

VE320 HW7 Solution

1.

$$\begin{aligned}
 \text{(a)} \quad V_{bi} &= \phi_{B0} - \phi_n \\
 \phi_n &= V_t \ln\left(\frac{N_c}{N_d}\right) \\
 &= (0.0259) \ln\left(\frac{2.8 \times 10^{19}}{5 \times 10^{15}}\right) \\
 &= 0.2235 \text{ V} \\
 V_{bi} &= 0.65 - 0.2235 = 0.4265 \text{ V} \\
 \text{(b)} \quad \phi_n &= (0.0259) \ln\left(\frac{2.8 \times 10^{19}}{10^{16}}\right) \\
 &= 0.2056 \text{ V} \\
 V_{bi} &= 0.65 - 0.2056 = 0.4444 \text{ V} \\
 V_{bi} \text{ increases, } \phi_{B0} \text{ remains constant} \\
 \text{(c)} \quad \phi_n &= (0.0259) \ln\left(\frac{2.8 \times 10^{19}}{10^{15}}\right) \\
 &= 0.2652 \text{ V} \\
 V_{bi} &= 0.65 - 0.2652 = 0.3848 \text{ V} \\
 V_{bi} \text{ decreases, } \phi_{B0} \text{ remains constant}
 \end{aligned}$$

2.

$$\begin{aligned}
 \text{(a)} \quad \phi_{B0} &\cong 0.63 \text{ V} \\
 J_{sT} &= (120)(300)^2 \exp\left(\frac{-0.63}{0.0259}\right) \\
 &= 2.948 \times 10^{-4} \text{ A/cm}^2 \\
 I_{sT} &= (10^{-4})(2.948 \times 10^{-4}) = 2.948 \\
 \text{(i)} \quad V_a &= V_t \ln\left(\frac{I}{I_{sT}}\right) \\
 &= (0.0259) \ln\left(\frac{10 \times 10^{-6}}{2.948 \times 10^{-8}}\right) \\
 &= 0.151 \text{ V} \\
 \text{(ii)} \quad V_a &= (0.0259) \ln\left(\frac{100 \times 10^{-6}}{2.948 \times 10^{-8}}\right) \\
 &= 0.211 \text{ V} \\
 \text{(iii)} \quad V_a &= (0.0259) \ln\left(\frac{10^{-3}}{2.948 \times 10^{-8}}\right) \\
 &= 0.270 \text{ V}
 \end{aligned}$$

$$\begin{aligned}
 \text{(b)} \quad kT &= (0.0259) \left(\frac{350}{300}\right) = 0.030217 \text{ eV} \\
 I_{sT} &= (10^{-4})(120)(350)^2 \exp\left(\frac{-0.63}{0.030217}\right) \\
 &= 1.296 \times 10^{-6} \text{ A} \\
 \text{(i)} \quad I &= I_{sT} \left[\exp\left(\frac{V_a}{V_t}\right) - 1 \right] \\
 V_a &= (0.030217) \ln\left[\frac{10 \times 10^{-6}}{1.296 \times 10^{-6}} + 1\right] \\
 &= 0.0654 \text{ V} \\
 \text{(ii)} \quad V_a &= (0.030217) \ln\left[\frac{100 \times 10^{-6}}{1.296 \times 10^{-6}} + 1\right] \\
 &= 0.1317 \text{ V} \\
 \text{(iii)} \quad V_a &\cong (0.030217) \ln\left(\frac{10^{-3}}{1.296 \times 10^{-6}}\right) \\
 &= 0.201 \text{ V}
 \end{aligned}$$

3.

For the pn junction,

$$\begin{aligned}
 I_s &= (8 \times 10^{-4})(8 \times 10^{-13}) = 6.4 \times 10^{-16} \text{ A} \\
 \text{(a)} \quad V_a &= (0.0259) \ln\left(\frac{150 \times 10^{-6}}{6.4 \times 10^{-16}}\right) \\
 &= 0.678 \text{ V} \\
 \text{(b)} \quad V_a &= (0.0259) \ln\left(\frac{700 \times 10^{-6}}{6.4 \times 10^{-16}}\right) \\
 &= 0.718 \text{ V} \\
 \text{(c)} \quad V_a &= (0.0259) \ln\left(\frac{1.2 \times 10^{-3}}{6.4 \times 10^{-16}}\right) \\
 &= 0.732 \text{ V}
 \end{aligned}$$

