

# An Information Minimization Based Contrastive Learning Model for Unsupervised Sentence Embeddings Learning

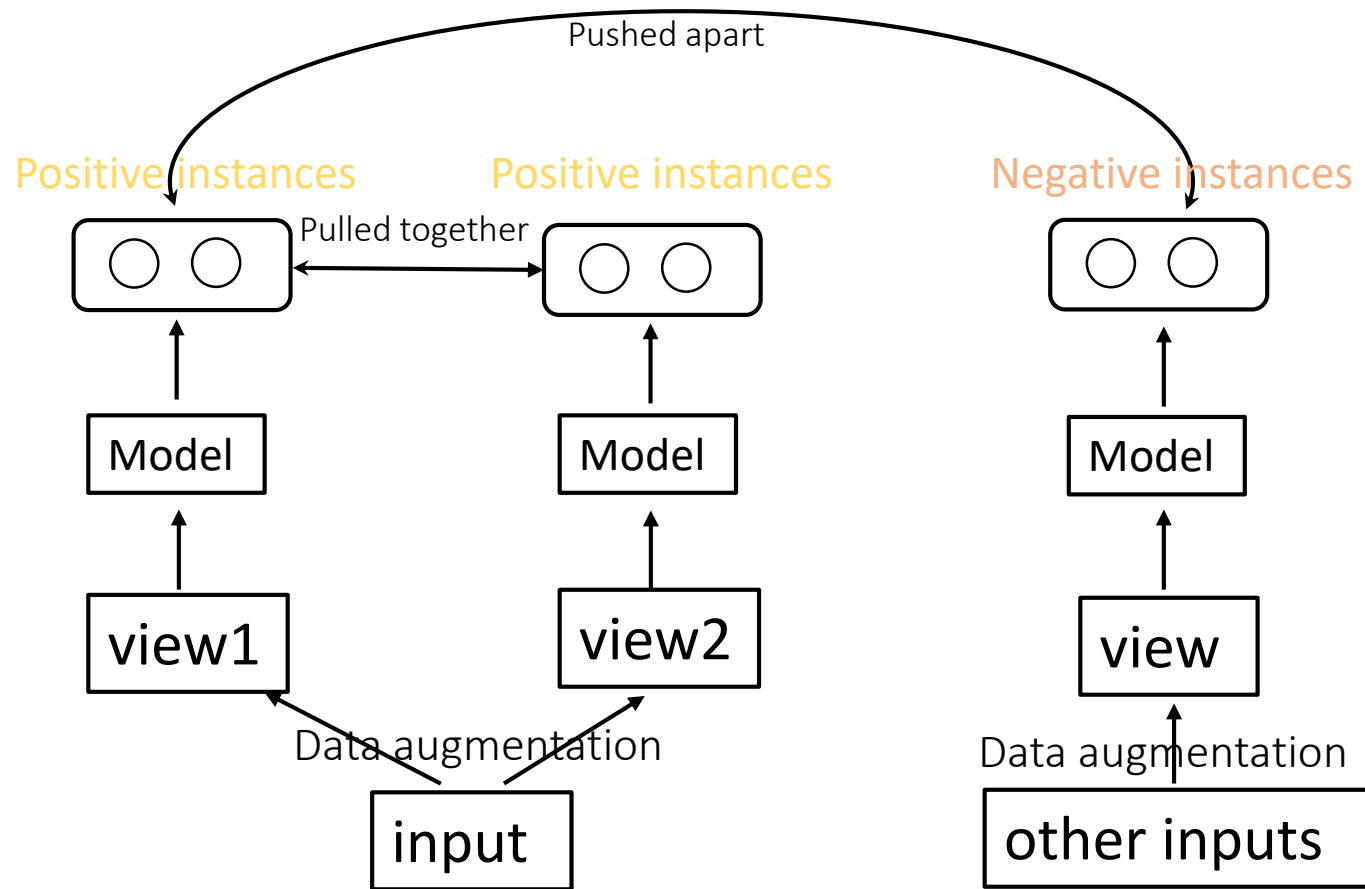
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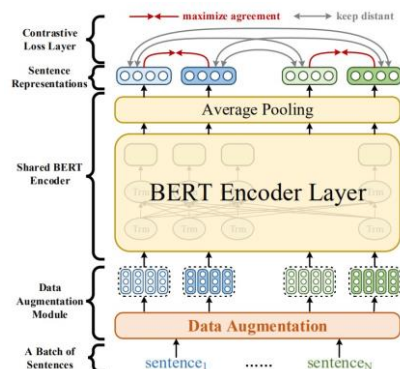
Code: <https://github.com/Bin199/InforMin-CL>

