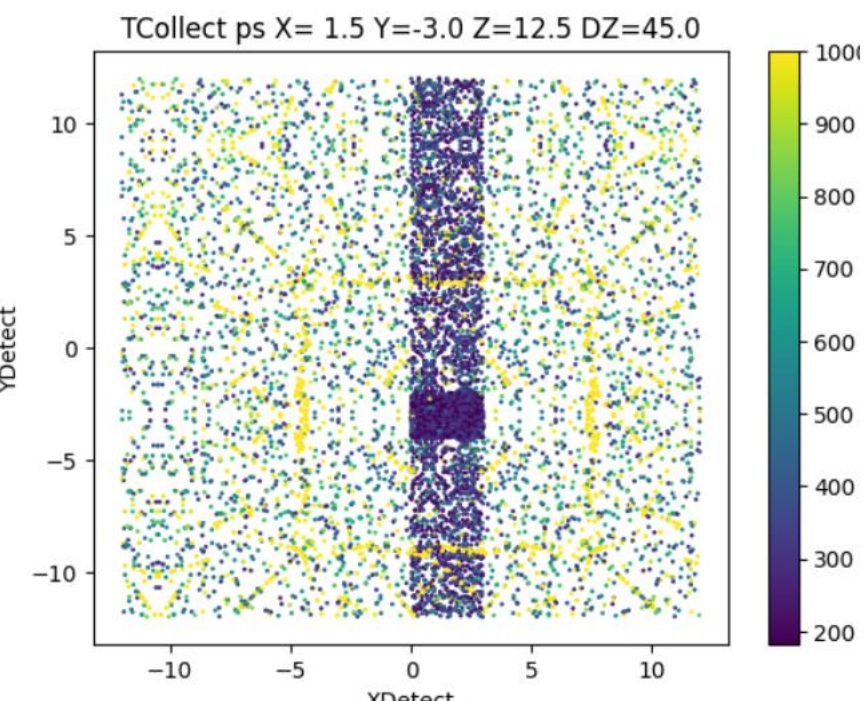
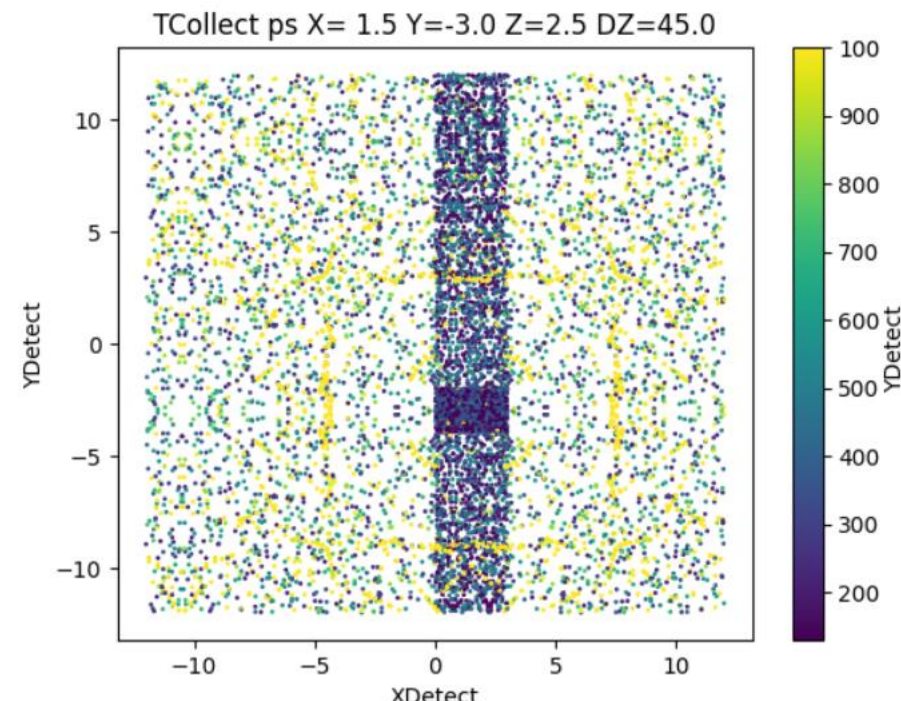
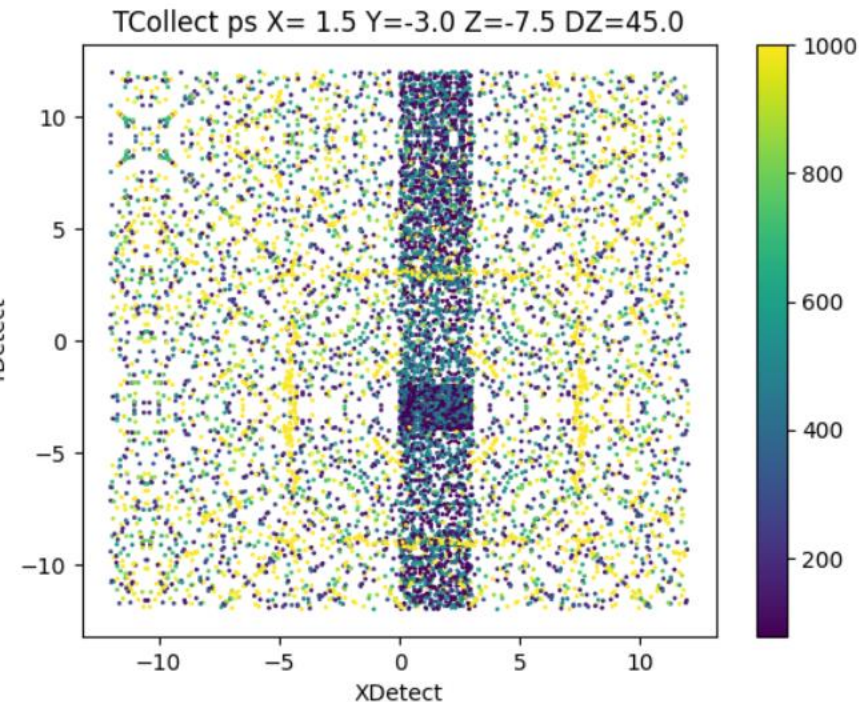
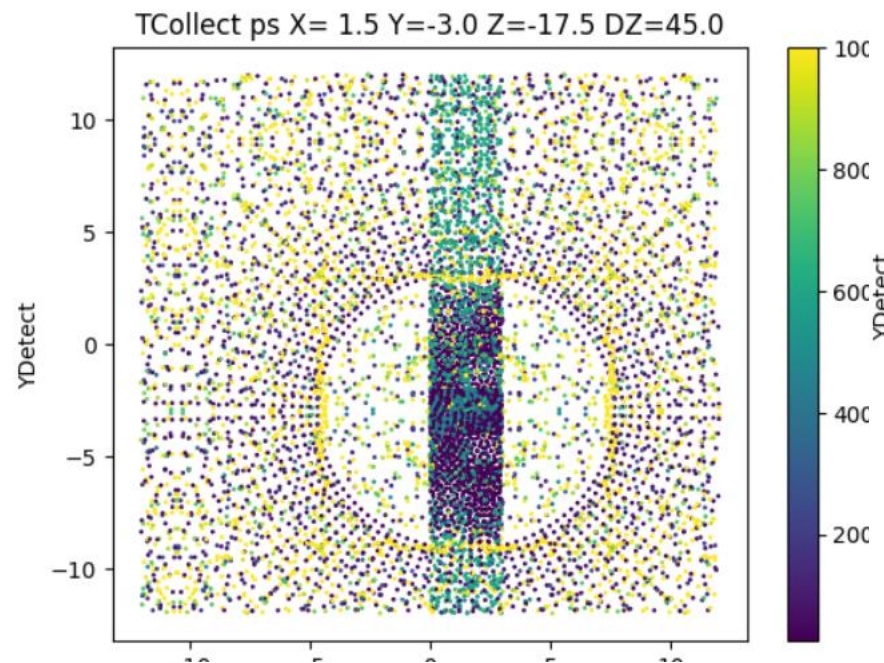
X=1.5

