

Machine Learning Autoencoder Applied to Communication Channels

Eduardo Dadalto Camara Gomes*

*Institut Supérieur de l'Aéronautique et de l'Espace (ISAE-SUPAERO), Université de Toulouse, 31055 Toulouse, FRANCE

Email: eduardo.dadalto-camara-gomes@student.isae-supaero.fr

Abstract—Communication channel error correction is key to enable digital critical communication systems to work efficiently. Although the optimal decoder for noisy channels, the maximum a posteriori (MAP) decoder, has already a mathematically proven optimal error probability minimization; its implementation cripples system applicability, since it introduces a large delay for large codewords. In this context, a deep neural network (DNN) is proposed to optimize the channel with an end-to-end autoencoder. The DNN autoencoder outperforms a MAP decoder from a given encoder in terms of delay, because of the first's *one-shot* capability once trained.

Index Terms—communication system, machine learning, autoencoder, channel decoding, maximum a posteriori (MAP) decoder

I. INTRODUCTION

A. Motivation

A point to point communication channel is a system in which two terminals exchange information through a noisy channel as Fig. 1 illustrates. As a result of channel imperfections, Shannon theorized in [1] the ultimate reliable data rate that can be transmitted through a communication system with an arbitrarily small probability error.

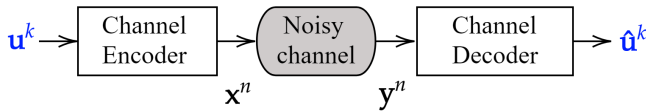


Fig. 1. Diagram of a simplified communication system.

Since then, the research community in digital communication developed a series of algorithms to minimize error probability over a channel. In practice, the bit error rate (BER), an approximation of the probability of error, is targeted. However, the challenge of finding an *efficient* solution i.e., with both low latency and low error probability, for low signal to noise ratio (SNR) channels, remains. Low latency and high bandwidth wireless communication are key to critical systems, such as airplanes, satellites, cellular communication and 5G operations. The latter was studied by F. D. Calabrese et al. in [2] which demonstrated that individual based radio resource management (RRM) algorithms were outperformed by a general learning framework, resulting in significant expense reductions, while increasing performance of the network.

Based on this vision, Tim O'Shea and Jakob Hoydis [3] pertinently noted that traditional algorithms in the field have

foundations in probability theory e.g. maximum a posteriori (MAP) rule, maximum likelihood decoder (MLD) and turbo codes. Hence, they are usually built on top of mathematically convenient models. Even though they are theoretically optimal error corrector codes, these models often do not account for all the real system's imperfections, which leads to errors when implemented in practice.

As opposite to structured algorithms, machine learning (ML) algorithms do not require rigidly designed models and can take non-linearities effortlessly into account. These characteristics make these algorithms candidates for being used as channel decoder. Moreover, with ML based channel encoder and channel decoder, the design of communication systems as independently working blocks becomes obsolete, as a deep neural network (DNN) is able to actuate end-to-end in the system. As a result, an optimized autoencoder with a stochastic layer that models channel's imperfections can substitute the block based representation. Therefore, ML based communication systems could be a better representation of realistic systems and could optimize information transmission of different blocklengths and with low decoding latency, resulting ultimately in gain of bandwidth over standard methods. Thereby, ML algorithms are cardinal for state of the art communication applications.

B. Related work

Recently, a significant amount of work in radio communication theory has emerged, introducing ML elements to the communication system. O'Shea et al. in [4] developed a channel autoencoder with optimized impairment and regularization layers to emulate channel impairments. They studied this architecture over an additive white Gaussian noise (AWGN) channel, founding "some promising initial capacity" for this scheme. In their research, results in terms of BER over SNR for a DNN based autoencoder and for a convolutional neural network (CNN) based autoencoder were treated. They used a range of SNR - from -10dB to 15dB - with QPSK and QAM16 modulation as benchmarks. This analysis was conducted for a binary input message.

T. Gruber et. al. in [5] proved that a deep learning-based channel decoder could actually learn a decoding algorithm rather than just being a simple classifier. They introduced codewords that were not been used in the training set, and the trained NN was able to correctly decode it. They also observed that structured codes are easier to learn than unstructured ones.

NN for structured codes are able to generalize to the full codebook even if they have not seen all the training examples. They trained the NN for very short blocklengths ($N \leq 64$) in order to compare with MAP decoding performance.