# Introduction of Contrastive Learning

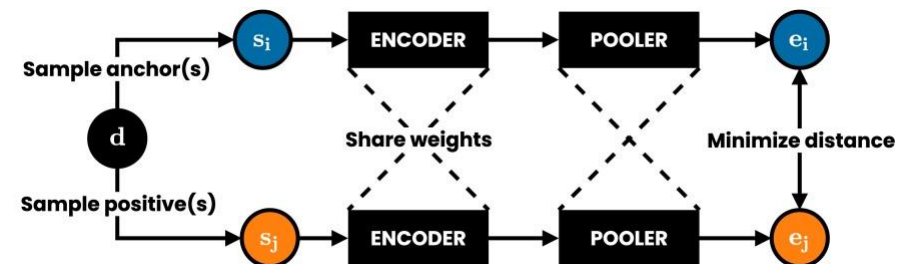


# Previous Contrastive Learning Based Methods

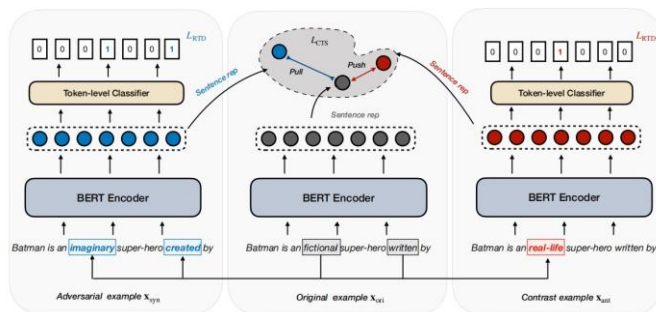
## ConSERT



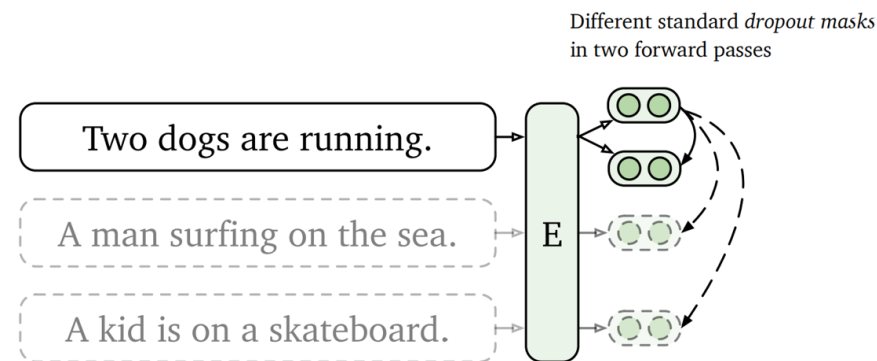
## DeCLUTER



## CLINE



## SimCSE



[ConSERT: A Contrastive Framework for Self-Supervised Sentence Representation Transfer. Yuanmeng Yan et al. ACL 2021.]

[DeCLUTER: Deep Contrastive Learning for Unsupervised Textual Representations. John Giorgi et al. ACL 2021.]

[CLINE: Contrastive Learning with Semantic Negative Examples for Natural Language Understanding. Dong Wang et al. ACL 2021.]

[SimCSE: Simple Contrastive Learning of Sentence Embeddings. Tianyu Gao et al. EMNLP 2021.]

# Previous Contrastive Learning Based Methods



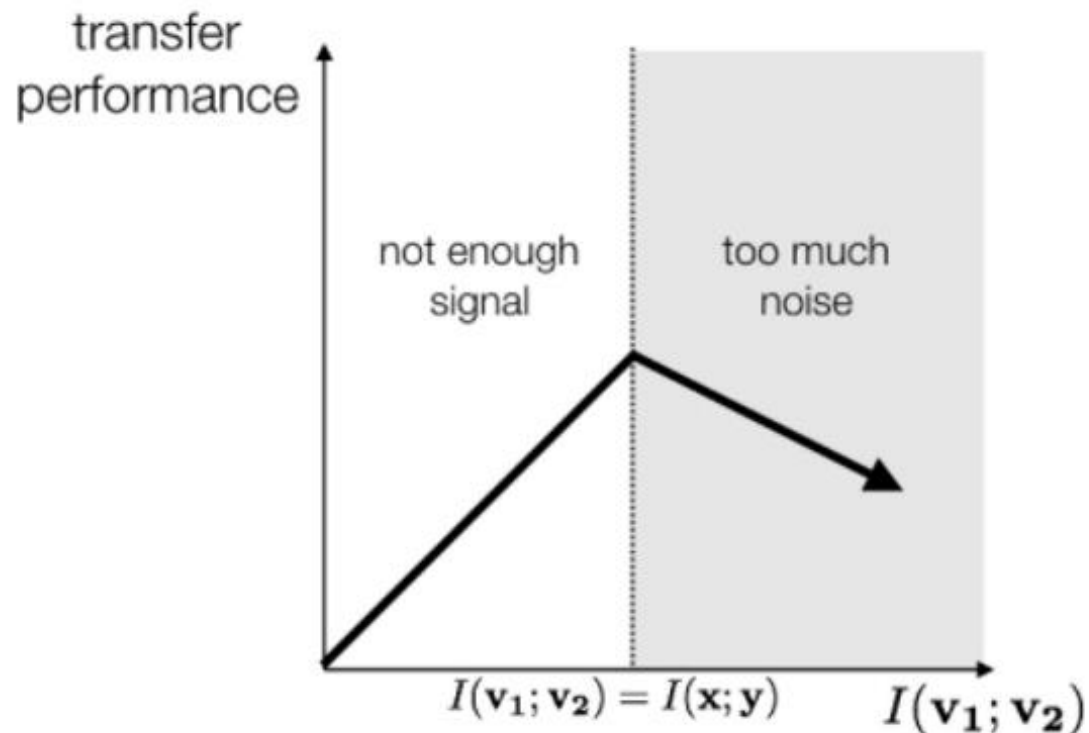
Focus on data augmentation skills, and model architecture

# Ignore the redundant information in the pre-training datasets



A kid is on a skateboard.

# Redundant Information



Redundant information leads to a drop in transfer performance!!!

[What makes good views for contrastive learning? Yonglong Tian et al. NeurIPS 2020.]

# Redundant Information

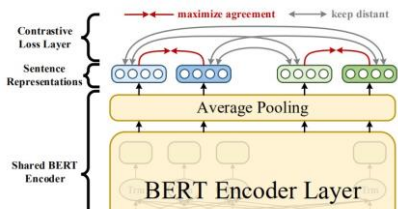
We care about two types of redundant information, stop words and **the style of the sentence** (e.g., restatement, capitalization, and hyphen.)

Original	Where is the party, it sounds great.
Stop words	Where <b>is the</b> party, <b>it</b> sounds great.
Restatement	The party sounds great, where is it.
Capitalization	Where Is The Party, It Sounds Great.
Hyphen	Where-is-the-party, it-sounds-great.

