

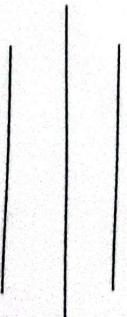


PATAN MULTIPLE CAMPUS

Patandhoka, Lalitpur

BCA 3rd semester

Probability and Statistics(CACS-202)



Presented by :- Bimal Acharya

Page No. 13

INDEX PAGE AND DETAILS

| S.N | Lab Works | Date | Signature |
|-----|---------------------------------|------------|-----------|
| 1. | Individual Series | 2022/01/11 | |
| 2. | Individual Series & Consistency | 2022/01/11 | |
| 3. | Discrete Series | 2022/01/11 | |
| 4. | Correlation Coefficient | 2022/01/16 | |
| 5. | Regression Equation | 2022/01/16 | |
| 6. | One-Way ANOVA | 2022/01/16 | |
| 7. | Two-Way ANOVA | 2022/01/22 | |
| 8. | Binomial Distribution | 2022/01/25 | |
| 9. | Poisson Distribution | 2022/01/30 | |
| 10. | Normal Distribution | 2022/01/31 | |

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Practical No. 1: Individual Series

Level:- TU BCA 3rd Semester

Date:- 2081/01/11

Subject:- Probability and Statistics (CACS-202)

Roll No:- 13/080

Name: Bimal Acharya

Question:-

Find no. of observations, minimum value, maximum value, mean, median, mode, quartiles, range, standard deviation, variance and coefficient of variation of the following observations:

100, 80, 79, 50, 52, 80, 79, 80, 105, 79, 82, 80, 84, 64, 70, 71, 80, 45, 54, 80, 95, 80

Working Expression:-

$n = \text{no. of observation}$

$s = \text{minimum value}$

$L = \text{maximum value}$

$\text{Mean } (\bar{x}) = \frac{\sum x}{n}$

$\text{Median } (M_d) = \left(\frac{n+1}{2} \right)^{\text{th}} \text{ item value}$

$\text{Mode } (M_o) = \text{Maximum repetition number}$

$\text{First Quartile } (Q_1) = \left(\frac{n+1}{4} \right)^{\text{th}} \text{ item value}$

$\text{Third Quartile } (Q_3) = 3 \left(\frac{n+1}{4} \right)^{\text{th}} \text{ item value}$

$\text{Range } (R) = L - s$

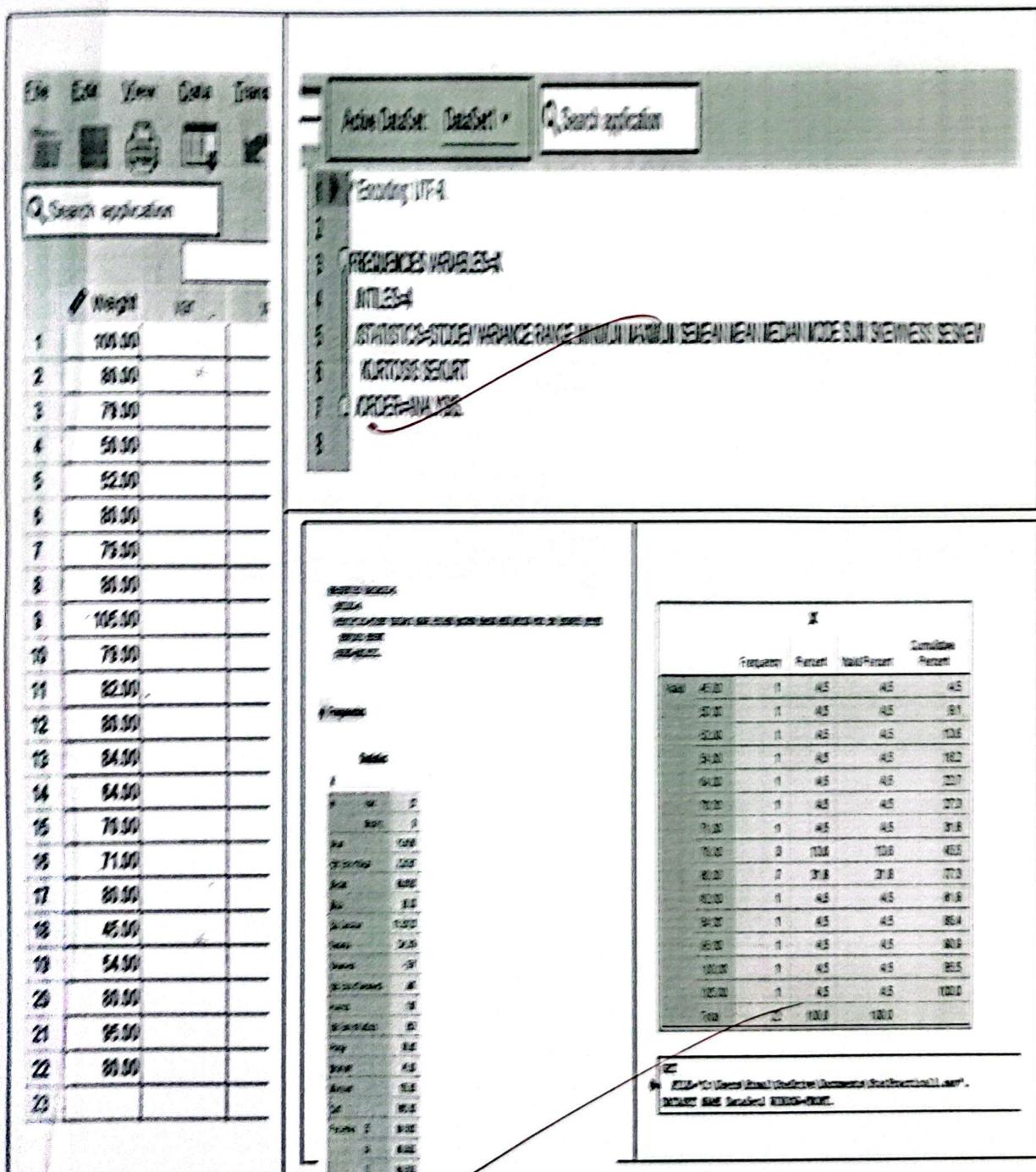
$\text{Coefficient of Range} = \frac{L-s}{L+s}$

$\text{Standard Deviation } (S.D) = \sqrt{\frac{\sum (x-\bar{x})^2}{n}}$

$\text{Coefficient of variation} = \frac{\sigma}{\bar{x}} \times 100\%$

Results

Info



Results :-

$$n = 22$$

$$S = 45$$

$$L = 105$$

$$\bar{X} = 75.8636$$

$$Md = 80$$

$$Mo = 80$$

$$Q_1 = 68.5$$

$$Q_3 = 80.5$$

$$R = 60$$

$$\text{Coefficient of Range} = \frac{105 - 45}{105 + 45} = \frac{60}{150} = \frac{2}{5}$$

$$S.d(\sigma) = 15.30420$$

$$\text{Variance} (\sigma^2) = 234.219$$

$$\text{Coefficient of Variation} = \left(\frac{\sigma}{\bar{X}} \right) \times 100\% = \frac{15.30420}{75.8636} \times 100 = 20.27\%$$

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0821112~~

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Practical No. 2: Individual Series & Consistency

Level:- TU BCA 3rd Semester

Date:- 2081/01/11

Subject:- Probability and Statistics (CACS-202)

Roll No:- 13/080

Name: Bimal Acharya

Question:-

Find no. of observations, minimum value, maximum value, mean, median, mode, quartiles, range, standard deviation, variance and coefficient of variation of the following observations:

| Height | Weight | Age |
|--------|--------|-------|
| 3.00 | 12.00 | 2.00 |
| 3.50 | 15.00 | 5.00 |
| 5.80 | 50.00 | 15.00 |
| 4.20 | 55.00 | 20.00 |
| 5.00 | 60.00 | 30.00 |
| 5.10 | 59.00 | 25.00 |
| 5.00 | 55.00 | 25.00 |
| 5.10 | 48.00 | 30.00 |
| 4.20 | 55.00 | 25.00 |
| 5.00 | 50.00 | 40.00 |
| 5.40 | 54.00 | 45.00 |

Working Expression:-

$n = \text{No. of observation}$

$S = \text{minimum value}$

$L = \text{maximum value}$

$\text{mean} (\bar{x}) = \frac{\sum x}{n}$

$\text{median} (Md) = \left(\frac{n+1}{2} \right)^{\text{th}} \text{ item value}$

$\text{Mode} (Mo) = \text{maximum repeated number}$

$\text{First Quartile} (Q_1) = \left(\frac{n+1}{4} \right)^{\text{th}} \text{ item value}$

$\text{Third Quartile} (Q_3) = 3 \left(\frac{n+1}{4} \right)^{\text{th}} \text{ item value}$

