

The Map-Reduce Programming Paradigm

M.Sc. course on “Technologies for Big Data Analysis” - Assignment 2

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1 Introduction

The current document is a technical report for the second programming assignment in the M.Sc. course on *Technologies for Big Data Analysis*, offered by the *DWS M.Sc Program*¹ of the Aristotle University of Thessaloniki, Greece. The course is taught by Professor Apostolos Papadopoulos². The authors attended the course during their first year of Ph.D. studies at the Institution.

The assignment contains 4 sub-problems and is part of a series, comprising 3 programming assignments on the following topics:

Assignment 1 Multi-threading Programming and Inter-Process Communication

Assignment 2 The Map-Reduce Programming Paradigm

Assignment 3 Big Data Analytics with Scala and Apache Spark

In this document we focus on Assignment 2 and its 4 sub-problems. We refer to them as *problems* in the rest of the document for simplicity. The source code of our solution has been made available at the following public repository in the GitHub platform: <https://github.com/Bilpapster/big-data-playground>.

Roadmap. The rest of our work is structured as follows. We devote one section to each one of the 4 problems. That means problems 1, 2, 3 and 4 are presented in section 2, section 3, section 4 and section 5 respectively. For each problem, we first provide the problem statement, as given by the assignment. Next, we thoroughly present the reasoning and/or methodology we have adopted to approach the problem and devise a solution. Wherever applicable, we also provide insights about the source code implementation we have developed. Finally, we conclude our work in section 6. The appendix includes the evaluation results for any issues that necessitated them.

2 Problem 1: Numeronyms

We discuss here the first problem of the assignment. The main target of the assignment is to get acquainted with the MapReduce programming model in Hadoop framework in Java programming language. This is a WordCount problem’s variation.

2.1 Problem Statement

Implement a **MapReduce** program, a variation of the **word-count** problem, to generate and count “numeronyms”. Numeronyms correspond to words as shown below:

- s5n – shorten
- h7k – hyperlink
- l10n – localization

¹<https://dws.csd.auth.gr/>

²<https://datalab-old.csd.auth.gr/~apostol/>

- i18n – internationalization

A numeronym of a word is defined as an alphanumeric string formed by taking the first and last character of the word and inserting between them the count of characters between the first and the last. More specifically, the program should process words with a length of 3 characters or more, generate numeronyms, and then output the frequency of each numeronym.

The program should ignore:

- words shorter than 3 characters
- punctuation marks
- uppercase/lowercase differences, i.e., it should be *case-insensitive*

Additionally, a parameter k will be given, representing the minimum number of occurrences of a numeronym that we are interested in. The program output should be a list of numeronyms and the frequency of each numeronym that is greater than or equal to the parameter k specified by the user.

2.2 Proposed approach

2.2.1 Setting. Our implementation is run and tested in a Linux environment with 12 cores, using the Java programming language. We have used the Java Development Kit (JDK) version 11.0.11. The source code is developed in IntelliJ IDEA Community Edition 2021.1.1 and managed using Maven as the build tool.

The project's dependencies, including Hadoop libraries, are defined in the `pom.xml` file located in the root of the repository. The project is compiled and executed directly from IntelliJ IDEA.

To run the project, open the `NumeronymsMaster` class in IntelliJ IDEA, and execute the main method. You will need to specify the following command-line arguments:

- `<input_path>` specifies the directory containing the input text files, located at `map-reduce/ numeronyms /input`.
- `<output_path>` specifies the directory where the MapReduce output will be written, which will be created in the `out` folder.
- `<k>` is the minimum frequency threshold for numeronyms to be included in the results.

IntelliJ IDEA will handle the compilation and execution automatically when the main method is run. Make sure to configure the input and output paths as required for your specific run.

Note that the command-line arguments must follow the specified order and format. If any of the arguments are missing or invalid, the program will terminate with an appropriate error message.

2.2.2 Implementation. The proposed approach leverages the MapReduce programming model to compute numeronyms from a given input dataset. A numeronym is a concise representation of a word, typically formed by retaining the first and last letters while replacing the intervening characters with their count. This section outlines the methodology implemented across three key components: the driver class, the mapper, and the reducer. This methodology supports flexible configuration through command-line arguments, enabling users to specify the threshold k and the minimum word length for numeronym generation. The use of the MapReduce paradigm ensures scalability and parallel processing for large datasets, making the approach well-suited for distributed systems.

The driver class, `NumeronymsMaster`, orchestrates the overall MapReduce job. It takes command-line arguments for the input and output directories as well as a threshold parameter k , which determines the minimum frequency for numeronyms to be included in the final output. The following steps are executed:

- Input and output paths are parsed, and any pre-existing output directory is deleted using the `Utilities.deleteDirectory` method.
- A Hadoop configuration object is initialized with two parameters:

- `numeronyms.k`: The threshold k .
- `numeronyms.l`: The minimum word length (default value is 3) required for numeronym generation.
- The job is configured to use the `NumeronymMapper` and `NumeronymReducer` classes, with input and output formats set to `TextInputFormat` and `TextOutputFormat`, respectively.
- Finally, the job waits for completion before terminating.

The `NumeronymMapper` class is responsible for processing each line of the input text file and emitting numeronym -frequency pairs. The following steps are performed:

- During setup, the minimum word length (`numeronyms.l`) is retrieved from the configuration.
- Each input line is tokenized into individual words, and non-alphabetic characters are removed from each token.
- For valid words (those with lengths greater than or equal to the specified minimum), a numeronym is constructed by concatenating the first character, the number of intervening characters, and the last character.
- A key-value pair is emitted, where the key is the numeronym and the value is a count of one.

The `NumeronymReducer` class aggregates the frequency counts for each numeronym and filters out those below the specified threshold k . The process includes:

- Retrieving the threshold value (`numeronyms.k`) from the configuration during the setup phase.
- Summing the values for each numeronym key received from the mapper.
- Emitting numeronyms that meet or exceed the threshold k along with their corresponding frequencies.

2.2.3 Evaluation. The experiments were executed using the dataset ‘`SherlockHolmes.txt`’ with a parameter setting of $k = 10$. This configuration was chosen to evaluate the performance and the behavior of the system under moderate conditions. The dataset, containing a series of textual records, was processed to analyze various patterns and results.

To provide a comprehensive overview, the results of the experiment, including the detailed values derived from the dataset, are presented in Appendix A in a 2-column format.

3 Problem 2: Movie Analytics

The second problem focuses on producing analytic insights from an IMDB dataset.

3.1 Problem Statement

Implement a **MapReduce** program to perform analytics tasks on an IMDB dataset about movies. The utter goal of your analysis would be to extract useful insights from the available movie data that will assist the IMDB team provide better recommendations for movies, based on their genre and/or country. In particular, the dataset (`movies.csv`) contains the following fields:

- `imdbID`: unique identifier of the movie in the IMDB database
- `title`: the movie title
- `year`: the year the movie was first released
- `duration`: the duration of the movie
- `genre(s)`: the genre or genres in which the movie is classified
- `premier date`: the date of the first showing of the movie
- `score`: the IMDB score of the movie
- `country/-ies`: the country or countries the movie was produced in

You are asked to implement Map-Reduce source code in Java programming language for the following analytics tasks:

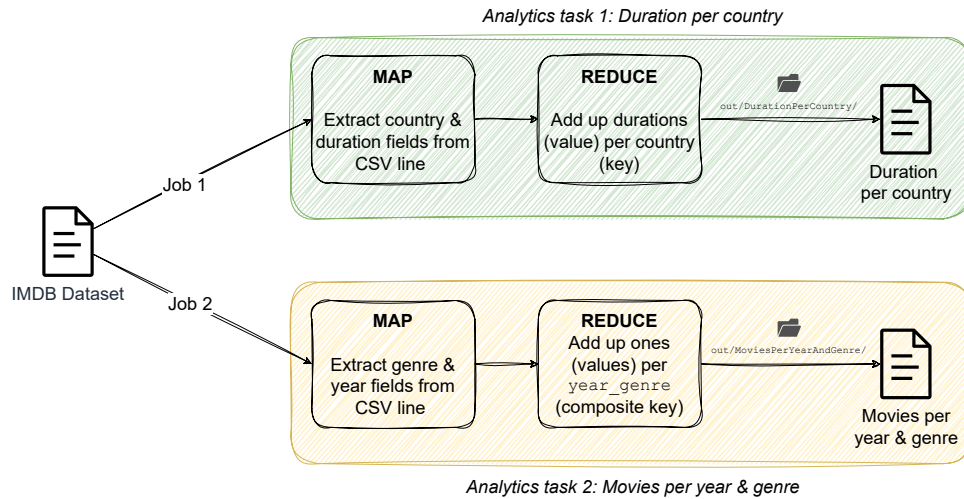


Fig. 1. The MapReduce solution architecture for the movie analytics problem. Two separate jobs are executed to solve the two tasks, namely duration per country (green) and movies per year & genre (yellow). The two tasks also create separate subdirectories for writing the results.

- Calculate the total duration of all movies per country. Note that in case multiple countries are recorded for a movie, the respective duration should be counted for all of them separately.
- Calculate the total number of movies per year and genre, having IMDB score over 8. For movies that have more than one genre, the sum should be separate for each genre.

3.2 Proposed approach

3.2.1 Setting. Our implementation is run and tested in a Linux environment with 12 cores, using the Java programming language. We have used the Java Development Kit (JDK) version 11.0.11. The source code is developed in IntelliJ IDEA Community Edition 2021.1.1 and managed using Maven as the build tool.

The project's dependencies, including Hadoop libraries, are defined in the `pom.xml` file located in the root of the repository. The project is compiled and executed directly from IntelliJ IDEA.

To run the project, open the `MovieAnalyticsMaster` class in IntelliJ IDEA, and execute the main method. You will need to specify the following command-line arguments:

- `<input_path>` specifies the directory containing the input text files, located at `map-reduce/movieAnalytics/input`.
- `<output_path>` specifies the directory where the MapReduce output will be written, which will be created in the `out` folder.

IntelliJ IDEA will handle the compilation and execution automatically when the main method is run. Make sure to configure the input and output paths as required for your specific run. Note that the command-line arguments must follow the specified order and format. If any of the arguments are missing or invalid, the program will terminate with an appropriate error message.

3.2.2 Implementation. The proposed approach leverages the MapReduce programming paradigm to compute the analytical insights for the two tasks. Figure 1 depicts the architecture of our solution as a diagram. We opt for executing two separate jobs; one for each task presented by the problem statement.

Task 1: Duration per country. One map-reduce cycle is enough to handle this task, as depicted in the top part of Figure 1 in green color. The map function parses the CSV file line by line and extracts the useful fields from each line. In this case, the useful fields are the country (or countries) the movie was produced and the movie duration, i.e., the fourth and ninth fields in the input line respectively. We employ more complex logic to handle cases where there are multiple countries in a single movie. In particular, we parse again the field and tokenize it into the separate countries, producing a key-value pair for each country-duration pair within a movie. The reduce function is, then, trivial; it just adds up the durations (value) per country (key) and outputs the results. The interested reader can refer to the `CSVProcessor.java` (mapper), `AnayticsEngine.java` (reducer) and `MovieAnalyticsMaster.java` (driver) files for the source code implementation of our solution.