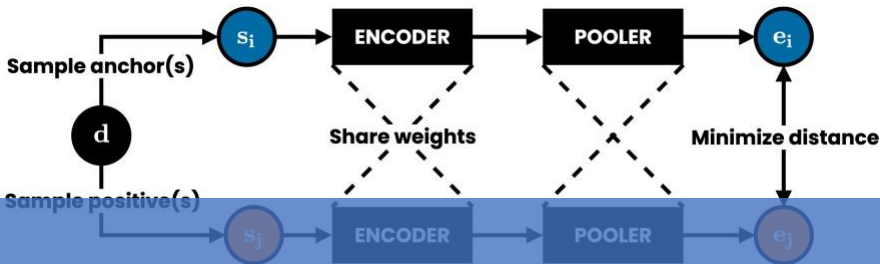
Less studied in  
previous work.

# Question

## ConSERT



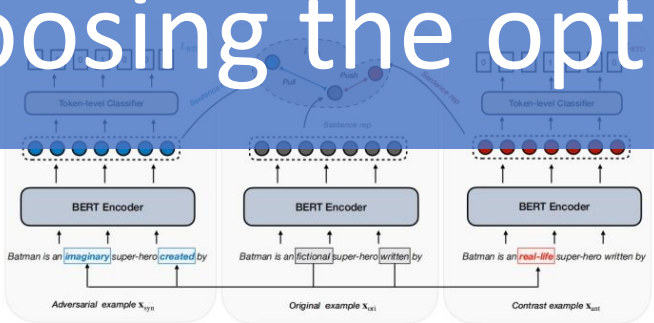
## DeCLUTER



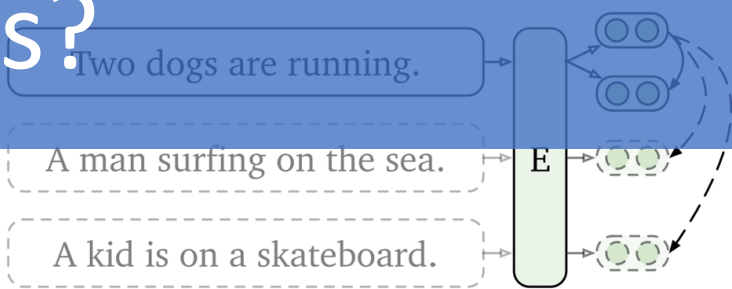
How to discard redundant information by choosing the optimal views?