Y=3.0

Z=[-12.5, -7.5, 2.5, 12.5]

**[X,Y] distribution
encodes [x,y]**

**[X,Y] distribution
independent of Z
except very near
low-Z end near
photodetectors
(fewest events)**



z Scan:

x=1.5

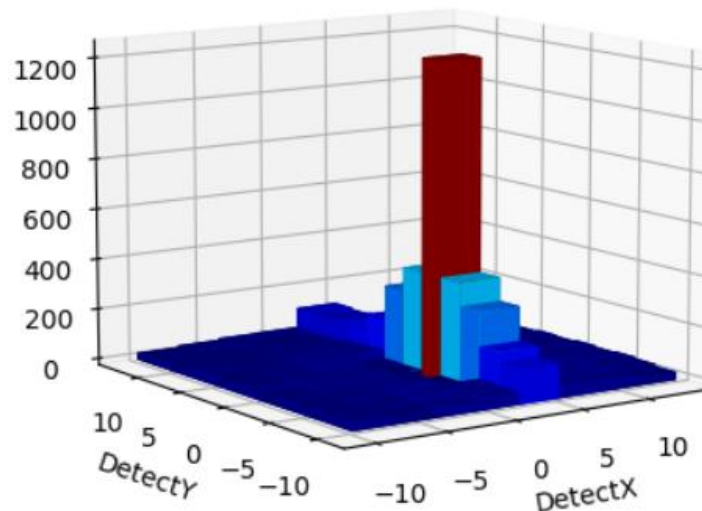
y=3.0

z=[-12.5, -7.5, 2.5, 12.5]

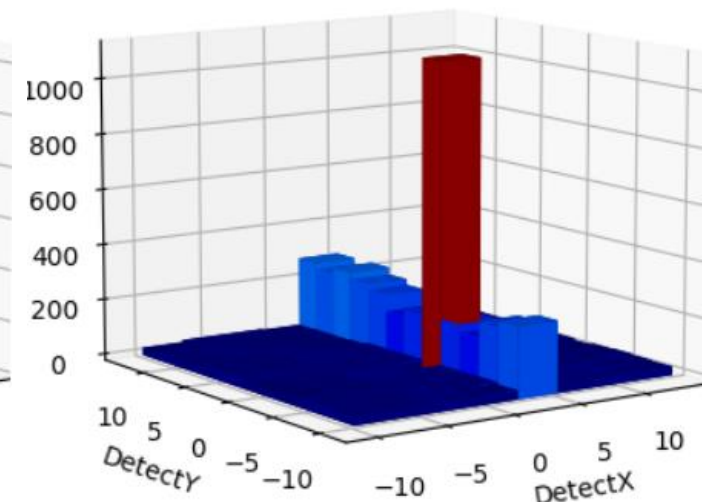
**[X,Y] distribution
encodes [x,y]**

**[X,Y] distribution
independent of Z
except very near
low-Z end near
Photodetectors
(fewest events)**

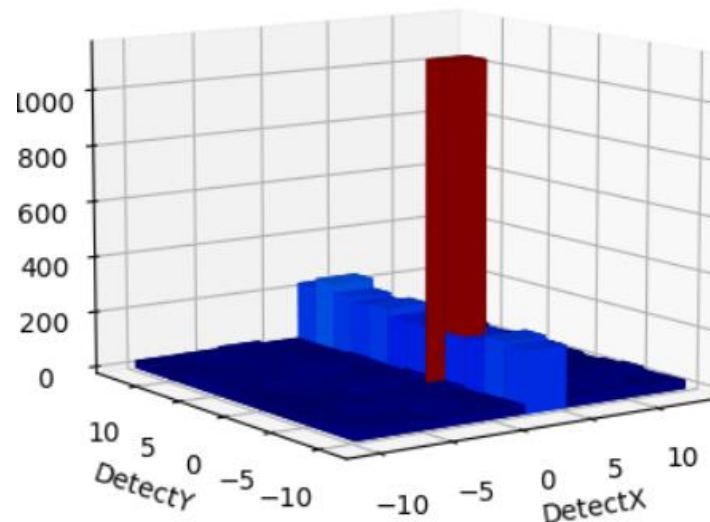
X= 1.5 Y=-3.0 Z=-17.5 DZ=45.0



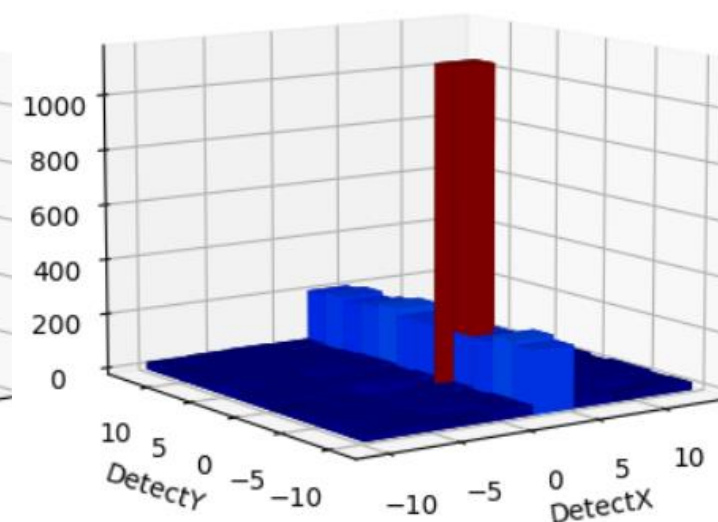
X= 1.5 Y=-3.0 Z=-7.5 DZ=45.0



X= 1.5 Y=-3.0 Z=2.5 DZ=45.0



X= 1.5 Y=-3.0 Z=12.5 DZ=45.0



z Scan:

