LEC005 Demand Forecasting

VG441 SS2020

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F0 = Initial Model = Taking the mean

Height (m)	Favorite Color	Gender	Weight (kg)
1.6	Blue	Male	88
1.6	Green	Female	76
1.5	Blue	Female	56
1.8	Red	Male	73
1.5	Green	Male	77
1.4	Blue	Female	57



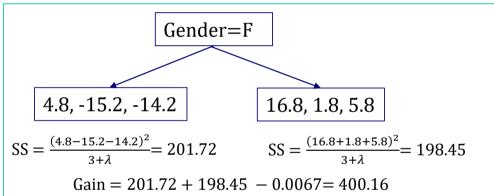
Height (m)	Favorite Color	Gender	Weight (kg)	F0	PR0
1.6	Blue	Male	88	71.2	16.8
1.6	Green	Female	76	71.2	4.8
1.5	Blue	Female	56	71.2	-15.2
1.8	Red	Male	73	71.2	1.8
1.5	Green	Male	77	71.2	5.8
1.4	Blue	Female	57	71.2	-14.2

Pseudo Residual (PR) = True Value - Predicted Value

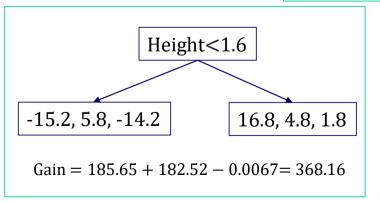
Compute the	similarity score	e and the	gain	with	

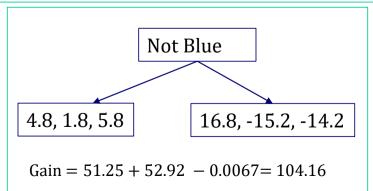
Height (m)	Favorite Color	Gender	PR0
1.6	Blue	Male	16.8
1.6	Green	Female	4.8
1.5	Blue	Female	-15.2
1.8	Red	Male	1.8
1.5	Green	Male	5.8
1.4	Blue	Female	-14.2

16.8, 4.8, -15.2, 1.8, 5.8, -14.2
$SS = \frac{(16.8+4.8-15.2+1.8+5.8-14.2)^2}{6+\lambda} = 0.0067$

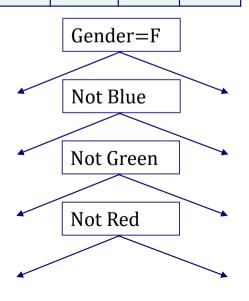


Regularization term $\lambda = 0$

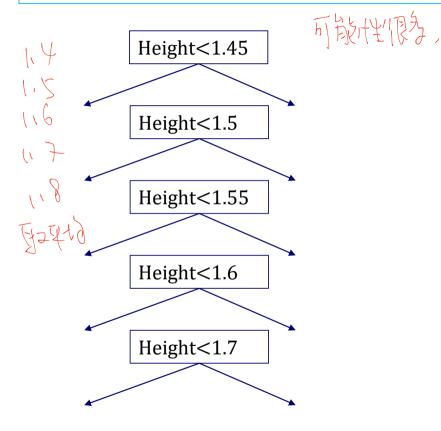




Height (m)	Favorite Color	Gender	PR0
1.6	Blue	Male	16.8
1.6	Green	Female	4.8
1.5	Blue	Female	-15.2
1.8	Red	Male	1.8
1.5	Green	Male	5.8
1.4	Blue	Female	-14.2



If numerical, sort and take average between adjacent

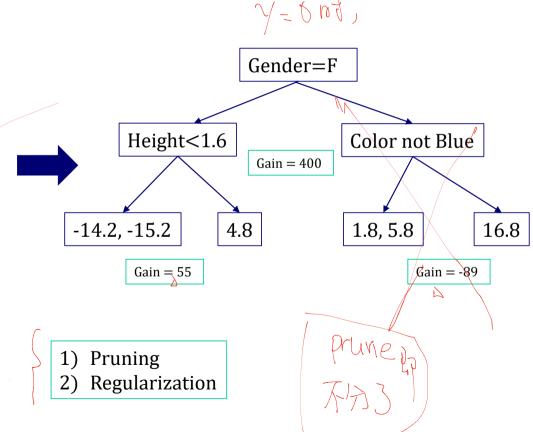


These can be re-used in building the DT.

DH reuse!

Fit PR0 into an XGBoost tree (up to four leaves)

Height (m)	Favorite Color	Gender	PR0
1.6	Blue	Male	16.8
1.6	Green	Female	4.8
1.5	Blue	Female	-15.2
1.8	Red	Male	1.8
1.5	Green	Male	5.8
1.4	Blue	Female	-14.2



tho features

Pruning Term y Etalearning rate

If the gain $< \gamma$, then we prune the tree!