Task 2: Movies per year & genre w.r.t. score constraint. The task is similar to the first one, with the only difference lying in the fields extracted from the input CSV line. In this case, we are interested about the year, the genre (or genres) and score fields, i.e., the third, fifth and seventh fields in the input CSV line. The map function produces key-value pairs in the form `(composite_key, 1)`, where the composite key consists of the year and the genre of the respective movie concatenated by an underscore, e.g., `2024_action`. We handle multiple genres per movie similarly with the multiple countries in task 1. We employ the same trivial reducer that adds up the values (ones) per (composite) key, as shown in the bottom part of Figure 1 in yellow color.

3.2.3 Evaluation. Our solution is tested using the provided IMDB dataset, namely `movies.csv`. We list the execution results in Appendix B.

4 Problem 3: DNA Sequence Patterns

The third problem focuses on mining unstructured data, namely DNA sequences, encoded in text format.

4.1 Problem Statement

A DNA sequence consists of four distinct symbols, namely A, G, C, and T. For instance, the following lines represent a part of the DNA sequence of the E. Coli bacterium ³:

```
AGCTTTTCATTCTGACTGCAACGGGCAATATGTCTCTGTGTGGATTAAAAAAGAGTGTCTGATAGCAGC
TTCTGAAGTGGTTACCTGCCGTGAGTAAATTTAAATTTTATTGACTTAGGTCACTAAATACTTTAACCAA
TATAGGCATAGCGCACAGACAGATAAAAATTACAGAGTACACAACATCCATGAAACGCATTAGCACCACC
ATTACCACCACCATCACCATTACCACAGGTAACGGTGCGGGCTGACGCGTACAGGAAACACAGAAAAAAG
```

Implement a **MapReduce** program that computes the frequency (i.e., number of occurrences) of all subsequences of lengths 2, 3, and 4 that are present in the input DNA sequence. Note that the processing of each line should be independent of all other lines. Use the file `ecoli.txt` to test your solution.

4.2 Proposed approach

4.2.1 Setting. Our implementation is run and tested in a Linux environment with 12 cores, using the Java programming language. We have used the Java Development Kit (JDK) version 11.0.11. The source code is developed in IntelliJ IDEA Community Edition 2021.1.1 and managed using Maven as the build tool.

The project's dependencies, including Hadoop libraries, are defined in the `pom.xml` file located in the root of the repository. The project is compiled and executed directly from IntelliJ IDEA. To run the project, open the `DNASquenceAnalyticsMaster` class in IntelliJ IDEA, and execute the main method. You will need to specify the following command-line arguments:

³https://en.wikipedia.org/wiki/Pathogenic_Escherichia_coli

Algorithm 1 Populating DNA subsequences

```

1: ▷ Input: a DNA sequence line (variable line)
2: for  $length \in \{2, 3, 4\}$  do
3:   Create a sliding window window of length length.
4:   Place left end of window at the start of line.
5:   while right end of window has not exceeded line do
6:      $subsequence \leftarrow$  contents of window
7:     Yield (subsequence, 1) key-value pair.
8:   Slide window to the right by 1.

```

- `<input_path>` specifies the directory containing the input text files, located at `map-reduce/dnaSequencePatterns/input`.
- `<output_path>` specifies the directory where the MapReduce output will be written, which will be created in the out folder.

IntelliJ IDEA will handle the compilation and execution automatically when the main method is run. Make sure to configure the input and output paths as required for your specific run. Note that the command-line arguments must follow the specified order and format. If any of the arguments are missing or invalid, the program will terminate with an appropriate error message.

4.2.2 Implementation. Algorithm 1 summarizes the most substantial part of our implementation, namely the logic that is implemented inside the mappers of our solution. At every execution of the map function, a DNA sequence line is given as input to the mapper. The latter is responsible for populating all possible subsequences of length 2, 3 and 4. We employ a sliding window that is nested inside a for-loop defining the subsequence length. The source code implementation of Algorithm 1 can be found in the `DNASequenceProcessor.java` file.

4.2.3 Evaluation. Our solution is tested using the provided DNA sequence, namely `ecoli.txt`. We list the execution results in Appendix C.

5 Problem 4: Probabilistic graph

We discuss here the fourth problem of the assignment. The main target of the assignment is to get acquainted with performing various MapReduce phases on a pipeline frame.

5.1 Problem Statement

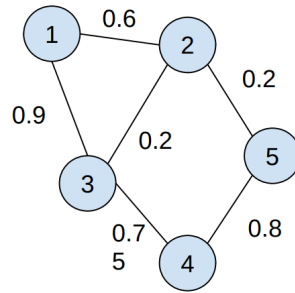
We are given an input file in text format where each line contains a connection between two vertices of a network and a probability value. For each edge e , there is a probability value $p(e)$ which indicates the probability that the two vertices are connected by the edge. Obviously, the values of $p(e)$ range between 0 and 1. The values in each line are separated by a space. Consider the network shown in the previous figure. The edge connecting vertices 4 and 5 has a probability of 0.8, the edge connecting vertices 2 and 3 has a probability of 0.2, etc.

The file corresponding to this graph would be:

1 2 0.6, 1 3 0.9, 2 3 0.2, 3 4 0.75, 2 5 0.2, 4 5 0.8,

The edges are generally stored in random order in the file, so we cannot assume they have a specific arrangement. The following tasks are requested:

- (1) Write a Java program that computes the average degree for all the vertices.
- (2) The average degree is defined as the sum of the probabilities of the edges that fall on a vertex.



- (3) For example, in the previous diagram, the average degree of vertex 3 is $0.9 + 0.2 + 0.75 = 1.85$.
- (4) Before performing this calculation, you should ignore all edges with a probability less than a threshold T , which should be passed as a parameter to the main function.
- (5) Modify the code from task 1 so that, at the end, only the vertices with an average degree greater than the average of the degrees of all the vertices are displayed in the output.

5.2 Proposed approach

5.2.1 Setting. Our implementation is run and tested in a Linux environment with 12 cores, using the Java programming language. We have used the Java Development Kit (JDK) version 11.0.11. The source code is developed in IntelliJ IDEA Community Edition 2021.1.1 and managed using Maven as the build tool.

The project's dependencies, including Hadoop libraries, are defined in the `pom.xml` file located in the root of the repository. The project is compiled and executed directly from IntelliJ IDEA.

To run the project, open the `GraphMaster` class in IntelliJ IDEA, and execute the main method. You will need to specify the following command-line arguments:

- `<input_path>` specifies the directory containing the input text files, located at `map-reduce/ probabilisticGraph /input`.
- `<output_path>` specifies the directory where the MapReduce output will be written, which will be created in the `out` folder.
- `<T>` is the minimum edge-degree threshold for vertices to be included in the results.

IntelliJ IDEA will handle the compilation and execution automatically when the main method is run. Make sure to configure the input and output paths as required for your specific run.

Note that the command-line arguments must follow the specified order and format. If any of the arguments are missing or invalid, the program will terminate with an appropriate error message.

5.2.2 Implementation. The problem at hand involves processing a probabilistic graph, where each edge connects two vertices with a probability value. The task is to compute the average degree for each vertex, considering only edges whose probability exceeds a given threshold T . The methodology proposed here utilizes a distributed MapReduce framework, implemented using Hadoop, to efficiently process and analyze large-scale graph data. The approach is divided into three main phases, each handled by separate MapReduce jobs, with intermediate results passed between the phases.

The `GraphMaster` class serves as the orchestrator of the entire MapReduce process. It manages the execution of the three phases, invoking the appropriate MapReduce jobs in sequence. The main steps executed by `GraphMaster` are:

- (1) It retrieves the command-line arguments, including the input and output directories as well as the threshold value T , which determines which edges to consider in the graph.

- (2) It initiates the first MapReduce job to compute the degree of each vertex in the graph. The input consists of edge data, and the output is a summation of edge probabilities for each vertex.
- (3) After the first job completes, the GraphMaster starts the second MapReduce job to calculate the mean degree of the graph, using the results from the first job.
- (4) Once the mean degree is computed, GraphMaster starts the third MapReduce job, which filters out the vertices with degrees lower than the mean degree.
- (5) It cleans up intermediate directories after each phase and moves the final output to the desired location.

GraphMaster coordinates these steps by configuring and executing the MapReduce jobs, ensuring that each phase depends on the results of the previous one.

The entire process consists of three MapReduce jobs, executed sequentially:

- (1) **Phase 1:** The first job computes the degree of each vertex by summing the probabilities of the edges connected to it. It produces intermediate results for each vertex.
- (2) **Phase 2:** The second job calculates the mean degree by summing the degrees from the first phase and dividing by the total number of vertices.
- (3) **Phase 3:** The third job filters out the vertices with a degree lower than the mean degree and produces the final filtered result.

After each job completes, intermediate data is written to disk and passed as input to the subsequent job. The final output consists of the vertices whose degree exceeds or equals the mean degree.

Phase 1: Calculating Vertex Degree The first MapReduce job is responsible for calculating the degree of each vertex in the graph, where the degree is defined as the sum of the probabilities of the edges connected to that vertex. The degree of each vertex is computed by the GraphMapper and GraphReducer classes.

The GraphMapper class reads each edge from the input data, which consists of lines containing two vertices and the associated probability value. It splits each line into two components (the two vertices), and for each vertex, it emits the corresponding probability value as the output. The mapper also checks if the probability value exceeds the threshold T , which is provided as a configuration parameter. If the probability is greater than or equal to T , it emits the vertex along with the corresponding probability.

The GraphReducer class receives the vertex and associated probability values emitted by the mapper. For each vertex, it sums up all the probabilities of the edges connected to that vertex, and emits the pair as output.

Phase 2: Calculating the Mean Degree The second phase of the approach calculates the mean degree of all vertices. This is done by summing the degree values from the previous phase and dividing by the total number of vertices.

The MeanMapper class receives the degree values from the output of the first MapReduce job. It emits two key-value pairs for each input line: a count of the number of vertices and the sum of the degree values. These are emitted with fixed keys ("count" and "sum") so that they can be aggregated in the reducer.

The MeanReducer class processes the count and sum values emitted by the mapper. It calculates the total sum and count of vertices and then writes these values as output. The mean degree is calculated by dividing the sum by the count, and the result is stored for use in the next phase.

Phase 3: Filtering Vertices by Mean Degree In the third phase, the vertices whose degree is greater than or equal to the mean degree calculated in Phase 2 are selected. This phase uses the results from Phase 1 and Phase 2, applying the filtering criteria to retain only those vertices with a degree greater than or equal to the mean.