$\text{Range} = L - S$

$\text{Standard Deviation} (\sigma) = \sqrt{\frac{\sum (x - \bar{x})^2}{n}}$

$\text{Coefficient of Variation} = \frac{\sigma}{\bar{x}} \times 100\%$

LAB2:-

| | Weight | Age | Height | Var |
|----|--------|-------|--------|-----|
| 1 | 100.00 | 25.00 | 4.11 | |
| 2 | 80.00 | 31.00 | 6.00 | |
| 3 | 79.00 | 32.00 | 6.11 | |
| 4 | 50.00 | 58.00 | 5.00 | |
| 5 | 52.00 | 45.00 | 4.10 | |
| 6 | 80.00 | 11.00 | 6.10 | |
| 7 | 79.00 | 58.00 | 4.50 | |
| 8 | 80.00 | 98.00 | 5.00 | |
| 9 | 105.00 | 65.00 | 5.11 | |
| 10 | 79.00 | 45.00 | 5.80 | |
| 11 | 82.00 | 32.00 | 6.00 | |
| 12 | 80.00 | | 5.50 | |
| 13 | 84.00 | | 5.60 | |
| 14 | 64.00 | | 4.90 | |
| 15 | 70.00 | | | |
| 16 | 71.00 | | | |
| 17 | 80.00 | | | |
| 18 | 45.00 | | | |
| 19 | 54.00 | | | |
| 20 | 80.00 | | | |
| 21 | 95.00 | | | |
| 22 | 80.00 | | | |
| 23 | | | | |

```
1 Encoding: UTF-8.
2
3 DATA SET ACTIVATE DataSet2.
4 FREQENCIES VARIABLES=Weight Age Height
5 NTILES=4
6 /STATISTICS=STDDEV VARIANCE RANGE MINIMUM MAXIMUM SEMEAN MEAN MEDIAN MODE SUM SKEWNESS SESKEW
7 KURTOSIS SEKURT
8 ORDER=ANALYSIS.
```

Double-click to
activate

| | | Frequency | Percent | Valid Percent | Cumulative Percent |
|---------|--------|-----------|---------|---------------|--------------------|
| Valid | System | | | | |
| 11.00 | | 1 | 4.5 | 9.1 | 9.1 |
| 25.00 | | 1 | 4.5 | 9.1 | 18.2 |
| 31.00 | | 1 | 4.5 | 9.1 | 27.3 |
| 32.00 | | 2 | 9.1 | 18.2 | 45.5 |
| 45.00 | | 2 | 9.1 | 18.2 | 63.6 |
| 56.00 | | 2 | 9.1 | 18.2 | 81.8 |
| 65.00 | | 1 | 4.5 | 9.1 | 90.9 |
| 98.00 | | 1 | 4.5 | 9.1 | 100.0 |
| Total | | 11 | 50.0 | 100.0 | |
| Missing | System | 11 | 50.0 | | |
| Total | | 22 | 100.0 | | |

Height

| | | Frequency | Percent | Valid Percent | Cumulative Percent |
|---------|--------|-----------|---------|---------------|--------------------|
| Valid | System | | | | |
| 4.10 | | 1 | 4.5 | 7.1 | 7.1 |
| 4.11 | | 1 | 4.5 | 7.1 | 14.3 |
| 4.50 | | 1 | 4.5 | 7.1 | 21.4 |
| 4.90 | | 1 | 4.5 | 7.1 | 28.6 |
| 5.00 | | 2 | 9.1 | 14.3 | 42.9 |
| 5.11 | | 1 | 4.5 | 7.1 | 50.0 |
| 5.50 | | 1 | 4.5 | 7.1 | 57.1 |
| 5.60 | | 1 | 4.5 | 7.1 | 64.3 |
| 5.80 | | 1 | 4.5 | 7.1 | 71.4 |
| 6.00 | | 2 | 9.1 | 14.3 | 85.7 |
| 6.10 | | 1 | 4.5 | 7.1 | 92.9 |
| 6.11 | | 1 | 4.5 | 7.1 | 100.0 |
| Total | | 14 | 63.6 | 100.0 | |
| Missing | System | 8 | 36.4 | | |
| Total | | 22 | 100.0 | | |

DATAVIEW ACTIVE WORKSHEET
 PROTECTED VARIABLES=Weight, Age, Height
 /TITLE=4
 /STATISTICS=STDEV VARIANCE RANGE MEAN MEDIAN MODE STD DEVIATION SEED
 MISSING SOURCE
 /FORMAT=DECIMALS.

↳ Frequencies

| Statistics | | | | |
|------------------------|---------|---------|---------|--------|
| | Weight | Age | Height | |
| N | 32 | 11 | 14 | |
| Valid | 32 | 11 | 14 | |
| Missing | 0 | 0 | 0 | |
| Mean | 73.9438 | 45.0959 | 62.7356 | |
| Std. Error of Mean | .126287 | .709732 | .18625 | |
| Median | 66.0000 | 46.0000 | 63.050 | |
| Mode | 60.00 | 32.00* | 5.04* | |
| Std. Deviation | 13.3642 | 23.5391 | .70811 | |
| Variance | 334.219 | 564.091 | .501 | |
| Skewness | -1.74 | .971 | -4.15 | |
| Std. Error of Skewness | .491 | .681 | .587 | |
| Kurtosis | -1.76 | 1.585 | -1.055 | |
| Std. Error of Kurtosis | .953 | 1.278 | 1.154 | |
| Range | 80.00 | 87.00 | 2.01 | |
| Minimum | 45.00 | 11.00 | 4.10 | |
| Maximum | 105.00 | 98.00 | 6.11 | |
| Sum | 1463.00 | 494.00 | 73.43 | |
| Percentiles | 25 | 68.5000 | 31.0000 | 4.8000 |
| | 50 | 80.0058 | 45.0000 | 5.2059 |
| | 75 | 89.5000 | 58.0000 | 8.0000 |

a. Multiple modes exist. The smallest value is shown

Frequency Table

| Weight | | | | |
|--------|-----------|---------|---------------|--------------------|
| | Frequency | Percent | Valid Percent | Cumulative Percent |
| Valid | 45.00 | 1 | 4.5 | 4.5 |
| | 50.00 | 1 | 4.5 | 4.5 |
| | 52.00 | 1 | 4.5 | 4.5 |
| | 54.00 | 1 | 4.5 | 4.5 |
| | 64.00 | 1 | 4.5 | 4.5 |
| | 70.00 | 1 | 4.5 | 4.5 |
| | 71.00 | 1 | 4.5 | 4.5 |
| | 79.00 | 3 | 13.6 | 13.6 |
| | 80.00 | 7 | 31.8 | 45.5 |
| | 82.00 | 1 | 4.5 | 4.5 |
| | 84.00 | 1 | 4.5 | 4.5 |
| | 95.00 | 1 | 4.5 | 4.5 |
| | 100.00 | 1 | 4.5 | 4.5 |
| | 105.00 | 1 | 4.5 | 4.5 |
| Total | 22 | 100.0 | 100.0 | 100.0 |

Results:-

n=72

| | Height | Weight | Age |
|--------------------------|---------|----------|----------|
| N | 72 | 72 | 72 |
| S | 3 | 22 | 2 |
| L | 5.8 | 60 | 45 |
| \bar{x} | 4.6636 | 46.6364 | 23.8182 |
| Md | 5 | 54 | 25 |
| M_0 | 5 | 55 | 25 |
| Q_1 | 4.2 | 48 | 15 |
| Q_3 | 5.1 | 55 | 30 |
| R | 2.8 | 4.8 | 43 |
| Coefficient of Range | 0.318 | 0.67 | 0.914 |
| σ | 0.84294 | 16.79448 | 13.09059 |
| σ^2 | 0.711 | 282.055 | 171.364 |
| Coefficient of Variation | 18.074% | 36.011% | 54.96% |

Since C.V of height (C.V.u) is less the data of height is more consistent.

~~EAS
0821114~~

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Practical No. 3: Descriptive Statistics

Level:- TU BCA 3rd Semester

Date:- 2081/01/11

Subject:- Probability and Statistics (CACS-202)

Roll No:- 13/080

Name: Bimal Acharya

Question:-

Find no. of observations, minimum value, maximum value, mean, median, mode, quartiles, range, standard deviation, variance and coefficient of variation of the following observations:

| Marks | 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 | 100 |
|----------------|----|----|----|----|----|----|----|----|----|-----|
| No.of students | 2 | 3 | 5 | 15 | 20 | 15 | 4 | 2 | 1 | 0 |

