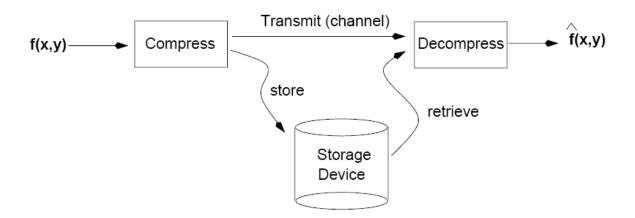
# EIE4512 - Digital Image Processing Image Compression



Zhen Li
lizhen@cuhk.edu.cn
School of Science and Engineering
The Chinese University of Hong Kong, Shen Zhen
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### **Image Compression**

• The goal of image compression is to reduce the amount of data required to represent a digital image.



#### Image Compression (cont'd)

#### Lossless

- Information preserving
- Low compression ratios

#### Lossy

- Information loss
- High compression ratios

<u>Trade-off:</u> information loss vs compression ratio

#### Data ≠ Information

- Data and information are <u>not</u> synonymous terms!
- Data is the means by which information is conveyed.
- Data compression aims to <u>reduce</u> the amount of data while <u>preserving</u> as much information as possible.

#### Data vs Information (cont'd)

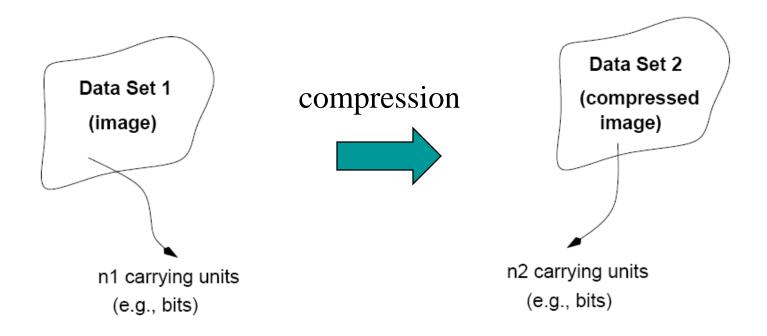
• The same information can be represented by different amount of data – for example:

Ex1: Your wife, Helen, will meet you at Logan Airport in Boston at 5 minutes past 6:00 pm tomorrow night

Ex2: Your wife will meet you at Logan Airport at 5 minutes past 6:00 pm tomorrow night

Ex3: Helen will meet you at Logan at 6:05 pm tomorrow night.

## **Compression Ratio**



Compression ratio: 
$$C_R = \frac{n_1}{n_2}$$

#### Relevant Data Redundancy

$$R_D = 1 - \frac{1}{C_R}$$

#### Example:

If 
$$C_R = \frac{10}{1}$$
, then  $R_D = 1 - \frac{1}{10} = 0.9$ 

(90% of the data in dataset 1 is redundant)

if 
$$n_2 = n_1$$
, then  $C_R = 1$ ,  $R_D = 0$ 

if 
$$n_2 \ll n_1$$
, then  $C_R \to \infty$ ,  $R_D \to 1$ 

#### Types of Data Redundancy

- (1) Coding Redundancy
- (2) Interpixel Redundancy
- (3) Psychovisual Redundancy
- Data compression attempts to reduce one or more of these redundancy types.

#### **Coding - Definitions**

- Code: a list of symbols (letters, numbers, bits etc.)
- Code word: a sequence of symbols used to represent some information (e.g., gray levels).
- Code word length: number of symbols in a code word.

Example: (binary code, symbols: 0,1, length: 3)

0: 000 4: 100 1: 001 5: 101 2: 010 6: 110 3: 011 7: 111

#### Coding - Definitions (cont'd)

N x M image

 $\mathbf{r_k}$ : k-th gray level

 $\mathbf{l}(\mathbf{r_k})$ : # of bits for  $\mathbf{r_k}$ 

 $\mathbf{P}(\mathbf{r_k})$ : probability of  $\mathbf{r_k}$ 

Average # of bits: 
$$L_{avg} = E(l(r_k)) = \sum_{k=0}^{L-1} l(r_k)P(r_k)$$

Total # of bits:  $NML_{avg}$ 

Expected value: 
$$E(X) = \sum_{x} xP(X = x)$$

#### Coding Redundancy

• Case 1:  $l(r_k) = constant length$ 

Example:

$p_r(r_k)$	Code 1	$l_1(r_k)$
0.19	000	3
0.25	001	3
0.21	010	3
0.16	011	3
0.08	100	3
0.06	101	3
0.03	110	3
0.02	111	3
	0.19 0.25 0.21 0.16 0.08 0.06 0.03	0.19     000       0.25     001       0.21     010       0.16     011       0.08     100       0.06     101       0.03     110

Assume an image with L = 8

Assume 
$$l(r_k) = 3$$
,  $L_{avg} = \sum_{k=0}^{7} 3P(r_k) = 3\sum_{k=0}^{7} P(r_k) = 3$  bits

Total number of bits: 3*NM* 

#### Coding Redundancy (cont'd)

• Case 2:  $l(r_k) = variable length$ 

Table 6.1	Variable-Leng	th Coding Exa	mple	variable length	
$r_k$	$p_r(r_k)$	Code 1	$l_1(r_k)$	Code 2	$l_2(r_k)$
$r_0 = 0$	0.19	000	3	11	2
$r_1 = 1/7$	0.25	001	3	01	2
$r_2 = 2/7$	0.21	010	3	10	2
$r_3 = 3/7$	0.16	011	3	001	3
$r_4 = 4/7$	0.08	100	3	0001	4
$r_5 = 5/7$	0.06	101	. 3	00001	5
$r_6 = 6/7$	0.03	110	3	000001	6
$r_7 = 1$	0.02	111	3	000000	6

$$L_{avg} = \sum_{k=0}^{7} l(r_k)P(r_k) = 2.7 \text{ bits}$$

$$C_R = \frac{3}{2.7} = 1.11 \text{ (about 10\%)}$$

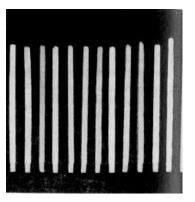
Total number of bits: 2.7NM

$$R_D = 1 - \frac{1}{1.11} = 0.099$$

#### Interpixel redundancy

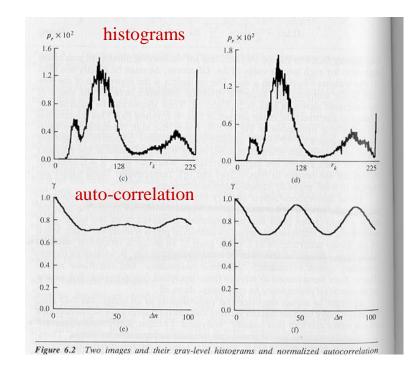
• Interpixel redundancy implies that pixel values are correlated (i.e., a pixel value can be reasonably predicted by its neighbors).





$$f(x) o g(x) = \int_{-\infty}^{\infty} f(x)g(x+a)da$$

auto-correlation: f(x)=g(x)

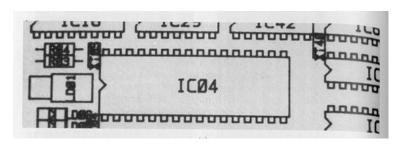


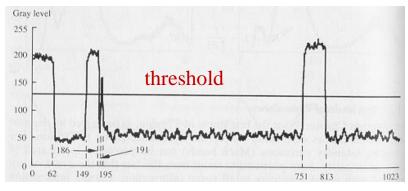
#### Interpixel redundancy (cont'd)

• To reduce interpixel redundancy, some kind of transformation must be applied on the data (e.g., thresholding, DFT, DWT)

#### Example:

original





## ICØ4

(4 -4 ) (6 -4 ) (4 -4 ) (6 -4 ) (4

(1,63) (0,87) (1,37) (0,5) (1,4) (0,556) (1,62) (0,210)

Using 11 bits/pair: (1+10) bits/pair

Run-length encoding:

88 bits are required (compared to 1024 !!)

thresholded

#### Psychovisual redundancy

• The human eye is more sensitive to the lower frequencies than to the higher frequencies in the visual spectrum.

<u>Idea:</u> discard data that is perceptually insignificant!

#### Psychovisual redundancy (cont'd)

**Example:** quantization

256 gray levels



16 gray levels



C=8/4=2:1

16 gray levels + random noise



add a small pseudo-random number to each pixel prior to quantization

#### Measuring Information

A key question in image compression is:

"What is the minimum amount of data that is sufficient to describe completely an image without loss of information?"

How do we measure the information content of an image?

#### Measuring Information (cont'd)

- We assume that information generation is a probabilistic process.
- <u>Idea</u>: associate information with probability!

A random event E with probability P(E) contains:

$$I(E) = log(\frac{1}{P(E)}) = -log(P(E))$$
 units of information

Note: I(E)=0 when P(E)=1

## How much information does a pixel value contain?

• Suppose that gray level values are generated by a random process, then rk contains:

$$I(r_k) = -\log(P(r_k))$$
 units of information!

(assume statistically independent random events)

#### How much information does an image contain?

• Average information content of an image:

$$E = \sum_{k=0}^{L-1} I(r_k) P(r_k)$$

using 
$$I(r_k) = -\log(P(r_k))$$

Entropy: 
$$H = -\sum_{k=0}^{L-1} P(r_k) log(P(r_k))$$
 units/pixel (e.g., bits/pixel)

#### Redundancy

• Redundancy:  $R = L_{avg} - H$  (data vs info)

where: 
$$L_{avg} = E(l(r_k)) = \sum_{k=0}^{L-1} l(r_k)P(r_k)$$

Note: if  $L_{avg} = H$ , then R = 0 (no redundancy)

#### **Entropy Estimation**

• It is not easy to estimate H reliably!

image 21 21 21 95 169 243 243 243 243 243 243 21 21 21 95 169 243 243 243 243 21 21 21 95 169 243 243 243 243 21 21 21 95 169 243 243 243

Gray Level	Count	Probability
21	12	3/8
95	4	1/8
169	4	1/8
243	12	3/8

#### Entropy Estimation (cont'd)

• First order estimate of H:

$$H = -\sum_{k=0}^{3} P(r_k)log(P(r_k)) = 1.81 \text{ bits/pixel}$$

$$L_{avg} = 8 \text{ bits/pixel}$$
  $R = L_{avg} - H$ 

The first-order estimate provides only a <u>lower-bound</u> on the compression that can be achieved.