x=1.5

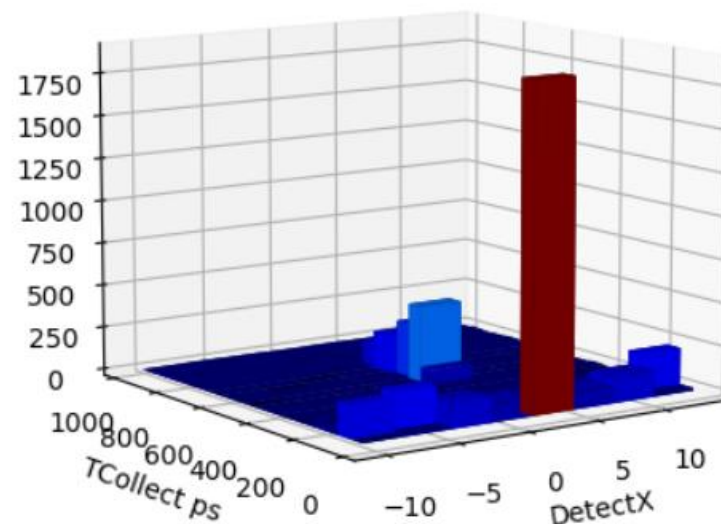
y=3.0

z=[-12.5, -7.5, 2.5, 12.5]

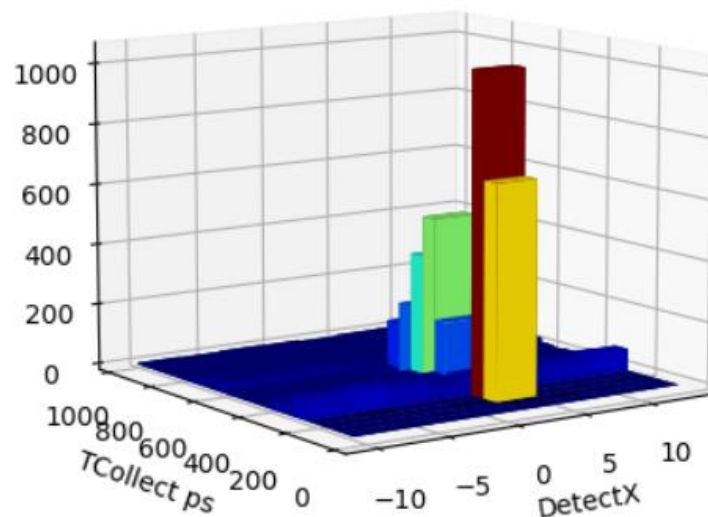
**[T] distribution
encodes [z,t]**

**[T] distribution at peak
[X,Y] shows two peaks
which move as a
function of z,
where the lower peak
+ z encodes t, while the
separation between
the peaks encodes z**

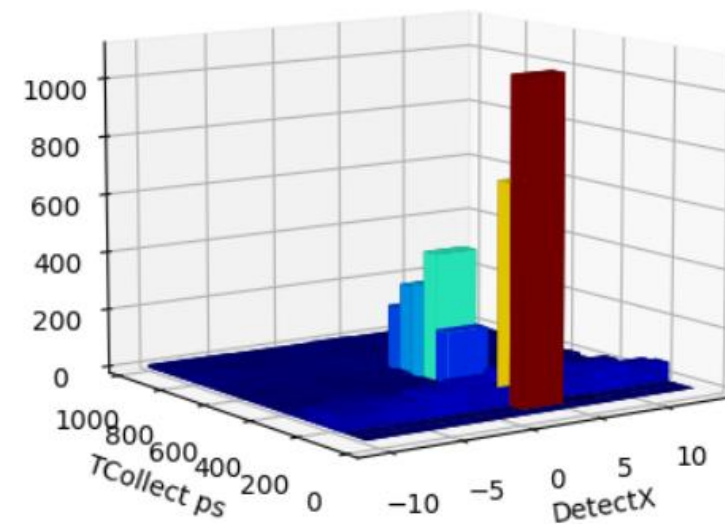
X= 1.5 Y=-3.0 Z=-17.5 DZ=45.0



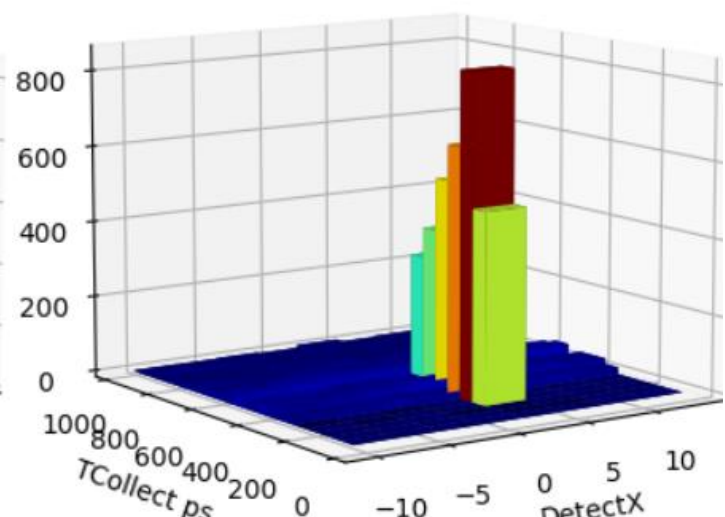
X= 1.5 Y=-3.0 Z=2.5 DZ=45.0



X= 1.5 Y=-3.0 Z=-7.5 DZ=45.0



X= 1.5 Y=-3.0 Z=12.5 DZ=45.0



z Scan:

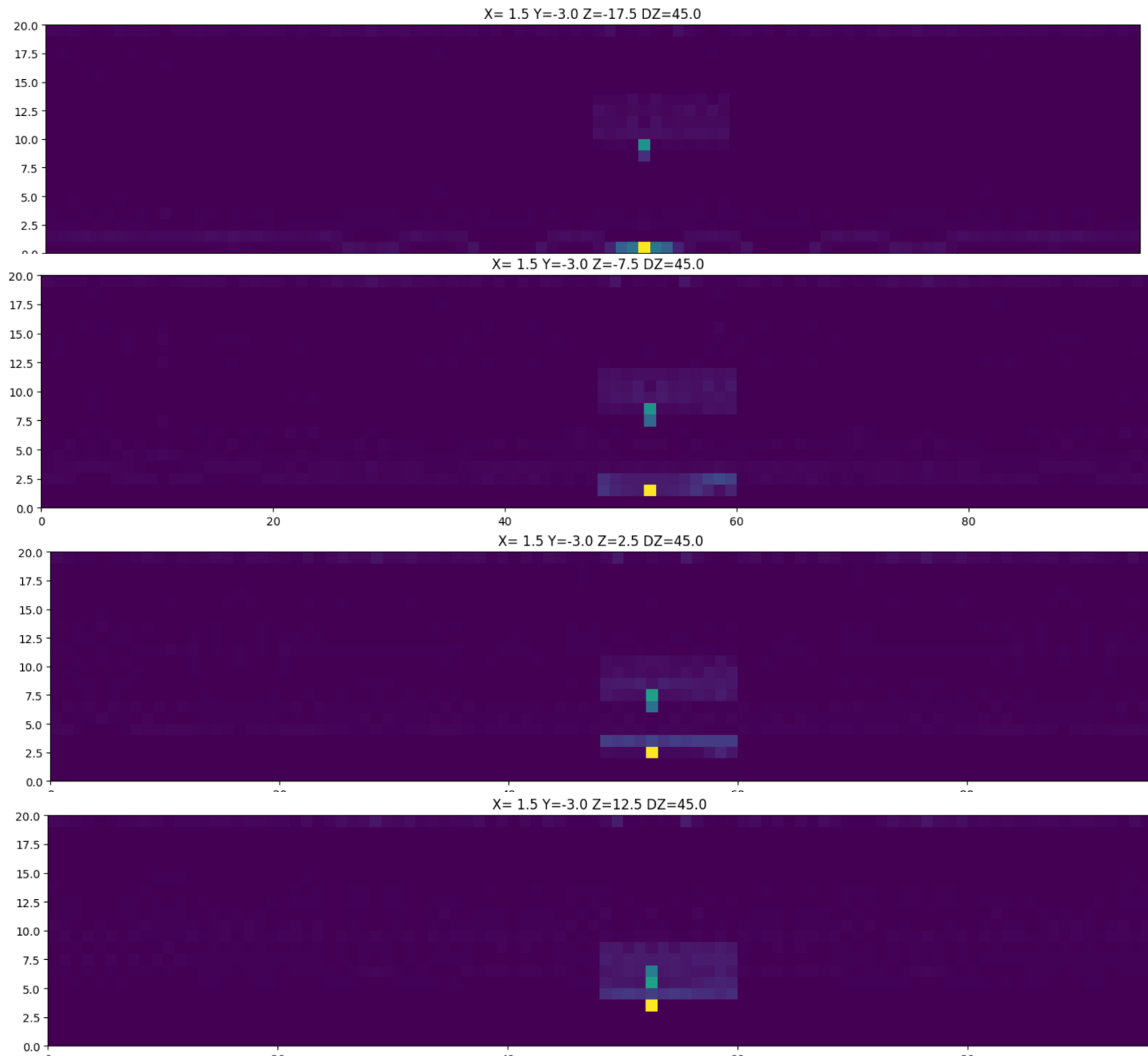
x=1.5

y=3.0

z=[-12.5, -7.5, 2.5, 12.5]

**[T] distribution
encodes [z,t]**

**[T] distribution at peak
[X,Y] shows two peaks
which move as a
function of z,
where the lower peak
+ z encodes t, while the