Working Expression:-

$$n = \sum f$$

S = Smallest value

L = Largest value

$$\text{mean} (\bar{x}) = \frac{\sum fx}{n}$$

$$\text{median} (Md) = \left(\frac{N+1}{2} \right)^{\text{th}} \text{ item value}$$

mode (Mo) = maximum frequency value

$$\text{first Quartile} (Q_1) = \left(\frac{N+1}{4} \right)^{\text{th}} \text{ item value}$$

$$\text{Third Quartile} (Q_3) = 3 \left(\frac{N+1}{4} \right)^{\text{th}} \text{ item value}$$

$$\text{Range} = L - S$$

$$\text{Standard Deviation} (\sigma) = \sqrt{\frac{\sum f(x-\bar{x})^2}{N}}$$

$$\text{Variance} = \frac{\sum f(x-\bar{x})^2}{N}$$

$$\text{Coefficient of Variation} = \frac{\sigma}{\bar{x}} \times 100\%$$

Lab3:-

| | x | r | var |
|----|--------|-------|-----|
| 1 | 5.00 | 1.00 | |
| 2 | 10.00 | 2.00 | |
| 3 | 15.00 | 3.00 | |
| 4 | 20.00 | 5.00 | |
| 5 | 25.00 | 6.00 | |
| 6 | 30.00 | 9.00 | |
| 7 | 35.00 | 20.00 | |
| 8 | 40.00 | 15.00 | |
| 9 | 45.00 | 4.00 | |
| 10 | 50.00 | 5.00 | |
| 11 | 55.00 | 65.00 | |
| 12 | 60.00 | 4.00 | |
| 13 | 65.00 | 32.00 | |
| 14 | 70.00 | 15.00 | |
| 15 | 75.00 | 45.00 | |
| 16 | 80.00 | 20.00 | |
| 17 | 85.00 | 15.00 | |
| 18 | 90.00 | 12.00 | |
| 19 | 95.00 | 30.00 | |
| 20 | 100.00 | 9.00 | |
| 21 | | | |

```
1 Encoding: UTF-8.
2
3 DATA SET ACTIVATE DataSet6.
4 WEIGHT BY l.
5
6 FREQUENCIES VARIABLES=x
7 /NTILES=4
8 /STATISTICS=STDDEV VARIANCE RANGE MINIMUM MAXIMUM SEMEAN MEAN MEDIAN MODE SUM SKEWNESS SESKEW
9 KURTOSIS SEKURT
10 /ORDER=ANALYSIS.
11 *
```

```

DATASET ACTIVATE Database;
WEIGHT BY F;
FREQUENCIES VARIABLES=Z
/NNTILES=4
/STATISTICS=STANDARD VARIABLE RANGE MINIMUM MAXIMUM SEMIAN MEAN MEDIAN MODE SEM SKEWNESS KURTOSIS
/ORDER=ANALYSIS.

```

↳ Frequencies

Statistics

| | Valid | 317 |
|------------------------|--|-----|
| | Missing | 0 |
| Mean | 64.1798 | |
| Std. Error of Mean | 1.20431 | |
| Median | 65.0000 | |
| Mode | 55.00 | |
| Std. Deviation | 21.44221 | |
| Variance | 459.768 | |
| Skewness | -0.43 | |
| Std. Error of Skewness | .137 | |
| Kurtosis | -0.07 | |
| Std. Error of Kurtosis | .273 | |
| Range | 95.00 | |
| Minimum | 5.00 | |
| Maximum | 100.00 | |
| Sum | 20345.00 | |
| Percentiles | 25 55.0000 50 65.0000 75 80.0000 | |

| | X | Frequency | Percent | Valid Percent | Cumulative Percent |
|--------|-----|-----------|---------|---------------|--------------------|
| Valid | | | | | |
| 5.00 | 1 | .3 | .3 | .3 | .3 |
| 10.00 | 2 | .6 | .6 | .6 | .9 |
| 15.00 | 3 | .9 | .9 | .9 | 1.9 |
| 20.00 | 5 | 1.6 | 1.6 | 1.6 | 3.5 |
| 25.00 | 6 | 1.9 | 1.9 | 1.9 | 5.4 |
| 30.00 | 9 | 2.8 | 2.8 | 2.8 | 8.2 |
| 35.00 | 20 | 6.3 | 6.3 | 6.3 | 14.5 |
| 40.00 | 15 | 4.7 | 4.7 | 4.7 | 19.2 |
| 45.00 | 4 | 1.3 | 1.3 | 1.3 | 20.5 |
| 50.00 | 5 | 1.6 | 1.6 | 1.6 | 22.1 |
| 55.00 | 65 | 20.5 | 20.5 | 20.5 | 42.6 |
| 60.00 | 4 | 1.3 | 1.3 | 1.3 | 43.8 |
| 65.00 | 32 | 10.1 | 10.1 | 10.1 | 53.9 |
| 70.00 | 15 | 4.7 | 4.7 | 4.7 | 58.7 |
| 75.00 | 45 | 14.2 | 14.2 | 14.2 | 72.9 |
| 80.00 | 20 | 6.3 | 6.3 | 6.3 | 79.2 |
| 85.00 | 15 | 4.7 | 4.7 | 4.7 | 83.9 |
| 90.00 | 12 | 3.8 | 3.8 | 3.8 | 87.7 |
| 95.00 | 30 | 9.5 | 9.5 | 9.5 | 97.2 |
| 100.00 | 9 | 2.8 | 2.8 | 2.8 | 100.0 |
| Total | 317 | 100.0 | | 100.0 | |

Result :-

$$n = 10$$

$$S = 10$$

$$L = 100$$

$$\bar{X} = 55$$

$$M_d = 55$$

$$M_0 = 10$$

$$Q_1 = 27.5$$

$$Q_3 = 82.5$$

$$\text{Range} = 90$$

$$\text{Coefficient of Range} = \frac{100 - 10}{100 + 10} = \frac{90}{110} = 0.818$$

$$S.d(\sigma) = 30.27655$$

$$\text{Variance} (\sigma^2) = 916.667$$

$$\text{Coefficient of Variation} = \frac{\sigma}{\bar{X}} \times 100\%$$

$$= \frac{30.2765}{55} \times 100\%$$

$$= 55.04\%$$

~~Fan~~
08/11/14

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Practical No. 4: Correlation and Regression

Level:- TU BCA 3rd Semester

Date:- 2081/01/16

Subject:- Probability and Statistics (CACS-202)

Roll No:- 13/080

Name: Bimal Acharya

Question:-

The students got the following percentage of marks in statistics and mathematics:

| | | | | | | | | | | | |
|-------------|----|----|----|----|----|----|----|----|----|----|----|
| Statistics | 78 | 36 | 98 | 25 | 75 | 82 | 90 | 62 | 65 | 39 | 80 |
| Mathematics | 84 | 51 | 91 | 60 | 68 | 62 | 86 | 58 | 63 | 25 | 47 |

- Find Karl-Pearson's correlation coefficient between marks in statistics and mathematics and interpret it.
- Find probable error and test for significance.
- Find units of population correlation coefficient.
- Find coefficient of determination and interpret it.

Working Expression:-

i) Karl-Pearson's Correlation Coefficient (r) is :-

$$r = \frac{n \sum xy - \sum x \sum y}{\sqrt{n \sum x^2 - (\sum x)^2} \cdot \sqrt{n \sum y^2 - (\sum y)^2}}$$

Interpretation of r :-

- If $r=0$, there is no correlation between x and y .
- If $r>0$, there is positive correlation between x and y .
- If $r<0$, there is negative correlation between x and y .

ii) Probable Error (PE) = $0.6745 \sqrt{1-n^2}$

For significance test,

- If $|r| < PE$, it is not significant
- If $|r| > 6PE$, it is significant
- Other than this, nothing is there to give conclusion to this correlation.

Ques. Write valid XML and CSS to display following ^o
and ^o details.

iii) Limits of population correlation coefficient (β) is :-
 $r \pm Pe$

\therefore lower limit of $\beta = r - Pe = 0.670 - 0.112 = 0.558$

\therefore Upper limit of $\beta = r + Pe = 0.670 + 0.112 = 0.782$

iv) Coefficient of determination $= r^2 = (0.670)^2 = 0.4489$

Interpretation of r^2

If $r^2 \times 100\%$ of variation is explained by total variation.

Since, $r^2 \times 100\% = 0.4489 \times 100\% = 44.89\%$ of variation explained by total variation, it means only 44.89% of relation exists between statistics and mathematics.

Lab4:-

| stat | math |
|-------|-------|
| 78.00 | 84.00 |
| 36.00 | 51.00 |
| 98.00 | 91.00 |
| 25.00 | 60.00 |
| 75.00 | 68.00 |
| 82.00 | 62.00 |
| 90.00 | 86.00 |
| 62.00 | 58.00 |
| 65.00 | 63.00 |
| 39.00 | 25.00 |
| 80.00 | 47.00 |
| | |
| | |
| | |
| | |
| | |

```
1 Encoding: UTF-8.  
2  
3 DATASET ACTIVATE DataSet0.  
4  
5 CORRELATIONS  
6 /VARIABLES=stat math  
7 /PRINT=TWOTAIL NOSIG  
8 /STATISTICS DESCRIPTIVES  
9 /MISSING=PAIRWISE.  
10 NONPAR CORR  
11 /VARIABLES=stat math  
12 /PRINT=SPEARMAN TWOTAIL NOSIG  
13 /MISSING=PAIRWISE.  
14
```

CORRELATIONS

/VARIABLES=stat math
/PRINT=TWOTAIL NOSIG
/STATISTICS DESCRIPTIVES
/MISSING=PAIRWISE.

Correlations**Descriptive Statistics**

| | Mean | Std. Deviation | N |
|------|---------|----------------|----|
| stat | 66.3636 | 23.66970 | 11 |
| math | 63.1818 | 19.12495 | 11 |

Correlations

| | | stat | math |
|------|---------------------|-------|-------|
| stat | Pearson Correlation | 1 | .670* |
| | Sig. (2-tailed) | | .024 |
| | N | 11 | 11 |
| math | Pearson Correlation | .670* | 1 |
| | Sig. (2-tailed) | .024 | |
| | N | 11 | 11 |

*. Correlation is significant at the 0.05 level (2-tailed).

