

Pre-semester Examination-2069

Bachelor Level/Second Year/Third Semester/Science

Numerical Method (CSC 204)

Pass marks: 24

Full marks: 60

Time: 3 hrs

Set A

1. Derive the formula for Newton Raphson method using an illustrative figure. Find a real root of the following equation using NR method correct up to two decimal places.

[3+5=8]

$$f(x)=x \sin x + \cos x \text{ using } x_0 = \pi$$

OR

Derive the formula for Secant method. Find a real root of following equation using Secant method.

$$f(x) = \sin x - 2x + 1 \text{ using } x_1 = 0, x_2 = \pi$$

2. Write down the application of interpolation in practical life. Find the value of f(x) at x=0 for the following data by using Lagrange interpolating polynomial formula. [2+6=8]

| X | -1 | -2 | 2 | 4 |
|------|----|----|----|----|
| f(x) | -1 | -9 | 11 | 69 |

3. (a). Fit a straight line to the following set of data.

[4]

| X | 1 | 2 | 3 | 4 | 5 |
|---|---|---|---|---|---|
| Y | 3 | 4 | 5 | 6 | 8 |

(b). Compute the integral

[4]

$$\int_{-1}^{1} e^{x} dx$$
 by using Simpson's 3/8 rule for n=4

4. In which situation system of linear equations are in ill-conditioned? Solve the following system of linear equations by using Gauss-Seidel iterative method. [2+6=8]

$$2x_1 - 2x_2 - x_3 - x_4 = -9$$

$$x_2 + 3x_3 + 2x_4 = 19$$

$$3x_2 + 2x_3 + 2x_4 = 20$$

$$x_1 + 4x_2 + 2x_4 = 17$$
OR

What do you mean by eigen-value eigen-vector problems? Find the largest eigen value correct to two significant digits and corresponding eigen vectors of the following matrix using power method. [2+6=8]

$$A = \begin{bmatrix} 241 \\ 013 \\ 103 \end{bmatrix}$$

- 5. What is initial value problem? How it is differ from boundary value problem? Solve the following equation by using Picard's method [2+1+5=8] $dy/dx = y^{\parallel}(x) = x^2 + 2x + y$ with y(0)=0 and estimate y(0.2). Hint: Solve up to 2^{nd} iteration.
- 6. What is ordinary differential equation? Given the following differential equation, $dy/dx = y^{||}(x) = 3x^2 + 1$ with y(1)=2 estimate y(2) by using [1+3+4=8]
 - a. Euler's Method
 - b. Heun's method with h=0.5

OR

Derive a difference equation to represent a Poison's equation. Solve the Poison's equation

$$\nabla^2 f = 2x^2y^2$$
 over the domain $0 \le x \le 3, 0 \le y \le 3$ with $f = 0$ on the boundary and h=0.

$$[3+5=8]$$

7. Write an algorithm and complete C-program to solve the given non-linear equation by using Bisection method (Half interval method). [5+7=12]

$$f(x) = x^2 - 4x - 10$$
 using initial guesses $x_1 = -2$ and $x_2 = -1$

In this program display final root, functional value of final root and number of steps required to solve such a non-linear equation.

The End



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Set B Time: 3 hours.

1. What is non-linear equation? Find the root of $f(x) = x^2-4x-10$ using Bisection Method. Compute initial guess of roots itself. [2+6=8]

OR

Derive the formula for Secant method. Find a real root of following equation using Secant method.

$$f(x) = \sin x - x + 5 \text{ using } x_1 = 0, x_2 = \pi$$

2. What do you mean by interpolation and extrapolation? Find the value of f(x) at x=3 for the following data by using Lagrange interpolating polynomial formula. [2+6=8]

| X | -1 | -2 | 2 | 4 |
|------|----|----|----|----|
| f(x) | -1 | -9 | 11 | 69 |

3. (a). Fit a straight line to the following set of data.

[4]

| X | 1 | 2 | 3 | 4 | 5 |
|---|---|---|---|---|---|
| Y | 3 | 4 | 5 | 6 | 8 |

(b). Compute the integral

[4]

$$\int_{-1}^{1} e^{x} dx$$
 by using Simpson's 1/3 rule for n=4

4. In which situation system of linear equations are in ill-conditioned? Solve the following system of linear equations by using Gauss-Seidel iterative method. [2+6=8]

$$x_1 - 2x_2 - x_3 = -9$$

$$x_2 + 9x_3 + 2x_4 = 15$$

$$3x_2 + 2x_3 + 2x_4 = 20$$

$$3x_1 + x_2 + 4x_4 = 16$$

What do you mean by eigen-value eigen-vector problems? Find the largest eigen value correct to two significant digits and corresponding eigen vectors of the following matrix using power method.

[2+6=8]

$$A = \begin{bmatrix} 120 \\ 210 \\ 00 - 1 \end{bmatrix}$$

5. What is initial value problem? How it is differ from boundary value problem? Solve the following equation by using Picard's method [2+1+5=8]

 $dy/dx = y^{\dagger}(x) = x^2 + 2y$ with y(0)=0 and estimate y(0.4).

Hint: Solve up to 2nd iteration.

6. What is ordinary differential equation? Given the following differential equation,

 $dy/dx = y'(x) = x^2 + y^2$ with y(1)=2 estimate y(1.6) by using

[1+3+4=8]

- c. Euler's Method
- d. Heun's method with h=0.3

OR

How can you solve Laplace's equation? Explain. The steady-state two dimensional heat

flows in a metal plate is defined by $\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} = 0$.

A steel plate of size 30 x 30cm is given. Two adjacent sides are placed at 100°C and other side at held at 0°C. Find the temperature at interior points, assuming the grid size of 10x10.

Write an algorithm and complete C-program to find the root of given equation by using Secant method.

 $f(x) = x^2-4x-10$ (use x1=4 and x2=2)

[5+7=12]

in a program display final root and number of iterations.