The FilterMapper class takes the degree values emitted by the first reducer and writes them as key-value pairs. Each key is a vertex, and the value is the degree of that vertex. The mapper does not perform any filtering; instead, it simply passes the values along to the reducer.

The `FilterReducer` class filters out the vertices whose degree is less than the mean degree. It retrieves the mean degree from the configuration, and for each vertex, it compares the degree value to the mean. If the degree is greater than or equal to the mean, it emits the vertex along with its degree. This final output contains only the vertices that satisfy the filtering criteria.

5.2.3 Evaluation. The experiments were executed using the dataset ‘collins.txt’ with a parameter setting of $T = 0.8$.

To provide a comprehensive overview, the results of the experiment, including the detailed values derived from the dataset, are presented in subsection C.1 in a 2-column format.

6 Conclusion

In this document we have presented our solutions and rationale for solving the second assignment of the M.Sc. course on *Technologies for Big Data Analysis*, offered by the *DWS M.Sc. Program*. For each one of the four problems of the assignment, we have presented their statement, as well as the solution approach we have adopted. All execution results with the provided datasets can be found in the appendices of our work.

A Problem 1 execution results

In the following 8-columned pages, the experimental results of section's 2 problem are presented, as the raw output of the MapReduce execution.

a10c: 34	a14e: 16	a6g: 214	a9d: 531	b3e: 11	b6h: 123	b8y: 78	c12s: 173
a10d: 486	a14n: 114	a6h: 21	a9e: 369	b3g: 145	b6i: 20	b9a: 26	c12t: 45
a10e: 386	a14s: 16	a6k: 151	a9g: 548	b3r: 22	b6l: 39	b9d: 95	c12y: 124
a10g: 175	a14t: 17	a6l: 192	a9l: 62	b3t: 5674	b6m: 41	b9e: 232	c13d: 80
a10h: 58	a14y: 38	a6m: 20	a9n: 555	b3w: 35	b6n: 329	b9g: 271	c13e: 35
a10l: 131	a15s: 33	a6n: 456	a9r: 235	b3x: 66	b6r: 436	b9h: 18	c13g: 61
a10m: 15	a16s: 18	a6p: 84	a9s: 622	b3y: 223	b6s: 390	b9i: 161	c13l: 29
a10n: 260	a3d: 38224	a6r: 523	a9t: 287	b4d: 268	b6t: 347	b9l: 175	c13n: 220
a10p: 48	a3e: 3767	a6s: 1197	a9v: 38	b4e: 883	b6u: 17	b9n: 274	c13s: 379
a10r: 68	a3k: 248	a6t: 811	a9y: 286	b4f: 10	b6w: 15	b9r: 19	c13y: 83
a10s: 429	a3l: 4077	a6w: 1078	b10a: 17	b4g: 96	b6y: 181	b9s: 163	c14a: 14
a10t: 72	a3m: 353	a6y: 204	b10d: 86	b4h: 538	b7a: 31	b9t: 150	c14c: 94
a10y: 190	a3o: 106	a7a: 431	b10e: 58	b4k: 969	b7c: 25	b9y: 19	c14e: 47
a10z: 50	a3r: 198	a7c: 52	b10g: 28	b4l: 288	b7d: 248	c10a: 49	c14l: 93
a11a: 36	a3t: 428	a7d: 1076	b10l: 20	b4m: 16	b7e: 1005	c10d: 460	c14n: 20
a11c: 36	a3y: 1193	a7e: 685	b10m: 12	b4n: 2688	b7g: 339	c10e: 395	c14s: 84
a11d: 165	a4a: 458	a7g: 71	b10n: 13	b4r: 102	b7h: 371	c10g: 362	c14y: 29
a11e: 136	a4d: 166	a7h: 12	b10r: 33	b4s: 119	b7i: 31	c10l: 129	c15d: 11
a11g: 101	a4e: 249	a7l: 116	b10s: 227	b4t: 458	b7k: 28	c10n: 689	c15e: 12
a11n: 202	a4h: 13	a7n: 83	b10t: 43	b4w: 98	b7l: 16	c10r: 18	c15s: 24
a11p: 16	a4n: 15	a7r: 843	b10y: 10	b4y: 459	b7m: 61	c10s: 818	c15y: 18
a11r: 13	a4o: 773	a7s: 1203	b11a: 10	b5a: 77	b7n: 861	c10t: 97	c16e: 39
a11s: 266	a4s: 483	a7t: 1011	b11d: 79	b5d: 934	b7o: 15	c10y: 256	c16f: 10
a11t: 115	a4t: 47	a7x: 17	b11g: 15	b5e: 330	b7r: 238	c11a: 21	c3b: 34
a11y: 119	a4y: 1588	a7y: 756	b11m: 34	b5f: 29	b7s: 741	c11d: 116	c3n: 872
a12c: 18	a5a: 41	a8a: 28	b11n: 21	b5g: 1080	b7t: 494	c11e: 272	c3p: 117
a12d: 94	a5d: 1360	a8c: 37	b11o: 48	b5h: 103	b7u: 16	c11g: 141	c3t: 210
a12e: 95	a5e: 1377	a8d: 1790	b11s: 75	b5k: 342	b7y: 196	c11l: 92	c3y: 140
a12g: 47	a5g: 841	a8e: 386	b11t: 13	b5l: 11	b8a: 121	c11n: 403	c4a: 35
a12l: 20	a5i: 11	a8g: 625	b11y: 19	b5m: 29	b8d: 308	c11p: 12	c4b: 72
a12n: 65	a5l: 112	a8h: 328	b12d: 36	b5n: 1190	b8e: 83	c11r: 16	c4d: 333
a12s: 139	a5m: 56	a8l: 125	b12e: 20	b5r: 60	b8g: 451	c11s: 341	c4e: 2548
a12t: 59	a5n: 916	a8m: 239	b12g: 10	b5s: 1288	b8h: 15	c11t: 74	c4f: 18
a12y: 36	a5r: 1604	a8n: 982	b12l: 18	b5t: 212	b8l: 55	c11y: 181	c4k: 36
a13e: 10	a5s: 213	a8r: 98	b12s: 25	b5w: 111	b8m: 41	c12d: 107	c4l: 246
a13g: 19	a5t: 1767	a8s: 469	b12t: 10	b5y: 101	b8n: 53	c12e: 284	c4m: 88
a13n: 22	a5w: 94	a8t: 440	b12w: 10	b6a: 42	b8o: 105	c12g: 46	c4n: 92
a13s: 112	a5y: 201	a8x: 10	b12y: 21	b6d: 865	b8r: 55	c12h: 11	c4p: 105
a13t: 36	a6a: 112	a8y: 328	b13e: 10	b6e: 3041	b8s: 795	c12l: 15	c4r: 31
a13y: 36	a6d: 785	a9a: 27	b13v: 13	b6f: 52	b8t: 62	c12n: 673	c4s: 42
a14c: 12	a6e: 615	a9c: 23	b3d: 352	b6g: 84	b8v: 148	c12r: 10	c4t: 739

c4w: 12	c7t: 612	d11l: 23	d4r: 935	d8c: 93	e12a: 11	e6g: 39	e9y: 634
c4y: 285	c7x: 23	d11m: 17	d4s: 900	d8d: 903	e12c: 16	e6h: 189	f10d: 228
c5a: 45	c7y: 1192	d11n: 352	d4t: 713	d8e: 536	e12d: 49	e6i: 12	f10e: 83
c5c: 10	c8a: 125	d11s: 176	d4u: 19	d8g: 305	e12g: 79	e6m: 10	f10g: 95
c5d: 2428	c8c: 46	d11t: 121	d4w: 203	d8h: 52	e12l: 13	e6n: 28	f10h: 29
c5e: 804	c8d: 582	d11y: 63	d4y: 161	d8k: 15	e12n: 38	e6r: 335	f10n: 128
c5f: 320	c8e: 638	d12d: 112	d5a: 11	d8l: 119	e12s: 88	e6s: 496	f10p: 42
c5g: 24	c8g: 570	d12e: 70	d5d: 114	d8m: 37	e12t: 23	e6t: 710	f10r: 20
c5h: 168	c8h: 26	d12g: 44	d5e: 296	d8n: 272	e12y: 20	e6y: 213	f10s: 124
c5i: 18	c8l: 573	d12l: 21	d5g: 250	d8r: 296	e13n: 15	e7a: 18	f10t: 63
c5k: 237	c8n: 523	d12n: 162	d5h: 374	d8s: 475	e13s: 59	e7c: 69	f10v: 12
c5l: 318	c8o: 18	d12s: 168	d5k: 109	d8t: 183	e13t: 75	e7d: 1198	f10y: 242
c5m: 77	c8r: 285	d12t: 32	d5l: 77	d8v: 284	e13y: 91	e7e: 588	f11d: 19
c5n: 161	c8s: 2081	d12y: 37	d5m: 43	d8y: 138	e14g: 10	e7g: 279	f11e: 46
c5p: 33	c8t: 341	d13d: 84	d5n: 209	d9a: 31	e14s: 24	e7h: 213	f11g: 73
c5r: 479	c8x: 16	d13e: 52	d5s: 415	d9d: 793	e14y: 14	e7l: 29	f11l: 21
c5s: 1360	c8y: 394	d13g: 13	d5t: 305	d9e: 326	e3a: 11	e7m: 11	f11n: 42
c5t: 1031	c9a: 39	d13n: 63	d5y: 245	d9g: 169	e3c: 18	e7n: 255	f11s: 142
c5y: 130	c9d: 1289	d13s: 29	d6a: 39	d9m: 14	e3d: 456	e7o: 10	f11t: 15
c6a: 44	c9e: 440	d13t: 13	d6d: 313	d9n: 202	e3e: 137	e7r: 569	f11y: 59
c6c: 40	c9g: 137	d14d: 17	d6e: 549	d9r: 48	e3r: 45	e7s: 575	f12g: 14
c6d: 871	c9l: 41	d14g: 16	d6g: 566	d9s: 855	e3t: 67	e7t: 209	f12n: 11
c6e: 1144	c9m: 42	d14n: 27	d6h: 10	d9t: 470	e4a: 12	e7v: 28	f12s: 33
c6g: 247	c9n: 616	d14s: 10	d6i: 14	d9v: 26	e4e: 304	e7y: 234	f13s: 10
c6h: 125	c9r: 485	d14t: 11	d6l: 146	d9y: 257	e4h: 409	e8a: 11	f3d: 18
c6l: 61	c9s: 836	d14y: 13	d6m: 27	e10c: 57	e4l: 53	e8c: 152	f3e: 47
c6m: 30	c9t: 198	d15n: 31	d6n: 177	e10d: 104	e4n: 941	e8d: 864	f3g: 340
c6n: 676	c9v: 10	d15s: 19	d6r: 617	e10e: 256	e4r: 253	e8e: 572	f3n: 26
c6r: 706	c9y: 381	d3c: 10	d6s: 281	e10g: 553	e4s: 1113	e8g: 232	f3o: 17
c6s: 929	d10a: 113	d3d: 1874	d6t: 341	e10h: 23	e4t: 149	e8l: 107	f3r: 7246
c6t: 568	d10c: 142	d3e: 335	d6y: 154	e10l: 67	e4y: 129	e8m: 19	f3t: 128
c6x: 23	d10d: 345	d3g: 71	d7b: 13	e10m: 91	e5a: 13	e8n: 348	f3w: 453
c6y: 363	d10e: 169	d3m: 55	d7c: 21	e10n: 431	e5d: 43	e8r: 62	f3x: 44
c7a: 23	d10g: 194	d3n: 29	d7d: 989	e10s: 136	e5e: 56	e8s: 531	f3y: 33
c7c: 148	d10l: 29	d3s: 11	d7e: 1011	e10t: 195	e5h: 117	e8t: 40	f4d: 493
c7d: 1329	d10n: 175	d3y: 882	d7g: 439	e10y: 610	e5k: 85	e8y: 174	f4e: 2351
c7e: 561	d10r: 15	d4a: 19	d7l: 18	e11a: 49	e5l: 164	e9c: 42	f4g: 31
c7g: 328	d10s: 211	d4d: 284	d7n: 43	e11d: 331	e5n: 46	e9d: 544	f4h: 16
c7h: 15	d10t: 120	d4e: 602	d7o: 10	e11e: 20	e5r: 210	e9e: 386	f4i: 27
c7k: 80	d10v: 44	d4g: 27	d7p: 56	e11g: 29	e5s: 98	e9g: 244	f4k: 35
c7l: 690	d10y: 259	d4h: 19	d7r: 107	e11l: 62	e5t: 327	e9h: 75	f4l: 859
c7m: 35	d11a: 13	d4k: 187	d7s: 665	e11m: 20	e5w: 87	e9l: 122	f4m: 6376
c7n: 703	d11d: 205	d4l: 170	d7t: 220	e11n: 195	e5y: 1240	e9n: 283	f4p: 28
c7o: 27	d11e: 106	d4m: 29	d7v: 366	e11s: 134	e6a: 13	e9r: 31	f4r: 444
c7r: 658	d11g: 78	d4n: 1183	d7y: 183	e11t: 95	e6d: 174	e9s: 330	f4s: 73
c7s: 834	d11h: 32	d4p: 258	d8a: 46	e11y: 115	e6e: 651	e9t: 153	f4t: 1443