Different standard dropout masks in two forward passes

## CLINE



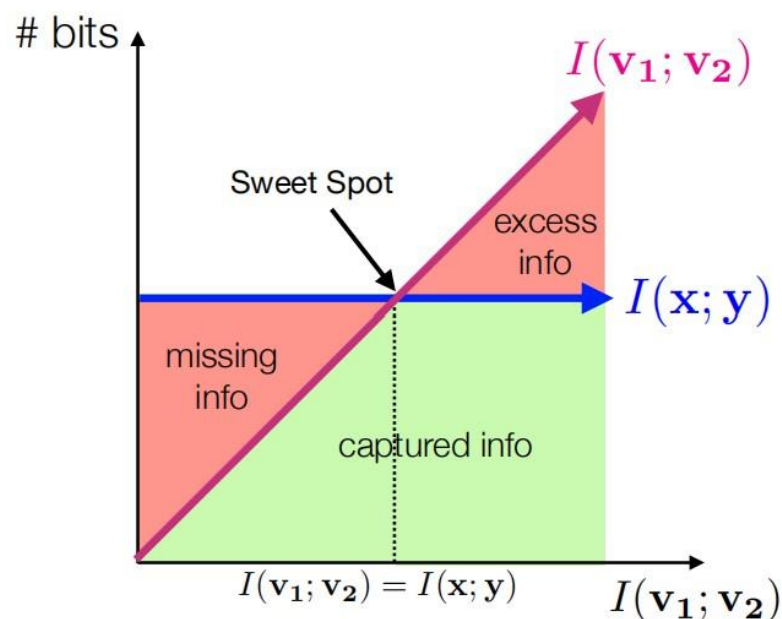
## SmCVR



# Solution

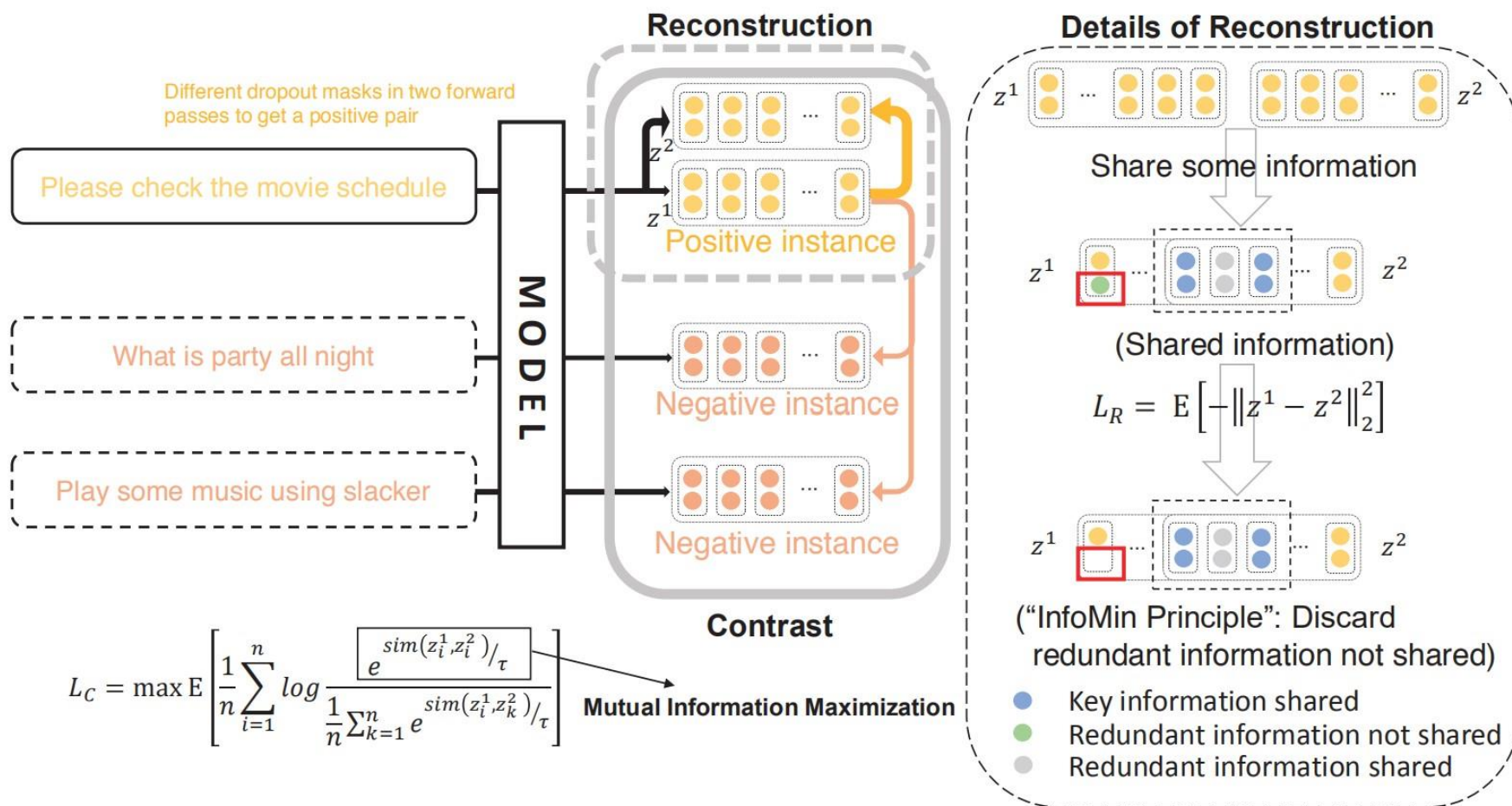
Draw inspiration from

Information minimization principle: A good set of views share the minimal information necessary to perform well at the downstream task.





# Architecture of Proposed Model: InforMin-CL



Total Loss function L:

$$\mathcal{L} = \mathcal{L}_C + \lambda * \mathcal{L}_R$$

# Contrast Keeps Almost All the Key Information

**Theorem 1:** The supervised learned representations contain all the key information in the input  $I(X; T)$ . The self-supervised representations contain all the key information in the input with a potential loss.

$$\begin{aligned} I(X; T) &= I(Z^{sup}; T) = I(Z^{sup_{min}}; T) \\ &\geq I(Z^{ssl}; T) \\ &\geq I(Z^{ssl_{min}}; T) \\ &\geq I(X; T) - \varepsilon \end{aligned}$$

X: input

Z: instance

S: self-supervised signal

T: key information

I: mutual information

H: information entropy

$$Z^{sup} = \arg \max_Z I(Z; T)$$

$$Z^{sup_{min}} = \arg \min_Z H(Z|T)$$

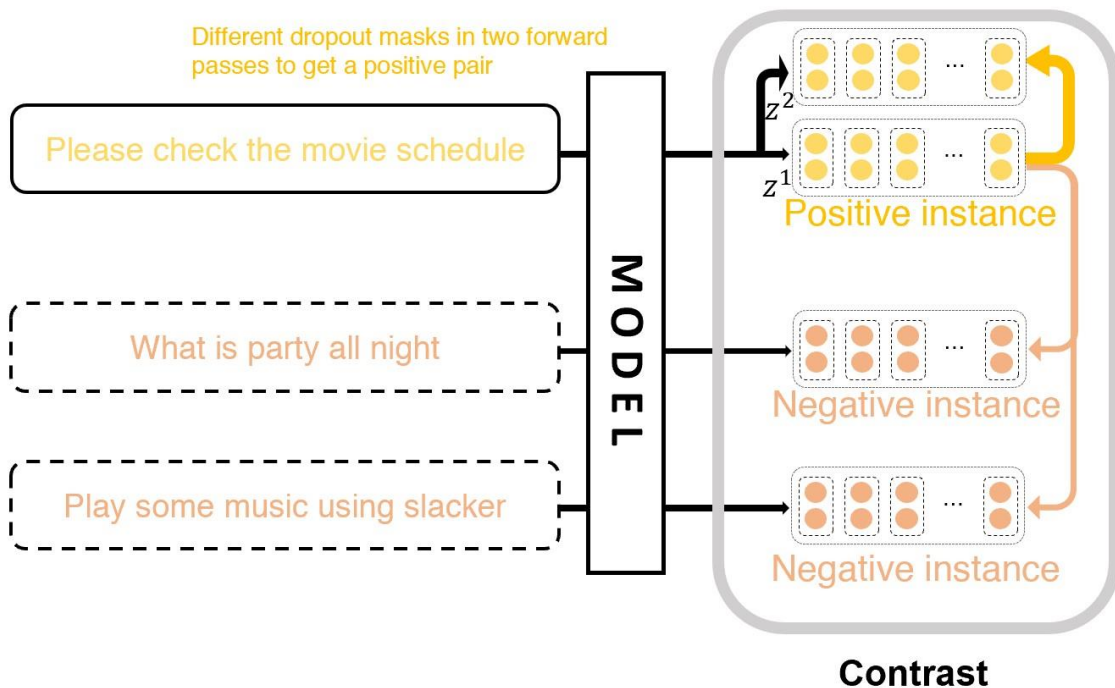
s.t.  $I(Z; T)$  is maximized

$$Z^{ssl} = \arg \max_Z I(Z; S)$$

$$Z^{ssl_{min}} = \arg \min_Z H(Z|S)$$

s.t.  $I(Z; S)$  is maximized

# Contrast Keeps Almost All the Key Information



Theorem 1 suggests maximizing  $I(z^1, z^2)$  results in  $z^1$  containing almost all the key information.