#### Estimating Entropy (cont'd)

- Second order estimate of H:
  - Use relative frequencies of <u>pixel blocks</u>:

			1	mage	9			
21	21	21	95	169	243	243	243	
21	21	21	95	169	243	243	243	
21	21	21	95	169	243	243	243	
21	21	21	95	169	243	243	243	

Gray Level Pair	Count	Probability
(21, 21)	8	1/4
(21, 95)	4	1/8
(95, 169)	4	1/8
(169, 243)	4	1/8
(243, 243)	8	1/4
(243, 21)	4	1/8

$$H = 2.5/2 = 1.25$$
 bits/pixel

#### Differences in Entropy Estimates

• Differences between higher-order estimates of entropy and the first-order estimate indicate the presence of interpixel redundancy!

• Need to apply some transformation to deal with interpixel redundancy!

#### Differences in Entropy Estimates (cont'd)

• Example: consider pixel differences

21	21	21	95	169	243	243	243	21	0	0	74	74	74	0	0
21	21	21	95	169	243	243	243	21	0	0	74	74	74	0	0
21	21	21	95	169	243	243	243	21	0	0	74	74	74	0	0
21	21	21	95	169	243	243	243	21	0	0	74	74	74	0	0

Gray Level or Difference	Count	Probability
0	16	1/2
21	4	1/8
74	12	3/8

#### Differences in Entropy Estimates (cont'd)

• What is the entropy of the <u>pixel differences</u> image?

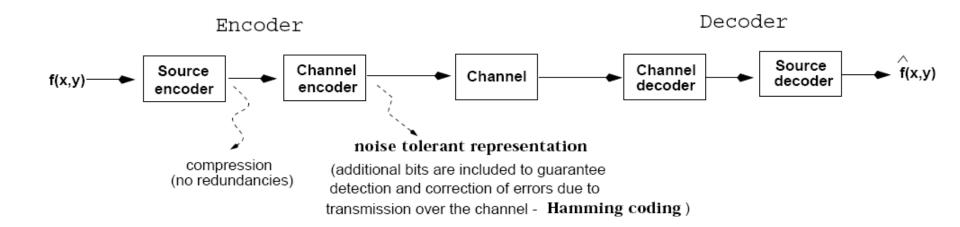
$$H = -\sum_{k=0}^{2} P(r_k)log(P(r_k)) = 1.41 \text{ bits/pixel}$$

(better than the entropy of the original image H=1.81)

• An even better transformation should be possible since the second order entropy estimate is lower:

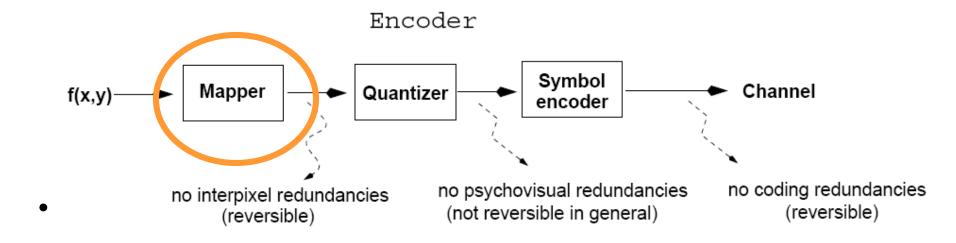
1.41 bits/pixel > 1.25 bits/pixel

#### Image Compression Model



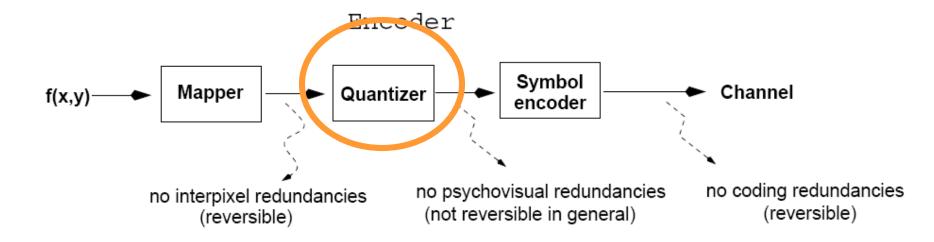
We will focus on the Source Encoder/Decoder only.

#### Image Compression Model (cont'd)



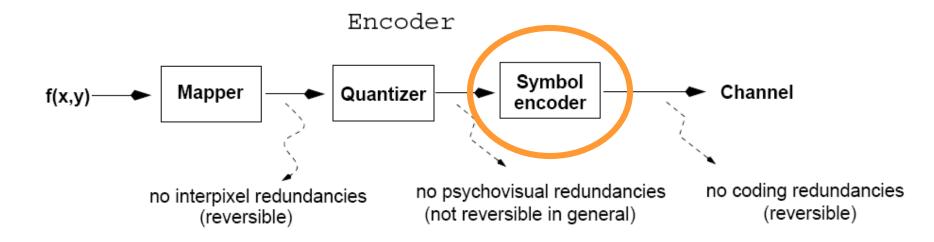
• Mapper: transforms data to account for interpixel redundancies.

#### Image Compression Model (cont'd)



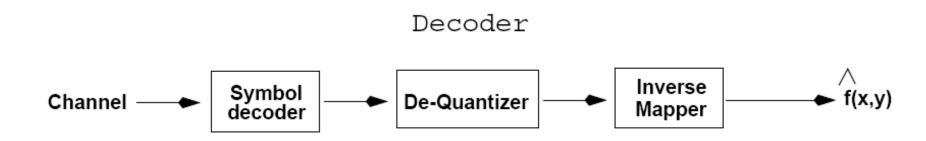
• Quantizer: quantizes the data to account for psychovisual redundancies.

#### Image Compression Model (cont'd)



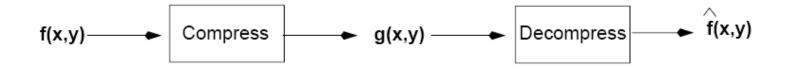
• Symbol encoder: encodes the data to account for coding redundancies.

#### Image Compression Models (cont'd)



- The decoder applies the inverse steps.
- Note that quantization is irreversible in general.

#### Fidelity Criteria



- How close is f(x,y) to  $\hat{f}(x,y)$  ?
- Criteria
  - Subjective: based on human observers
  - <u>Objective</u>: mathematically defined criteria

## Subjective Fidelity Criteria

Value	Rating	Description
1	Excellent	An image of extremely high quality, as good as you could desire.
2	Fine	An image of high quality, providing enjoyable viewing. Interference is not objectionable.
3	Passable	An image of acceptable quality. Interference is not objectionable.
4	Marginal	An image of poor quality; you wish you could improve it. Interference is somewhat objectionable.
5	Inferior	A very poor image, but you could watch it. Objectionable interference is definitely present.
6	Unusable	An image so bad that you could not watch it.

#### Objective Fidelity Criteria

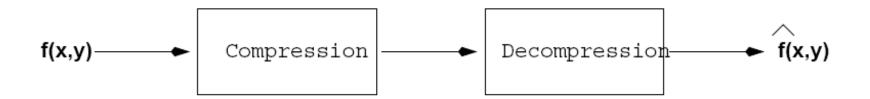
• Root mean square error (RMS)

$$e_{rms} = \sqrt{\frac{1}{MN} \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} (\hat{f}(x,y) - f(x,y))^2}$$

Mean-square signal-to-noise ratio (SNR)

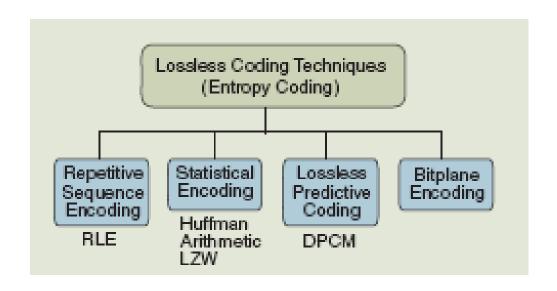
$$SNR_{ms} = \frac{\sum_{x=0}^{M-1} \sum_{y=0}^{N-1} (\hat{f}(x, y))^{2}}{\sum_{x=0}^{M-1} \sum_{y=0}^{N-1} (\hat{f}(x, y) - f(x, y))^{2}}$$

### **Lossless Compression**

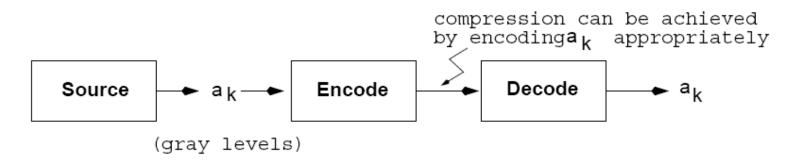


$$e(x, y) = \hat{f}(x, y) - f(x, y) = 0$$

#### Taxonomy of Lossless Methods



## Huffman Coding (addresses coding redundancy)



- A variable-length coding technique.
- Source symbols are encoded one at a time!
  - There is a one-to-one correspondence between source symbols and code words.
- Optimal code minimizes code word length per source symbol.

## Huffman Coding (cont'd)

- Forward Pass
  - 1. Sort probabilities per symbol
  - 2. Combine the lowest two probabilities
  - 3. Repeat *Step2* until only two probabilities remain.