f4w: 96	f8m: 21	g3t: 752	g7p: 15	h12s: 90	h6r: 443	i10y: 163	i5c: 25
f4x: 11	f8n: 226	g3y: 33	g7r: 167	h13d: 13	h6s: 1051	i11d: 212	i5e: 118
f4y: 21	f8r: 152	g4d: 855	g7s: 328	h13s: 20	h6t: 96	i11e: 172	i5h: 20
f5a: 22	f8s: 473	g4e: 1349	g7t: 31	h3d: 7393	h6w: 55	i11g: 127	i5l: 32
f5d: 1113	f8t: 118	g4f: 13	g7y: 216	h3e: 11	h6y: 274	i11l: 15	i5n: 39
f5e: 402	f8y: 223	g4l: 185	g8c: 29	h3m: 5193	h7a: 16	i11m: 10	i5r: 65
f5g: 32	f9a: 17	g4m: 20	g8d: 221	h3p: 37	h7d: 544	i11n: 300	i5s: 91
f5h: 404	f9c: 12	g4n: 91	g8e: 185	h3r: 5252	h7e: 44	i11r: 23	i5t: 20
f5k: 140	f9d: 147	g4p: 14	g8g: 232	h3s: 11727	h7f: 1487	i11s: 229	i5x: 17
f5l: 132	f9e: 131	g4s: 269	g8l: 37	h3t: 268	h7g: 535	i11t: 191	i5y: 73
f5n: 23	f9g: 266	g4t: 44	g8n: 73	h3w: 1296	h7h: 13	i11y: 354	i6a: 11
f5r: 353	f9h: 26	g4w: 255	g8r: 139	h3y: 47	h7l: 48	i12d: 19	i6c: 10
f5s: 867	f9k: 31	g4y: 110	g8s: 306	h4d: 2139	h7m: 25	i12e: 359	i6d: 291
f5t: 1749	f9l: 51	g5a: 40	g8t: 83	h4e: 4797	h7n: 48	i12g: 33	i6e: 216
f5y: 346	f9n: 454	g5d: 278	g8y: 37	h4f: 251	h7r: 466	i12l: 55	i6f: 264
f6a: 61	f9o: 16	g5e: 276	g9a: 19	h4g: 59	h7s: 490	i12n: 505	i6m: 34
f6d: 958	f9r: 24	g5f: 47	g9d: 33	h4h: 286	h7t: 118	i12s: 141	i6n: 64
f6e: 500	f9s: 309	g5g: 369	g9e: 65	h4k: 11	h7y: 683	i12t: 52	i6s: 110
f6g: 183	f9t: 53	g5h: 15	g9g: 188	h4l: 277	h8c: 47	i12y: 145	i6t: 119
f6h: 1159	f9y: 59	g5i: 10	g9n: 179	h4m: 38	h8d: 313	i13e: 100	i6y: 127
f6l: 60	g10a: 20	g5m: 59	g9r: 45	h4n: 22	h8e: 182	i13l: 51	i7a: 32
f6n: 122	g10d: 16	g5n: 594	g9s: 160	h4o: 53	h8g: 47	i13n: 35	i7d: 420
f6o: 13	g10g: 52	g5p: 168	g9t: 37	h4p: 259	h8h: 10	i13r: 20	i7e: 352
f6r: 892	g10n: 37	g5s: 549	g9y: 190	h4r: 557	h8l: 66	i13s: 32	i7g: 18
f6s: 520	g10r: 12	g5t: 935	h10a: 55	h4s: 66	h8n: 150	i13t: 33	i7h: 14
f6t: 319	g10s: 120	g5y: 136	h10c: 17	h4t: 229	h8o: 22	i13y: 222	i7l: 35
f6w: 344	g10t: 643	g6a: 13	h10d: 35	h4y: 50	h8s: 254	i14e: 26	i7n: 37
f6y: 435	g10y: 40	g6d: 281	h10e: 22	h5d: 709	h8t: 33	i14n: 20	i7s: 296
f7a: 76	g11d: 60	g6e: 336	h10g: 26	h5e: 1028	h8y: 89	i14s: 16	i7t: 134
f7d: 590	g11g: 22	g6g: 256	h10h: 21	h5h: 23	h9a: 19	i14y: 13	i7y: 44
f7e: 324	g11l: 21	g6h: 223	h10l: 76	h5i: 10	h9c: 10	i15y: 17	i8a: 25
f7g: 756	g11m: 126	g6l: 22	h10n: 44	h5l: 22	h9d: 139	i16e: 39	i8d: 845
f7h: 48	g11n: 89	g6n: 305	h10s: 207	h5n: 184	h9e: 136	i3e: 78	i8e: 317
f7l: 282	g11r: 20	g6p: 63	h10y: 38	h5o: 10	h9g: 70	i3i: 91	i8g: 88
f7m: 220	g11s: 71	g6r: 47	h11a: 19	h5r: 193	h9k: 10	i3k: 12	i8l: 221
f7n: 410	g12d: 10	g6s: 717	h11c: 13	h5s: 1072	h9n: 61	i3l: 278	i8m: 41
f7r: 333	g12l: 16	g6t: 10	h11d: 17	h5t: 311	h9s: 256	i3n: 24	i8n: 96
f7s: 1066	g12s: 74	g6y: 229	h11e: 143	h5y: 509	h9t: 18	i3s: 2045	i8r: 90
f7t: 43	g13y: 10	g7a: 83	h11g: 21	h6a: 30	h9y: 121	i4a: 188	i8s: 247
f7y: 265	g14g: 10	g7d: 366	h11n: 16	h6c: 33	i10d: 309	i4e: 25	i8t: 414
f8d: 604	g18g: 13	g7e: 126	h11s: 32	h6d: 321	i10e: 645	i4h: 11	i8y: 305
f8e: 190	g3d: 305	g7g: 314	h11y: 13	h6e: 212	i10g: 134	i4n: 128	i9a: 14
f8g: 218	g3m: 13	g7h: 19	h12a: 17	h6g: 718	i10l: 234	i4o: 2120	i9d: 418
f8h: 39	g3n: 54	g7l: 848	h12c: 12	h6h: 170	i10n: 306	i4s: 12	i9e: 538
f8k: 11	g3p: 44	g7m: 25	h12f: 55	h6i: 14	i10s: 253	i4t: 50	i9g: 250
f8l: 56	g3s: 11	g7n: 29	h12g: 12	h6n: 214	i10t: 99	i5a: 23	i9h: 35