NONPAR CORR

/VARIABLES=stat math
/PRINT=SPEARMAN TWOTAIL NOSIG
/MISSING=PAIRWISE.

Nonparametric Correlations

| Correlations | | | stat | math |
|----------------|------|-------------------------|-------|-------|
| Spearman's rho | stat | Correlation Coefficient | 1.000 | .645* |
| | | Sig. (2-tailed) | | .032 |
| | | N | 11 | 11 |
| math | | Correlation Coefficient | .645* | 1.000 |
| | | Sig. (2-tailed) | .032 | |
| | | N | 11 | 11 |

* Correlation is significant at the 0.05 level (2-tailed).

SAVE OUTFILE='C:\Users\Hp\Documents\Statpractical4.sav'

Result:-

$$r = 0.670, n = 11, \bar{r}^{\text{(upper limit)}} = 0.558, r(\text{lower limit}) = 0.782, r^2 = 0.4489$$

Interpretation of r

Since, $r = 0.670 > 0$, positive correlation exists between Statistics and Mathematics.

$$\rho_E = \frac{0.6745(1 - 0.670^2)}{\sqrt{11}} = 0.112$$

$$6 \times \rho_E = 6 \times 0.112 = 0.672$$

Since $|r| < 6\rho_E$, there is no significant relationship between Statistics & Mathematics.

~~Enu
08/21/14~~

Patan Multiple Campus

Practical No. 5: Correlation and Regression

Level:- TU BCA 3rd Semester

Date:- 2081/01/16

Subject: Probability and Statistics (CACS-202)

Roll No:- 13/080

Name: Bimal Acharya

Question:-

In a study between the amount of daily rainfall(X) and the quantity of air pollution removed(Y), following data were collected:

| | | | | | | | | | | |
|---|------|------|------|------|------|------|------|------|------|------|
| X | 4.3 | 4.5 | 5.9 | 5.6 | 6.1 | 5.2 | 3.8 | 2.1 | 2 | 1.5 |
| Y | 12.6 | 12.1 | 11.6 | 11.8 | 11.4 | 11.8 | 11.2 | 13.2 | 15.1 | 18.2 |

- i) Estimate the regression equation of pollution removed on daily rainfall.
- ii) Estimate the population removed when rainfall is 6.2.
- iii) Interpret the regression coefficient.
- iv) Find TSS, SSR and SSE.
- v) Find coefficient of determination and interpret it.
- vi) Find Standard error of estimate.

Working Expression:

Let rainfall (x) be independent variable and pollution (y) be dependent variable.

Then,

i) let regression model of pollution (y) on rainfall (x) be

$$y = a + bx$$

where,

$$b = b_{xy} = \frac{n \sum xy - \sum x \sum y}{n \sum x^2 - (\sum x)^2} = \text{Regression Coefficient}$$

$$a = \bar{y} - b \bar{x} = \text{General mean effect}$$

$$\bar{x} = \frac{\sum x}{n}, \bar{y} = \frac{\sum y}{n}$$

ii) The estimation of pollution removed (\hat{y}) for a specific value of rainfall ($x = 6.2$) is obtained by substituting the values into regression equation.

$$\hat{y} = a + bx.$$

ii) Interpretation of b :

- a) If $b=0$, there is no any effects.
- b) If $b>0$, then dependent variable y is increased by $|b|$ times per unit change in x .
- c) If $b<0$, then dependent variable y is decreased by $|b|$ times per unit change in independent variable x .

iii) $TSS = \text{Total Sum of Square} = \sum (y - \bar{y})^2 = \text{Total variation}$
 $SSE = \text{Sum of Square due to error} = \sum (y - \hat{y})^2 = \text{Unexplained variation}$

$SSR = \text{Sum of Square due to regression} = TSS - SSE = \text{Explained variation}$

v) Coefficient of determination (R^2) = $\frac{SSR}{TSS}$

Interpretation of R^2

If $R^2 \times 100\%$ of variation explained by total variation.

$$\# \text{Standard Error (Se)} = \sqrt{\frac{SSE}{n-k-2}}$$
$$= \sqrt{\frac{14.98}{10-1}}$$
$$= 2.29$$

Lab5:-

| X | Y | var |
|------|-------|-----|
| 4.30 | 12.60 | |
| 4.50 | 12.10 | |
| 5.90 | 11.60 | |
| 5.60 | 11.80 | |
| 6.10 | 11.40 | |
| 5.20 | 11.80 | |
| 3.80 | 11.20 | |
| 2.10 | 13.20 | |
| 2.00 | 15.10 | |
| 1.50 | 18.20 | |
| | | |
| | | |

```
1 ► | Encoding: UTF-8.  
2  
3 DATASET ACTIVATE DataSet0.  
4 REGRESSION  
5 /DESCRIPTIVES MEAN STDDEV CORR SIG N  
6 /MISSING LISTWISE  
7 /STATISTICS COEFF OUTS R ANOVA CHANGE  
8 /CRITERIA=PIN(.05) POUT(.10)  
9 /NOORIGIN  
10 /DEPENDENT Y  
11 /METHOD=ENTER X.
```

```
DATASET ACTIVATE DataSet0.  
REGRESSION  
 /DESCRIPTIVES MEAN STDDEV CORR SIG N  
 /MISSING LISTWISE  
 /STATISTICS COEFF OUTS R ANOVA CHANGE  
 /CRITERIA=PIN(.05) PCUT(.10)  
 /NOORIGIN  
 /DEPENDENT Y  
 /METHOD=ENTER X.
```

→ Regression

[DataSet0]

Descriptive Statistics

| | Mean | Std. Deviation | N |
|---|---------|----------------|----|
| Y | 12.9000 | 2.18581 | 10 |
| X | 4.1000 | 1.70489 | 10 |

Correlations

| | Y | X |
|---------------------|---|-------------|
| Pearson Correlation | Y | 1.000 -.807 |
| | X | -.807 1.000 |
| Sig. (1-tailed) | Y | .002 |
| | X | .002 |
| N | Y | 10 10 |
| | X | 10 10 |

Variables Entered/Removed^a

| Model | Variables Entered | Variables Removed | Method |
|-------|-------------------|-------------------|--------|
| 1 | X ^b | | Enter |

a. Dependent Variable: Y

b. All requested variables entered.

Model Summary

| Model | R | R Square | Adjusted R Square | Std. Error of the Estimate | Change Statistics | | | | |
|-------|-------------------|----------|-------------------|----------------------------|-------------------|----------|-----|-----|---------------|
| | | | | | R Square Change | F Change | df1 | df2 | Sig. F Change |
| 1 | .807 ^a | .651 | .608 | 1.36877 | .651 | 14.951 | 1 | 8 | .005 |

a. Predictors: (Constant), X

ANOVA^a

| Model | | Sum of Squares | df | Mean Square | F | Sig. |
|-------|------------|----------------|----|-------------|--------|-------------------|
| 1 | Regression | 28.012 | 1 | 28.012 | 14.951 | .005 ^b |
| | Residual | 14.988 | 8 | 1.874 | | |
| | Total | 43.000 | 9 | | | |

a. Dependent Variable: Y

b. Predictors: (Constant), X

Coefficients^a

| Model | Unstandardized Coefficients | | | Standardized Coefficients | t | Sig. |
|-------|-----------------------------|------------|-------|---------------------------|--------|------|
| | B | Std. Error | Beta | | | |
| 1 | (Constant) | 17.143 | 1.180 | | 14.534 | .000 |
| | X | -1.035 | .268 | -.807 | -3.867 | .005 |

a. Dependent Variable: Y

Results :-

i) $a = 27.143$

$b = -1.035$

∴ Required estimated regression equation of pollution on rainfall is :-

$$\hat{y} = 27.143 + (-1.035)x$$

$$= 27.143 - 1.035x$$

ii) When rainfall (x) = 6.2,

$$\hat{y} = 27.143 - 1.035 \times 6.2$$

$$= 10.726$$

iii) Since $b = -1.035 < 0$, then pollution is decreased by per unit change in rainfall.

iv) TSS = 43

SSR = 28.012

SSE = 14.988

v) Since $R^2 = 0.807^2 = 0.651 \times 100\% = 65.1\%$ of variation is explained by total variation, it means only 65.1% of relation exists between rainfall and pollution.

vi) Standard error (se) = $\sqrt{\frac{SSE}{n-k-1}}$

$$= \sqrt{\frac{14.988}{10-1}}$$

$$= 1.29$$

~~Ec'y~~
0.821117

Patan Multiple Campus

Practical No. 6: Design of Experiments (One-way ANOVA)

Level:- TU BCA 3rd Semester

Date:- 2081/01/16

Subject: Probability and Statistics (CACS-202)

Roll No:- 13/080

Name: Bimal Acharya

Question:-

The following data show the number of claims processed per day for a group of insurance company employees observed for a number of days. Test the hypothesis is that the employee's mean claim per day are all the same. Use the 0.05 level of significance.

| | | | | | | | |
|-----------|----|----|----|----|----|----|---|
| Employee1 | 15 | 17 | 14 | 12 | | | |
| Employee2 | 12 | 10 | 13 | 17 | 18 | 15 | |
| Employee3 | 11 | 14 | 13 | 15 | 12 | | |
| Employee4 | 13 | 12 | 12 | 14 | 10 | 9 | 8 |

Working Expression:

1) NULL Hypothesis (H_0): $\mu_1 = \mu_2 = \mu_3 = \dots = \mu_k$, performance of all the k-sample means are similar.