C. Problem statement

In this work, we will implement a ML autoencoder for a BSC that performs similar to the MAP decoder in real applications for a range of SNR from -10dB to 10dB . In its most simple form, a channel autoencoder includes an encoder, a noisy channel and a decoder. Using state-of-the-art DNN algorithms to find the best solution of the problem, this work aims to contribute to set up a higher standard in terms of performance in bit-error correction and reduced delay for digital communication applications. In a near future, this disruptive methodology for error correction using ML could replace mathematically optimal decoders which are the current guideline.

D. Notation

Throughout the work, vectors will be written in bold font weight and may have a subscript which indicates their layer in a NN and may have a superscript which indicates their size length. In order to homogenize notation, for the encoding phase of the communication system, \mathbf{u}^k represents an input *source message* and \mathbf{x}^n its correspondent codeword. For the decoding portion, \mathbf{y}^n represents the output of the noisy channel and $\hat{\mathbf{u}}^k$ the estimated source message. These definitions are illustrated in Fig. 1.

In addition, every indispensable concept is introduced either in *italics* or is defined by a commonly used abbreviation present in others scientific works.

II. THEORETICAL BACKGROUND

A. Maximum a posteriori decoder

The concept of a MAP decoder algorithm for sequences, is choosing a message which maximizes the a posteriori probability of the corrupted codeword y received by the decoder [6]. This algorithm is known for its optimal error correction capability for white noise interference. This algorithm is also referred as the Viterbi decoder [7].

Mathematically, we want to maximize the average probability of making a correct decision when analysing the channel output \mathbf{y} , which is written as

$$P_c := \Pr[\mathbf{X} = f(\mathbf{Y})] \quad (1)$$

where $x \sim X$ and $y \sim Y$ are multivariate random variables. We derive below the decoder that maximizes P_c .

$$\Pr[X = f(Y)] = \sum_{f(y)|y \in \mathcal{X} \times \mathcal{Y}} P_{XY}(f(y)|y) \quad (2)$$

$$= \sum_{y \in \mathcal{Y}} P_Y(y) P_{X|Y}(f(y)|y) \quad (3)$$

The optimal decoder is finally given by

$$f(y) = \arg \max_{x \in \mathcal{X}} P_{X|Y}(x|y) \quad (4)$$

$$= \arg \max_{x \in \mathcal{X}} P_X(x) P_{Y|X}(y|x). \quad (5)$$

However, the MAP decoder is practically nonviable to implement [8]. Thus, its variants cited in this paragraph are better suited for practical cases. The Log-MAP is an optimal decoder, having equivalent performance to the MAP decoder. While the Max-Log-MAP is a suboptimal decoder and will not be treated in this paper. these variants are widely used as decoders for turbo codes [9]. Refer to [8] for specific details in the derivation of the Log-MAP algorithm. Furthermore, the Bahl-Cocke-Jelinek-Raviv (BCJR) algorithm is a bit-wise MAP rule with lower complexity widely used in practice, even for long data packets.

Turbo decoding using Log-MAP decoder for an additive white Gaussian noise (AWGN) channel and for a BSC was studied in [10]. They analyzed the BER for small SNR and concluded that the results are sensible to SNR estimation of the real channel, since the estimation of this parameter is required for the metric calculation of the algorithm [8]. It means that if the real SNR is smaller, the decoder will not perform well. Hence, for channel characteristics that change over time, the application of a MAP algorithm is debatable. This conclusion serve as motivation for ML autoencoders, which could adapt to different SNR conditions, outperforming the MAP decoder for realistic applications.

B. Neural network basics

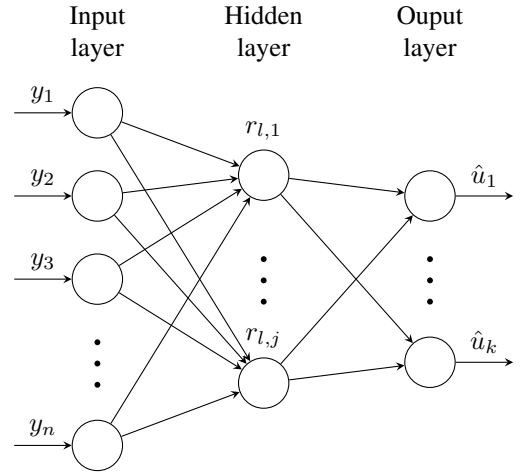


Fig. 2. MLNN representative diagram, where \mathbf{y}^n is the input vector, \mathbf{r}_l^j is a hidden layer vector and $\hat{\mathbf{u}}^k$ is the output vector.

Neural networks (NN) are a set of connected *neurons* able to approximate any kind of function through an architecture composed of several single processing units (neurons) connected together forming a network. They are defined by [11] as parallel distributed, learning- and self-organizing information processing systems.

