

$$1. n_i^2 = N_c N_v \exp \left[\frac{-E_g}{kT} \right] \Rightarrow n_i = \sqrt{2.8 \times 10^{19} \times 4.7 \times 10^{17} \times \left(\frac{550}{300} \right)^3 \exp \left(\frac{1.12 \times 1.6 \times 10^{-19}}{1.38 \times 10^{-23} \times 330} \right)}$$

$$= 3.16 \times 10^{14} \text{ cm}^{-3}$$

According to the question, we have $N_d = (1 - 0.05) \cdot n_0$ since the total electron concentration has both the electron concentration that comes from the donor and the electron concentration that the semiconductor itself produces which is just the intrinsic excitation.

$$n_0 = n_{oi} + N_d \text{ here } n_{oi} \neq n_i \text{ and } n_{oi} = 0.05 n_0$$

$$\text{Also we have } n_0 = \frac{N_d - N_a}{2} + \sqrt{\left(\frac{N_d - N_a}{2} \right)^2 + n_i^2} \quad N_a = 0$$

$$\text{So then } \begin{cases} n_0 = \frac{1}{0.95} N_d \\ n_0 = \frac{N_d}{2} + \sqrt{\left(\frac{N_d}{2} \right)^2 + n_i^2} \end{cases} \Rightarrow N_d = 1.4 \times 10^{15} \text{ cm}^{-3}$$

2. ① Decrease Temperature

② Decrease Ionized Impurity