2) Alternative Hypothesis (H_1): $\mu_1 \neq \mu_2 \neq \mu_3 \neq \dots \neq \mu_k$, performance of at least one sample mean is different.

3) Test Statistics : Under H_1 , test statistics is,

$$F = \frac{MST}{MSE}$$

where, $MST = \frac{SST}{K-1}$, $SST = \sum \frac{T_i^2}{n_i} - C$. F = Sum of Square due to treatment.

$MSE = \frac{SSE}{N-k}$, $SSE = TSS - SST$ = Sum of Square due to error.

$TSS = \sum y_i^2 - C.F$ = Total sum of Square

$k-1$ = Degree of freedom of treatment

$N-k$ = Degree of freedom of error

$N-1$ = Degree of freedom of total

4) Critical value = The tabulated value of $F_{\alpha k, N-k}$ level
of significance and $(k-1, N-k)$ degree of freedom
is $F_{\alpha, (k-1, N-k)}$

5) Decision = If $F_{cal} \leq F_{tab}$ we accept H_0 , otherwise
reject H_0 .

Lab6:-

| Score | Emp | var |
|-------|------|-----|
| 15.00 | 1.00 | |
| 17.00 | 1.00 | |
| 14.00 | 1.00 | |
| 12.00 | 1.00 | |
| 12.00 | 2.00 | |
| 10.00 | 2.00 | |
| 13.00 | 2.00 | |
| 17.00 | 2.00 | |
| 18.00 | 2.00 | |
| 15.00 | 2.00 | |
| 11.00 | 3.00 | |
| 14.00 | 3.00 | |
| 13.00 | 3.00 | |
| 15.00 | 3.00 | |
| 12.00 | 3.00 | |
| 13.00 | 4.00 | |
| 12.00 | 4.00 | |
| 12.00 | 4.00 | |
| 14.00 | 4.00 | |
| 10.00 | 4.00 | |
| 9.00 | 4.00 | |
| 8.00 | 4.00 | |

```
1 ► * Encoding: UTF-8.  
2  
3 DATASET ACTIVATE DataSet1.  
4 ONEWAY Score BY Emp  
5 /MISSING ANALYSIS.
```

DATASET ACTIVATED DataSet1.

ONEWAY Score BY Emp

MISSING ANALYSIS.

→ Oneway

ANOVA

Score

| | Sum of Squares | df | Mean Square | F | Sig. |
|----------------|----------------|----|-------------|-------|------|
| Between Groups | 41.310 | 3 | 13.770 | 2.511 | .091 |
| Within Groups | 98.690 | 18 | 5.483 | | |
| Total | 140.000 | 21 | | | |

Results :-

$$K = 4$$

$$SST = 41.30$$

$$SSE = 98.690$$

$$TSS = 140.00$$

$$K-1 = 3$$

$$N-K = 18$$

$$N-1 = 21$$

$$MST = 13.770$$

$$MSE = 5.483$$

$$F_{cal} = \frac{MST}{MSE} = 2.511$$

Now,

$$H_0: \mu_1 = \mu_2 = \mu_3 = \mu_4$$

$$H_1: \mu_1 \neq \mu_2 \neq \mu_3 \neq \mu_4$$

Test statistics : Under H_0 , test statistic is

$$F = 2.511$$

Critical value : The tabulated value of $F_{\alpha/2} = 0.05$ and $(K-1, N-K) = (3, 18)$ is $F_{0.05, (3, 18)}$

$$= F_{0.05, (3, 18)}$$

Decision :- Since $F_{cal} < F_{0.05, (3, 18)}$, we accept H_0 . It is not significant.

~~Feb 08
08/21/19~~

Patan Multiple Campus

Practical No. 7: Design of Experiments (Two-way ANOVA)

Level: TU BCA 3rd Semester

Date: 2081/01/22

Subject: Probability and Statistics (CACS-202)

Roll No: 13/080

Name: Bimal Acharya

Question:-

The following table gives the data on the performance of three different detergents at three different Water temperatures. The performance was obtained on the 'Whiteness' reading based on specially designed equipment for twelve loads of washing.

| Water \ Detergents | A | B | C | D |
|--------------------|----|----|----|----|
| Cold Water | 45 | 43 | 55 | 60 |
| Warm Water | 37 | 40 | 56 | 62 |
| Hot Water | 42 | 44 | 46 | 55 |

Perform two-way ANOVA, using level of significance $\alpha = 0.05$

Working Expression:

Procedure of two-way ANOVA test

For Water:

Null hypothesis (H_{0W}): $\mu_1 = \mu_2 = \mu_3$; Performance of all the three types of water is similar.

Alternative hypothesis (H_{1W}): $\mu_1 \neq \mu_2 \neq \mu_3$; performance of at least one type of water is different.

For detergent:

Null hypothesis (H_{0c}): $\mu_1 = \mu_2 = \mu_3 = \mu_4$; performance of all the detergent is similar.

Alternative hypothesis (H_{1c}): $\mu_1 \neq \mu_2 \neq \mu_3 \neq \mu_4$; performance of at least one detergent is different.

Test statistics: Under H_0 , test statistic is

$$\textcircled{I} F_R = \frac{MSR}{MSE}$$

$$\textcircled{II} F_c = \frac{MSC}{MSE}$$

Critical value:

\textcircled{I} The tabulated value of F at $\alpha\%$ level for row is $F_{\alpha, [t-1, (t-1)(r-1)]}$

\textcircled{II} The tabulated value of F at $\alpha\%$ level of significance for column is $F_{\alpha, [(r-1), (t-1)(r-1)]}$

Decision :-

\textcircled{I} If $F_R \leq F_{\alpha, [t-1, (t-1)(r-1)]}$, we accept H_{0c} otherwise reject H_{0c}

\textcircled{II} If $F_c \leq F_{\alpha, [(r-1), (t-1)(r-1)]}$, we accept H_{0c} otherwise reject H_{0c} .

where,

t = No. of treatment = No. of water

r = No. of block = No. of detergent

$CF = \frac{C^2}{N}$ = Correction factor

$TSS = \sum \sum Y_{ij}^2 - CF$ = Total sum of square

$SSR = \frac{\sum T_R^2}{r} - CF$ = Sum of square due to treatment

$SSC = \frac{\sum T_c^2}{t} - CF$ = Sum of square due to block (detergent)

Lab 7

$$SSE = TSS - SSR - SSC = \text{sum of square due to error}$$

$$MSR = \frac{SSR}{t-1}, t-1 = \text{Df. of treatment}$$

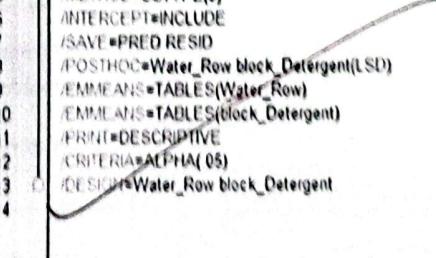
$$MSC = \frac{SSC}{r-1}, r-1 = \text{Df. of block}$$

$$MSE = \frac{SSE}{(t-1)(r-1)}; (t-1)(r-1) = \text{Df. of error}$$

Result of lab 7:



| | block_Detergent | Water_Row | Value | Var |
|----|-----------------|-----------|-------|-----|
| 1 | A | 1.00 | 45.00 | |
| 2 | A | 2.00 | 37.00 | |
| 3 | A | 3.00 | 42.00 | |
| 4 | B | 1.00 | 43.00 | |
| 5 | B | 2.00 | 40.00 | |
| 6 | B | 2.00 | 44.00 | |
| 7 | C | 1.00 | 55.00 | |
| 8 | C | 2.00 | 56.00 | |
| 9 | C | 3.00 | 46.00 | |
| 10 | D | 1.00 | 60.00 | |
| 11 | D | 2.00 | 62.00 | |
| 12 | D | 3.00 | 55.00 | |
| 13 | | | | |
| 14 | | | | |
| 15 | | | | |
| 16 | | | | |
| 17 | | | | |



```
lab7.sps - IBM SPSS Statistics Syntax Editor
File Edit View Data Transform Analyze DirectMarketing Graphs Utilities Add-ons
Encoding: UTF-8
DATASET ACTIVATE DataSet0
UNIANOVA Value BY Water_Row block_Detergent
/METHOD=SSTYPE(3)
/INTERCEPT=INCLUDE
/SAVE =PRED RESID
/POSTHOC=Water_Row block_Detergent(LSD)
/EMMEANS=TABLES(Water_Row)
/EMMEANS=TABLES(block_Detergent)
/PRINT=DESCRIPTIVE
/CRITERIA=ALPHA(.05)
/DESIGN=Water_Row block_Detergent
```

SPSS Output (Lab7.sav)