i9l: 24	j8y: 72	k9i: 17	l5e: 965	l9r: 46	m4h: 671	m7r: 38	n11s: 35
i9n: 557	j9d: 21	k9s: 32	l5g: 114	l9s: 137	m4k: 98	m7s: 1188	n11t: 16
i9r: 89	j9n: 108	k9t: 22	l5h: 291	l9y: 53	m4l: 32	m7t: 11	n11y: 62
i9s: 381	j9s: 24	l10d: 24	l5l: 303	m10c: 11	m4n: 233	m7y: 221	n12d: 18
i9t: 371	j9y: 17	l10e: 52	l5n: 102	m10d: 82	m4s: 396	m8a: 24	n12g: 18
i9w: 34	k11a: 25	l10g: 13	l5r: 934	m10e: 72	m4t: 2077	m8c: 41	n12s: 83
i9y: 124	k11d: 10	l10n: 42	l5s: 739	m10g: 27	m4y: 1246	m8d: 222	n13d: 18
j10n: 23	k11n: 15	l10p: 56	l5t: 480	m10l: 50	m5a: 308	m8e: 505	n13n: 33
j10s: 33	k3y: 23	l10s: 135	l5y: 49	m10m: 13	m5c: 59	m8g: 123	n13s: 12
j12n: 27	k4d: 194	l10t: 27	l6a: 41	m10n: 58	m5d: 312	m8i: 56	n15d: 12
j13e: 10	k4e: 135	l10y: 15	l6d: 1083	m10r: 12	m5e: 66	m8k: 29	n17s: 13
j13n: 15	k4g: 211	l11d: 16	l6e: 1215	m10s: 199	m5h: 389	m8l: 137	n3p: 10
j3w: 33	k4l: 64	l11e: 112	l6g: 269	m10t: 63	m5l: 109	m8m: 17	n3r: 275
j3y: 103	k4n: 35	l11g: 15	l6h: 66	m10y: 69	m5m: 27	m8n: 158	n3t: 6590
j4e: 80	k4p: 151	l11n: 56	l6l: 31	m11a: 133	m5n: 51	m8r: 283	n3w: 2862
j4k: 10	k4s: 59	l11s: 40	l6n: 315	m11d: 16	m5o: 12	m8s: 535	n4d: 156
j4n: 208	k4t: 279	l11y: 10	l6r: 930	m11e: 51	m5r: 150	m8t: 448	n4e: 683
j4p: 13	k4v: 17	l12a: 19	l6s: 314	m11g: 26	m5s: 701	m8y: 608	n4k: 193
j4s: 45	k4w: 1529	l12d: 13	l6t: 52	m11i: 81	m5t: 832	m9a: 25	n4l: 58
j4t: 773	k5e: 45	l12g: 11	l6x: 25	m11n: 10	m5y: 567	m9c: 18	n4r: 286
j4y: 62	k5k: 12	l12n: 22	l6y: 241	m11r: 10	m6a: 46	m9d: 138	n4s: 237
j5e: 106	k5l: 48	l12s: 129	l7c: 10	m11s: 90	m6d: 390	m9e: 125	n4t: 281
j5n: 22	k5n: 379	l13n: 11	l7d: 391	m11t: 20	m6e: 621	m9g: 46	n4y: 35
j5s: 137	k5s: 255	l13s: 19	l7e: 80	m11y: 26	m6f: 223	m9h: 10	n5d: 75
j5t: 329	k5y: 18	l3d: 274	l7g: 952	m12d: 10	m6g: 365	m9i: 28	n5e: 457
j5y: 14	k6a: 26	l3e: 109	l7l: 90	m12e: 155	m6l: 117	m9l: 28	n5h: 222
j6d: 170	k6d: 279	l3g: 157	l7n: 92	m12h: 22	m6m: 62	m9m: 24	n5i: 10
j6e: 10	k6r: 22	l3p: 63	l7r: 47	m12n: 24	m6n: 227	m9n: 49	n5l: 79
j6g: 19	k6s: 52	l3s: 20	l7s: 505	m12r: 32	m6o: 72	m9o: 30	n5o: 22
j6h: 47	k6y: 118	l3t: 573	l7t: 46	m12s: 88	m6r: 1005	m9r: 36	n5r: 590
j6l: 53	k7a: 20	l3w: 486	l7v: 10	m12y: 31	m6s: 452	m9s: 505	n5s: 189
j6s: 239	k7d: 49	l3y: 289	l7y: 211	m13g: 38	m6t: 569	m9t: 124	n5t: 335
j6t: 39	k7e: 29	l4b: 213	l8d: 221	m13l: 11	m6u: 10	m9y: 92	n5y: 58
j6y: 49	k7g: 213	l4d: 791	l8e: 195	m13n: 29	m6v: 12	n10a: 11	n6a: 20
j7e: 83	k7h: 15	l4e: 3014	l8g: 201	m13s: 160	m6w: 803	n10c: 16	n6d: 138
j7g: 71	k7m: 24	l4g: 942	l8n: 79	m14s: 65	m6x: 10	n10d: 20	n6e: 345
j7n: 87	k7n: 117	l4h: 10	l8r: 97	m15s: 10	m6y: 443	n10e: 41	n6g: 13
j7r: 20	k7s: 39	l4k: 658	l8s: 142	m3b: 26	m7a: 163	n10g: 23	n6i: 10
j7s: 26	k7v: 448	l4n: 42	l8t: 42	m3d: 61	m7c: 23	n10h: 21	n6l: 107
j7y: 127	k8a: 21	l4p: 53	l8y: 75	m3n: 2654	m7d: 388	n10k: 18	n6n: 210
j8e: 15	k8f: 11	l4s: 1182	l9a: 102	m3p: 40	m7e: 302	n10n: 29	n6r: 379
j8g: 12	k8g: 26	l4t: 1734	l9c: 23	m3s: 58	m7g: 624	n10s: 57	n6s: 243
j8l: 26	k8s: 131	l4y: 164	l9d: 105	m3t: 547	m7h: 27	n10y: 30	n6t: 10
j8n: 52	k8v: 70	l5a: 17	l9e: 45	m3y: 2535	m7l: 178	n11g: 24	n6w: 77
j8s: 46	k8y: 70	l5c: 15	l9g: 121	m4d: 514	m7m: 40	n11m: 22	n6y: 268
j8t: 34	k9e: 71	l5d: 371	l9n: 29	m4e: 3829	m7n: 265	n11n: 11	n7a: 1119

n7d: 203	o12g: 17	o7c: 14	p10s: 413	p4n: 463	p7t: 1435	q6s: 12	r14y: 39
n7e: 76	o12n: 94	o7d: 336	p10t: 142	p4p: 11	p7x: 39	q6y: 15	r15s: 104
n7g: 662	o12s: 23	o7e: 273	p10y: 317	p4r: 186	p7y: 237	q7l: 31	r3b: 10
n7k: 12	o12y: 91	o7f: 26	p11c: 22	p4s: 205	p8a: 149	q7r: 62	r3d: 252
n7l: 164	o13s: 108	o7g: 151	p11d: 50	p4t: 1040	p8c: 136	q7y: 276	r3e: 18
n7n: 10	o3d: 1140	o7k: 10	p11e: 166	p4y: 256	p8d: 819	q8d: 17	r3g: 12
n7r: 179	o3e: 3233	o7n: 232	p11g: 88	p5a: 255	p8e: 1405	q8n: 339	r3m: 24
n7s: 364	o3f: 625	o7r: 491	p11n: 117	p5c: 17	p8g: 312	q8s: 77	r3n: 458
n7t: 73	o3g: 15	o7s: 236	p11r: 25	p5d: 98	p8h: 16	q8y: 38	r3p: 15
n7y: 71	o3h: 13	o7t: 11	p11s: 289	p5e: 1330	p8i: 16	q9d: 28	r3t: 11
n8a: 25	o3k: 27	o7y: 47	p11t: 24	p5f: 30	p8k: 12	q9g: 18	r3w: 79
n8d: 33	o3l: 33	o8a: 30	p11y: 240	p5h: 143	p8l: 356	q9s: 218	r4d: 472
n8e: 134	o3n: 777	o8d: 564	p12a: 159	p5k: 10	p8m: 66	r10d: 398	r4e: 1174
n8g: 64	o3r: 1064	o8e: 194	p12d: 37	p5l: 69	p8n: 539	r10e: 234	r4f: 30
n8l: 288	o3t: 1956	o8g: 69	p12e: 46	p5n: 102	p8r: 160	r10g: 175	r4g: 78
n8n: 619	o4d: 13	o8h: 12	p12g: 14	p5o: 26	p8s: 2343	r10l: 75	r4h: 129
n8p: 11	o4e: 567	o8k: 37	p12l: 106	p5p: 31	p8t: 221	r10m: 39	r4k: 124
n8r: 84	o4h: 27	o8l: 189	p12n: 115	p5r: 766	p8y: 390	r10n: 640	r4l: 129
n8s: 932	o4l: 24	o8m: 34	p12r: 13	p5s: 870	p9a: 56	r10r: 11	r4m: 905
n8y: 47	o4n: 302	o8n: 59	p12s: 131	p5t: 299	p9c: 35	r10s: 168	r4n: 90
n9a: 35	o4o: 159	o8r: 29	p12t: 18	p5y: 332	p9d: 714	r10t: 29	r4o: 22
n9d: 68	o4r: 1263	o8s: 467	p12y: 223	p6a: 44	p9e: 216	r10y: 99	r4p: 11
n9e: 56	o4s: 213	o8t: 117	p13e: 19	p6c: 307	p9g: 257	r11d: 110	r4r: 49
n9g: 16	o4y: 1890	o8w: 18	p13g: 10	p6d: 1413	p9h: 43	r11e: 78	r4s: 142
n9i: 66	o5a: 16	o8y: 100	p13k: 11	p6e: 4994	p9l: 405	r11g: 87	r4t: 262
n9l: 17	o5d: 19	o9a: 13	p13l: 20	p6g: 85	p9m: 20	r11h: 14	r4y: 39
n9n: 23	o5e: 27	o9d: 111	p13n: 38	p6h: 106	p9n: 169	r11l: 13	r5d: 675
n9r: 23	o5g: 44	o9e: 220	p13r: 22	p6l: 75	p9o: 13	r11n: 151	r5e: 195
n9s: 168	o5m: 23	o9g: 218	p13s: 62	p6n: 277	p9r: 73	r11s: 259	r5h: 130
n9t: 53	o5n: 465	o9h: 11	p13y: 20	p6o: 11	p9s: 633	r11t: 28	r5l: 142
n9y: 486	o5r: 2249	o9n: 252	p14s: 14	p6r: 213	p9t: 494	r11y: 55	r5m: 20
o10d: 65	o5s: 20	o9p: 28	p15s: 11	p6s: 813	p9y: 262	r12d: 15	r5n: 75
o10e: 91	o5t: 173	o9s: 367	p3a: 11	p6t: 205	q10d: 23	r12e: 26	r5r: 210
o10g: 26	o5y: 12	o9t: 11	p3d: 19	p6w: 26	q10g: 13	r12g: 29	r5s: 525
o10h: 28	o6a: 76	o9w: 19	p3n: 31	p6y: 342	q10s: 20	r12n: 115	r5t: 714
o10l: 26	o6d: 243	o9y: 56	p3r: 88	p7a: 93	q11g: 27	r12s: 72	r5w: 12
o10n: 177	o6e: 181	p10a: 38	p3s: 170	p7c: 94	q13n: 10	r12y: 59	r5y: 426
o10s: 177	o6g: 17	p10c: 17	p3t: 465	p7d: 592	q13r: 16	r13d: 11	r6a: 185
o10y: 31	o6k: 100	p10d: 138	p3y: 123	p7e: 843	q14s: 26	r13e: 17	r6d: 791
o11d: 36	o6n: 171	p10e: 184	p4a: 67	p7g: 540	q3e: 16	r13n: 13	r6e: 290
o11g: 54	o6r: 13	p10g: 464	p4d: 122	p7k: 18	q4t: 11	r13s: 25	r6f: 65
o11n: 51	o6s: 913	p10h: 54	p4e: 410	p7l: 134	q5e: 500	r13y: 71	r6g: 174
o11s: 94	o6t: 159	p10l: 128	p4h: 115	p7m: 147	q5k: 75	r14e: 39	r6k: 46
o11y: 79	o6y: 47	p10m: 121	p4k: 99	p7n: 223	q5n: 18	r14g: 10	r6l: 115
o12a: 14	o6z: 22	p10n: 521	p4l: 60	p7r: 246	q5r: 13	r14n: 87	r6m: 135
o12d: 30	o7a: 31	p10r: 124	p4m: 39	p7s: 1374	q5t: 145	r14s: 24	r6n: 775

