

# Mini-batch & distributed SAGA

## Incremental Gradient Methods

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# Introduction

$$\text{Problem: } \min_{x \in \mathbb{R}^d} \frac{1}{n} \sum_{i=1}^n f_i(x) + h(x)$$

## SAGA

Given a learning rate  $\gamma$ , the value of  $x^k$  and of each  $f'_i(\phi_i^k)$  at the end of iteration  $k$ , the updates for iteration  $k + 1$  are given by:

- 1** Pick a  $j$  uniformly at random.
- 2** Take  $\phi_j^{k+1} = x^k$ , and store  $f'_j(\phi_j^{k+1})$  in the table.
- 3** Update  $x$ :

$$w^{k+1} = x^k - \gamma \left[ f'_j(\phi_j^{k+1}) - f'_j(\phi_j^k) + \frac{1}{n} \sum_{i=1}^n f'_i(\phi_i^k) \right],$$

$$x^{k+1} = \text{prox}_{\gamma}^h(w^{k+1}).$$

# Improvements

- Memory-efficiency → **mini-batch** SAGA
- Time-efficiency → **distributed** SAGA

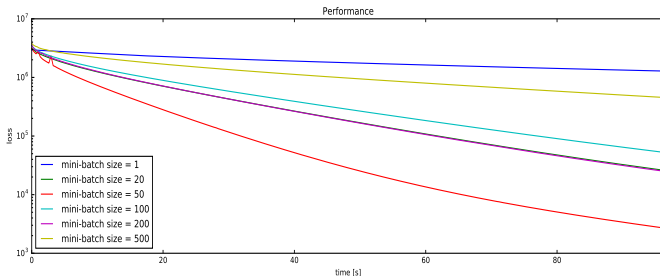
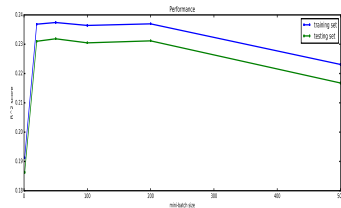
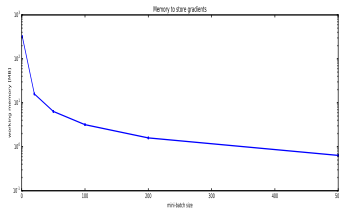
# Mini-batch SAGA

- 1 Pick a  $i$  uniformly at random in  $[1, \frac{n}{m}]$ .
- 2 Take  $\phi_j^{k+1} = x^k \ \forall j \in \mathcal{B}_i$ , and store  $\frac{1}{m} \sum_{j \in \mathcal{B}_i} f'_j(\phi_j^{k+1})$  in the table.
- 3 Update  $x$ :

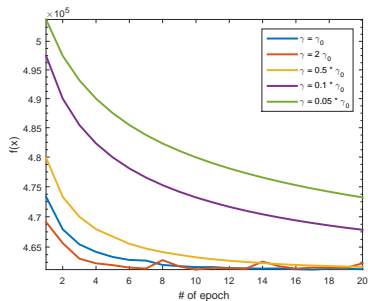
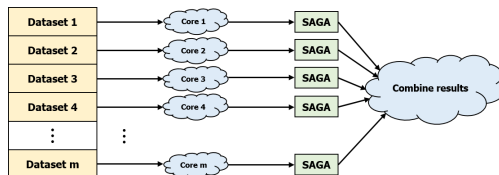
$$w^{k+1} = x^k - \gamma \left[ \frac{1}{m} \sum_{j \in \mathcal{B}_i} f'_j(\phi_j^{k+1}) - \frac{1}{m} \sum_{j \in \mathcal{B}_i} f'_j(\phi_j^k) + \frac{1}{n} \sum_{i=1}^m \sum_{j \in \mathcal{B}_i} f'_j(\phi_j^k) \right],$$

$$x^{k+1} = \text{prox}_{\gamma}^h(w^{k+1}).$$

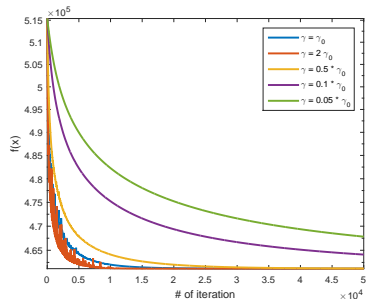
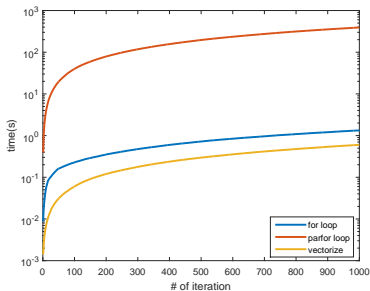
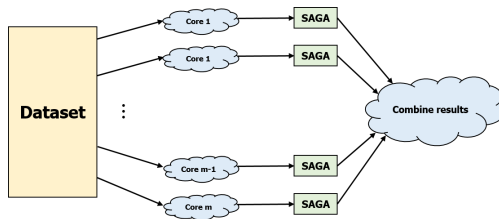
# Results



# Variant I



# Variant II



# Comparison