For the Schottky junction,

$$\begin{aligned}
 I_{sT} &= (8 \times 10^{-4})(6 \times 10^{-9}) = 4.8 \times 10^{-12} \text{ A} \\
 \text{(a)} \quad V_a &= (0.0259) \ln\left(\frac{150 \times 10^{-6}}{4.8 \times 10^{-12}}\right) \\
 &= 0.447 \text{ V} \\
 \text{(b)} \quad V_a &= (0.0259) \ln\left(\frac{700 \times 10^{-6}}{4.8 \times 10^{-12}}\right) \\
 &= 0.487 \text{ V} \\
 \text{(c)} \quad V_a &= (0.0259) \ln\left(\frac{1.2 \times 10^{-3}}{4.8 \times 10^{-12}}\right) \\
 &= 0.501 \text{ V}
 \end{aligned}$$

4.

$$(a) \quad R = \frac{R_c}{A} = \frac{5 \times 10^{-5}}{10^{-5}} = 5 \Omega$$

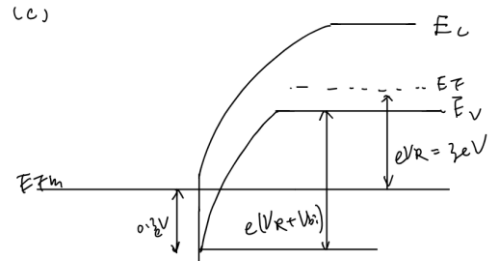
$$(i) \quad V = IR = (1)(5) = 5 \text{ mV}$$

$$(ii) \quad V = IR = (0.1)(5) = 0.5 \text{ mV}$$

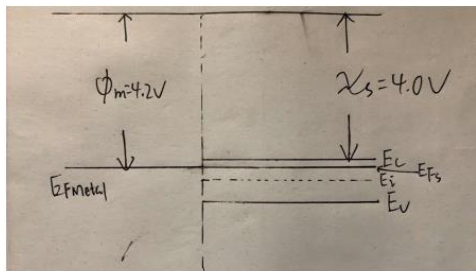
$$(b) \quad R = \frac{5 \times 10^{-5}}{10^{-6}} = 50 \Omega$$

$$(i) \quad V = IR = (1)(50) = 50 \text{ mV}$$

$$(ii) \quad V = IR = (0.1)(50) = 5 \text{ mV}$$



5.



(b) We need $\phi_n = \phi_m - \chi = 4.2 - 4.0 = 0.20 \text{ V}$
And

$$\phi_n = V_t \ln \left(\frac{N_c}{N_d} \right)$$

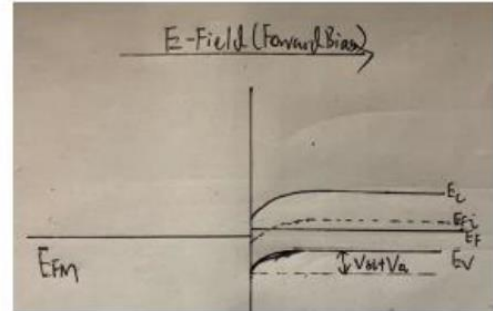
or

$$0.20 = (0.0259) \ln \left(\frac{2.8 \times 10^{19}}{N_d} \right)$$

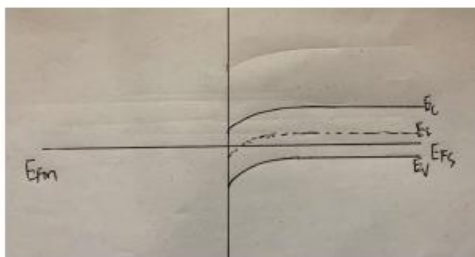
which yields

$$N_d = 1.24 \times 10^{16} \text{ cm}^{-3}$$

(c) Barrier height = 0.20 V



6.



$$(b) \quad \phi_{BO} = \phi_p = V_t \ln \left(\frac{N_v}{N_a} \right)$$

$$= (0.0259) \ln \left(\frac{1.04 \times 10^{19}}{5 \times 10^{16}} \right)$$

or

$$\phi_{BO} = 0.138 \text{ V}$$