r6r: 415	s10o: 32	s16n: 14	s5w: 24	s8r: 325	t12h: 23	t5t: 146	t9e: 291
r6s: 464	s10r: 44	s16s: 10	s5y: 451	s8s: 1622	t12n: 10	t5w: 142	t9g: 139
r6t: 710	s10s: 469	s3a: 74	s6a: 44	s8t: 287	t12s: 121	t5y: 165	t9h: 45
r6v: 715	s10t: 204	s3b: 18	s6b: 12	s8v: 15	t12y: 42	t6a: 40	t9k: 31
r6w: 43	s10y: 114	s3c: 72	s6c: 51	s8x: 30	t13d: 10	t6d: 1075	t9l: 16
r6y: 402	s11a: 24	s3d: 87	s6d: 3507	s8y: 1160	t13e: 14	t6e: 817	t9n: 39
r7a: 32	s11c: 28	s3e: 4950	s6e: 1353	s9a: 35	t13n: 16	t6f: 115	t9o: 11
r7d: 1139	s11d: 98	s3m: 55	s6g: 824	s9c: 50	t13s: 23	t6g: 502	t9r: 13
r7e: 542	s11e: 98	s3n: 409	s6h: 368	s9d: 806	t13y: 18	t6h: 658	t9s: 250
r7g: 496	s11g: 154	s3r: 176	s6k: 162	s9e: 371	t14n: 32	t6l: 94	t9t: 406
r7h: 25	s11h: 43	s3t: 801	s6l: 238	s9g: 1178	t14s: 22	t6n: 384	t9x: 17
r7i: 15	s11l: 141	s3w: 600	s6m: 373	s9h: 14	t15n: 11	t6r: 481	t9y: 166
r7l: 179	s11m: 17	s3x: 160	s6n: 423	s9i: 67	t3a: 104	t6s: 1255	u10d: 775
r7n: 502	s11n: 206	s3y: 858	s6r: 559	s9k: 21	t3e: 79438	t6t: 198	u10e: 20
r7r: 111	s11r: 21	s4a: 109	s6s: 2097	s9l: 98	t3n: 223	t6x: 17	u10g: 69
r7s: 1095	s11s: 151	s4b: 23	s6t: 927	s9m: 13	t3o: 1608	t6y: 417	u10l: 22
r7t: 329	s11t: 51	s4d: 3697	s6w: 135	s9n: 429	t3p: 45	t7a: 30	u10n: 74
r7y: 473	s11w: 12	s4e: 3848	s6y: 689	s9o: 13	t3t: 20	t7c: 48	u10r: 12
r8c: 69	s11y: 108	s4f: 26	s7a: 153	s9r: 137	t3x: 75	t7d: 340	u10s: 23
r8d: 2212	s12d: 79	s4g: 123	s7b: 12	s9s: 1044	t3y: 137	t7e: 126	u10t: 56
r8e: 325	s12e: 107	s4h: 1441	s7c: 26	s9t: 194	t4d: 590	t7f: 32	u10y: 71
r8g: 237	s12g: 40	s4k: 207	s7d: 1327	s9y: 486	t4e: 2747	t7g: 579	u11d: 54
r8h: 68	s12h: 15	s4l: 309	s7e: 1364	t10a: 13	t4k: 903	t7h: 891	u11e: 78
r8l: 24	s12i: 17	s4m: 135	s7g: 1121	t10d: 74	t4l: 849	t7l: 104	u11g: 42
r8n: 327	s12n: 81	s4n: 1527	s7h: 163	t10e: 100	t4m: 2353	t7n: 101	u11s: 41
r8r: 184	s12r: 15	s4p: 361	s7i: 13	t10g: 49	t4n: 3322	t7o: 49	u11t: 15
r8s: 560	s12s: 239	s4r: 148	s7l: 555	t10h: 15	t4p: 45	t7r: 119	u11y: 111
r8t: 254	s12t: 10	s4s: 446	s7m: 74	t10l: 32	t4r: 83	t7s: 882	u12d: 29
r8y: 147	s12y: 148	s4t: 1025	s7n: 390	t10n: 41	t4s: 4312	t7t: 950	u12e: 43
r9c: 15	s13d: 49	s4w: 355	s7o: 14	t10r: 53	t4t: 12263	t7y: 163	u12s: 17
r9d: 317	s13e: 38	s4y: 85	s7r: 627	t10s: 521	t4u: 40	t8a: 23	u12y: 82
r9e: 186	s13g: 17	s5a: 449	s7s: 1252	t10t: 128	t4y: 3875	t8c: 32	u13d: 21
r9g: 642	s13l: 15	s5d: 886	s7t: 434	t10y: 60	t5a: 66	t8d: 414	u13e: 32
r9m: 32	s13n: 29	s5e: 2969	s7v: 34	t11d: 112	t5b: 50	t8e: 370	u13g: 85
r9n: 141	s13r: 10	s5f: 189	s7w: 29	t11e: 135	t5c: 30	t8g: 350	u13s: 10
r9r: 21	s13s: 67	s5g: 42	s7y: 655	t11g: 36	t5d: 552	t8h: 15	u13y: 43
r9s: 475	s13t: 43	s5h: 371	s8a: 29	t11h: 33	t5e: 6460	t8l: 76	u14e: 21
r9t: 164	s13y: 51	s5k: 522	s8c: 43	t11l: 27	t5f: 10	t8n: 157	u14y: 16
r9y: 15	s14e: 17	s5l: 2431	s8d: 882	t11n: 68	t5g: 303	t8o: 31	u15y: 10
s10c: 158	s14n: 11	s5m: 131	s8e: 550	t11r: 11	t5h: 365	t8r: 292	u16l: 15
s10d: 321	s14s: 29	s5n: 545	s8g: 1342	t11s: 324	t5k: 820	t8s: 365	u3e: 313
s10e: 125	s14t: 55	s5o: 17	s8h: 211	t11t: 32	t5l: 88	t8t: 34	u3m: 11
s10g: 230	s14y: 47	s5p: 350	s8k: 203	t11y: 34	t5n: 516	t8w: 120	u4a: 12
s10l: 69	s15n: 10	s5r: 145	s8l: 219	t12d: 29	t5p: 12	t8y: 235	u4d: 271
s10m: 50	s15r: 10	s5s: 1274	s8m: 19	t12e: 58	t5r: 3002	t9c: 48	u4h: 18
s10n: 196	s15y: 10	s5t: 1035	s8n: 509	t12g: 18	t5s: 1525	t9d: 151	u4n: 1106

u4o: 13	u8g: 38	v4l: 21	v7o: 10	w10s: 62	w5h: 4911	w8g: 108	y4d: 94
u5d: 52	u8l: 16	v4n: 136	v7r: 72	w11d: 34	w5l: 29	w8l: 16	y4k: 193
u5e: 192	u8n: 50	v4s: 60	v7s: 497	w11g: 21	w5n: 664	w8n: 44	y4r: 1539
u5g: 47	u8s: 67	v4t: 65	v7t: 68	w11s: 45	w5r: 194	w8o: 19	y5d: 33
u5l: 497	u8y: 68	v4w: 173	v7y: 265	w12d: 11	w5s: 1155	w8r: 176	y5e: 119
u5n: 265	u9d: 228	v4y: 1394	v8a: 153	w3b: 20	w5t: 165	w8s: 160	y5g: 622
u5r: 1283	u9e: 42	v5a: 93	v8d: 92	w3n: 74	w5y: 84	w8t: 10	y5h: 65
u5s: 17	u9g: 41	v5d: 61	v8e: 152	w3o: 2992	w6d: 743	w8w: 41	y5l: 76
u5t: 30	u9l: 77	v5e: 630	v8g: 35	w3r: 844	w6e: 45	w8y: 17	y5s: 656
u5y: 17	u9n: 40	v5l: 45	v8h: 31	w3s: 11367	w6g: 66	w9d: 139	y5v: 11
u6d: 608	u9s: 56	v5r: 25	v8l: 18	w3t: 64	w6h: 89	w9e: 35	y6d: 11
u6e: 216	u9t: 10	v5s: 296	v8n: 37	w3x: 21	w6m: 25	w9g: 81	y6s: 21
u6g: 15	u9y: 56	v5t: 134	v8r: 50	w3y: 1522	w6n: 580	w9i: 29	y6w: 55
u6l: 87	v10d: 18	v5x: 31	v8s: 242	w4d: 469	w6r: 152	w9k: 20	y7d: 16
u6n: 32	v10e: 18	v6a: 77	v8t: 25	w4e: 4923	w6s: 495	w9l: 33	y7g: 11
u6r: 19	v10n: 14	v6d: 93	v8y: 104	w4f: 56	w6t: 114	w9n: 96	y7r: 40
u6s: 336	v10r: 16	v6e: 97	v9a: 17	w4g: 47	w6w: 187	w9r: 37	y8f: 160
u6t: 45	v10s: 72	v6i: 214	v9e: 86	w4h: 9956	w6y: 187	w9s: 72	y8g: 20
u6y: 26	v10y: 46	v6l: 144	v9g: 20	w4k: 625	w7d: 411	w9t: 28	y8l: 15
u7a: 10	v11n: 12	v6m: 17	v9i: 12	w4l: 2928	w7e: 173	w9y: 21	y8n: 10
u7d: 96	v11y: 12	v6n: 29	v9l: 18	w4m: 556	w7g: 745	x3i: 74	y8t: 11
u7e: 19	v12n: 24	v6r: 17	v9n: 24	w4n: 2930	w7l: 10	x3v: 34	y9l: 11
u7g: 21	v13h: 11	v6s: 372	v9r: 12	w4p: 68	w7m: 60	x3x: 19	y9y: 56
u7l: 37	v13t: 20	v6t: 33	v9s: 164	w4r: 28	w7n: 260	x4i: 56	z4e: 23
u7m: 119	v3i: 32	v6y: 118	v9y: 46	w4s: 160	w7r: 503	x4y: 30	z4l: 24
u7n: 97	v3l: 80	v7a: 37	w10d: 28	w4t: 4856	w7s: 213	x5i: 33	z5m: 12
u7o: 42	v3n: 27	v7d: 31	w10e: 13	w4y: 16	w7t: 1070	x5s: 53	z6r: 12
u7s: 93	v4a: 72	v7e: 312	w10g: 28	w5d: 2652	w7w: 34	y10s: 20	z7s: 10
u7y: 591	v4d: 20	v7g: 42	w10l: 18	w5e: 3284	w7y: 80	y3s: 675	z7v: 37
u8d: 65	v4e: 171	v7k: 10	w10n: 180	w5f: 11	w8d: 187	y3t: 476	
u8e: 44	v4i: 39	v7n: 31	w10r: 21	w5g: 116	w8e: 13	y3u: 5361	

B Problem 2 execution results

We list here the execution results of our solution for the second problem (movie analytics) tested on the movies.csv dataset. Task 1 (duration per country) produces the following results:

Afghanistan: 815	Austria: 22925	Bolivia: 797	Cameroon: 615
Albania: 646	Bahamas: 560	Bosnia and Herzegovina: 2207	Canada: 210826
Algeria: 2115	Bahrain: 87	Botswana: 295	Chad: 493
American Samoa: 247	Bangladesh: 429	Brazil: 27333	Chile: 6178
Angola: 357	Barbados: 92	Bulgaria: 5430	China: 42089
Argentina: 28813	Belarus: 427	Burkina Faso: 903	Colombia: 3810
Armenia: 264	Belgium: 54192	Burma: 95	Congo: 88
Aruba: 739	Bermuda: 95	Cambodia: 894	Costa Rica: 431
Australia: 66068	Bhutan: 291		Croatia: 4340

Cuba: 2899	Iraq: 1365	Morocco: 4525	Somalia: 90
Cyprus: 948	Ireland: 26506	Namibia: 105	South Africa: 14688
Czech Republic: 15317	Isle Of Man: 396	Nepal: 797	South Korea: 56245
Czechoslovakia: 8434	Israel: 16662	Netherlands: 47054	Soviet Union: 51353
Côte d'Ivoire: 180	Italy: 288407	New Zealand: 14561	Spain: 116651
Denmark: 44186	Jamaica: 807	Nicaragua: 183	Sri Lanka: 318
Dominican Republic: 866	Japan: 178558	Nigeria: 494	Suriname: 105
East Germany: 2095	Jordan: 1313	North Korea: 508	Sweden: 68956
Ecuador: 893	Kazakhstan: 2145	Norway: 26476	Switzerland: 34516
Egypt: 3090	Kenya: 523	Pakistan: 1728	Syria: 447
El Salvador: 167	Korea: 90	Palestine: 1530	Taiwan: 16618
Estonia: 4651	Kosovo: 188	Panama: 903	Tajikistan: 351
Ethiopia: 537	Kuwait: 273	Papua New Guinea: 295	Tanzania: 441
Faroe Islands: 97	Kyrgyzstan: 400	Paraguay: 317	Thailand: 10189
Federal Republic of Yugoslavia: 2167	Laos: 289	Peru: 2436	The Democratic Republic Of Congo: 98
Finland: 48990	Latvia: 2297	Philippines: 7882	Trinidad and Tobago: 86
France: 467279	Lebanon: 1289	Poland: 35543	Tunisia: 2236
Gabon: 80	Liberia: 283	Portugal: 15232	Turkey: 20068
Georgia: 1846	Libya: 520	Puerto Rico: 1322	UK: 492616
Germany: 226808	Liechtenstein: 1011	Qatar: 1036	USA: 2276142
Ghana: 655	Lithuania: 3772	Republic of Macedonia: 1515	Uganda: 243
Greece: 20305	Luxembourg: 11976	Reunion: 38	Ukraine: 4616
Greenland: 90	Macao: 175	Romania: 15739	United Arab Emirates: 3202
Grenada: 79	Madagascar: 204	Russia: 50757	Uruguay: 2038
Guatemala: 638	Malaysia: 1338	Rwanda: 527	Uzbekistan: 324
Guinea: 90	Mali: 220	Samoa: 110	Vanuatu: 100
Haiti: 498	Malta: 885	Saudi Arabia: 490	Venezuela: 2014
Honduras: 80	Martinique: 103	Senegal: 1462	Vietnam: 1261
Hong Kong: 66567	Mauritania: 515	Serbia: 4337	West Germany: 58480
Hungary: 19668	Mexico: 35560	Serbia and Montenegro: 1314	Yugoslavia: 8742
Iceland: 7839	Micronesia: 85	Singapore: 4557	Zaire: 80
India: 110215	Moldova: 95	Slovakia: 2525	Zimbabwe: 210
Indonesia: 3931	Monaco: 189	Slovenia: 2956	
Iran: 11762	Mongolia: 186		
	Montenegro: 439		

Task 2 (movies per year and genre) produces the following results:

1973_Adventure: 1	1979_Adventure: 1	1988_Drama: 2	2004_Adventure: 1
1973_Drama: 1	1979_Crime: 1	1988_Sci-Fi: 1	2004_Documentary: 2
1973_History: 1	1979_Mystery: 1	1996_Documentary: 1	2004_Drama: 1
1976_Comedy: 2	1982_Comedy: 1	1996_Music: 1	2004_Music: 1
1976_Drama: 1	1982_Drama: 1	2001_Documentary: 1	2004_Romance: 1
1976_History: 1	1985_Documentary: 1	2001_Music: 1	2006_Animation: 1
1976_Mystery: 1	1985_History: 1	2002_Documentary: 1	2006_Crime: 1
1976_Romance: 1	1988_Comedy: 1	2002_Music: 1	2006_Drama: 1

2007_Documentary: 1	2008_Crime: 1	2015_Action: 1
2007_War: 1	2008_Drama: 1	2015_Adventure: 1
2008_Action: 1	2009_Documentary: 1	2015_Animation: 1

C Problem 3 execution results

We list here the execution results of our solution for the third problem (mining DNA sequence patterns).

AA: 328236	ACTA: 6151	ATGC: 20429	CCCG: 15287	CTAT: 8656	GCA: 92010	GGTC: 12705
AAA: 104317	ACTC: 9238	ATGG: 18458	CCCT: 8538	CTC: 40893	GCAA: 25483	GGTG: 21949
AAAA: 33151	ACTG: 19234	ATGT: 13456	CCG: 83289	CTCA: 11330	GCAC: 17151	GGTT: 19244
AAAC: 23753	ACTT: 12409	ATT: 79882	CCGA: 14961	CTCC: 9005	GCAG: 27535	GT: 248313
AAAG: 21525	AG: 231133	ATTA: 18033	CCGC: 27044	CTCG: 9953	GCAT: 20449	GTA: 50415
AAAT: 24342	AGA: 54161	ATTC: 16435	CCGG: 22950	CTCT: 9969	GCC: 88989	GTAA: 17001
AAC: 79028	AGAA: 17403	ATTG: 19826	CCGT: 17149	CTG: 98461	GCCA: 29986	GTAC: 11373
AACA: 20648	AGAC: 10050	ATTT: 24372	CCT: 48210	CTGA: 23008	GCCC: 14823	GTAG: 8902
AACC: 19257	AGAG: 10211	CA: 316026	CCTA: 3855	CTGC: 26589	GCCG: 26984	GTAT: 12435
AACG: 22994	AGAT: 15668	CAA: 73266	CCTC: 7577	CTGG: 31803	GCCT: 15890	GTC: 51835
AACT: 14967	AGC: 77456	CAAA: 22726	CCTG: 23291	CTGT: 15584	GCG: 109836	GTCA: 17297
AAG: 60678	AGCA: 21971	CAAC: 20654	CCTT: 12788	CTT: 60920	GCGA: 23903	GTCC: 7788
AAGA: 16071	AGCC: 16675	CAAG: 9104	CG: 336756	CTTA: 9264	GCGC: 33151	GTCG: 16319
AAGC: 18678	AGCG: 25147	CAAT: 19716	CGA: 67889	CTTC: 19829	GCGG: 26823	GTCT: 9694
AAGG: 12858	AGCT: 12547	CAC: 63948	CGAA: 17983	CTTG: 9033	GCGT: 24346	GTG: 63314
AAGT: 12151	AGG: 48468	CACA: 12311	CGAC: 16249	CTTT: 21881	GCT: 76778	GTGA: 17966
AAT: 79476	AGGA: 10559	CACC: 22156	CGAG: 9748	GA: 259534	GCTA: 10018	GTGC: 16924
AATA: 19820	AGGC: 15860	CACG: 15464	CGAT: 22883	GAA: 79933	GCTC: 12590	GTGG: 17237
AATC: 19663	AGGG: 8625	CACT: 13051	CGC: 110789	GAAA: 25923	GCTG: 34350	GTGT: 10240
AATG: 20320	AGGT: 12704	CAG: 100434	CGCA: 24078	GAAC: 16861	GCTT: 18657	GTT: 79059
AATT: 18529	AGT: 47616	CAGA: 20813	CGCC: 33151	GAAG: 19665	GG: 262488	GTTA: 16434
AC: 249408	AGTA: 9965	CAGC: 35398	CGCG: 26624	GAAT: 16328	GGA: 53753	GTTC: 17014
ACA: 56161	AGTC: 8810	CAGG: 23383	CGCT: 25227	GAC: 52428	GGAA: 19116	GTTG: 20618
ACAA: 15670	AGTG: 12816	CAGT: 19337	CGG: 83179	GACA: 12301	GGAC: 7800	GTTT: 23816
ACAC: 10371	AGTT: 15280	CAT: 73632	CGGA: 16056	GACC: 13006	GGAG: 9031	TA: 205922
ACAG: 15775	AT: 300819	CATA: 12645	CGGC: 27287	GACG: 17325	GGAT: 16986	TAA: 65882
ACAT: 13477	ATA: 60954	CATC: 24906	CGGG: 15314	GACT: 8996	GGC: 88242	TAAA: 21016
ACC: 71689	ATAA: 20773	CATG: 14370	CGGT: 23289	GAG: 40596	GGCA: 25961	TAAC: 16559
ACCA: 22611	ATAC: 12580	CATT: 20651	CGT: 70033	GAGA: 11040	GGCC: 11862	TAAG: 9452
ACCC: 11515	ATAG: 8878	CC: 263858	CGTA: 13496	GAGC: 12222	GGCG: 32556	TAAT: 17886
ACCG: 23794	ATAT: 17794	CCA: 82832	CGTC: 17128	GAGG: 7602	GGCT: 16561	TAC: 50347
ACCT: 12668	ATC: 82787	CCAA: 12835	CGTG: 15524	GAGT: 9126	GGG: 45460	TACA: 10059
ACG: 70094	ATCA: 26028	CCAC: 17548	CGTT: 22855	GAT: 82717	GGGA: 10600	TACC: 16192
ACGA: 13381	ATCC: 17273	CCAG: 32327	CT: 229235	GATA: 19089	GGGC: 14376	TACG: 13286
ACGC: 24945	ATCG: 22966	CCAT: 18863	CTA: 25613	GATC: 17963	GGGG: 8241	TACT: 10026
ACGG: 17017	ATCT: 15258	CCC: 45696	CTAA: 7124	GATG: 24737	GGGT: 11534	TAG: 26041
ACGT: 13674	ATG: 72908	CCCA: 12842	CTAC: 8601	GATT: 19727	GGT: 71145	TAGA: 5424
ACT: 47752	ATGA: 19462	CCCC: 8337	CTAG: 832	GC: 373030	GGTA: 16193	TAGC: 9993

TAGG: 3925	TCAC: 17939	TCGC: 24051	TGAA: 24226	TGGA: 15772	TTA: 65815	TTG: 73641
TAGT: 6296	TCAG: 23293	TCGG: 15163	TGAC: 17537	TGGC: 29388	TTAA: 19955	TTGA: 18260
TAT: 60595	TCAT: 19783	TCGT: 13856	TGAG: 11019	TGGG: 12603	TTAC: 17042	TTGC: 25756
TATA: 8542	TCC: 53611	TCT: 53062	TGAT: 25925	TGGT: 22534	TTAG: 7013	TTGG: 12823
TATC: 18970	TCCA: 16156	TCTA: 5213	TGC: 91073	TGT: 55861	TTAT: 20781	TTGT: 15705
TATG: 12412	TCCC: 10346	TCTC: 10881	TGCA: 18677	TGTA: 9995	TTC: 80237	TTT: 105118
TATT: 19788	TCCG: 15949	TCTG: 20097	TGCC: 25972	TGTC: 12434	TTCA: 24566	TTTA: 21113
TC: 259648	TCCT: 10428	TCTT: 16105	TGCG: 23857	TGTG: 12072	TTCC: 18731	TTTC: 25763
TCA: 80436	TCG: 68674	TG: 312973	TGCT: 21277	TGTT: 20499	TTCG: 18383	TTTG: 23085
TCAA: 18194	TCTGA: 14613	TGA: 79892	TGG: 81523	TT: 329732	TTCT: 17327	TTTT: 33542

C.1 Problem 4 execution results

In the following 4-columned pages, the experimental results of section's 5 problem are presented, as the raw output of the 3rd MapReduce phase execution.