separation between
the peaks encodes z**



x Scan:

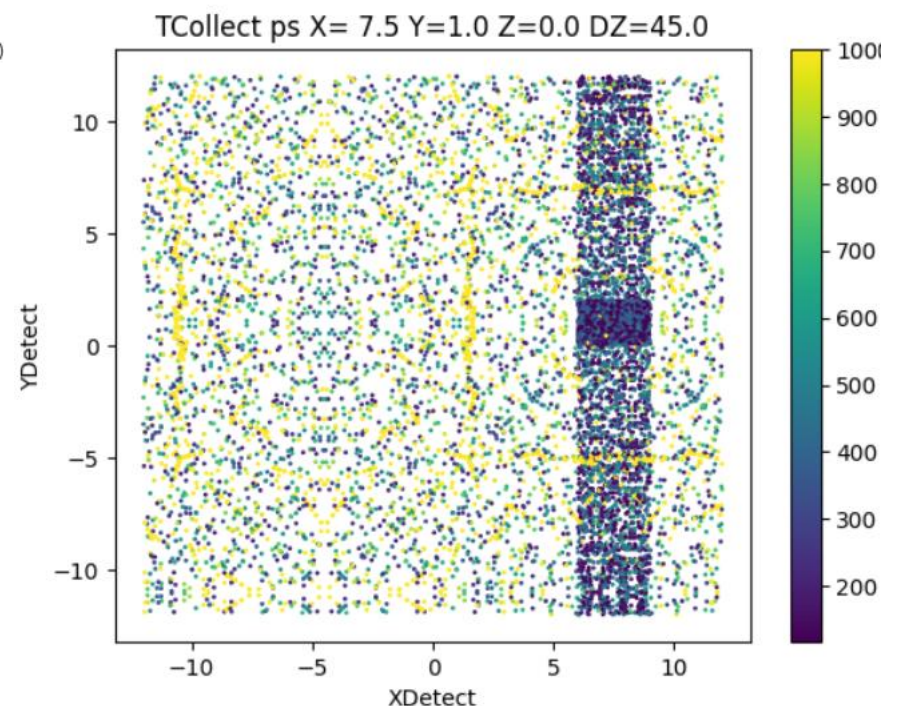
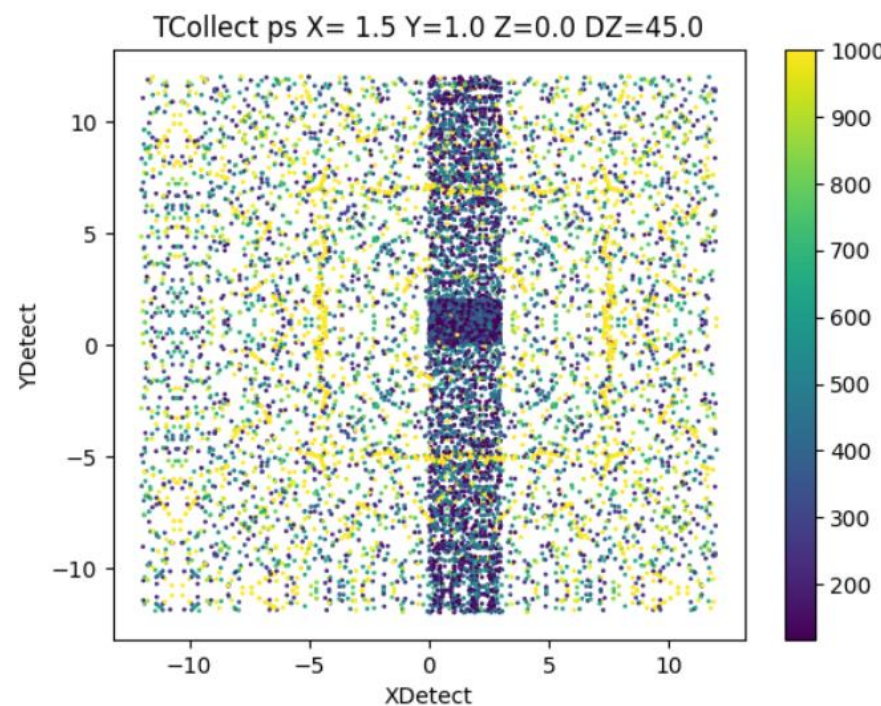
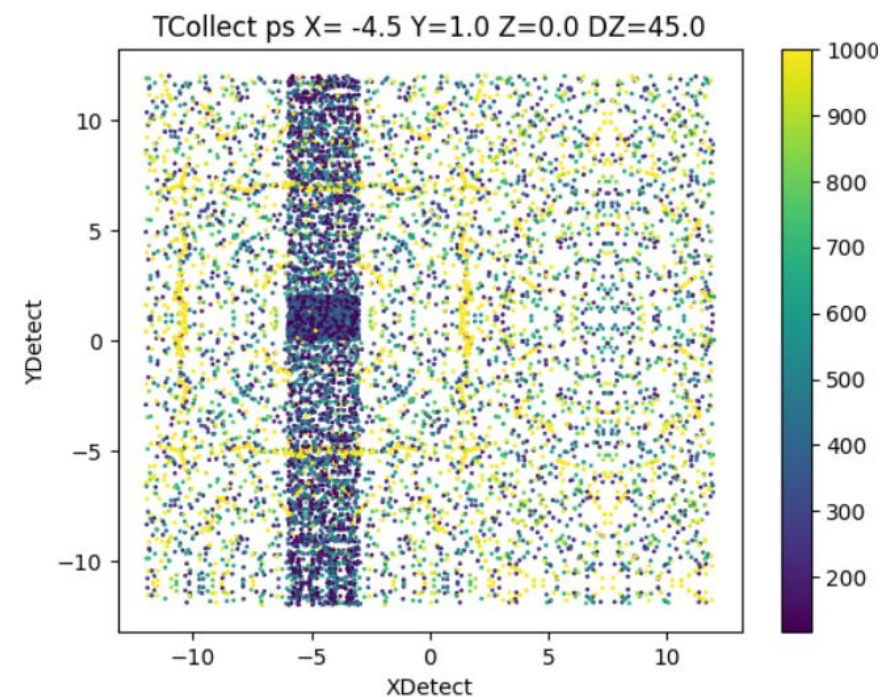
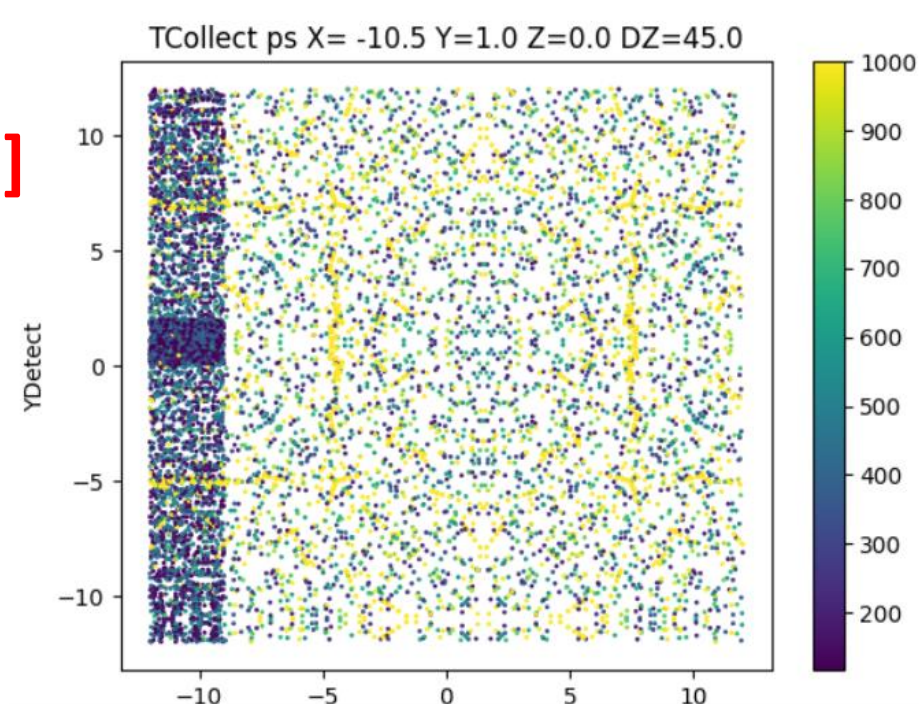
$x = [-10.5, -4.5, 1.5, 7.5]$

