

Study hours, Sleep hours vs Exam score

Study hours	Sleep hours	Exam score
5	8	88
3	6	75
8	7	90
2	5	60

$$r = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum (x_i - \bar{x})^2 \sum (y_i - \bar{y})^2}}$$

$$\text{Mean of study hours } (\bar{x}) = \frac{5+3+8+2}{4} = \frac{18}{4} = 4.5$$

$$\text{Mean of sleep hours } (\bar{y}) = \frac{8+6+7+5}{4} = \frac{26}{4} = 6.5$$

$$\text{Mean of exam score } (\bar{y}) = \frac{88+75+90+60}{4} = \frac{313}{4} = 78.25$$

Study hours vs Exam score

Sample	x_i	y_i	$x_i - \bar{x}$	$y_i - \bar{y}$	$(x_i - \bar{x})(y_i - \bar{y})$
1	5	88	0.5	9.75	4.875
2	3	75	-1.5	-3.25	4.875
3	8	90	3.5	11.75	41.125
4	2	60	-2.5	-18.25	45.625

$$\sum (x_i - \bar{x})(y_i - \bar{y}) = 96.5$$

$$\sum (x_i - \bar{x})^2 = 21$$

$$\sum (y_i - \bar{y})^2 = 576.75$$

Sleep hours vs Exam score

sample	x_i	y_i	$x_i - \bar{x}$	$y_i - \bar{y}$	$(x_i - \bar{x})(y_i - \bar{y})$
1	8	88	1.5	9.75	14.625
2	6	75	-0.5	-3.25	-1.625
3	7	90	0.5	11.75	5.875
4	5	60	-1.5	-18.25	27.375

$$\sum (x_i - \bar{x})(y_i - \bar{y}) = 49.5$$

$$\sum (x_i - \bar{x})^2 = 5$$

$$\sum (y_i - \bar{y})^2 = 576.75$$

Study hours

$$r = \frac{96.5}{\sqrt{21 \times 576.75}}$$

$$= \frac{96.5}{\sqrt{12122.75}}$$

$$= \frac{96.5}{110.11}$$

$$r = 0.876$$

$$\approx 0.88$$

Sleep hours

$$r = \frac{49.5}{\sqrt{5 \times 576.75}}$$

$$= \frac{49.5}{\sqrt{2883.75}}$$

$$= \frac{49.5}{53.71}$$

$$r = 0.921$$

$$\approx 0.92$$