Original source			. Source re	eduction	
Symbol	Probability	1	2	3	4
$a_2$	0.4	0.4	0.4	0.4	-06
$-\frac{a_{2}}{a_{6}}$	0.3	0.3	0.3	0.3	- 0.6 0.4
$a_1$	0.1	0.1	<b>→</b> 0.2 <b>→</b>	▶ 0.3 🗆	0.4
$a_4$	0.1	0.1	0.1		
$a_3$	0.06	- 0.1			
$a_5$	0.04				

## Huffman Coding (cont'd)

#### • Backward Pass

Assign code symbols going backwards

Ori	iginal sou	rce				Source red	uction		7/10	
Sym.	Prob.	Code	Sala	1		2		3	4	4
$a_{2}$ $a_{6}$ $a_{1}$ $a_{4}$ $a_{3}$ $a_{5}$	0.4 0.3 0.1 0.1 0.06 0.04	1 00 011 0100 01010 01011	0.4 0.3 0.1 0.1 - 0.1	1 00 011 0100 0101	0.4 0.3 0.2 0.1	00	0.4 0.3 — 0.3	00 -	0.6 0.4	0

## Huffman Coding (cont'd)

• L<sub>avg</sub> assuming Huffman coding:

$$L_{avg} = E(l(a_k)) = \sum_{k=1}^{6} l(a_k)P(a_k) =$$

$$3x0.1 + 1x0.4 + 5x0.06 + 4x0.1 + 5x0.04 + 2x0.3 = 2.2$$
 bits/symbol

• L<sub>avg</sub> assuming binary coding:

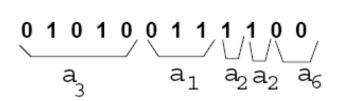
6 symbols, we need a 3-bit code

$$(a_1: 000, a_2: 001, a_3: 010, a_4: 011, a_5: 100, a_6: 101)$$

$$L_{avg} = \sum_{k=1}^{6} l(a_k)P(a_k) = \sum_{k=1}^{6} 3P(a_k) = 3 \sum_{k=1}^{6} P(a_k) = 3 \text{ bits/symbol}$$

## Huffman Coding/Decoding

- Coding/Decoding can be implemented using a look-up table.
- Decoding can be done unambiguously.



Original source					
Sym.	Prob.	Code			
a.	0.4	1			
$a_2$ $a_6$ $a_1$	0.3	00			
a.	0.1	011			
a.	0.1	0100			
a <sub>a</sub>	0.06	01010			
a <sub>4</sub> a <sub>3</sub> a <sub>5</sub>	0.04	01011			

# Arithmetic (or Range) Coding (addresses coding redundancy)

- Huffman coding encodes source symbols one at a time.
- Arithmetic coding encodes sequences of source symbols.
  - Slower than Huffman coding but can achieve better compression.
  - There is no one-to-one correspondence between source symbols and code words.

## Arithmetic Coding (cont'd)

• Represent a sequence of source symbols by a subinterval in [0,1) which can be encoded using an arithmetic code.



- Start with the interval [0, 1)
- As more symbols are encoded, a sub-interval is chosen to represent the message which keeps shrinking as the message increases.

## Arithmetic Coding (cont'd)

Suppose there are four symbols  $\alpha_1 \alpha_2 \alpha_3 \alpha_4$ 

1) Start with interval [0, 1)

0		1

Source Symbol	Probability
$a_1$	0.2
$a_2$	0.2
$a_3$	0.4
$a_4$	0.2

2) Subdivide [0, 1) based on the probabilities of  $\alpha_i$ 

0			₩
$a_1$	$a_2$	$a_3$	$a_4$

Initial Subinterval
[0.0, 0.2) [0.2, 0.4) [0.4, 0.8) [0.8, 1.0)

3) Update interval by processing message

## Example

Encode

 $\alpha_1 \alpha_2 \alpha_3 \alpha_3 \alpha_4$ 



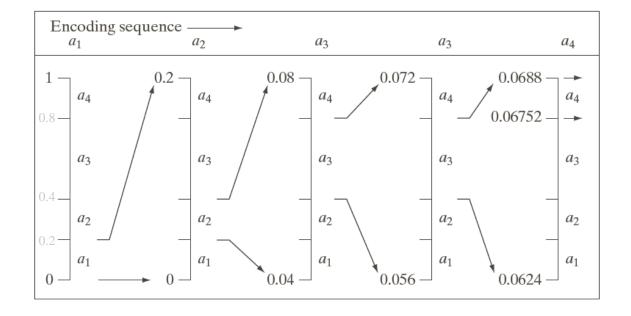
[0.06752, 0.0688)



code: 0.068

(must be inside sub-interval)

Source Symbol	Probability	Initial Subinterval
$a_1$	0.2	[0.0, 0.2)
$a_2$	0.2	[0.2, 0.4)
$a_3$	0.4	[0.4, 0.8)
$a_4$	0.2	[0.8, 1.0)



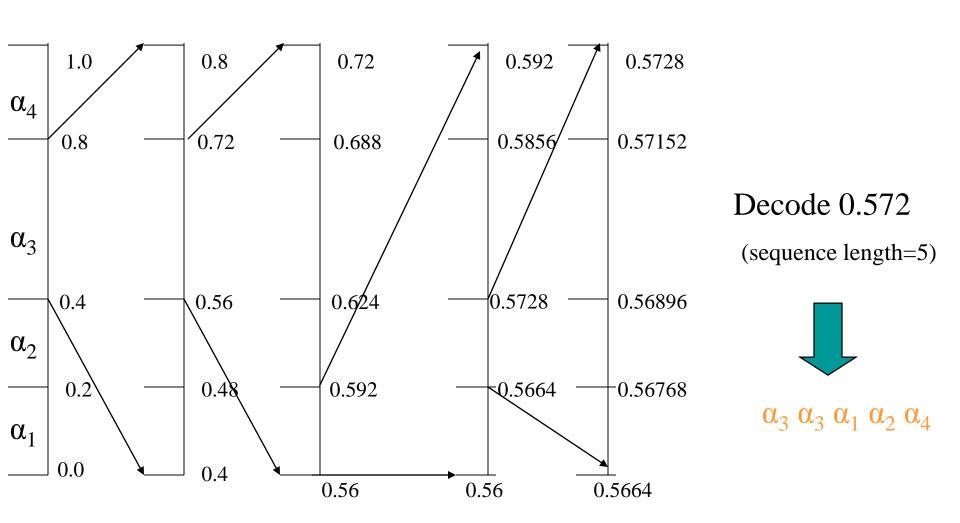
### Example (cont'd)

- The message  $\alpha_1 \alpha_2 \alpha_3 \alpha_4$  is encoded using 3 decimal digits or 3/5 = 0.6 decimal digits per source symbol.
- The entropy of this message is:  $H = -\sum_{k=0}^{3} P(r_k) log(P(r_k))$

 $-(3 \times 0.2\log_{10}(0.2) + 0.4\log_{10}(0.4)) = 0.5786 \text{ digits/symbol}$ 

**Note:** finite precision arithmetic might cause problems due to truncations!

## Arithmetic Decoding



# LZW Coding (addresses interpixel redundancy)

- Requires no prior knowledge of symbol probabilities.
- Assigns fixed length code words to variable length symbol sequences.
  - There is no one-to-one correspondence between source symbols and code words.
- Included in GIF, TIFF and PDF file formats

### LZW Coding

- A codebook (or dictionary) needs to be constructed.
- Initially, the first 256 entries of the dictionary are assigned to the gray levels 0,1,2,..,255 (i.e., assuming 8 bits/pixel)

#### **Initial Dictionary**

<b>Dictionary Location</b>	Entry
0	0
1	1
255	255
256	-
511	-

## LZW Coding (cont'd)

#### Example:

39	39	126	126
39	39	126	126
39	39	126	126
39	39	126	126

As the encoder examines image pixels, gray level sequences (i.e., blocks) that are not in the dictionary are assigned to a new entry.

Dictionary Location	Entry
0	0
1	1
255	255
256	39-39
511	_

- Is 39 in the dictionary.....Yes
- What about 39-39.....No
  - \* Add 39-39 at location 256

## Example

39 39 126 126 39 39 126 126 39 39 126 126 39 39 126 126

CR = empty

#### repeat

P=next pixel

CS=CR+P

#### If CS is found:

- (1) No Output
- (2) CR=CS

#### else:

- (1) Output D(CR)
- (2) Add CS to D
- (3) CR=P

#### Concatenated Sequence: CS = CR + P

(CR) (P)

Currently Recognized Sequence	Pixel Being Processed	Encoded Output	Dictionary Location (Code Word)	Dictionary Entry
	39	/ \		
39	39	39	256	39-39
39	126	39	257	39-126
126	126	126	258	126-126
126	39	126	259	126-39
39	39			
39-39	126	256	260	39-39-126
126	126			
126-126	39	258	261	126-126-39
39	39	1 1		
39-39	126	1 1		
39-39-126	126	260	262	39-39-126-126
126	39			
126-39	39	259	263	126-39-39
39	126	\ /		
39-126	126	257	264	39-126-126
126		126		
		-		

### **Decoding LZW**

- Use the dictionary for decoding the "encoded output" sequence.
- The dictionary need not be sent with the encoded output.
- Can be built on the "fly" by the decoder as it reads the received code words.

#### Lempel-Ziv-Welch (LZW) Compression Algorithm

• Introduction to the LZW Algorithm

LZW Encoding Algorithm

• LZW Decoding Algorithm

LZW Limitations

#### LZW Encoding Algorithm (cont'd)

Initialize Dictionary with 256 single character strings and their corresponding ASCII codes;

```
Prefix ← first input character;
CodeWord \leftarrow 256:
while(not end of character stream){
     Char ← next input character;
     if(Prefix + Char exists in the Dictionary)
         Prefix ← Prefix + Char;
     else{
         Output: the code for Prefix;
         insertInDictionary( (CodeWord, Prefix + Char));
         CodeWord++;
         Prefix ← Char;
```

Output: the code for Prefix;

#### **Example 1: Compression using LZW**

Encode the string **BABAABAAA** by the **LZW** encoding algorithm.

