

Mini-batch & distributed SAGA

Incremental Gradient Methods

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Introduction

$$\text{Problem: } \min_{x \in \mathbb{R}^d} \frac{1}{n} \sum_{i=1}^n f_i(x) + h(x)$$

SAGA

Given a learning rate γ , the value of x^k and of each $f'_i(\phi_i^k)$ at the end of iteration k , the updates for iteration $k + 1$ are given by:

- 1** Pick a j uniformly at random.
- 2** Take $\phi_j^{k+1} = x^k$, and store $f'_j(\phi_j^{k+1})$ in the table.
- 3** Update x :

$$w^{k+1} = x^k - \gamma \left[f'_j(\phi_j^{k+1}) - f'_j(\phi_j^k) + \frac{1}{n} \sum_{i=1}^n f'_i(\phi_i^k) \right],$$

$$x^{k+1} = \text{prox}_{\gamma}^h(w^{k+1}).$$

Improvements

- Memory-efficiency → **mini-batch** SAGA
- Time-efficiency → **distributed** SAGA

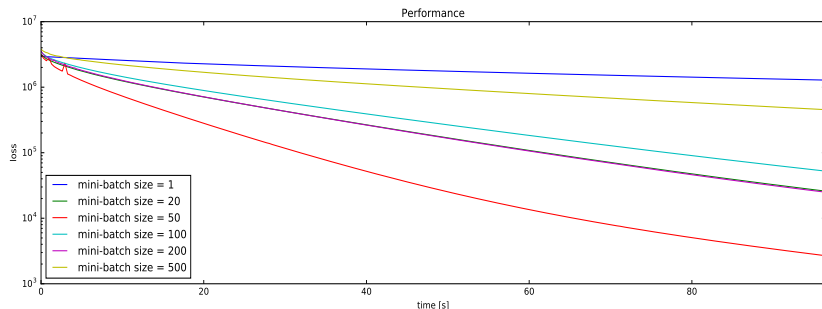
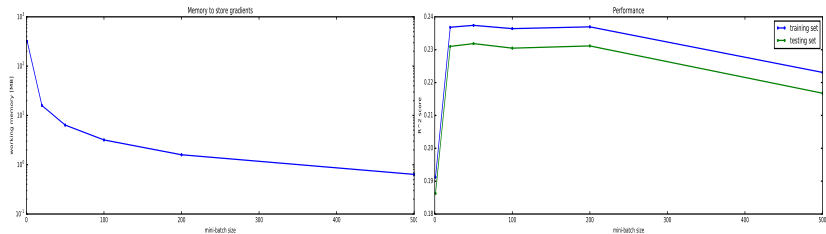
Mini-batch SAGA

- 1 Pick a i uniformly at random in $[1, \frac{n}{m}]$.
- 2 Take $\phi_j^{k+1} = x^k \ \forall j \in \mathcal{B}_i$, and store $\frac{1}{m} \sum_{j \in \mathcal{B}_i} f'_j(\phi_j^{k+1})$ in the table.
- 3 Update x :

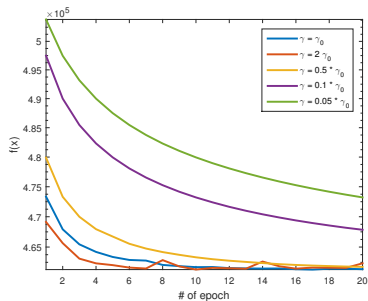
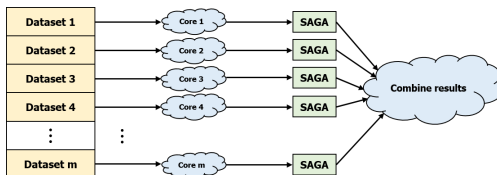
$$w^{k+1} = x^k - \gamma \left[\frac{1}{m} \sum_{j \in \mathcal{B}_i} f'_j(\phi_j^{k+1}) - \frac{1}{m} \sum_{j \in \mathcal{B}_i} f'_j(\phi_j^k) + \frac{1}{n} \sum_{i=1}^m \sum_{j \in \mathcal{B}_i} f'_j(\phi_j^k) \right],$$

$$x^{k+1} = \text{prox}_{\gamma}^h(w^{k+1}).$$

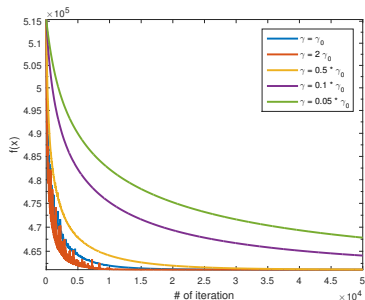
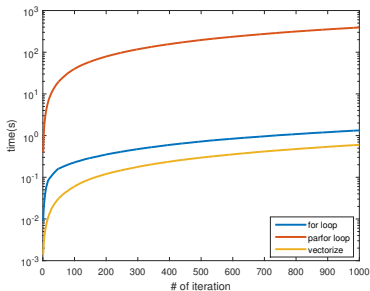
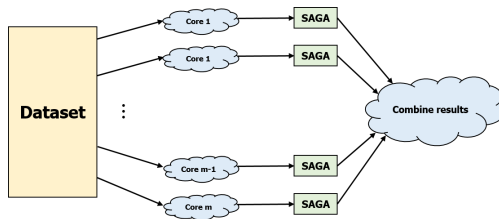
Results



Variant I



Variant II



Comparison