Between Subjects Factors

| | N |
|-----------------|---|
| Water_Row | 4 |
| 2.00 | 3 |
| 3.00 | 3 |
| block_Detergent | 4 |
| A | 3 |
| B | 3 |
| C | 3 |
| D | 3 |

Descriptive Statistics

| Dependent Variable | Value | Mean | Std. Deviation | N |
|--------------------|-------|---------|----------------|---------|
| 1.00 | A | 45.0000 | | 1 |
| | B | 41.0000 | | 1 |
| | C | 55.0000 | | 1 |
| | D | 60.0000 | | 1 |
| | Total | 50.7500 | 8.09835 | 4 |
| 2.00 | A | 37.0000 | | 1 |
| | B | 42.0000 | 2.82843 | 2 |
| | C | 58.0000 | | 1 |
| | D | 62.0000 | | 1 |
| | Total | 47.6000 | 10.73313 | 5 |
| 3.00 | A | 42.0000 | | 1 |
| | C | 48.0000 | | 1 |
| | D | 55.0000 | | 1 |
| | Total | 47.6667 | 6.65833 | 3 |
| | Total | A | 41.7333 | 4.04145 |
| B | | 42.7333 | 2.08197 | 2 |
| C | | 52.7333 | 5.60757 | 3 |
| D | | 59.0000 | 3.60555 | 3 |
| Total | | 48.7500 | 8.36746 | 12 |

Tests of Between-Subjects Effects

| Dependent Variable | Value | F | Mean Square | F | Sig. |
|--------------------|-----------------|----------|-------------|----------|------|
| Water_Row | Intercept | 2748.418 | 1 | 2649.418 | .000 |
| | block_Detergent | 669.567 | 3 | 223.189 | .171 |
| | Error | 74.659 | 6 | 12.775 | .383 |
| | Total | 3289.006 | 12 | | |
| | Corrected Total | 773.159 | 11 | | |

R-Squared = .903 Adjusted R-Squared = .898

Estimated Marginal Means

1. Water_Row

| Dependent Variable | Value | 95% Confidence Interval | | |
|--------------------|--------|-------------------------|-------------|-------------|
| Water_Row | Mean | Std. Error | Lower Bound | Upper Bound |
| 1.00 | 50.750 | 1.787 | 46.377 | 55.123 |
| 2.00 | 49.288 | 1.644 | 45.266 | 53.311 |
| 3.00 | 41.166 | 2.161 | 39.459 | 43.472 |

2. block_Detergent

| Dependent Variable | Value | 95% Confidence Interval | | |
|--------------------|--------|-------------------------|-------------|-------------|
| block_Detergent | Mean | Std. Error | Lower Bound | Upper Bound |
| A | 41.733 | 2.064 | 36.284 | 46.383 |
| B | 42.733 | 2.285 | 35.423 | 46.509 |
| C | 52.733 | 2.064 | 47.284 | 57.363 |
| D | 59.000 | 2.014 | 53.951 | 64.049 |

LSD

| Dependent Variable | Value | 95% Confidence Interval | | | |
|--------------------|-----------|-------------------------|---------|------------|--------|
| Water_Row | Water_Row | Mean Difference (Df) | J | Std. Error | Sig. |
| 1.00 | 2.00 | 2.8100 | 2.16165 | .265 | .81648 |
| 2.00 | 1.00 | -2.8100 | 2.39765 | .265 | .81648 |
| 3.00 | 1.00 | 13.331 | 2.61923 | .961 | .02537 |
| 3.00 | 2.00 | -13.331 | 2.72384 | .961 | .02537 |
| 3.00 | 2.00 | -13.331 | 2.61373 | .961 | .02537 |

Based on observed means
The error term is Mean Square(Error) = 12.775

Homogeneous Subsets

block_Detergent

| Multiple Comparisons | | | | | |
|----------------------|---|----------------------|---------|-------------------------|--------|
| Dependent Variable | | LSD | | | |
| | | Mean Difference (Df) | J | Std. Error | Sig. |
| block_Detergent | | block_Detergent | | 95% Confidence Interval | |
| A | B | -1.000 | 2.61832 | .744 | .81429 |
| | C | 11.000 | 2.61832 | .068 | .81429 |
| | D | -17.000 | 2.61832 | .001 | .24375 |
| B | A | 1.000 | 2.61832 | .744 | .81429 |
| | C | 10.000 | 2.61832 | .014 | .81429 |
| | D | -16.000 | 2.61832 | .001 | .24375 |
| C | A | 11.000 | 2.61832 | .068 | .63931 |
| | B | 10.000 | 2.61832 | .014 | .63931 |
| | D | -16.000 | 2.61832 | .001 | .24375 |
| D | A | 17.000 | 2.61832 | .001 | .13525 |
| | B | 16.000 | 2.61832 | .001 | .13525 |
| | C | 6.000 | 2.61832 | .062 | .4742 |

Result:-

$$t=3, r=4$$

$$N = kr = 3 \times 4 = 12$$

$$SSR = 32$$

$$SSC = 642.250$$

$$SS\epsilon = 96$$

$$TSS = 770.250$$

Now,

for water

$$H_0: \mu_1 = \mu_2 = \mu_3$$

$$H_1: \mu_1 \neq \mu_2 \neq \mu_3$$

Test statistic: Under H_0 , test statistic is: $F_R = 1$

Critical value:

The tabulated value of F at $\alpha = 0.05$ is $F_{0.05}(2,6) = 5.1433$

Decision:

Since $F_R < F_{0.05}(3,6)$, we accept null hypothesis and it is not significant.

for Detergent:

$$H_0: \mu_1 = \mu_2 = \mu_3 = \mu_4$$

$$H_1: \mu_1 \neq \mu_2 \neq \mu_3 \neq \mu_4$$

Test statistic: Under H_0 , test statistic is:

$$F_c = 13.380$$

Critical Value:

The tabulated value of F at $\alpha = 0.05$ is $F_{0.05}(3,6) = 4.7572$

Decision

since $F_c > F_{0.05}(3,6)$, we reject null hypothesis.

~~For 0.05~~
13.380

PATAN MULTIPLE CAMPUS

Practical No. 8: Binomial Distribution

Level: BCA 3rd Semester

Date: 2082-01-25

Subject: Probability and Statistics (STA-202)

Roll no: 13/80

Name: Bimal Acharya

Question:

Fit binomial distribution of the following Observation.

| | | | | | | | | | |
|---|---|---|----|-----|-----|----|----|----|---|
| X | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| F | 2 | 8 | 75 | 250 | 210 | 70 | 50 | 20 | 5 |

Also, Find

- i) $P(X \leq 2)$
- ii) $P(X \geq 6)$
- iii) $P(4 \leq X \leq 6)$

Working Expression:

working Expression :-

The probability mass function of n is

$$P(n=n) = B(n, n, p) = \begin{cases} {}^n C_n p^n q^{n-n}, & n=0, 1, 2, \dots, n. \\ 0, & \text{otherwise} \end{cases}$$

where,

n = parameter = No. of trials

$p = \frac{\bar{x}}{n}$ = parameter = probability of success events in a single trial

$$q = 1 - p$$

$$\bar{x} = \frac{\sum f_n}{N}, N = \sum f$$

$$\text{Expected frequency (EF)} = N \cdot p (R=n)$$

Result of lab8:-

| | x | f | p | pdf | EF | REF | v |
|----|------|--------|-------|-------|--------|--------|---|
| 1 | .00 | 2.00 | .4670 | .0065 | 4.49 | 4.00 | |
| 2 | 1.00 | 8.00 | .4670 | .0456 | 31.49 | 31.00 | |
| 3 | 2.00 | 75.00 | .4670 | .1400 | 96.59 | 97.00 | |
| 4 | 3.00 | 250.00 | .4670 | .2453 | 169.27 | 169.00 | |
| 5 | 4.00 | 210.00 | .4670 | .2687 | 185.41 | 185.00 | |
| 6 | 5.00 | 70.00 | .4670 | .1884 | 129.97 | 130.00 | |
| 7 | 6.00 | 50.00 | .4670 | .0825 | 56.95 | 57.00 | |
| 8 | 7.00 | 20.00 | .4670 | .0207 | 14.26 | 14.00 | |
| 9 | 8.00 | 5.00 | .4670 | .0023 | 1.56 | 2.00 | |
| 10 | | | | | | | |
| 11 | | | | | | | |

```
1 Encoding: UTF-8
2
3 DATASET ACTIVATE DataSet0.
4 WEIGHT BY t.
5
6 FREQENCIES VARIABLES=x
7 /STATISTICS=MEAN
8 /ORDER=ANALYSIS.
9
10 COMPUTE p=3.7362/8
11 EXECUTE.
12
13 COMPUTE pdf=PDF.BINOM(x,8,p).
14 EXECUTE.
15
16 COMPUTE EF=690 * pdf.
17 EXECUTE.
18
19 COMPUTE REF=RND(EP).
20 EXECUTE.
21
```

Result of lab8:-

```
WEIGHT BY z.  
FREQUENCIES VARIABLES=x  
/STATISTICS=MEAN  
/CORDER=ANALYSIS.
```

→ Frequencies

[DataSet0]

Statistics

| x | N | Valid | 690 |
|---|---------|-------|--------|
| | Missing | | 0 |
| | Mean | | 3.7362 |

| x | Frequenc y | Percent | Valid Percent | Cumulati ve Percent |
|-----------|---------------|---------|------------------|---------------------------|
| Valid .00 | 2 | .3 | .3 | .3 |
| 1.00 | 8 | 1.2 | 1.2 | 1.4 |
| 2.00 | 75 | 10.9 | 10.9 | 12.3 |
| 3.00 | 250 | 36.2 | 36.2 | 48.6 |
| 4.00 | 210 | 30.4 | 30.4 | 79.0 |
| 5.00 | 70 | 10.1 | 10.1 | 89.1 |
| 6.00 | 50 | 7.2 | 7.2 | 96.4 |
| 7.00 | 20 | 2.9 | 2.9 | 99.3 |
| 8.00 | 5 | .7 | .7 | 100.0 |
| Total | 690 | 100.0 | 100.0 | |

COMPUTE p=3.7362 / 8.