1	2	3		4	5	6
lacksquare	<u>B</u>	A	A	В	A	<b>A A</b>

- 1. BA is not in the Dictionary; insert BA, output the code for its prefix: code(B)
- 2. AB is not in the Dictionary; insert AB, output the code for its prefix: code(A)
- **3. BA** is in the Dictionary.

BAA is not in Dictionary; insert BAA, output the code for its prefix: code(BA)

**4. AB** is in the Dictionary.

ABA is not in the Dictionary; insert ABA, output the code for its prefix: code(AB)

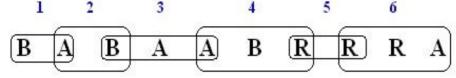
- 5. AA is not in the Dictionary; insert AA, output the code for its prefix: code(A)
- 6. AA is in the Dictionary and it is the last pattern; output its code: code(AA)

output	Dictionary			
	Code Word	String		
66	256	BA		
65	257	AB		
256	258	BAA		
257	259	ABA		
65	260	AA		
260		j		

The compressed message is: <66><65><256><257><65><260>

#### **Example 2: Compression using LZW**

Encode the string **BABAABRRRA** by the LZW encoding algorithm.



- 1. **BA** is not in the Dictionary; insert **BA**, output the code for its prefix: **code**(**B**)
- 2. **AB** is not in the Dictionary; insert **AB**, output the code for its prefix: **code(A)**
- 3. **BA** is in the Dictionary.
  - **BAA** is not in Dictionary; insert **BAA**, output the code for its prefix: **code**(**BA**)
- 4. **AB** is in the Dictionary.
  - **ABR** is not in the Dictionary; insert **ABR**, output the code for its prefix: **code**(**AB**)
- 5. **RR** is not in the Dictionary; insert **RR**, output the code for its prefix: **code**(**R**)
- 6. RR is in the Dictionary.

**RRA** is not in the Dictionary and it is the last pattern; insert **RRA**, output code for its prefix: **code(RR)**, then output code for last character: **code(A)** 

output	Dictionary			
	Code Word	String		
66	256	BA		
65	257	AB		
256	258	BAA		
257	259	ABR		
82	260	RR		
260	261	RRA		
65				

The compressed message is: <66><65><256><257><82><260> <65>

#### LZW: Number of bits transmitted

Example: Uncompressed String: aaabbbbbbaabaaba

Number of bits = Total number of characters \* 8

$$= 16 * 8$$

= 128 bits

Compressed string (codewords): <97><256><98><258><259><257><261>

Number of bits = Total Number of codewords \* 12

$$= 7 * 12$$

Note: Each codeword is 12 bits because the minimum Dictionary size is taken as 4096, and

$$2^{12} = 4096$$

#### **LZW Decoding Algorithm**

The LZW decompressor creates the same string table during decompression.

```
Initialize Dictionary with 256 ASCII codes and corresponding single character strings as
   their translations:
PreviousCodeWord ← first input code;
Output: string(PreviousCodeWord);
Char \leftarrow character(first input code);
CodeWord \leftarrow 256;
while(not end of code stream){
   CurrentCodeWord ← next input code;
   if(CurrentCodeWord exists in the Dictionary)
      String \leftarrow string(CurrentCodeWord);
   else
      String \leftarrow string(PreviousCodeWord) + Char;
   Output: String;
   Char \leftarrow first character of String;
   insertInDictionary( (CodeWord , string(PreviousCodeWord) + Char ) );
   PreviousCodeWord ← CurrentCodeWord;
   CodeWord++;
```

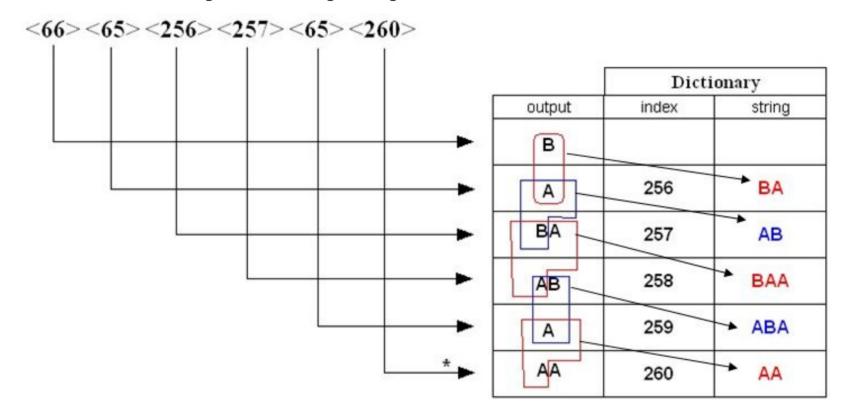
#### LZW Decoding Algorithm (cont'd)

Summary of **LZW** decoding algorithm:

```
output: string(first CodeWord);
while(there are more CodeWords){
  if(CurrentCodeWord is in the Dictionary)
   output: string(CurrentCodeWord);
 else
   output: PreviousOutput + PreviousOutput first character;
 insert in the Dictionary: PreviousOutput + CurrentOutput first character;
```

#### **Example 1: LZW Decompression**

Use LZW to decompress the output sequence <66> <65> <256> <257> <65> <260>

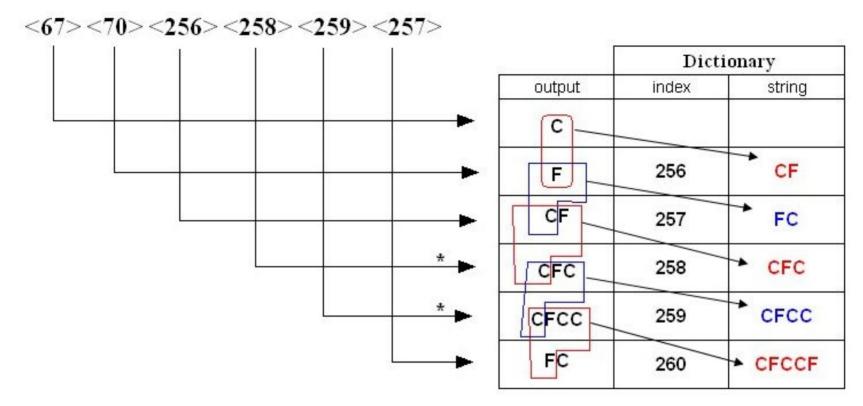


- **1. 66** is in Dictionary; output **string(66)** i.e. **B**
- 2. 65 is in Dictionary; output string(65) i.e. A, insert BA
- 3. 256 is in Dictionary; output string(256) i.e. BA, insert AB
- 4. 257 is in Dictionary; output string(257) i.e. AB, insert BAA
- 5. 65 is in Dictionary; output string(65) i.e. A, insert ABA
- **6. 260** is **not** in Dictionary; output

previous output + previous output first character: AA, insert AA

#### **Example 2: LZW Decompression**

Decode the sequence  $\langle 67 \rangle \langle 70 \rangle \langle 256 \rangle \langle 258 \rangle \langle 259 \rangle \langle 257 \rangle$  by LZW decode algorithm.



- 1. 67 is in Dictionary; output string(67) i.e. C
- 2. 70 is in Dictionary; output string(70) i.e. F, insert CF
- 3. 256 is in Dictionary; output string(256) i.e. CF, insert FC
- 4. 258 is <u>not</u> in Dictionary; output **previous output** + C i.e. CFC, insert CFC
- 5. 259 is <u>not</u> in Dictionary; output **previous output** + C i.e. CFCC, insert CFCC
- 6. 257 is in Dictionary; output string(257) i.e. FC, insert CFCCF

#### **LZW: Limitations**

- What happens when the dictionary gets too large?
- One approach is to clear entries 256-4095 and start building the dictionary again.
- The same approach must also be used by the decoder.

# Run-length coding (RLC) (addresses interpixel redundancy)

• Reduce the size of a repeating string of symbols (i.e., runs):

$$1\ 1\ 1\ 1\ 1\ 0\ 0\ 0\ 0\ 0\ 1 \rightarrow (1,5)\ (0,6)\ (1,1)$$
a a a b b b b b c c  $\rightarrow$  (a,3) (b, 6) (c, 2)

- Encodes a run of symbols into two bytes: (symbol, count)
- Can compress any type of data but cannot achieve high compression ratios compared to other compression methods.

## Combining Huffman Coding with Run-length Coding

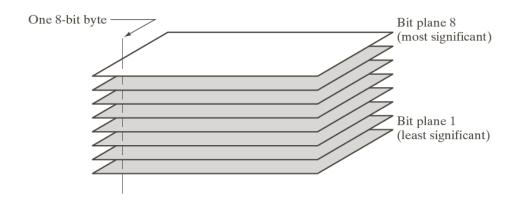
• Assuming that a message has been encoded using Huffman coding, additional compression can be achieved using run-length coding.