$y = 3.0$

$z = 0.$

**[X,Y] distribution
encodes [x,y]**

**[X,Y] distribution
similar in Y but
shifted in X
according to x**



x Scan:

$x = [-10.5, -4.5, 1.5, 7.5]$

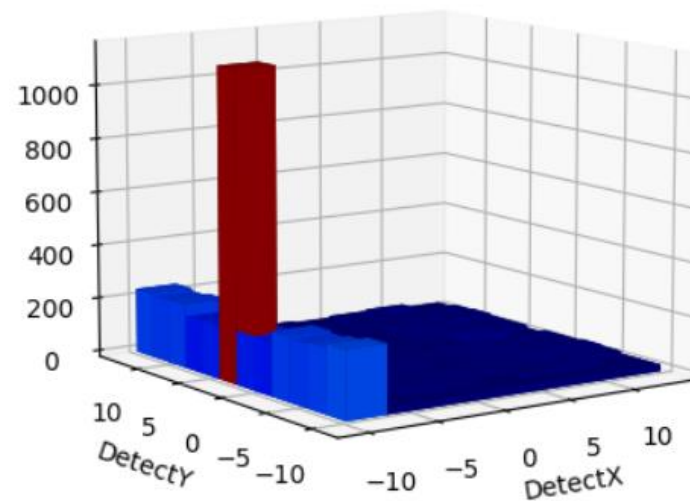
$y = 3.0$

$z = 0.0$

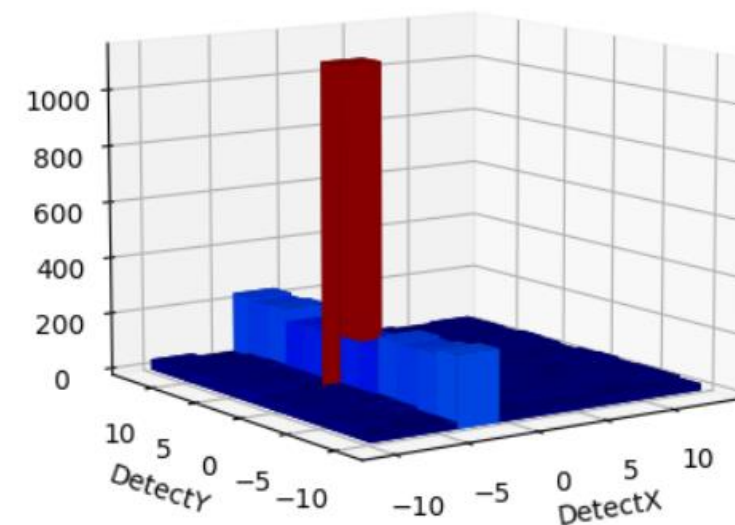
**[X,Y] distribution
encodes [x,y]**

**[X,Y] distribution
similar in Y but
shifted in X
according to x**

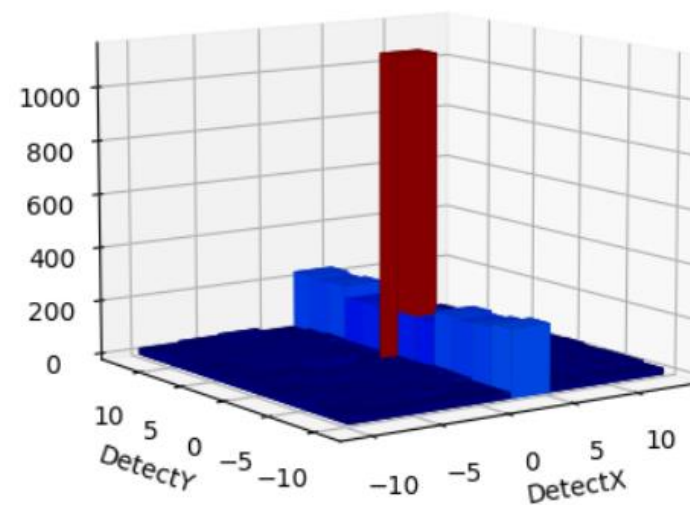
X= -10.5 Y=1.0 Z=0.0 DZ=45.0



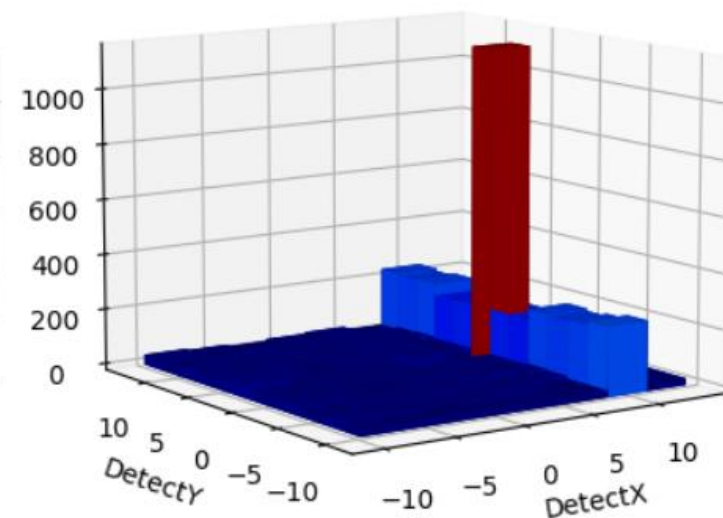
X= -4.5 Y=1.0 Z=0.0 DZ=45.0



X= 1.5 Y=1.0 Z=0.0 DZ=45.0



X= 7.5 Y=1.0 Z=0.0 DZ=45.0



x Scan:

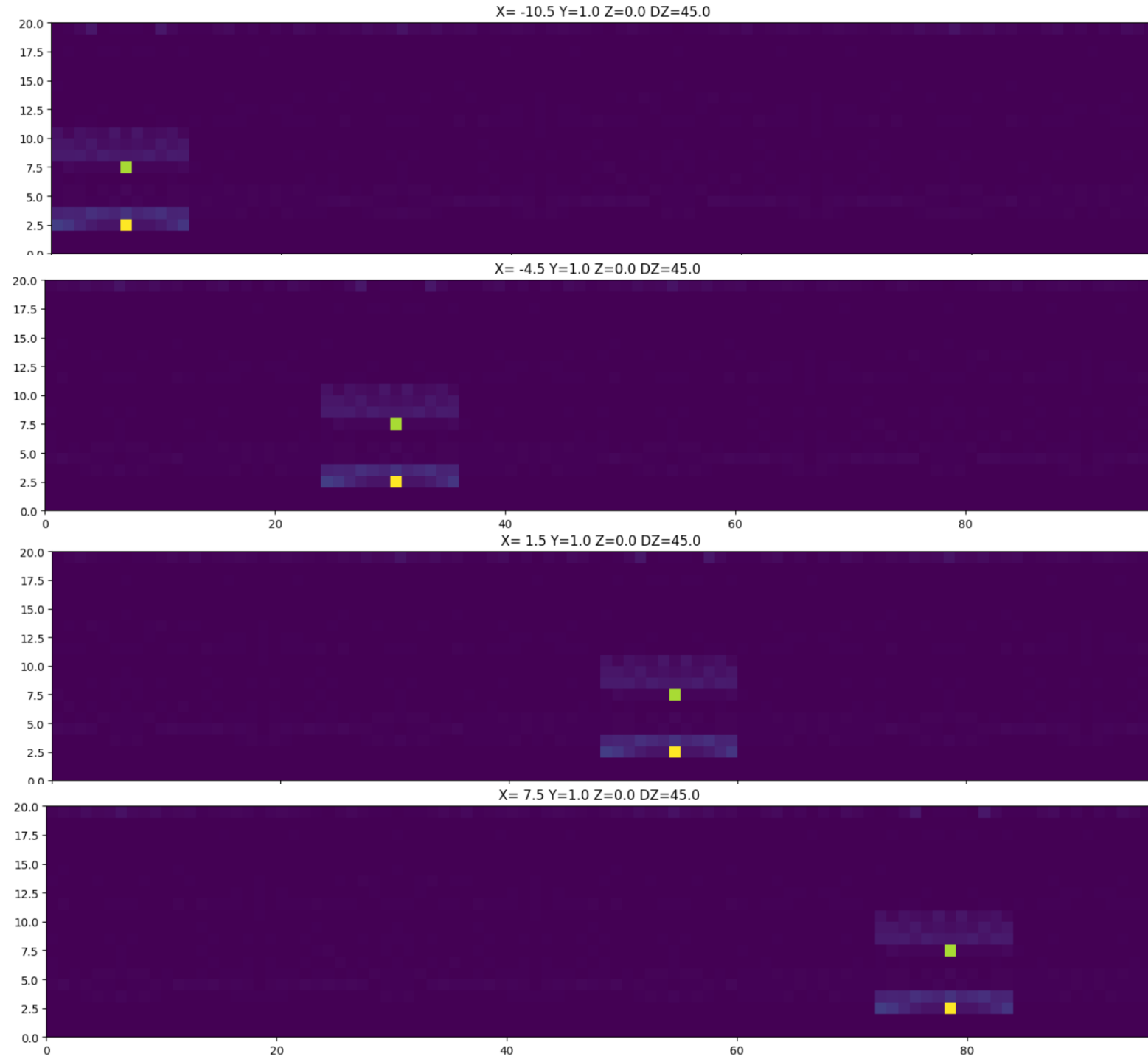
$x = [-10.5, -4.5, 1.5, 7.5]$

$y = 3.0$

$z = 0.$

**[X,Y] distribution
encodes [x,y]**

**[X,Y] distribution
similar in Y but
shifted in X
according to x**



y Scan:

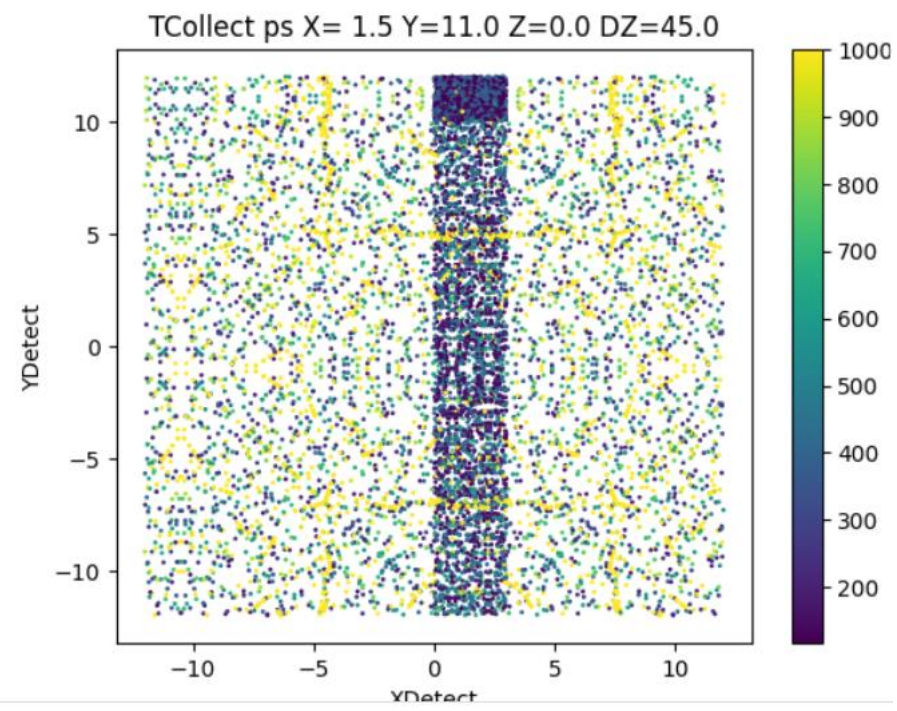
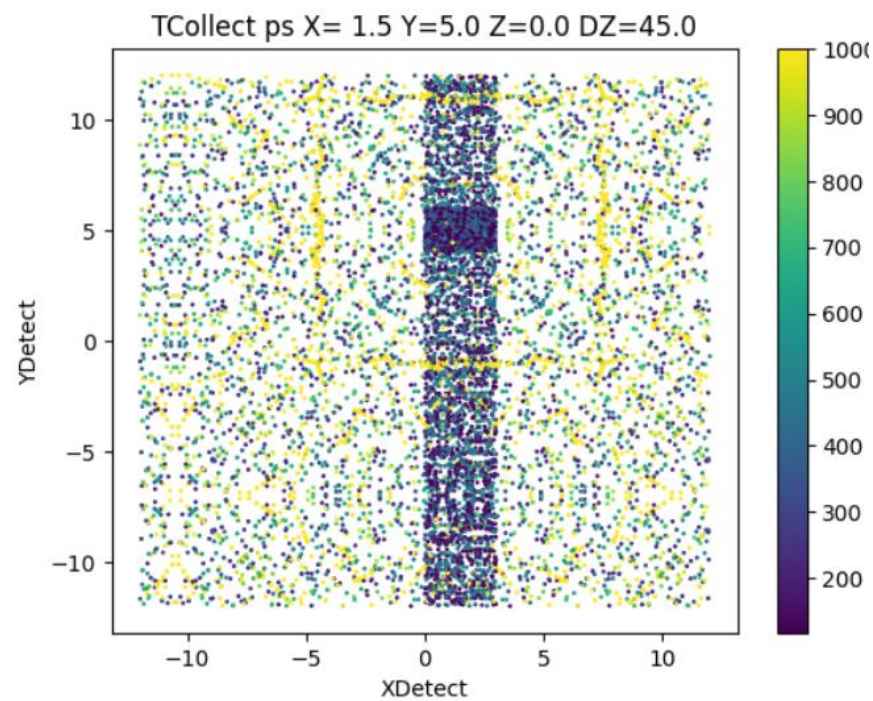
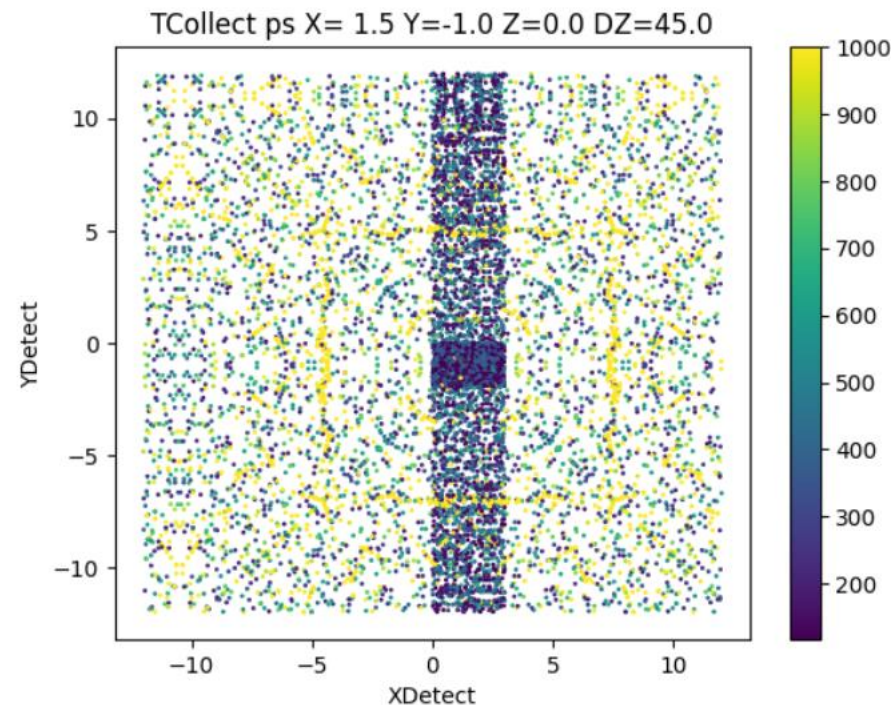
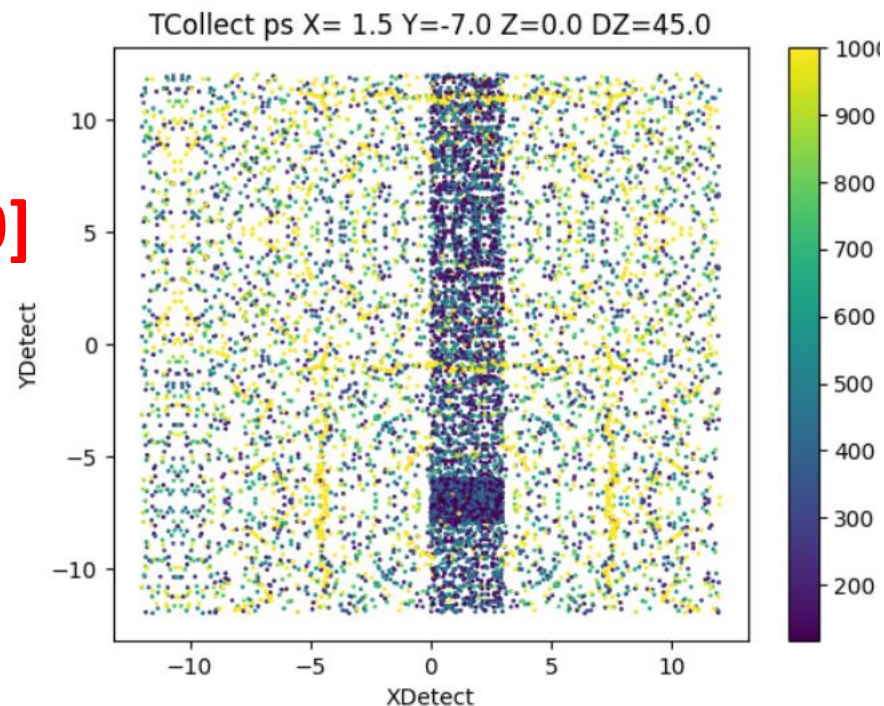
$x=1.5$