The tree could be pruned even if we set $\gamma = 0$.

Regularization Term λ

If the regularization term grows large, then the gain will be decreased, and thus the node becomes harder to split and easier to prune. This is used to prevent overfitting (of the training data).

The regularization affects children nodes more than their parent node.

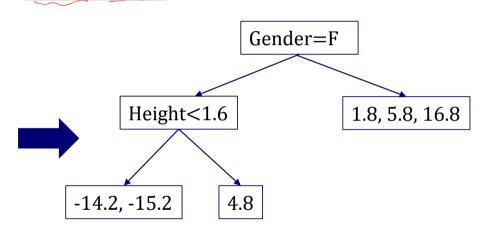
NASS V harder to split
(Pasier to prune)

i By Roverfitting

Fit PR0 into an XGBoost tree (up to four leaves)

$$\lambda = 0, \gamma = 0$$

Height (m)	Favorite Color	Gender	PR0
1.6	Blue	Male	16.8
1.6	Green	Female	4.8
1.5	Blue	Female	-15.2
1.8	Red	Male	1.8
1.5	Green	Male	5.8
1.4	Blue	Female	-14.2



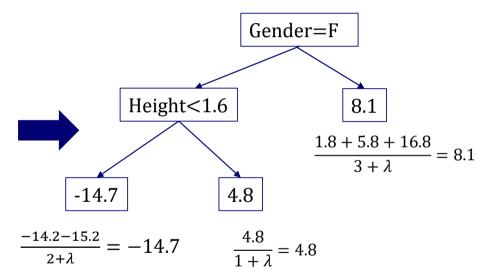
Pseudo Residual (PR) = True Value - Predicted Value

XGBoost Output

Output Value = Sum of PR / (#PRs + regularization term)

$$\lambda = 0, \gamma = 0$$

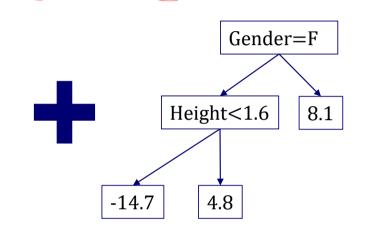
Height (m)	Favorite Color	Gender	PR0
1.6	Blue	Male	16.8
1.6	Green	Female	4.8
1.5	Blue	Female	-15.2
1.8	Red	Male	1.8
1.5	Green	Male	5.8
1.4	Blue	Female	-14.2



Learning rate = 0.1

$$F1(x) = F0(x) + v_1 \times Output \text{ of } DT(x)$$

Height (m)	Favorite Color	Gender	Weight (kg)	F0
1.6	Blue	Male	88	71.2
1.6	Green	Female	76	71.2
1.5	Blue	Female	56	71.2
1.8	Red	Male	73	71.2
1.5	Green	Male	77	71.2
1.4	Blue	Female	57	71.2

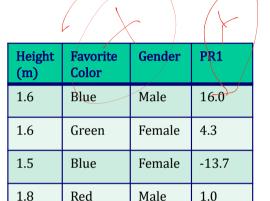


F1((1.6, Blue, Male)) = $71.2 + 0.1 \times 8.1 = 72.0$ F1((1.6, Green, Female)) = $71.2 + 0.1 \times 4.8 = 71.7$ F1((1.5, Blue, Female)) = $71.2 + 0.1 \times -14.7 = 69.7$ F1((1.8, Red, Male)) = $71.2 + 0.1 \times 8.1 = 72.0$ F1((1.5, Green, Male)) = $71.2 + 0.1 \times 8.1 = 72.0$ F1((1.4, Blue, Female)) = $71.2 + 0.1 \times -14.7 = 69.7$

So after building the first DT, we obtain...

Height (m)	Favorite Color	Gender	Weight (kg)	F0	PR0	F1	PR1
1.6	Blue	Male	88	71.2	16.8	72.0	16.0
1.6	Green	Female	76	71.2	4.8	71.7	4.3
1.5	Blue	Female	56	71.2	-15.2	69.7	-13.7
1.8	Red	Male	73	71.2	1.8	72.0	1.0
1.5	Green	Male	77	71.2	5.8	72.0	5.0
1.4	Blue	Female	57	71.2	-14.2	69.7	-12.7

Fit PR1 into an XGBoost tree (up to four leaves)