0 1 0 1 0 0 1 1 1 1 0 0

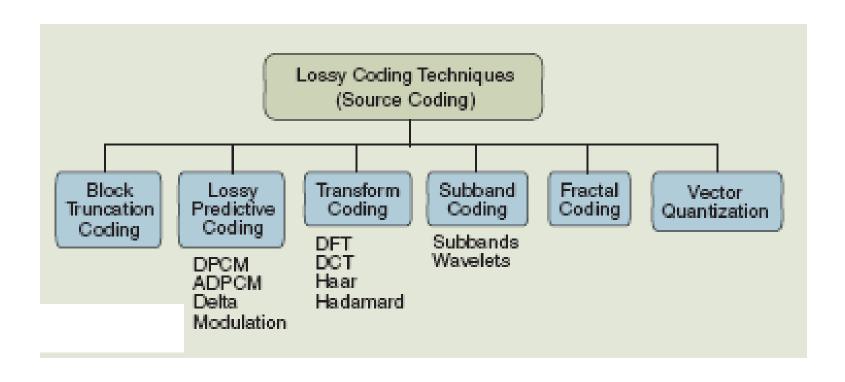
e.g., (0,1)(1,1)(0,1)(1,0)(0,2)(1,4)(0,2)

## Bit-plane coding (addresses interpixel redundancy)

- Process each bit plane individually.
- (1) Decompose an image into a series of binary images.
- (2) Compress each binary image (e.g., using run-length coding)

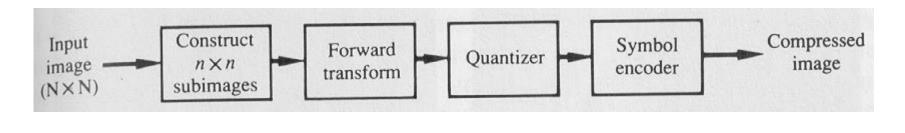


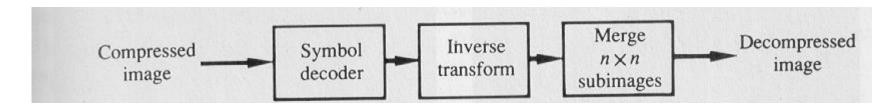
### Lossy Methods - Taxonomy



## **Lossy Compression**

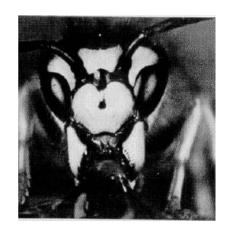
• Transform the image into some other domain to reduce interpixel redundancy.

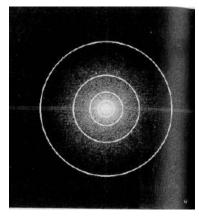




### **Example: Fourier Transform**

$$f(x,y) = \frac{1}{N} \sum_{u=0}^{N-1} \sum_{v=0}^{N-1} F(u,v) e^{\frac{j2\pi(ux+vy)}{N}}, \quad \text{x,y=0,1,...,N-1}$$





Note that the magnitude of the FT decreases, as *u*, *v* increase!

 $K \ll N$ 

$$\hat{f}(x,y) = \frac{1}{N} \sum_{u=0}^{K-1} \sum_{v=0}^{K-1} F(u,v) e^{\frac{j2\pi(ux+vy)}{N}}, \quad x,y=0,1,...,N-1$$

 $\sum_{x,y} (\hat{f}(x,y) - f(x,y))^2 \text{ is very small } !!$ 

#### **Transform Selection**

$$f(x,y) = \sum_{u=0}^{N-1} \sum_{v=0}^{N-1} T(u,v)h(x,y,u,v)$$

- T(u,v) can be computed using various transformations, for example:
  - DFT
  - DCT (Discrete Cosine Transform)
  - KLT (Karhunen-Loeve Transformation) or Principal Component Analysis (PCA)
- JPEG uses DCT for handling interpixel redundancy.

### DCT (Discrete Cosine Transform)

Forward: 
$$C(u, v) = \alpha(u)\alpha(v) \sum_{x=0}^{N-1} \sum_{y=0}^{N-1} f(x, y) cos(\frac{(2x+1)u\pi}{2N}) cos(\frac{(2y+1)v\pi}{2N}),$$
  
 $u, v = 0, 1, ..., N-1$ 

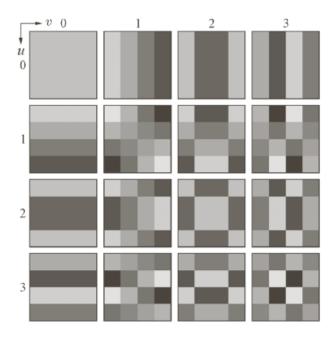
Inverse: 
$$f(x,y) = \sum_{u=0}^{N-1} \sum_{v=0}^{N-1} \alpha(u)\alpha(v)C(u,v)cos(\frac{(2x+1)u\pi}{2N})cos(\frac{(2y+1)v\pi}{2N}),$$

x, y=0,1,...,N-1

$$\alpha(u) = \begin{cases} \sqrt{1/N} & \text{if } u=0\\ \sqrt{2/N} & \text{if } u>0 \end{cases} \quad \alpha(v) = \begin{cases} \sqrt{1/N} & \text{if } v=0\\ \sqrt{2/N} & \text{if } v>0 \end{cases}$$

## DCT (cont'd)

• Basis functions for a 4x4 image (i.e., cosines of different frequencies).



## DCT (cont'd)

Using 8 x 8 sub-images yields 64 coefficients per sub-image.

Reconstructed images by truncating 50% of the coefficients

DCT is a more compact transformation!



**DFT** 

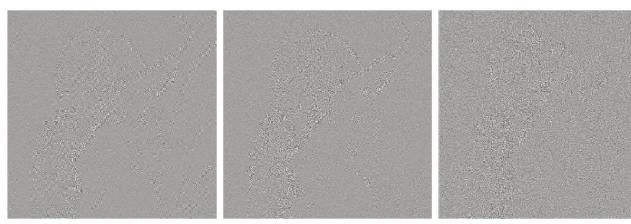




WHT

( Walsh–Hadamard transform )

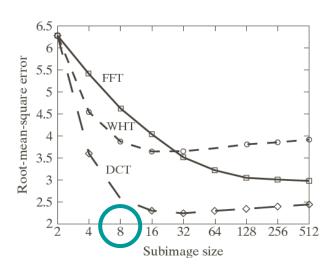




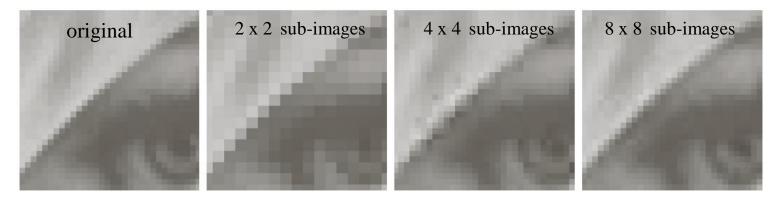
RMS error: 2.32 1.78 1.13

# DCT (cont'd)

• Sub-image size selection:



#### Reconstructions



# DCT (cont'd)

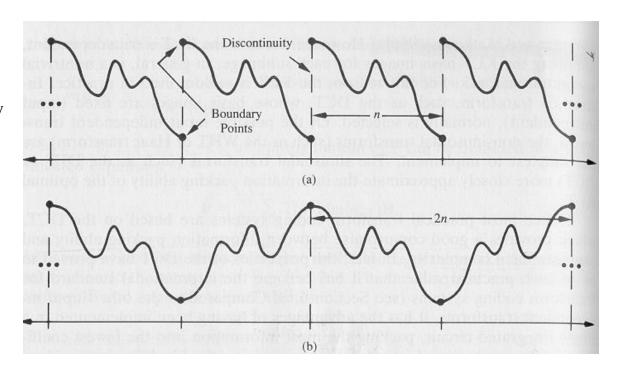
• DCT minimizes "blocking artifacts" (i.e., boundaries between subimages do not become very visible).

#### **DFT**

has n-point periodicity

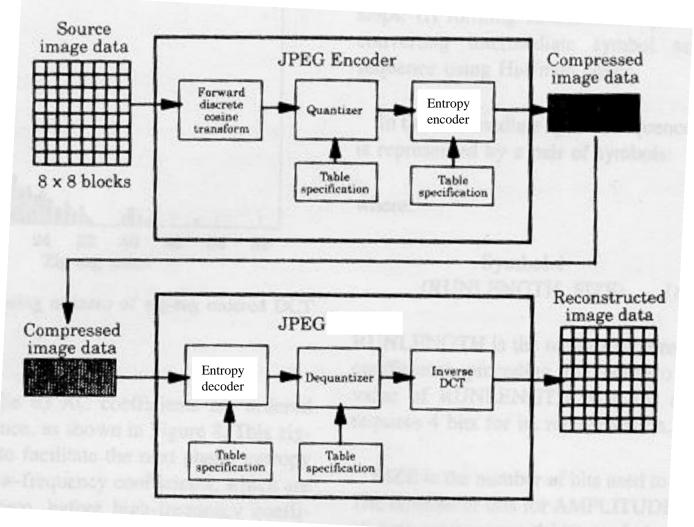
#### DCT

has 2n-point periodicity



# JPEG Compression

Accepted as an international image compression standard in 1992.



#### JPEG - Steps

1. Divide image into 8x8 subimages.

#### For each subimage do:

- 2. Shift the gray-levels in the range [-128, 127]
- 3. Apply DCT  $\rightarrow$  64 coefficients

1 DC coefficient: F(0,0)

63 AC coefficients: F(u,v)

# Example

(a) Original 8 8 block	(b) Shifted block	(c) Block after FDCT Eqn. (5)
	12 16 19 12 11 27 51 47	185 -17 14 -8 23 -9 -13 -18
140 144 1471140 140 155 179 175	16 24 12 19 12 20 39 51	20 -34 26 -9 -10 10 13 6
144 152 140 147 140 148 167 179	24 27 8 39 35 34 24 44	-10-23 -1 6-18 3-20
152 155 136 167 163 162 152 172	40 17 28 32 24 27 8 32	-8 -5 14 -14 -8 -2 -3 8
168 145 156 160 152 155 136 160	34 20 28 20 12 8 19 34	-3 9 7 1-11 17 18 15
162 148 156 148 140 136 147 162	19 39 12 27 27 12 8 34	3 -2 -18 8 8 -3 0 -6
147 167 140 155 155 140 136 162		8 0 -2 3 -1 -7 -1 -1
136 156 123 167 162 144 140 147	8 28 -5 39 34 16 12 19	0 -7 -2 1 1 4 -6 0
148 155 136 155 152 147 147 136	20 27 8 27 24 19 19 8	0 -7 -2 1 1 4 -0 0

[-128, 127]

(DCT)

#### JPEG Steps

4. Quantize the coefficients (i.e., reduce the amplitude of coefficients that do not contribute a lot).

$$C_q(u, v) = Round[\frac{C(u, v)}{Q(u, v)}]$$



Q(u,v): quantization table

### Example

Quantization Table Q[i][j]