EXECUTE.

COMPUTE pdf=PDF.BINOM(x,8,p).

EXECUTE.

COMPUTE EF=690 * pdf.

EXECUTE.

COMPUTE REF=RND(EF).

EXECUTE.

SAVE OUTFILE='E:\parctical8.sav'

/COMPRESSED.

Result

$$\bar{n} = 3.7362$$

$$P = 0.4670$$

$$N = 690$$

| n | F | P | Pdf | Ef | Ref |
|---|--------|-------|--------|--------|--------|
| 0 | 2.00 | 0.467 | 0.0065 | 4.49 | 4.00 |
| 1 | 8.00 | 0.467 | 0.0456 | 31.49 | 31.00 |
| 2 | 75.00 | 0.467 | 0.1400 | 96.59 | 97.00 |
| 3 | 250.00 | 0.467 | 0.2453 | 169.27 | 169.00 |
| 4 | 210.00 | 0.467 | 0.2687 | 185.41 | 185.00 |
| 5 | 70.00 | 0.467 | 0.1884 | 129.02 | 130.00 |
| 6 | 50.00 | 0.467 | 0.825 | 56.95 | 57.00 |
| 7 | 20.00 | 0.467 | 0.0207 | 14.26 | 14.00 |
| 8 | 5.00 | 0.467 | 0.0023 | 1.56 | 2.00 |

$$1) P(n \leq 2)$$

$$\begin{aligned}
 &= P(n=0) + P(n=1) + P(n=2) \\
 &= 0.0065 + 0.0456 + 0.1400 \\
 &= 0.19
 \end{aligned}$$

$$2) P(n \geq 6)$$

$$\begin{aligned}
 &= P(n=6) + P(n=7) + P(n=8) \\
 &= 0.825 + 0.00207 + 0.0023 \\
 &= 0.11
 \end{aligned}$$

$$3) P(4 \leq n \leq 6)$$

$$\begin{aligned}
 &= P(n=4) + P(n=5) + P(n=6) \\
 &= 0.2453 + 0.2687 + 0.1884 \\
 &= 0.70
 \end{aligned}$$

~~10/21/2021~~

PATAN MULTIPLE CAMPUS

Practical No. 9: Poisson Distribution

Level: BCA 3rd Semester

Date: 2082-01-30

Subject: Probability and Statistics (STA-202)

Roll no: 13/80

Name: Bimal Acharya

Question:

Fit Poisson distribution of the following Observation.

| X | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
|---|-----|-----|----|----|---|---|---|
| F | 211 | 250 | 70 | 21 | 7 | 2 | 1 |

Also, Find

- i) $P(X \leq 2)$
- ii) $P(X \geq 4)$
- iii) $P(X > 4)$
- iv) $P(2 < X \leq 4)$

Working Expression:

Working Expression:-

1) The probability mass function of Poisson distribution is

$$P(n=m) = P(n, \lambda) = \begin{cases} \frac{e^{-\lambda} \lambda^m}{m!}, & m=0, 1, 2, \dots, 6 \\ 0, & \text{otherwise} \end{cases}$$

where, $\lambda = \text{parameter} = \text{mean}(\bar{n}) = \text{variance}(\sigma^2) = \frac{\sum f_n n}{N}$

2) Expected Frequency (EF) = $N p(n=m)$

where,

$$N = \Sigma F$$

$$P(n=m) = \text{pmf (pdf)}$$

$$3) P(n \leq 2) = P(n=0) + P(n=1) + P(n=2)$$

$$4) P(n \geq 4) = P(n=4) + P(n=5) + P(n=6)$$

$$5) P(n > 4) = P(n=5) + P(n=6)$$

$$6) P(2 < n \leq 4) = P(n=3) + P(n=4)$$

result of lab9:-

| x | f | Pdf | EF | REF | % |
|------|--------|---------|----------|--------|---|
| .00 | 211.00 | .413003 | 232.1078 | 232.00 | |
| 1.00 | 250.00 | .385219 | 205.2529 | 205.00 | |
| 2.00 | 70.00 | .161481 | 90.7526 | 91.00 | |
| 3.00 | 21.00 | .047599 | 26.7508 | 27.00 | |
| 4.00 | 7.00 | .010523 | 5.9139 | 6.00 | |
| 5.00 | 2.00 | .001861 | 1.0459 | 1.00 | |
| 6.00 | 1.00 | .000274 | .1542 | .00 | |

```
1 ► EXECUTE UNTIL 6
2
3 DATASET ACTIVATE DataSet0.
4 WEIGHT BY f.
5
6 FREQUENCIES VARIABLES=x
7 /STATISTICS=MEAN
8 /ORDER=ANALYSIS.
9
10 COMPUTE Pdf=PDF.POISSON(x,0.8843)
11 EXECUTE.
12
13 COMPUTE EF=562 * Pdf
14 EXECUTE.
15
16 COMPUTE REF=RND(EF).
17 EXECUTE.
18
```

Result of lab9:-

```
DATASET ACTIVATE DataSet0.  
WEIGHT BY f.  
FREQUENCIES VARIABLES=x  
/STATISTICS=MEAN  
/ORDER=ANALYSIS.
```

→ Frequencies

[DataSet0]

Statistics

| x | N | Valid | 562 |
|---|---------|-------|------|
| | Missing | | 0 |
| | Mean | | 8843 |

| x | Frequenc y | Percent | Valid Percent | Cumulati ve Percent |
|-----------|---------------|---------|------------------|---------------------------|
| Valid .00 | 211 | 37.5 | 37.5 | 37.5 |
| 1.00 | 250 | 44.5 | 44.5 | 82.0 |
| 2.00 | 70 | 12.5 | 12.5 | 94.5 |
| 3.00 | 21 | 3.7 | 3.7 | 98.2 |
| 4.00 | 7 | 1.2 | 1.2 | 99.5 |
| 5.00 | 2 | .4 | .4 | 99.8 |
| 6.00 | 1 | .2 | .2 | 100.0 |
| Total | 562 | 100.0 | 100.0 | |

```
COMPUTE Pdf=PDF.POISSON(x,0.8843).
```

```
EXECUTE.
```

```
COMPUTE EF=562 * Pdf.
```

```
EXECUTE.
```

```
COMPUTE REF=RND(EF).
```

```
EXECUTE.
```

```
SAVE OUTFILE='E:\New folder\9\pr  
/COMPRESSED.
```

Double-click to
activate

Result

$$N = 562$$

$$\lambda = \bar{n} = 0.884$$

| n | F | PdF | EF | RF |
|------|--------|----------|---------|--------|
| 0.00 | 211.00 | 0.413003 | 232.102 | 252.00 |
| 1.00 | 250.00 | 0.365219 | 205.52 | 206.00 |
| 2.00 | 70.00 | 0.161481 | 90.75 | 91.00 |
| 3.00 | 21.00 | 0.047599 | 26.75 | 27.00 |
| 4.00 | 7.00 | 0.010523 | 5.91 | 6.00 |
| 5.00 | 2.00 | 0.001861 | 1.04 | 1.09 |
| 6.00 | 1.00 | 0.000274 | 0.18 | 0.00 |

Also,

$$\text{i)} P(n \leq 2) = 0.413003 + 0.365219 + 0.161481 \\ = 0.94$$

$$\text{ii)} P(n \geq 4) = 0.010523 + 0.001861 + 0.000274 \\ = 0.022$$

$$\text{iii)} P(n > 4) = 0.001861 + 0.000274 \\ = 0.0021$$

$$\text{iv)} P(2 < n \leq 4) = 0.047599 + 0.010523 \\ = 0.0581$$

~~0.821131~~

Patan Multiple Campus

Practical No. 10: Normal Distribution

Level:- TU BCA 3rd Semester

Date:- 2081/01/31

Subject: Probability and Statistics (CACS-202)

Roll No:- 13/080

Name: Bimal Acharya

Question:-

Fit normal distribution of the following observations:-

| Marks | 0-10 | 10-20 | 20-30 | 30-40 | 40-50 | 50-60 | 60-70 | 70-80 | 80-90 | 90-100 |
|----------------|------|-------|-------|-------|-------|-------|-------|-------|-------|--------|
| No.of students | 5 | 20 | 10 | 100 | 150 | 125 | 50 | 20 | 5 | 2 |