$y = [-7.0, -1.0, 5.0, 11.0]$

$z = 0.$

[X,Y] distribution
encodes [x,y]

[X,Y] distribution
similar in X but
shifted in Y
according to y



y Scan:

$x=1.5$

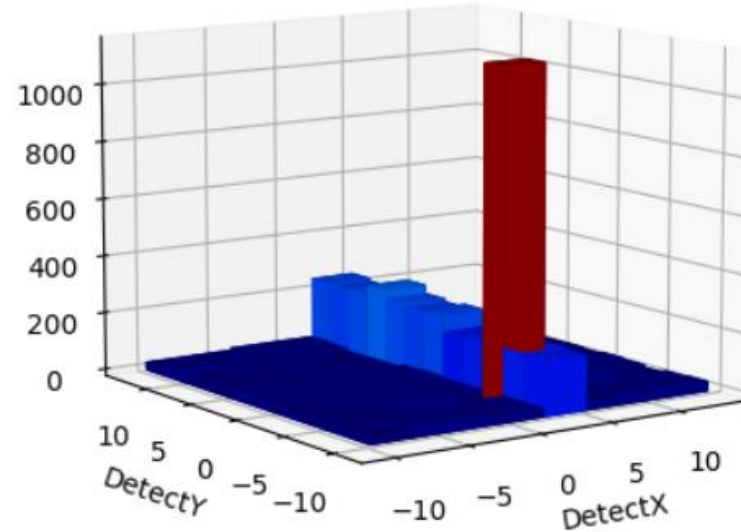
$y = [-7.0, -1.0, 5.0, 11.0]$

$z = 0.$

[X,Y] distribution
encodes [x,y]

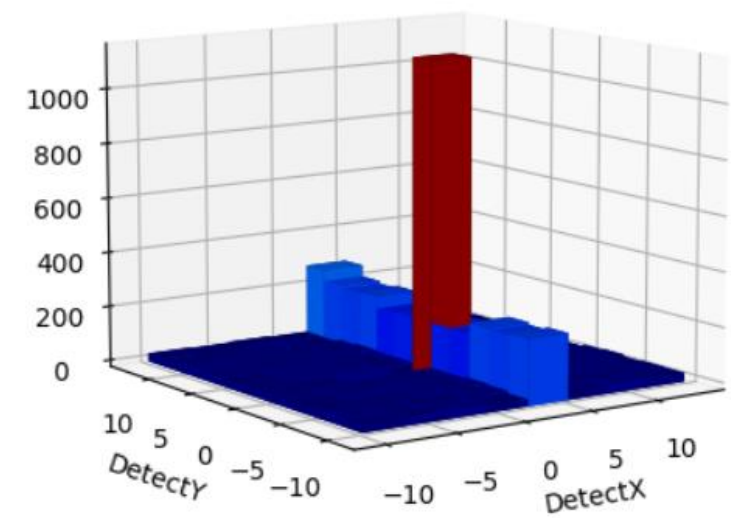
[X,Y] distribution
similar in X but
shifted in Y
according to y

X= 1.5 Y=-7.0 Z=0.0 DZ=45.0

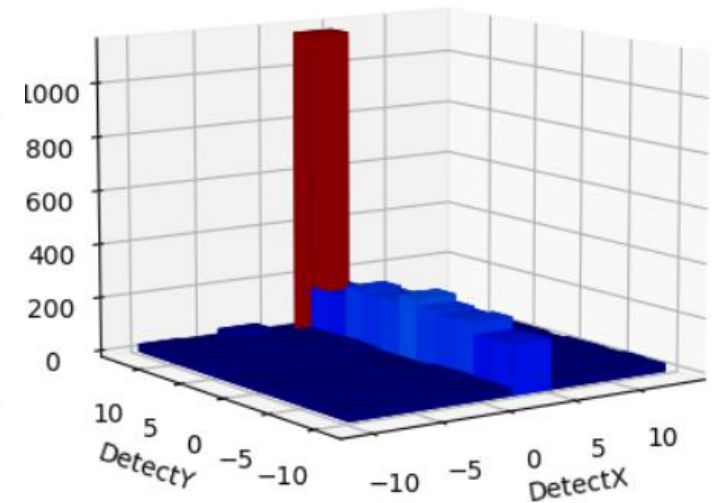
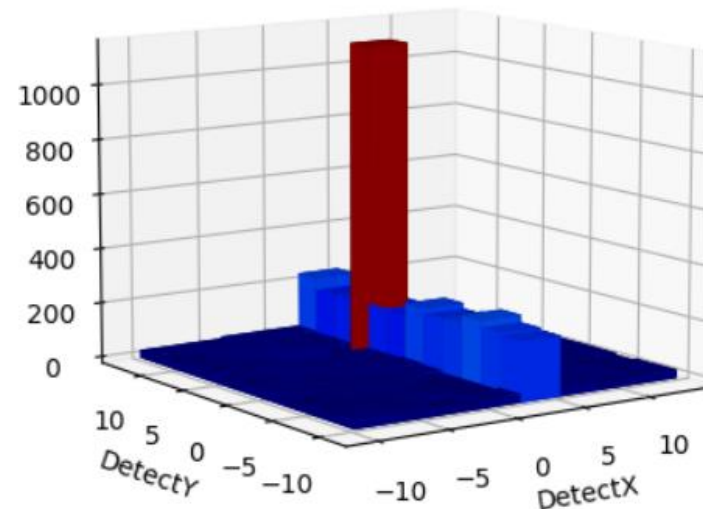


X= 1.5 Y=5.0 Z=0.0 DZ=45.0

X= 1.5 Y=-1.0 Z=0.0 DZ=45.0



X= 1.5 Y=11.0 Z=0.0 DZ=45.0



y Scan:

x=1.5

y =[-7.0, -1.0, 5.0, 11.0]

z =0.

**[X,Y] distribution
encodes [x,y]**

**[X,Y] distribution
similar in X but
shifted in Y
according to y**