#### for i=0 to n; for j=0 to n; Q[i,j]=1+(1+i+j)\*quality; end j; end i;

 $1 \le quality \le 25$ 

3 5 7 9 11 13 15 17 5 7 9 11 13 15 17 19 7 9 11 13 15 17 19 21 9 11 13 15 17 19 21 23 11 13 15 17 19 21 23 25 13 15 17 19 21 23 25 27 15 17 19 21 23 25 27 29 17 19 21 23 25 27 29 31

(best - low compression)

(worst - high compression)

# Example (cont'd)

#### (c) Block after FDCT Eqn. (5)

185 -17 14 -8 23 -9 -13 -18 20 -34 26 -9 -10 10 13 6 -10 -23 -1 6 -18 3 -20 0 -8 -5 14 -14 -8 -2 -3 8 -3 9 7 1 -11 17 18 15 3 -2 -18 8 8 -3 0 -6 8 0 -2 3 -1 -7 -1 -1 0 -7 -2 1 1 4 -6 0

#### Quantization



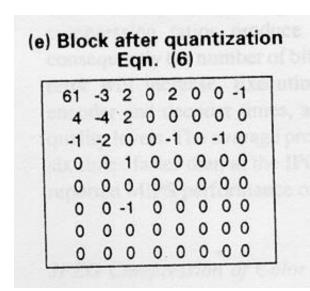
#### (e) Block after quantization Eqn. (6)

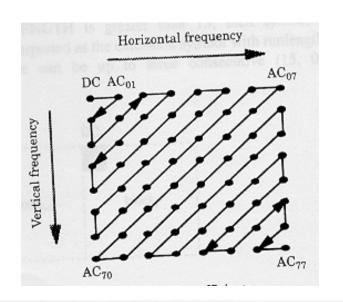
#### (d) Quantization table (quality = 2)

3 5 7 9 11 13 15 17 5 7 9 11 13 15 17 19 7 9 11 13 15 17 19 21 9 11 13 15 17 19 21 23 11 13 15 17 19 21 23 25 13 15 17 19 21 23 25 27 15 17 19 21 23 25 27 29 17 19 21 23 25 27 29 31

## JPEG Steps (cont'd)

- 5. Order the coefficients using **zig-zag** ordering
  - Creates long runs of zeros (i.e., ideal for run-length encoding)





#### (f) Zig-zag sequence

### JPEG Steps (cont'd)

- 6. Encode coefficients:
  - 6.1 Form "intermediate" symbol sequence.
  - 6.2 Encode "intermediate" symbol sequence into a binary sequence.

## Intermediate Symbol Sequence – DC coeff

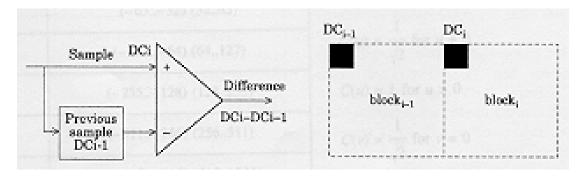
```
(g) Intermediate symbol sequence
(6)(61),(0,2)(-3),(0,3)(4),(0,1)(-1),(0,3)(-4),(0,2)(2),(1,2)(2),(0,2)(-2),
(5,2)(2),(3,1)(1),(6,1)(-1),(2,1)(-1),(4,1)(-1),(7,1)(-1),(0,0)
```

SIZE: # bits need to encode the coefficient

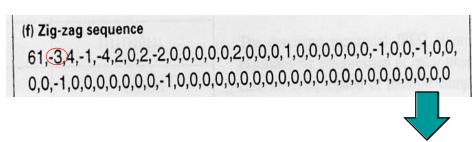
DC

## DC Coefficient Encoding

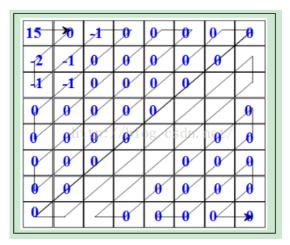
predictive coding:



## Intermediate Symbol Sequence – AC coeff



(g) Intermediate symbol sequence  $(6)(61), (0,2)(-3), (0,3)(4), (0,1)(-1), (0,3)(-4), (0,2)(2), (1,2)(2), (0,2)(-2), \\ (5,2)(2), (3,1)(1), (6,1)(-1), (2,1)(-1), (4,1)(-1), (7,1)(-1), (0,0)$ 



end of block

(1,-2),(0,-1),(0,-1),(0,-1),(2,-1), (0,0) --EOB (continuous zeros, next non-zero)

RUN-LENGTH: run of zeros preceding coefficient SIZE: # bits for encoding the amplitude of coefficient

**Note:** If RUN-LENGTH > 15, use symbol (15,0),

### Example: JPEG compression

Y 分量 DC 系数 Huffman 表				Y 分量 AC 系数 Huffman 表			
Size	Code length	code		Run/size	Length of code	code	
0	2	00		0/0(EOB)	4	1010	
1	3	010		0/1	2	00	
<u> </u>				0/2	2	01	
2	3	011		0/3	3	100	
3	3	100		0/4	4	1011	
4	3	101					
5	3	110tp://	$_{0}1$	<del>g. cs<mark>4/1</mark>. net</del> /	4	1100	
	-			0 1/2	5	11011	
6	4	1110					
7	5	11110		2/1	5	11100	
8	6	111110		3/1	6	111010	
9	7	1111110					
	,			6/1	/	1111011	
10	8	11111110					
11	9	111111110		F/0(ZRL)	11	11111111001	

15	0	-1	0	0	0	0	0
-2	-1	0	0	0	0	0	0
-1	-1	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	http <b>0</b>	0	og.ocs	dn ne <b>O</b>	<b>o</b>	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0

Assume previous DC=12, the coefficient after quantization is :

DC encoder:  $3 \rightarrow (2,3) \rightarrow (011,11)$ 

#### AC encoder:

$$(1,-2)$$
- $(1/2, -2)$  -T2-> 11011,  $(-2-1)$ mod2 -> 11011,01

$$(0,-1)$$
-> $(0/1, -1)$  -T2-> 00,  $(-1-1)$ mod2 -> 00,0

$$(0,-1)$$
-> $(0/1, -1)$  -T2-> 00,  $(-1-1)$ mod2 -> 00,0

$$(0,-1)$$
-> $(0/1, -1)$  -T2-> 00,  $(-1-1)$ mod2 -> 00,0

#### After compression:

$$5+7+3+3+3+6+4 = 31$$
 bits; (previous  $8*8*8=512$  bits)

## What is the effect of the "Quality" parameter?



(58k bytes)



(21k bytes)



(8k bytes)

lower compression

higher compression

 $1 \le quality \le 25$ 

# What is the effect of the "Quality" parameter? (cont'd)

Table 6. Results of JPEG Compression for Grayscale Image 'Lisa' (320 ×240 pixels)

Quality factors	Original number of bits	Compressed number of bits	Compression ratio (Cr)	Bits/pixel (Nb)	RMS
1	512,000	48,021	10-66	0.75	2.25
2	512,000	30,490	16·79 0·48 25·27 0·32	0.48	2.75
4	512,000 512,000	20,264		3.43	
8		14,162	36-14	0.22	4.24
15	512,000	10,479	48-85	0-16	5.36
25	512,000	9,034	56-64	0-14	6-40

# Effect of Quantization: homogeneous 8 x 8 block



An 8 × 8 block from the Y image of 'Lena'

Fig. 9.2: JPEG compression for a smooth image block.

# Effect of Quantization: homogeneous 8 x 8 block (cont'd)

#### Quantized

# 

#### De-quantized

# Effect of Quantization: homogeneous 8 x 8 block (cont'd)

#### Reconstructed

199 196 191 186 182 178 177 176 201 199 196 192 188 183 180 178 203 203 202 200 195 189 183 180 202 203 204 203 198 191 183 179 200 201 202 201 196 189 182 177 200 200 199 197 192 186 181 177 204 202 199 195 190 186 183 181 207 204 200 194 190 187 185 184

#### Original



#### Error is low!

1 6 -2 2 7 -3 -2 -1 -1 4 2 -4 1 -1 -2 -3 0 -3 -2 -5 5 -2 2 -5 -2 -3 -4 -3 -1 -4 4 8 0 4 -2 -1 -1 -1 5 -2 0 0 1 3 8 4 6 -2 1 -2 0 5 1 1 4 -6 3 -4 0 6 -2 -2 2 2

200 202 189 188 189 175 175 175 200 203 198 188 189 182 178 175 203 200 200 195 200 187 185 175 200 200 200 200 197 187 187 187 200 205 200 200 195 188 187 175 205 200 199 200 191 187 187 186 210 200 200 200 188 185 187 186

# Effect of Quantization: non-homogeneous 8 x 8 block



Another  $8 \times 8$  block from the Y image of 'Lena'

```
-80 -40 89 -73 44 32 53 -3
   70 100 70 87 87 150 187
85 100 96 79 87 154 87 113
                              -135-59-26 6 14 -3-13-28
100 85 116 79 70 87 86 196
                               47 - 76 66 - 3 - 108 - 78 33 59
136 69 87 200 79 71 117 96
                           -2 10-18 0 33 11-21
161 70 87 200 103 71 96 113
                            -1 -9-22 8 32 65-36 -1
161 123 147 133 113 113 85 161 5 - 20 28 - 46 3 24 - 30 24
                           6-20 37-28 12-35 33 17
146 147 175 100 103 103 163 187
156 146 189 70 113 161 163 197
                                -5-23 33-30 17 -5 -4 20
           f(i,j)
                                       F(u,v)
```

# Effect of Quantization: non-homogeneous 8 x 8 block (cont'd)

#### Quantized

#### 

#### De-quantized

# Effect of Quantization: non-homogeneous 8 x 8 block (cont'd)

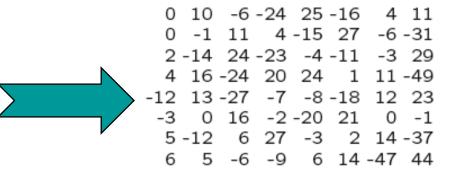
#### Reconstructed

70 60 106 94 62 103 146 176 85 101 85 75 102 127 93 144 98 99 92 102 74 98 89 167 132 53 111 180 55 70 106 145 173 57 114 207 111 89 84 90 164 123 131 135 133 92 85 162 141 159 169 73 106 101 149 224 150 141 195 79 107 147 210 153

#### Original:

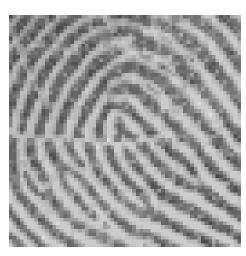
70 70 100 70 87 87 150 187 85 100 96 79 87 154 87 113 100 85 116 79 70 87 86 196 136 69 87 200 79 71 117 96 161 70 87 200 103 71 96 113 161 123 147 133 113 113 85 161 146 147 175 100 103 103 163 187 156 146 189 70 113 161 163 197

#### Error is high!



## Case Study: Fingerprint Compression

- FBI is digitizing fingerprints at 500 dots per inch with 8 bits of grayscale resolution.
- A single fingerprint card turns into about 10 MB of data!