We minimize the following loss:

$$\mathcal{L}_C = \max \mathbb{E} \left[ \frac{1}{N} \sum_{i=1}^N \log \frac{e^{\text{sim}(z_i^1, z_i^2) / \tau}}{\frac{1}{N} \sum_{k=1}^N e^{\text{sim}(z_i^1, z_k^2) / \tau}} \right]$$

# Reconstruction Discards the Redundant Information

*Theorem 2:* The sufficient self-supervised representation contains more redundant information in the input than the sufficient and minimal self-supervised representation. The latter contains an amount of the information,  $I(X; S|T)$  that cannot be discarded from the input.

$$\begin{aligned} I(Z^{ssl}; X|T) &= I(X; S|T) + I(Z^{ssl}; X|S, T) \\ &\geq I(Z^{ssl_{min}}; X|T) = I(X; S|T) \\ &\geq I(Z^{sup_{min}}; X|T) = 0 \end{aligned}$$

$$Z^{ssl} = \arg \max_Z I(Z; S)$$

$$Z^{ssl_{min}} = \arg \min_Z H(Z|S)$$

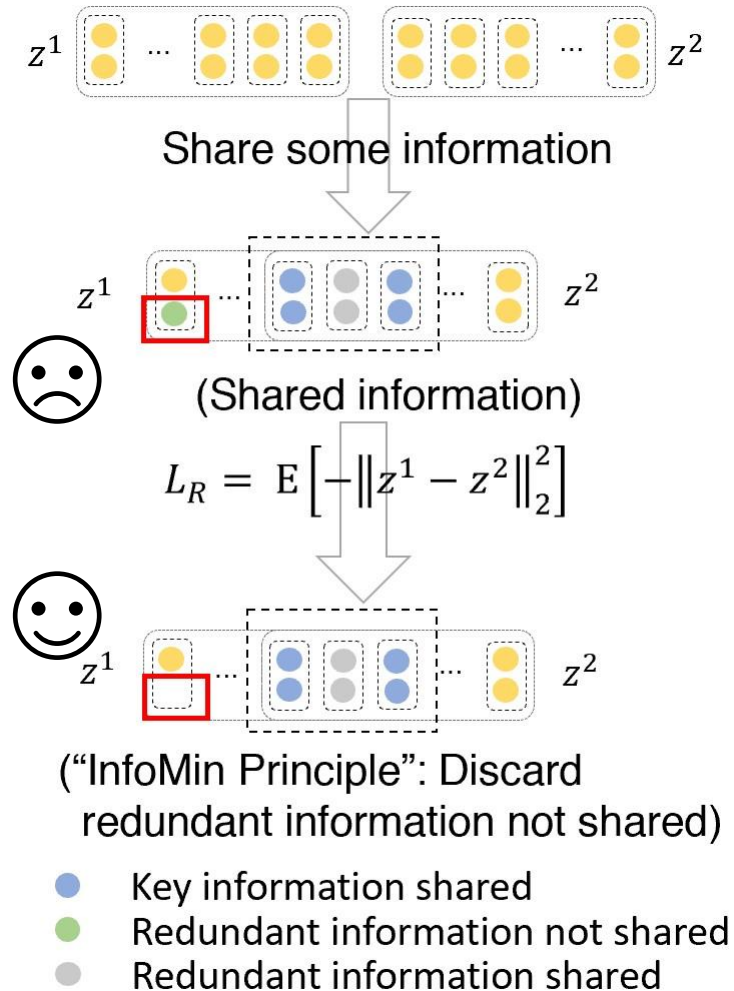
$$s.t. \ I(Z; S) \text{ is maximized}$$

$$Z^{sup} = \arg \max_Z I(Z; T)$$

$$Z^{sup_{min}} = \arg \min_Z H(Z|T)$$

$$s.t. \ I(Z; T) \text{ is maximized}$$

# Reconstruction Discards the Redundant Information



$$\text{Maximize } \mathbb{E}_{P_{Z^1, Z^2}} [\log P(Z^1|Z^2)] = \text{Minimize } H(Z^1|Z^2)$$

Reconstruct  $z^1$  via  $z^2$

$$\text{maximize } \mathbb{E}_{P_{Z^1, Z^2}} [\log P(Z^1|Z^2)]$$

under the constraint that

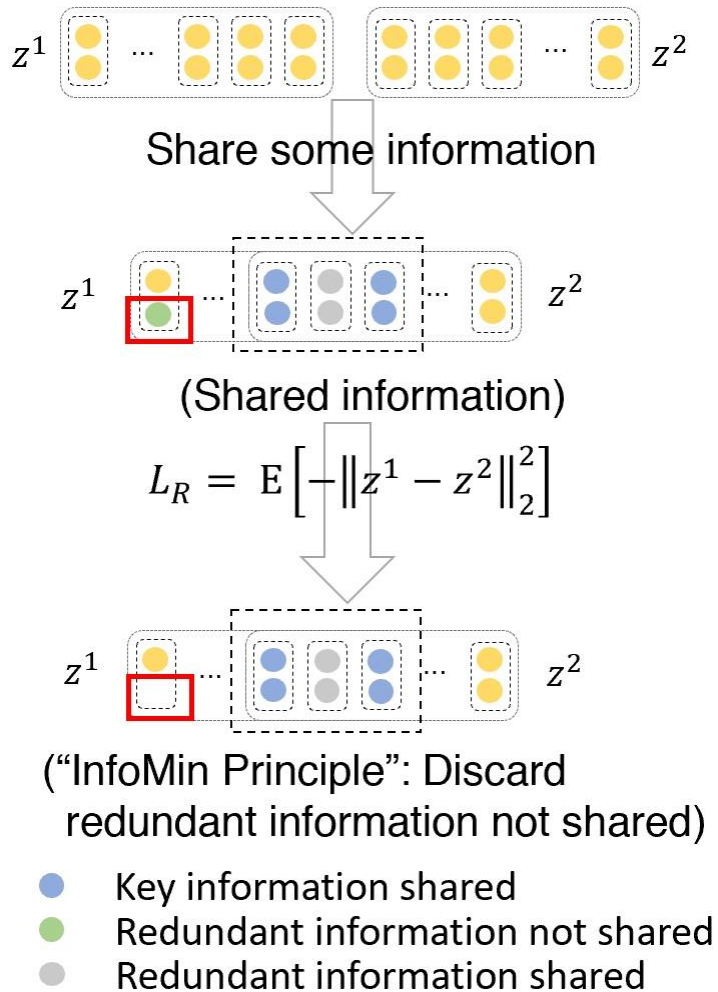
$I(z^1, z^2)$  is maximized: (by contrast operation)

We obtain:

$$z^{1ssl_{min}}$$

Which contains **the least redundant information** according to Theorem 2.