Also find:-

1. $P(x \leq 30)$
2. $P(x \geq 50)$
3. $P(20 < x < 30)$
4. $P(35 < x < 65)$

Working Expression:

Result :-

$$N = 487$$

$$\mu = 42.3614$$

$$\sigma = 14.40053$$

$$\sigma^2 = 207.375$$

Then,

| Marks | No. of Student (f) | $P(n < n < n_2)$ Pmf | EF | REF |
|--------|--------------------|-------------------------|--------|--------|
| 0-10 | 5 | •004234 | 2.06 | 2.00 |
| 10-20 | 20 | •023978 | 11.68 | 12.00 |
| 20-30 | 10 | •085269 | 41.53 | 42.00 |
| 30-40 | 100 | •190625 | 92.83 | 93.00 |
| 40-50 | 150 | •268082 | 130.56 | 131.00 |
| 50-60 | 125 | •237242 | 115.54 | 116.00 |
| 60-70 | 50 | •132100 | 64.53 | 64.00 |
| 70-80 | 20 | •046253 | 22.53 | 23.00 |
| 80-90 | 5 | •016177 | 4.96 | 5.00 |
| 90-100 | 2 | •001405 | 0.68 | 1.00 |

Also,

$$\text{i)} P(n \leq 30) = 0.1140$$

$$\text{ii)} P(n \geq 50) = 0.4273$$

$$\text{iii)} P(20 < n < 30) = 0.0853$$

$$\text{iv)} P(35 < n < 65) = 0.6943$$

10>

DATA

proc10ser (DataSet0) - IBM SPSS Statistics Data Editor

File Edit View Data Transform Analyze Direct Marketing Graphs Utilities Add-ons Window Help

| | lowerlt | upperlt | x | I | p01 | EF | REF | p01 | p02 | p03 | p04 | @ |
|----|---------|---------|-------|--------|--------|---------|--------|-------|-------|-------|-------|---|
| 1 | .00 | 10.00 | 5.00 | 5.00 | 004234 | 2.06 | 2.00 | .1140 | .4273 | .0853 | .6943 | |
| 2 | 10.00 | 20.00 | 15.00 | 20.00 | 023978 | 11.68 | 12.00 | .1140 | .4273 | .0853 | .6943 | |
| 3 | 20.00 | 30.00 | 25.00 | 10.00 | 085269 | 41.53 | 42.00 | .1140 | .4273 | .0853 | .6943 | |
| 4 | 30.00 | 40.00 | 35.00 | 100.00 | 190625 | 92.83 | 93.00 | .1140 | .4273 | .0853 | .6943 | |
| 5 | 40.00 | 50.00 | 45.00 | 150.00 | 268082 | '130.56 | 131.00 | .1140 | .4273 | .0853 | .6943 | |
| 6 | 50.00 | 60.00 | 55.00 | 125.00 | 237242 | 115.54 | 116.00 | .1140 | .4273 | .0853 | .6943 | |
| 7 | 60.00 | 70.00 | 65.00 | 50.00 | 132100 | 64.33 | 64.00 | .1140 | .4273 | .0853 | .6943 | |
| 8 | 70.00 | 80.00 | 75.00 | 20.00 | 046257 | 22.53 | 23.00 | .1140 | .4273 | .0853 | .6943 | |
| 9 | 80.00 | 90.00 | 85.00 | 5.00 | 010177 | 4.95 | 5.00 | .1140 | .4273 | .0853 | .6943 | |
| 10 | 90.00 | 100.00 | 95.00 | 2.00 | 001405 | .68 | 1.00 | .1140 | .4273 | .0853 | .6943 | |
| 11 | | | | | | | | | | | | |
| 12 | | | | | | | | | | | | |
| 13 | | | | | | | | | | | | |
| 14 | | | | | | | | | | | | |
| 15 | | | | | | | | | | | | |
| 16 | | | | | | | | | | | | |
| 17 | | | | | | | | | | | | |

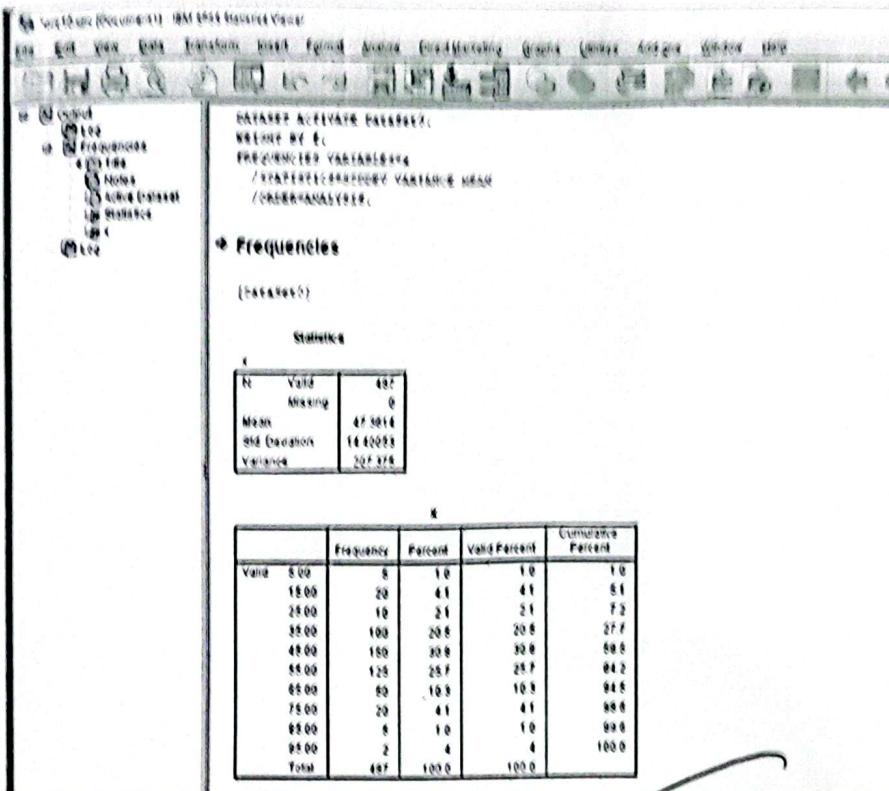
SYNTAX

*prc10.sps - IBM SPSS Statistics Syntax Editor

Edit View Data Transform Analyze Direct Marketing Graphs Utilities Add ons Run Tools Window Help

```
1 Encoding: UTF-8
2
3 DATASET ACTIVATE DataSet0.
4 WEIGHT BY f.
5
6 FREQUENCIES VARIABLES=x
7 /STATISTICS=STDEV VARIANCE MEAN
8 /ORDER=ANALYSIS.
9
10 COMPUTE pdf=CDF NORMAL(upper1.47 3614.14.40053)-CDF NORMAL(lower1.47 3614.14.40053).
11 EXECUTE.
12
13 COMPUTE EF=487 * pdf.
14 EXECUTE.
15
16 COMPUTE REF=RND(EF).
17 EXECUTE.
18
19 COMPUTE pdf1=CDF NORMAL(30.47 3614.14.40053).
20 EXECUTE.
21
22 COMPUTE pdf2=1-CDF NORMAL(50.47 3614.14.40053).
23 EXECUTE.
24
25 COMPUTE pdf3=CDF NORMAL(30.47 3614.14.40053)-CDF NORMAL(20.47 3614.14.40053).
26 EXECUTE.
27
28 ▶
29
```

OUTPUT



```
COMPUTE pdf=CDF.NORMAL(upperlt,47.3614,14.40053)-CDF.NORMAL(lowerlt,47.3614,14.40053).
EXECUTE.
COMPUTE EF=487 * pdf.
EXECUTE.
COMPUTE REF=RND(EF).
EXECUTE.

SAVE OUTFILE='E:\New folder\10\pro10.sav'
/COMPRESSED.
COMPUTE pdf1=CDF.NORMAL(30,47.3614,14.40053).
EXECUTE.
COMPUTE pdf2=1-CDF.NORMAL(50,47.3614,14.40053).
EXECUTE.
COMPUTE pdf3=CDF.NORMAL(30,47.3614,14.40053)-CDF.NORMAL(20,47.3614,14.40053).
EXECUTE.
COMPUTE pdf4=CDF.NORMAL(65,47.3614,14.40053)-CDF.NORMAL(35,47.3614,14.40053).
EXECUTE.
DATASET ACTIVATE DataSet0.

SAVE OUTFILE='E:\New folder\10\pro10.sav'
/COMPRESSED.
```

working expression :-

1) The probability density function of normal distribution is

$$f(n) = \begin{cases} \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2}(\frac{n-\mu}{\sigma})^2}, & -\infty < n < \infty \\ 0, & \text{otherwise} \end{cases}$$

where, μ = parameter = mean (\bar{n}) = $\frac{\sum f_n}{N}$

σ^2 = parameter = variance (σ^2) = $\frac{\sum f(n-\bar{n})^2}{N}$

σ = standard deviation

2) Expected frequency (Ef) = $N \cdot P(n_1 \leq n \leq n_2)$

where,

n_1 = lower limit of the class

n_2 = upper limit of the class

~~Eas 2
082/2/6~~