A sample fingerprint image 768 x 768 pixels =589,824 bytes

### WSQ Fingerprint Compression

- An image coding standard for digitized fingerprints employing the Discrete Wavelet Transform (Wavelet/Scalar Quantization or WSQ).
- Developed and maintained by:
  - FBI
  - Los Alamos National Lab (LANL)
  - National Institute for Standards and Technology (NIST)

## Need to Preserve Fingerprint Details



The "white" spots in the middle of the black ridges are *sweat pores* and they are admissible points of identification in court.

These details are just a couple pixels wide!

#### What compression scheme should be used?

- Lossless or lossy compression?
- In practice lossless compression methods haven't done better than 2:1 on fingerprints!
- Does JPEG work well for fingerprint compression?

### Results using JPEG compression

file size 45853 bytes compression ratio: 12.9



Fine details have been lost.

Image has an artificial "blocky" pattern superimposed on it.

Artifacts will affect the performance of fingerprint recognition.

### Results using WSQ compression

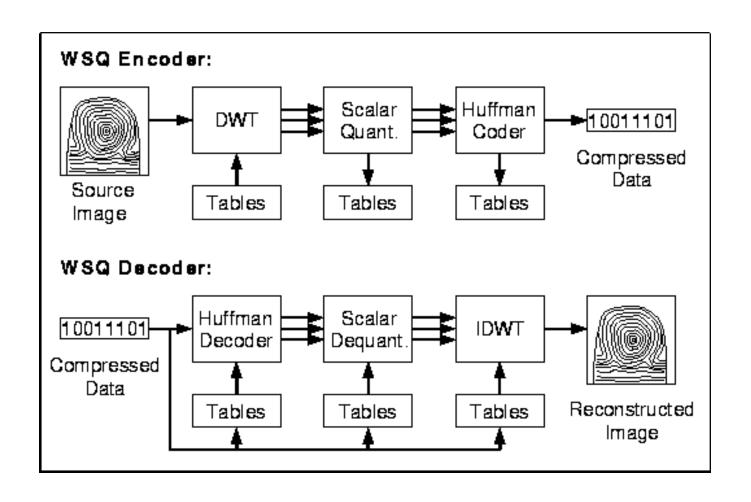
file size 45621 bytes compression ratio: 12.9



Fine details are better preserved.

No "blocky" artifacts.

### WSQ Algorithm



### Compression ratio

- FBI's target bit rate is around 0.75 bits per pixel (bpp)
- This corresponds to a compression ratio of 8/0.75=10.7

• Target bit rate can set via a parameter, similar to the "quality" parameter in JPEG.

# Varying compression ratio (cont'd)

Original image 768 x 768 pixels (589824 bytes)



# Varying compression ratio (cont'd) 0.9 bpp compression

WSQ image, file size 47619 bytes, compression ratio 12.4



JPEG image, file size 49658 bytes, compression ratio 11.9



# Varying compression ratio (cont'd) 0.75 bpp compression

WSQ image, file size 39270 bytes compression ratio 15.0



JPEG image, file size 40780 bytes, compression ratio 14.5



# Varying compression ratio (cont'd) 0.6 bpp compression

WSQ image, file size 30987 bytes, compression ratio 19.0



JPEG image, file size 30081 bytes, compression ratio 19.6



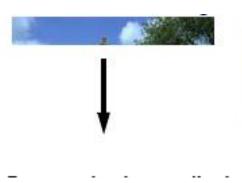
#### JPEG Modes

- JPEG supports several different modes
  - Sequential Mode
  - Progressive Mode
  - Hierarchical Mode
  - Lossless Mode
- The default mode is "sequential"
  - Image is encoded in a single scan (left-to-right, top-to-bottom).

# Progressive JPEG

• Image is encoded in multiple scans, in order to produce a quick, rough decoded image when transmission time is long.

Sequential







Progressive







# Progressive JPEG (cont'd)

Each scan encodes a subset of DCT coefficients.

- We'll examine the following algorithms:
  - (1) Progressive spectral selection algorithm
  - (2) Progressive successive approximation algorithm
  - (3) Combined progressive algorithm

# Progressive JPEG (cont'd)

#### (1) Progressive spectral selection algorithm

- Group DCT coefficients into several spectral bands
- Send low-frequency DCT coefficients first
- Send higher-frequency DCT coefficients next

Band 1: DC coefficient only

Band 2:  $AC_1$  and  $AC_2$  coefficients

Band 3:  $AC_3$ ,  $AC_4$ ,  $AC_5$ ,  $AC_6$ , coefficients

Band 4:  $AC_7...AC_{63}$ , coefficients

# Example

Table 8. Progressive spectral selection JPEG. (Image 'Cheetah': 320 × 240 pixels -> 512,000 bits)

Scan number	Bits transmitted	Compression ratio	Bits/pixel	RMS error
1	29,005	17-65	0-45	
2	37,237	7.73	1-04	13-67
3	71,259	3-72	2-15	7.90
4	32,489	3-01	2-66	4-59
Sequential JPEG	172,117	2.97	2-69	4-59

## Progressive JPEG (cont'd)

#### (2) Progressive successive approximation algorithm

- Send all DCT coefficients but with lower precision.
- Refine DCT coefficients in later scans.

Band 1: All DCT coefficients (divided by four)

Band 2: All DCT coefficients (divided by two)

Band 3: All DCT coefficients (full resolution)

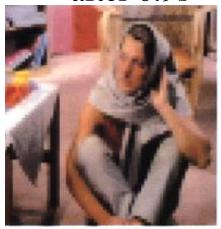
# Example

Table 9. Progressive successive approximation JPEG. (Image 'Cheetah': 320 × 240 pixels -> 512,000 bits)

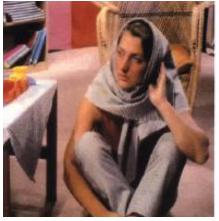
Scan number	Bits transmitted	Compression ratio	Bits/pixel	RMS error
1	26,215	19-53	0.41	22-48
2	34,506	8-43	0.95	12:75
3	63,792	4-11	1.95	7-56
4	95,267	2.33	2-43	4-59
Sequential JPEG	172,117	2.97	2-69	4.59

# Example

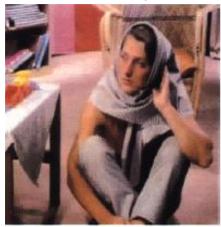
after 0.9s



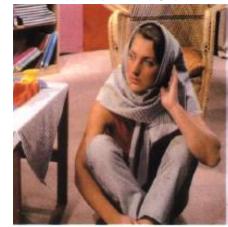
after 3.6s



after 1.6s



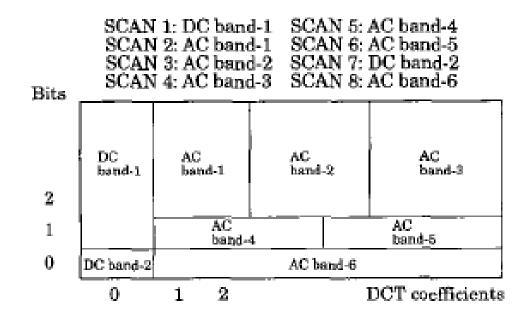
after 7.0s



## Progressive JPEG (cont'd)

#### (3) Combined progressive algorithm

Combines spectral selection and successive approximation.



### Hierarchical JPEG

• Hierarchical mode encodes the image at different resolutions.

• Image is transmitted in multiple passes with increased resolution at each pass.

### Hierarchical JPEG (cont'd)

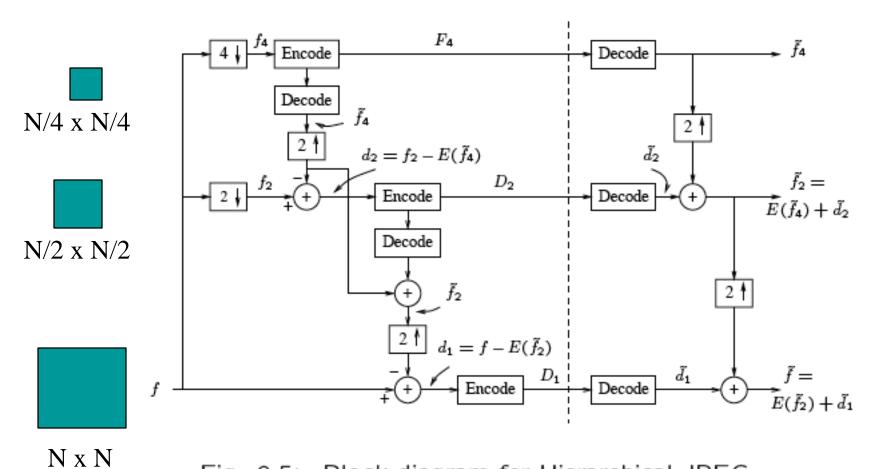


Fig. 9.5: Block diagram for Hierarchical JPEG.