# Reconstruction Discards the Redundant Information



For easier optimization, we use

$$\mathbb{E}_{P_{Z^1, Z^2}} [\log Q_{\Phi} (Z^1 | Z^2)]$$

As a lower bound of

$$\mathbb{E}_{P_{Z^1, Z^2}} [\log P (Z^1 | Z^2)]$$

Where  $Q_{\Phi} (Z^1 | Z^2) \sim N (Z^1 | Z^2, \sigma I)$  ( $\sigma I$  is a diagonal matrix)

We minimize the following loss:

$$\mathcal{L}_R = \mathbb{E}_{z^1, z^2 \sim P_{Z^1, Z^2}} \left[ -\|z^1 - z^2\|_2^2 \right]$$



# Performance on Unsupervised (semantic textual similarity) Tasks

Model	STS12	STS13	STS14	STS15	STS16	STS-B	SICK-R	Avg.
GloVe embeddings (avg.) <sup>†</sup>	55.14	70.66	59.73	68.25	63.66	58.02	53.76	61.32
BERT <sub>base</sub> (first – last avg.) <sup>†</sup>	39.70	59.38	49.67	66.03	66.19	53.87	62.06	56.70
BERT <sub>base</sub> –flow <sup>†</sup>	58.40	67.10	60.85	75.16	71.22	68.66	64.47	66.55
BERT <sub>base</sub> –whitening <sup>†</sup>	57.83	66.90	60.90	75.08	71.31	68.24	63.73	66.28
IS – BERT <sub>base</sub> <sup>†</sup>	56.77	69.24	61.21	75.23	70.16	69.21	64.25	66.58
CT – BERT <sub>base</sub> <sup>†</sup>	61.63	76.80	68.47	77.50	76.48	74.31	69.19	72.05
SCD – BERT <sub>base</sub> <sup>♡</sup>	66.94	78.03	69.89	78.73	76.23	76.30	<b>73.18</b>	74.19
SimCSE – BERT <sub>base</sub>	67.01	82.14	73.76	80.49	79.01	77.04	69.94	75.63
InforMin-CL – BERT <sub>base</sub>	<b>70.22</b>	<b>83.48</b>	<b>75.51</b>	<b>81.72</b>	<b>79.88</b>	<b>79.27</b>	71.03	<b>77.30</b>
RoBERTa <sub>base</sub> (first – last avg.) <sup>†</sup>	40.88	58.74	49.07	65.63	61.48	58.55	61.63	56.57
RoBERTa <sub>base</sub> –whitening <sup>†</sup>	46.99	63.24	57.23	71.36	68.99	61.36	62.91	61.73
DeCLUTR – RoBERTa <sub>base</sub> <sup>†</sup>	52.41	75.19	65.52	77.12	78.63	72.41	68.62	69.99
SCD – RoBERTa <sub>base</sub> <sup>♡</sup>	63.53	77.79	69.79	80.21	77.29	76.55	72.10	73.89
SimCSE – RoBERTa <sub>base</sub>	<b>70.32</b>	82.48	<b>74.84</b>	<b>82.13</b>	<b>82.14</b>	<b>81.57</b>	68.62	<b>77.44</b>
InforMin-CL – RoBERTa <sub>base</sub>	69.79	<b>82.57</b>	73.36	80.91	81.28	81.07	<b>70.30</b>	77.04
SimCSE – RoBERTa <sub>large</sub>	<b>72.64</b>	83.78	<b>75.83</b>	<b>84.24</b>	<b>80.12</b>	<b>81.10</b>	69.81	<b>78.22</b>
InforMin-CL – RoBERTa <sub>large</sub>	70.91	<b>84.20</b>	75.57	82.26	79.68	<b>81.10</b>	<b>72.81</b>	78.08

InforMin-CL outperforms all baselines significantly with BERT as an encoder.

# Analysis of Experimental Result

Datasets	
BERT (16GB)	RoBERTa (160GB)
BooksCorpus	BooksCorpus
English Wikipedia	English Wikipedia
-	CC-NEWS
-	OPENWEB-TEXT
-	STORIES

The diverse large-scale high-quality pre-training datasets of RoBERTa contain less noise information, which results in InforMin-CL struggling to present its effects.