Male

Female

5.0

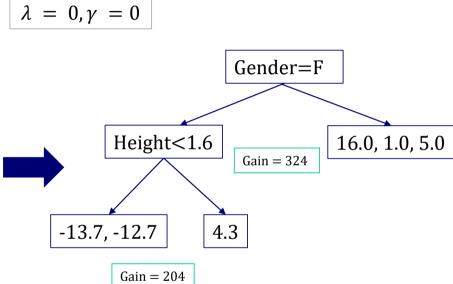
-12.7

1.5

1.4

Green

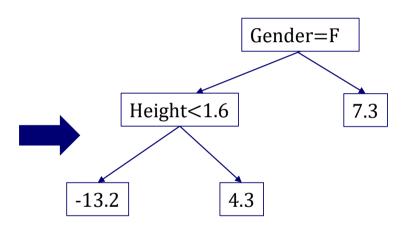
Blue



Output Value = Sum of PR / (#PRs + regularization term)

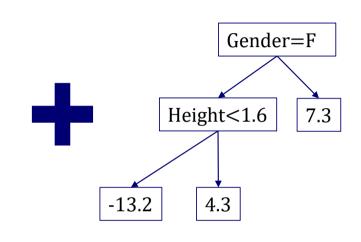
$$\lambda = 0, \gamma = 0$$

Height (m)	Favorite Color	Gender	PR1
1.6	Blue	Male	16.0
1.6	Green	Female	4.3
1.5	Blue	Female	-13.7
1.8	Red	Male	1.0
1.5	Green	Male	5.0
1.4	Blue	Female	-12.7



F2(x) = F1(x) + ν_2 × Output of DT(x)

Height (m)	Favorite Color	Gender	Weight (kg)	F1	
1.6	Blue	Male	88	72.9	
1.6	Green	Female	76	71.7	
1.5	Blue	Female	56	69.7	
1.8	Red	Male	73	71.6	
1.5	Green	Male	Male 77		
1.4	Blue	Female	57	69.7	



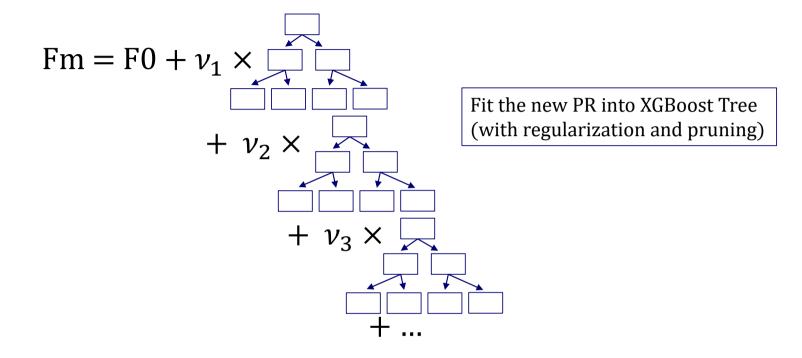
F2((1.6, Blue, Male)) = $72.9 + 0.1 \times 7.3 = 73.6$ F2((1.6, Green, Female)) = $71.7 + 0.1 \times 4.3 = 72.1$ F2((1.5, Blue, Female)) = $69.7 + 0.1 \times -13.2 = 68.4$ F2((1.8, Red, Male)) = $71.6 + 0.1 \times 7.3 = 72.3$ F2((1.5, Green, Male)) = $71.6 + 0.1 \times 7.3 = 72.3$ F2((1.4, Blue, Female)) = $69.7 + 0.1 \times -13.2 = 68.4$

So after building the second DT, we obtain...

Height (m)	Favorite Color	Gender	Weight (kg)	F0	PR0	F1	PR1	F2	PR2
1.6	Blue	Male	88	71.2	16.8	72.9	15.1	73.6	14.4
1.6	Green	Female	76	71.2	4.8	71.7	4.3	72.1	3.9
1.5	Blue	Female	56	71.2	-15.2	69.7	-13.7	68.4	-12.4
1.8	Red	Male	73	71.2	1.8	71.6	1.4	72.3	0.7
1.5	Green	Male	77	71.2	5.8	71.6	5.4	72.3	4.7
1.4	Blue	Female	57	71.2	-14.2	69.7	-12.7	68.4	-11.4

Notice the RR's are shrinking: Small steps towards the right direction!

Converge, J. J.



Stop until the pre-specified #DTs or the PR stops improving!



Python Time!



- pip install xgboost
- Import xgboost as xgb
- Install graphviz-2.38.zip for visualization



- Works exceptionally well in practice
- Won a series of Kaggle competitions
- More robust and explainable than DNN
- Comes with regularization and pruning