#### More Methods ...

• See "Image Compression Techniques", IEEE Potentials, February/March 2001

# Deep Learning Image Compression

- Learned-transform
  - Auto-encoders learn latent-space representation of images
- Differentiable approximation to quantization
  - Soft quantization
- Generative Codecs
  - O. Rippel and L. Bourdev, "Real-time adaptive image compression," ICML 2017, arXiv, 16 May 2017.
  - S. Santurkar, D. Budden, and N. Shavit, "Generative compression," arXiv, June 2017.

# Soft Quantization

Hard quantization for d-bits:

$$q = Q(z) = |z| \times 2^d$$

- However this function yields zero gradients except at decision boundaries. Therefore soft quantization is employed in training phase.
- Soft quantization for d-bits:

$$\tilde{z} = \sum_{i=0}^{2^{d}-1} \frac{\exp(-\|z \times 2^{d} - i\|)}{\sum_{j=0}^{2^{d}-1} \exp(-\|z \times 2^{d} - j\|)} \times i$$

E. Agustsson, et al. Soft-to-hard vector quantization for end-to-end learning compressible representations. NIPS, 2017

# **Enhancing Standard Codecs**

- Deep networks learn free parameters of state of the art standards-based encoders
  - Block partitioning
  - Mode selection
  - Quantization parameter selection
  - In-loop filter
- Pre-processing and/or post-processing
  - Learned smoothing for pre-processing
  - Artifact removal

# CVPR-CLIC 2018

### Challenge on Learned Image Compression

#### Rules

- Compression rate of the whole test set must not exceed 0.15 bpp (average).
- Participants are ranked according to
  - PSNR
  - Scores provided by human raters (MOS)

#### Dataset

- New: 1633 training, 102 validation, 286 test images.
  - DatasetP (professional)
  - DatasetM (mobile)

### CLIC 2018 Winners

- Best MOS (also best MS-SSIM)
  - An Autoencoder-based Learned Image Compressor: Description of Challenge Proposal by NCTU
- Best PSNR
  - CNN-Optimized Image Compression with Uncertainty based Resource Allocation
- Fastest:
  - xvc codec

## CLIC 2018 Results

## Only submissions which are evaluated for MOS scores are shown.

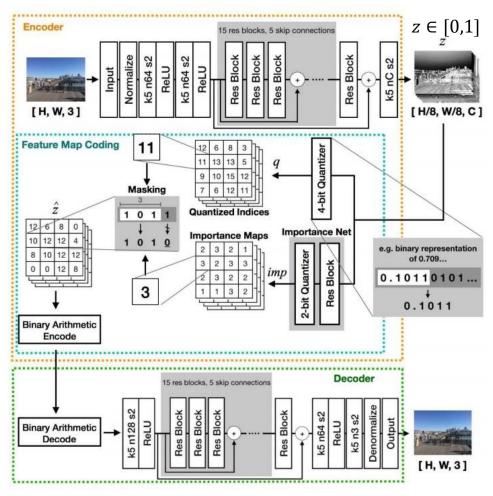
Entry	PSNR	MOS	MS-SSIM	Images Size (Bytes)	Decoding Time (ms)	Decoder Size (Bytes)
TucodecTNGcnn4p	27.67	3.587823941	0.964	13323808	15412641	97043988
XVC	27.09	3.580864198	0.954	13328076	535566	853416
iipTiramisu	30.89	3.56129165	0.955	13320299	111905135	9034988
TucodecTNG	30.76	3.552263374	0.955	13325574	46535029	2596395
yfan	30.43	3.531069959	0.951	13324840	74712678	4779153
tangzhimin	30.24	3.490740741	0.951	13308588	30311917	4984420
Amnesiack	30.30	3.450020568	0.950	13327732	179313414	7070429
AmnesiackLite	28.77	3.440510498	0.956	13325728	29297186	1220246
MVGL	30.14	3.3571723	0.948	13328219	219961195	25873249
BPG	29.64	3.175066859	0.943	13189634	333725	377858
JPEG	25.66	1.170987654	0.863	13326518	136074	166

### **Fastest**

- xvc A conventional codec
  - proprietary
  - Block based
  - Traditional approach for prediction, residual representation
- Originally developed for video compression.
- No machine learning is involved.

J.Samuelsson, P. Hermansson, Image compression with xvc, IEEE Conf. on Computer Vision and Pattern Recognition (CVPR) Workshops, June, 2018

# Best MOS and MS-SSIM



- Based on autoencoder
- 4-bit quantization
- Soft quantization
- Importance Network

D. Alexandre, et al., An autoencoder-based learned image compressor: Description of challenge proposal by NCTU, IEEE Conf. on Computer Vision and Pattern Recognition (CVPR) Workshops, June, 2018

# Importance Net

- Importance Net learns the important parts of the representation so that the system allocates more bits to complicated areas.
- It is made of residual blocks and another quantizer to select the number of bits

# Optimization - Loss Function

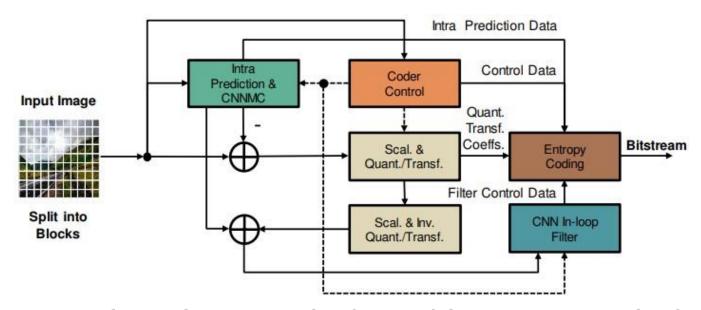
Loss function is a weighted sum of rate and distortion

• 
$$L = \lambda \times H(imp) + L_d$$
  
where

$$L_d = \frac{MSE}{2\sigma_1^2} + \frac{MSSSIM}{2\sigma_2^2} + \log(\sigma_1^2) + \log(\sigma_2^2)$$

- Rate loss H(imp) is estimated by summing up all values of the importance maps imp
- $\sigma_1$  and  $\sigma_2$  are learnable parameters

### Best PSNR

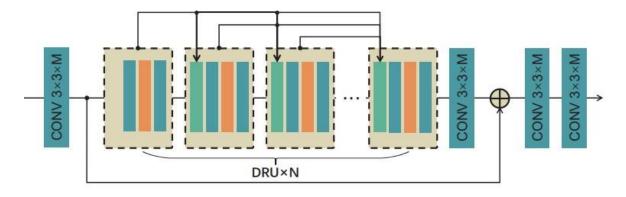


- Based on the JEM platform (the HEVC codec)
- Contributions:
  - CNN based in-loop filter (CNNIF) and
  - CNN based mode coding (CNNMC)

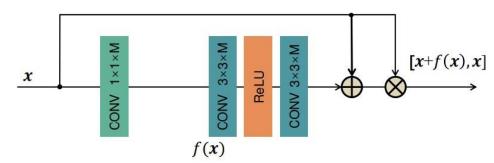
Z. Chen, et al., CNN-optimized image compression with uncertainty based resource allocation, IEEE Conf. on Computer Vision and Pattern Recognition (CVPR) Workshops, June, 2018

# CNN based In-Loop Filter (CNNIF)

 In-loop filter consists of stacked Dense Residual Units (DRU)

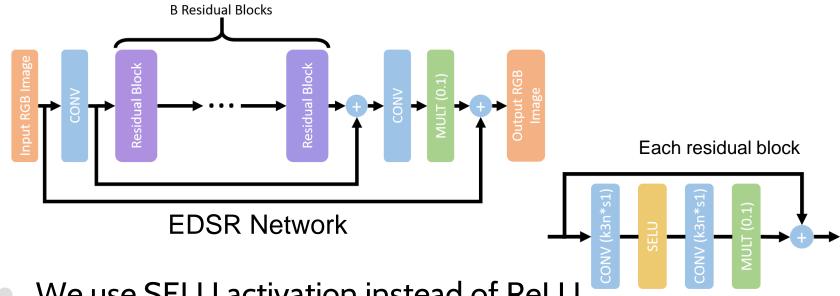


A Dense Residual Unit (DRU)



# Learned Artifact Suppression

Compression artifacts have structure that can be learned



- We use SELU activation instead of ReLU
- It is trained to remove artifacts introduced by BPG codec.
- Although we trained our network with a single QP (40), it can improve images encoded by QP between 39 and 43.

O. Kirmemis, G. Bakar and A.M. Tekalp, Learned Compression artifact removal by deep residual networks, IEEE Conf. on Computer Vision and Pattern Recognition (CVPR) Workshops, June 2018

# Residual GRU (RGRU)

Instead of using a DCT to generate a new bit representation they train two sets of neural networks - one encoder and another decoder

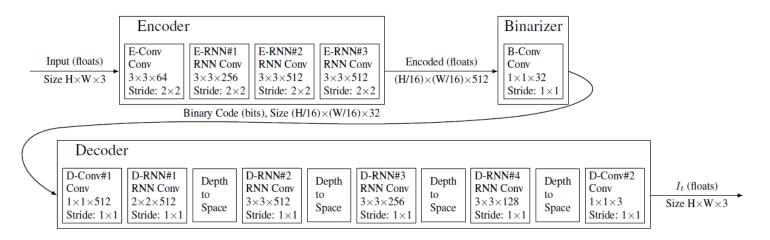


Figure 1. A single iteration of our shared RNN architecture.

https://ai.googleblog.com/2016/09/image-compression-with-neural-networks.html

https://www.youtube.com/watch?v=RRPuXMyKIWw

https://zhuanlan.zhihu.com/p/38248372