In the context of learning algorithms implemented by a NN, the key issue is to find a suitable architecture that delivers the best results. To define and build this infrastructure, the activation function, the loss function and the structure must be decided. Nielson [12] in his book explores a vast amount of NN architectures and how they work.

Multi-layer feed forward neural network (MLNN) as shown in Fig. 2 will be applied in this work. They are known for the universal approximation property [11] and for the versatility of increasing the number of layers, creating a DNN able to undertake complex classification problems with low classification error and low dimensionality. In more general terms, a MLNN with L layers, also called *depth*, and parameter θ is a mapping of an input $\mathbf{y}^n \in \mathbb{R}^n$ to an output $\hat{\mathbf{u}}^k \in \mathbb{R}^k$ through L iterative steps. For a fully-connected network, each layer vector is calculated iteratively in the forward propagation. Each neuron is composed of a linear combiner and an activation function defined as

$$f_l(\mathbf{r}_{l-1}; \theta_l) = \sigma(\mathbf{W}_l \mathbf{r}_{l-1} + \mathbf{b}_l) \quad (6)$$

where $\mathbf{W}_l \in \mathbb{R}^{N_l \times N_{l-1}}$ is the weight matrix between layers $l-1$ and l , $\mathbf{r}_{l-1} \in \mathbb{R}^{N_{l-1}}$ is a vector containing the hidden layer $l-1$ values, $\mathbf{b}_l \in \mathbb{R}^{N_l}$ is the bias vector and σ is the activation function [3].

Two common activation functions are the rectified linear unit (ReLU) and the sigmoid function. Both will be applied in the NN treated in this paper. Their mathematical expressions are shown below.

$$\text{ReLU: } \sigma_1(x) = \max\{0, x\} \quad (7)$$

$$\text{Sigmoid: } \sigma_2(x) = \frac{1}{1 + e^{-\lambda x}} \quad (8)$$

where $x \in \mathbb{R}$ and $\lambda > 0$.

For a classification problem in communication, the *categorical cross-entropy* loss function $l(\mathbf{p}, \mathbf{q}) : \mathbb{R}^{N_L} \times \mathbb{R}^{N_L} \mapsto \mathbb{R}$ defined in (9) is most common. It is derived from the log-likelihood of a training set where q_j is the estimated probability of the outcome j and p_j is the true probability. Basically, the function measures the dissimilarity between p_j (what you expected) and q_j (what you obtained) [13] where $j = 1, \dots, N_L$.

$$l(\mathbf{p}, \mathbf{q}) = - \sum_j p_j \log(q_j) \quad (9)$$

With all these elements set, training the neural network to calculate an accurate weight matrix \mathbf{W} for forward propagation requires a labeled *training data set*. This set is composed of pairs $(\mathbf{y}_i^n, \mathbf{u}_i^k)$, where $i = 1, \dots, S$ and S is the number of training sets. It matches the input and its respective desired output. The objective is to minimize the overall loss function defined in (10) in terms of the parameter θ [3].

$$L(\theta) = \frac{1}{S} \sum_{i=1}^S l(\mathbf{u}_i^k, \mathbf{y}_i^n) \quad (10)$$

This problem is an optimization problem and can be solved through different algorithms. For NN, an efficient way of computing this minimization is implementing the back-propagation (BP) algorithm. BP is classified as a supervised learning algorithm that is able to optimize a function based on some parameter and is highly parallelizable in computational terms [11] [12].

One of the greatest advantage of NN is its ability to generalize the training set, delivering the right results even for input data not contained in the training set. With the weight matrix trained, the NN finds the correct output values for unseen inputs. In order to validate this principle, a *validation data set* is used and the loss is measured. Based on this value, we can evaluate the NN overall accuracy.

For implementing all the algorithms, Keras, a high-level python API for ML, will be used together with TensorFlow 1.13.1, a ML python friendly open-source library [14] [15]. Both are available on a free license terms.

C. Autoencoders

Autoencoders based on DNN can learn an appropriate correspondence between input source messages and estimated source message output through different noisy channels. The statistics of the channel's noise is shown in [5] to be irrelevant, since the NN extract it during training phase. Their applicability is tantamount compelling because the weights computed during training can be separated in two groups, one correspondent to the nodes before the channel and one posterior to the channel. As a consequence, we are able to design a non linear encoder and its correspondent non linear decoder with substantial ease. This new representation has ultimately far more possibilities than conventional encoding patterns.