# Performance on Supervised Tasks

Model	MR	CR	SUBJ	MPQA	SST	TREC	MRPC	Avg.
GloVe embeddings (avg.) <sup>†</sup>	77.25	78.30	91.17	87.85	80.18	83.00	72.87	81.52
Skip – thought <sup>†</sup>	76.50	80.10	93.60	87.10	82.00	92.20	73.00	83.50
Avg. BERT embeddings <sup>†</sup>	78.66	86.25	94.37	88.66	84.40	<b>92.80</b>	69.54	84.94
BERT – [CLS] embeddings <sup>†</sup>	78.68	84.85	94.21	88.23	84.13	91.40	71.13	84.66
IS – BERT <sub>base</sub> <sup>†</sup>	81.09	<b>87.18</b>	94.96	88.75	85.96	88.64	74.24	85.83
SCD – BERT <sub>base</sub> <sup>♡</sup>	73.21	85.80	<b>99.56</b>	88.67	85.59	89.80	75.71	85.52
SimCSE – BERT <sub>base</sub>	81.47	86.86	94.79	89.25	86.27	89.40	72.81	85.84
InforMin-CL – BERT <sub>base</sub>	80.99	85.72	94.63	<b>89.47</b>	85.67	88.20	73.97	85.52
w/ MLM	<b>82.87</b>	87.05	95.22	88.43	<b>87.15</b>	92.20	<b>75.77</b>	<b>86.96</b>
SimCSE – RoBERTa <sub>base</sub>	81.26	87.36	93.58	87.56	86.93	84.80	75.01	85.21
SCD – RoBERTa <sub>base</sub> <sup>♡</sup>	82.17	87.76	93.67	85.69	88.19	83.40	76.23	85.30
InforMin-CL – RoBERTa <sub>base</sub>	82.22	88.08	93.57	<b>87.75</b>	87.59	86.60	76.99	86.11
w/ MLM	<b>83.49</b>	<b>88.69</b>	<b>94.79</b>	86.81	<b>88.30</b>	<b>89.40</b>	<b>77.57</b>	<b>87.01</b>
SimCSE – RoBERTa <sub>large</sub>	80.85	85.99	93.08	87.65	86.33	89.00	72.46	85.05
InforMin-CL – RoBERTa <sub>large</sub>	<b>82.50</b>	<b>88.32</b>	<b>93.81</b>	<b>89.38</b>	<b>87.64</b>	<b>90.80</b>	<b>74.49</b>	<b>86.71</b>

InforMin-CL outperforms all baselines with BERT or RoBERTa as the encoder.

# Ablation Study

Influence of  $\lambda$  (the coefficient of reconstruction objective)

$\lambda$	Avg. Sup	Avg. Unsup
0.04	85.20	76.09
0.4	<b>85.52</b>	<b>77.30</b>
4	85.03	77.18

The performance of InforMin-CL on both unsupervised and supervised tasks rises first and falls later.

# Ablation Study

Influence of  $\beta$  (the coefficient of MLM objectives)

Model	Avg. Sup	Avg. Unsup
w/o MLM	85.52	<b>77.30</b>
w/ MLM		
$\beta = 0.01$	86.46	<b>63.59</b>
$\beta = 0.1$ (ours)	86.96	63.25
$\beta = 1.0$	<b>87.04</b>	60.85

Consistently helps improve performance on supervised tasks but brings a significant drop on unsupervised tasks.

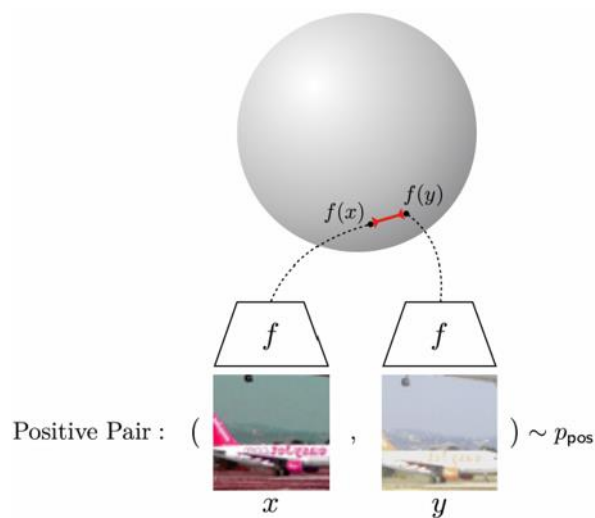
# Ablation Study

## Influence of Batch Size

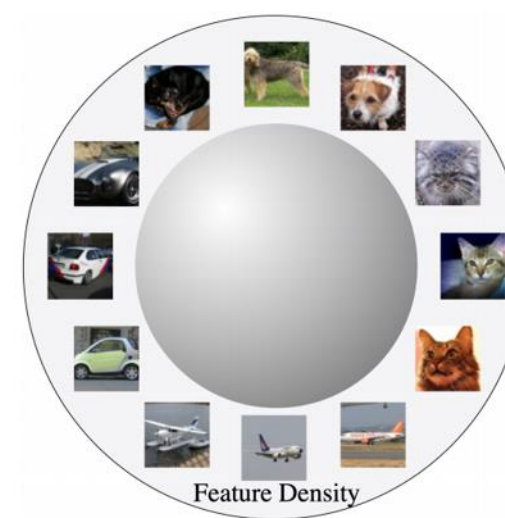
<b>Batch size</b>	<b>64</b>	<b>128</b>	<b>256</b>
Avg. Sup	85.38	85.52	<b>85.77</b>
Avg. Unsup	76.64	<b>77.30</b>	76.14

Not sensitive to batch size

# Why does InforMin-CL Work Well?




**Alignment:** How well positive pairs are aligned



**Uniformity:** How well the embeddings are uniformly distributed

# Why does InforMin-CL Work Well?

Qualitative Analysis:

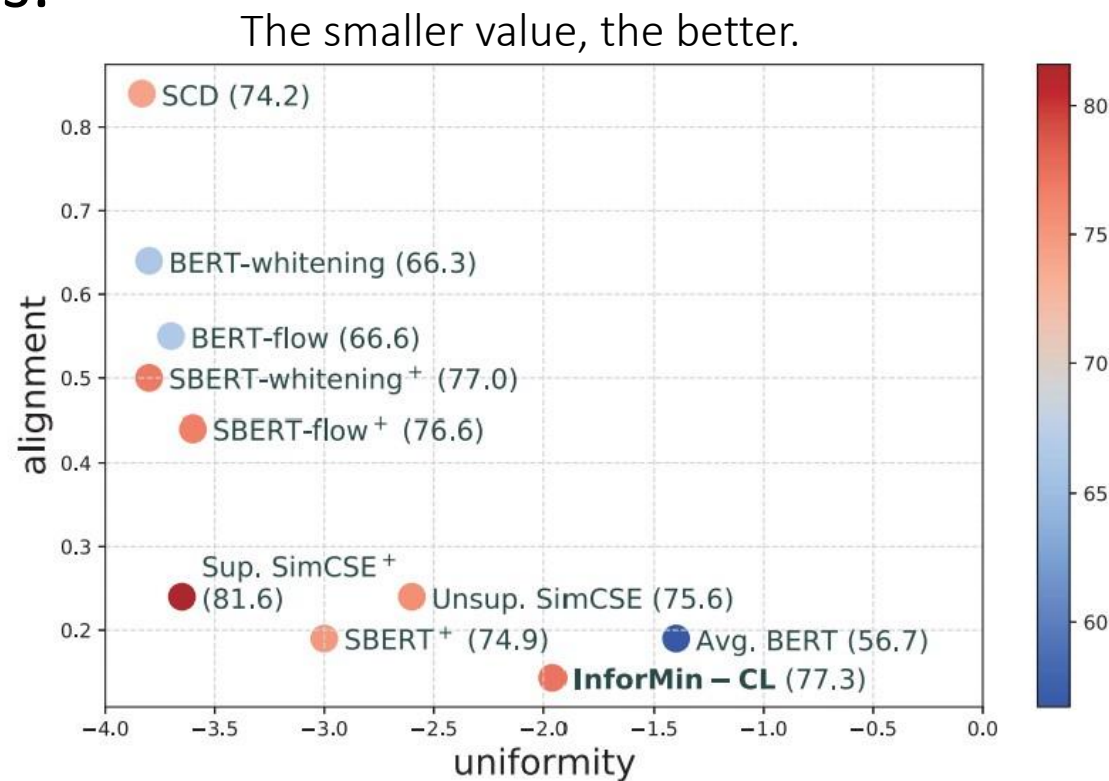
$$\mathcal{L}_C = \max \left[ \frac{1}{N} \sum_{i=1}^N \mathbb{E} \left[ \boxed{\text{sim}(z_i^1, z_i^2)} / \tau \right] \right. \\ \left. - \frac{1}{N} \sum_{i=1}^N \mathbb{E} \left[ \log \frac{1}{N} \sum_{k=1}^N e^{\text{sim}(z_i^1, z_k^2) / \tau} \right] \right]$$


Optimizing  $\mathcal{L}_R$  pulls  $z^1$  and  $z^2$  closer

$$\mathcal{L}_R = \mathbb{E}_{z^1, z^2 \sim P_{Z^1, Z^2}} \left[ - \|z^1 - z^2\|_2^2 \right]$$

# Why does InforMin-CL Work Well?

## Quantitative Analysis:



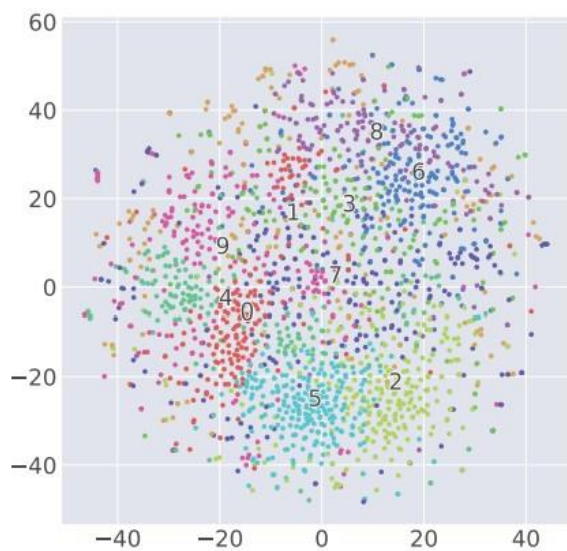
InforMin-CL achieves best in terms of *alignment*



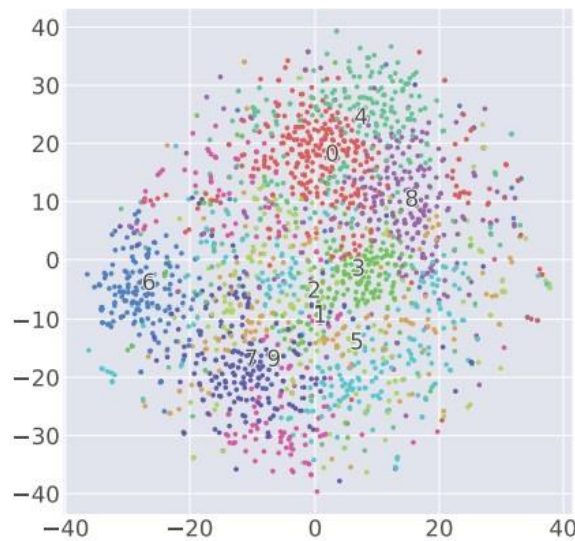
# Why does InforMin-CL Work Well?

## Quantitative Analysis:

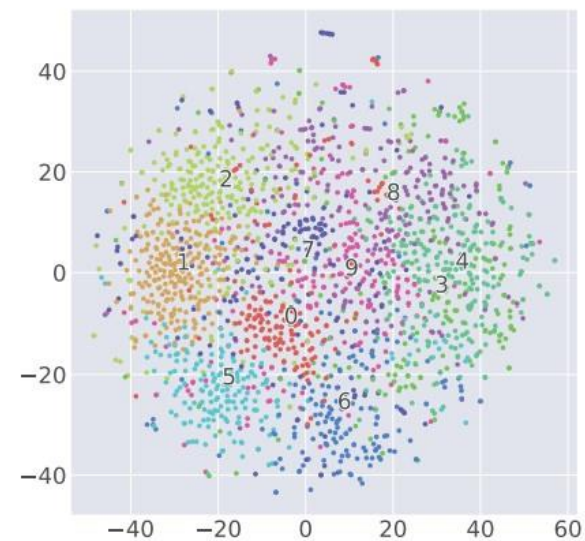
The t-SNE of sentence representations learned with models.



(a) SimCSE



(b) SCD



(c) InforMin-CL

Similar sentence pairs generated by InforMin-CL are more aligned.



# Thanks!

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知乎 临江仙