102: 20.772281	136: 13.721149	214: 19.8097530000000004	260: 33.4835729999999986
104: 29.609879	137: 13.6608030000000001	215: 22.8341349999999996	261: 32.5087429999999996
105: 27.5980469999999998	138: 13.7382540000000001	216: 22.4504079999999996	264: 12.784288
107: 14.8008850000000003	140: 11.448863	217: 12.86093	265: 17.312394
109: 27.1637019999999994	141: 12.826131	219: 13.857943	266: 16.947997
110: 16.304225	143: 12.803862	220: 26.2796809999999997	267: 26.829961999999999
111: 42.771938	154: 13.7232900000000002	221: 15.3660220000000003	268: 13.1438280000000001
112: 9.6700650000000001	170: 35.833753999999999	222: 10.174368	269: 9.54012
113: 28.5879290000000003	174: 39.9352240000000005	223: 31.7837630000000004	27: 18.6506389999999998
114: 17.5736529999999997	175: 42.116396999999999	226: 11.4641259999999998	270: 12.2007840000000002
115: 33.936378	176: 33.7809369999999994	227: 9.910114	272: 27.8627
116: 25.7654580000000002	180: 9.1118289999999998	228: 26.034533	273: 20.4493260000000003
117: 30.000875	187: 10.061923	229: 17.984762	274: 21.7819690000000004
1180: 9.566474	191: 21.271617	23: 8.068862	275: 18.9216940000000002
1181: 8.554887	192: 22.4150239999999995	231: 11.600534	277: 13.8993770000000001
1182: 10.499468	193: 24.8158819999999995	232: 21.0444219999999994	278: 45.286856999999998
1183: 8.2721589999999998	194: 15.367017	24: 15.9123600000000001	279: 36.9332219999999994
1186: 8.551493	197: 19.721797	244: 20.7399240000000002	280: 36.452380999999999
120: 8.667856	198: 20.10406	245: 26.425946999999999	283: 21.347036
121: 24.6786660000000003	200: 26.785185	246: 12.422665	285: 39.845339
122: 62.881582	202: 20.5546109999999998	247: 12.1988110000000001	287: 15.863291
124: 23.14891	203: 26.4377099999999992	249: 19.9119659999999996	288: 24.1747109999999995
128: 13.8600000000000001	204: 21.1938610000000002	25: 9.950251999999999	289: 20.5074600000000005
129: 13.828262	205: 18.0542059999999997	250: 20.2316329999999995	29: 10.500267
130: 12.778032	206: 12.843962	251: 35.698739999999999	290: 15.8023840000000002
131: 14.548629	208: 18.285626	252: 13.8558760000000002	292: 34.518677
132: 13.7801120000000003	209: 9.478037	254: 8.187458	293: 42.414617
133: 12.777426	210: 18.4637749999999995	255: 27.296618	294: 39.387104
134: 17.525341	211: 26.206232	257: 20.1679989999999995	295: 33.3199829999999986
135: 12.8588820000000001	213: 8.21817	258: 13.3437840000000001	296: 26.437148

30: 13.124654000000001	355: 13.838998000000002	442: 22.468430999999992	546: 8.689068
300: 16.612497	356: 13.709090000000002	443: 22.236632999999994	547: 17.435207
301: 35.508855000000004	36: 7.751157000000001	444: 12.668758	548: 14.626078000000001
302: 40.46924	361: 13.740885	445: 21.391153999999997	549: 8.902671000000002
303: 30.324057999999997	37: 9.843972	446: 20.229419	550: 15.475738000000002
304: 34.186174	378: 7.955433	447: 23.098830999999993	563: 12.416060000000002
306: 12.180608	379: 11.753690999999998	448: 23.389274999999994	604: 14.693641000000001
308: 49.780783000000014	38: 10.698117	449: 21.425622999999995	605: 14.628854
309: 21.140049	380: 9.03648	450: 20.304112999999994	606: 13.673755000000003
310: 16.898876	381: 31.255191	451: 21.309653999999995	607: 13.823655000000002
311: 9.782459	385: 16.697326	452: 21.574356999999992	608: 13.666609
318: 11.424189000000002	386: 13.088604999999998	453: 21.216737999999992	609: 14.749676000000001
32: 7.906732000000001	389: 43.118911000000001	454: 21.305387999999994	610: 14.726731000000003
320: 15.995923000000003	39: 10.792126000000001	455: 22.443621999999994	611: 12.480203
322: 12.928547	391: 7.855742000000001	456: 18.427684	612: 21.530917999999996
323: 12.95803	40: 7.842008000000001	457: 23.612626999999996	639: 16.345097000000003
324: 14.145467000000002	405: 18.636048	458: 20.137554999999995	64: 11.651773
325: 16.820611	406: 30.941025999999999	468: 16.434241	640: 26.795459999999999
326: 9.210550999999999	408: 16.025723	473: 15.624302000000002	641: 27.955416999999999
327: 8.77006	409: 21.124420999999998	490: 15.118589000000002	642: 22.714243999999994
328: 11.502478	410: 19.690642	492: 29.037201999999994	643: 28.925386
329: 9.477534	412: 12.448818000000001	494: 14.964478999999999	644: 27.951106
330: 7.819681999999999	413: 21.007549999999995	497: 7.779587000000001	645: 9.891883
331: 12.199909	414: 19.201738999999996	505: 22.493396999999998	646: 22.266540999999997
333: 17.355712	415: 20.822085	507: 16.502023	647: 17.500691000000003
334: 16.773555	416: 20.244446999999994	508: 13.205226000000001	653: 31.201086999999998
335: 12.816709	417: 20.336876999999998	509: 10.297368000000002	654: 11.212689
336: 9.472820000000002	418: 20.905703999999997	510: 17.989523	655: 15.470210000000002
337: 16.717836	419: 16.571078	511: 14.096020000000003	656: 13.714576000000001
338: 14.435681000000002	420: 14.833722000000003	512: 7.909458999999998	659: 14.530663000000002
34: 8.902532	421: 22.127405999999997	529: 16.491923000000003	660: 14.484713000000001
341: 13.712019000000002	422: 20.207241999999997	530: 20.546952999999999	661: 14.486255000000002
342: 12.777168000000001	423: 19.837138999999997	531: 13.581469	663: 14.393031
343: 21.602388999999999	424: 22.204759999999993	532: 18.63035	664: 15.657084000000003
344: 13.763916	425: 20.3222	533: 16.137291	665: 12.470333000000002
345: 9.50445	427: 18.573423000000002	534: 15.585291000000002	666: 15.570483000000001
346: 13.803495	428: 18.402874999999998	535: 13.489995	667: 8.476292
347: 13.770425000000001	429: 20.996679999999998	536: 15.663219000000002	668: 8.400375
348: 13.696388000000002	431: 17.247738000000005	537: 15.558095000000002	669: 12.719472000000001
349: 12.777321	432: 7.730989	538: 20.604023999999995	670: 12.759070000000001
35: 8.831461000000001	433: 20.990592000000003	539: 15.567038000000002	671: 18.786868000000002
350: 13.700356000000001	437: 13.467927000000001	540: 10.592666000000001	672: 12.737939000000003
351: 12.82703	438: 22.538098999999995	541: 13.301682	673: 11.354866
352: 18.913772999999996	439: 20.257774999999995	542: 13.708515000000002	674: 12.464726000000002
353: 13.840302000000001	440: 18.640948999999996	544: 8.796812000000001	675: 14.512069
354: 12.026345	441: 22.565751999999993	545: 7.992185	676: 12.633483

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679: 22.209649	778: 9.388625000000001	853: 19.714644999999994	902: 18.710283
680: 26.495342999999999	779: 8.382993	854: 20.674989999999998	915: 9.631426000000001
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682: 11.780345000000002	79: 18.829224	859: 13.744827	918: 10.553774
683: 10.837639	792: 9.650819	86: 9.620828000000001	919: 8.431745
684: 11.369396	793: 21.405161999999994	860: 13.392533000000002	922: 10.480677000000002
685: 20.680481999999994	794: 7.747058000000001	861: 12.716919	926: 20.516713999999997
686: 28.644553999999992	796: 7.746258000000001	862: 14.757012000000001	927: 18.237036999999997
687: 13.618457000000001	797: 20.176615999999996	863: 14.737124000000001	928: 18.419195
70: 12.576885000000003	80: 19.708188999999997	870: 12.684738000000001	929: 20.752049999999997
702: 15.804968	81: 27.764969999999987	871: 12.674369	930: 13.043696999999998
703: 18.989590999999997	82: 8.954957	872: 11.814398	931: 18.611175
711: 8.769808000000001	822: 7.824752000000001	873: 12.763509	932: 20.685094999999997
72: 13.937429	827: 26.284926	874: 10.89	933: 20.786459999999995
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73: 33.317902999999994	83: 16.828261	876: 12.794634000000002	936: 21.667931999999997
739: 14.833940000000002	830: 12.777338	877: 9.48321	937: 19.520974999999996
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741: 17.572777	845: 19.799999999999997	879: 13.635698000000001	948: 16.893155
743: 16.54965	846: 23.372872999999995	880: 12.768133	950: 20.797809999999995
744: 13.711973000000002	847: 21.634598999999994	881: 12.801868000000002	951: 19.461768999999997
745: 14.759685000000001	848: 21.599697999999993	882: 10.89	953: 18.305716999999998
746: 14.843160000000001	849: 20.692736999999997	893: 7.887907	
75: 8.17184	85: 17.810776	894: 9.918199	
76: 35.164774999999998	850: 21.486940999999995	895: 16.402685000000005	