Whilst autoencoders are more complex dimensional wise when compared to NN decoders, the readily access to graphical processing units (GPUs) contributed to the feasibility of this technique, tackling the *curse of dimensionality* challenge in ML. This type of hardware made possible the approach of the layer-by-layer unsupervised pre-training followed by stochastic gradient descent applied in this work. [16]

III. PROCEDURE AND METHODOLOGY

Explain what I Should do to achieve my goal Talk about decoder + autoencoder and the OBJECTIVE of each one, G matrix of choice, Batch size, The reader should be able to replicate what I ve done

A. Decoder

Hamming coding

The linear encoding matrix $\mathbf{G}_{8 \times 16}$ is shown below.

$\mathbf{G} =$

1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0
1	1	0	0	1	1	0	0	0	0	0	0	0	0	0	0	0
1	1	1	1	1	1	1	1	0	0	0	0	0	0	0	0	0
1	1	0	0	0	0	0	0	1	1	0	0	0	0	0	0	0
1	1	1	1	0	0	0	0	1	1	1	1	0	0	0	0	0
1	1	0	0	1	1	0	0	1	1	0	0	1	1	0	0	0
1	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	0
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1

Introduce encoding equations

1) *Array Decoder*: Architecture, Training parameters, cite choice of p train [17], number of epochs, Talk about noise layer and its removal in prediction,

2) *One-hot Decoder*: Architecture, Training parameters, Explain what is a One hot decoding, talk about the matrix transformation from one hot to messages, p train equals 0, number of epochs

B. Autoencoder

Architecture, Training and simulation parameters, procedure to find a M epoch suitable, choices of p train, Talk about NN separation,

IV. RESULTS AND ANALYSIS

A. Decoders

BER Curves from both decoders, analyse why the number of epochs is so different.

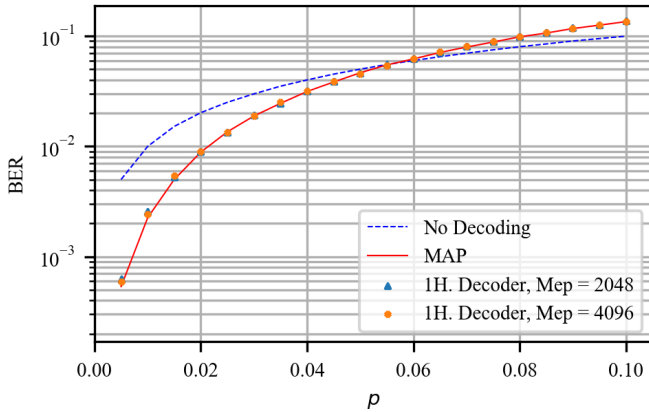


Fig. 3. Test caption to test image.

B. Autoencoder

BER Curves of simulation varying p , best choice of p , analyse autoencoder with best choice of p

C. Decoding time analysis

compare time in decoding between map, autoencoder and a decoder.

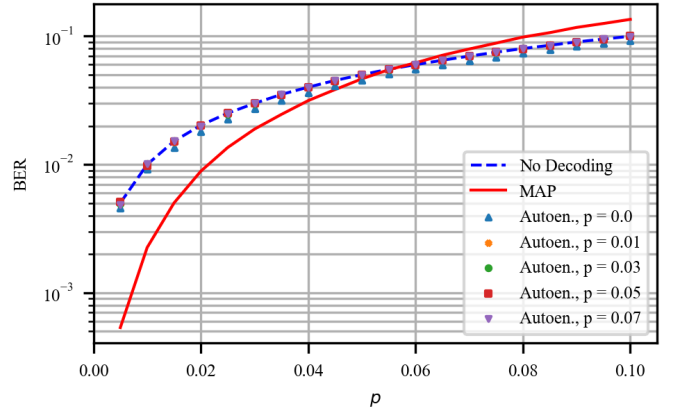


Fig. 4. Test caption to test image.

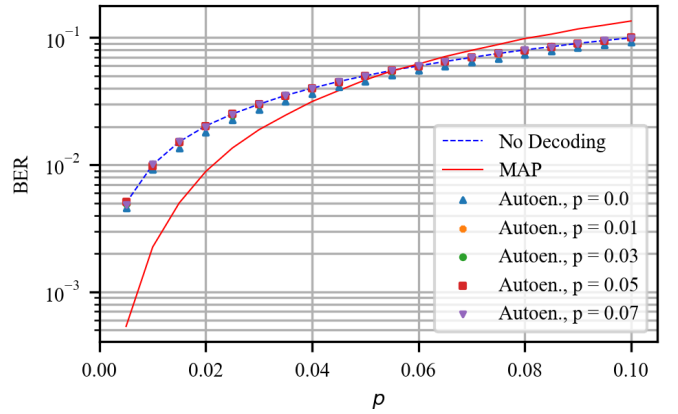


Fig. 5. Test caption to test image.

V. CONCLUSIONS

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