Alignment of short/long-read sequencing data

2019 Dragon Star Bioinformatics Course (Day 2)

Sequence similarity

- For any two sequences
 - Mutation: mismatch
 - Insertion
 - Deletion

DNA-sequence-1

```
tcctctgcctcgatgccatcat--caaccacaagt
```

DNA-sequence-2

Sequence alignment

- Sequence alignment
 - Consider matches, mismatches, insertions and deletions (indels are gaps in alignment)
 - Find an alignment between sequences with an optimal score defined by a scoring matrix
 - Applications
 - Reference-based read mapping
 - Genome assembly
 - Gene finding
 - Motif finding

Pairwise alignment

- Sequence alignment between two sequences
- Dynamic programming is a widely used for this purpose
 - Input
 - Two sequences
 - Scoring matrix

Dynamic programming - score matrix

- Simple scoring matrix
 - Assume: a, b are two bases

$$\emptyset(a,b) = \begin{cases} 1 & \text{if } a = b \\ -1 & \text{if } a \neq b \\ -1 & \text{if } a = gap \\ -2 & \text{if } b = gap \end{cases} \qquad \emptyset(a,b) = \begin{cases} 1 & \text{if } a = b \\ -1 & \text{if } a \neq b \\ -2 & \text{for open gaps} \\ -1 & \text{for extended gaps} \end{cases}$$

or

	_			
	Α	С	G	Т
А	2	-3	-3	-1
С	-2	3	-1	-2
G	-2	-1	4	-3
Т	-1	-1	-2	1

Dynamic programming

- Purpose:
 - To find an alignment between two sequences with best matching scores using scoring matrix
- Three components
 - Recursive calculation
 - Tabular arrangement
 - Traceback
- Three common types of pairwise alignments
 - Global alignment: Needleman-Wunsch
 - Local alignment: Smith-Waterman
 - Semi-global alignment

- Best global alignment
 - Have maximal alignment score with all bases in two sequences
 - Assume we have two sequences: P and Q
 - **P** = TCATGGC
 - **Q** = TCATC
 - Score functions

$$\emptyset(a,b) = \begin{cases} 1 & \text{if } a = b \\ -1 & \text{if } a \neq b \\ -1 & \text{if } a = gap \\ -1 & \text{if } b = gap \end{cases}$$

- 1. Tabular arrangement
 - $C(0,j) = \sum_{1 \le k \le ||P||} \emptyset(-,P(k))$
 - $C(i,0) = \sum_{1 \le k \le ||Q||} \emptyset(Q(k), -)$

$\emptyset(a,b) = \langle$	$\begin{cases} 1 & \text{if } a = b \\ -1 & \text{if } a \neq b \\ -1 & \text{if } a = gap \\ -1 & \text{if } b = gap \end{cases}$
$\psi(a,b) = 1$	-1 if a = gap
	1 - 1 if $b = gap$

<u> </u>								
	-	Т	С	А	Т	G	G	С
-	0	-1	-2	-3	-4	-5	-6	-7
Т	-1							
С	-2							
А	-3							
Т	-4							
С	-5							

• 2. Recursive calculation C(i,j) = max $\begin{cases} C(i-1,j-1) + \emptyset(Q(i),P(j)) \\ C(i-1,j) + \emptyset(Q(i),-) \\ C(i,j-1) + \emptyset(-,P(j)) \end{cases}$

<u>Q</u>								
	-	Т	С	А	Т	G	G	(
-	0	-1	-2	-3	-4	-5	-6	1
Т	-1							
С	-2							

$\emptyset(a,b) = \langle$	$\begin{cases} 1 & \text{if } a = b \\ -1 & \text{if } a \neq b \\ -1 & \text{if } a = gap \\ -1 & \text{if } b = gap \end{cases}$
----------------------------	--

• 2. Recursive calculation C(i,j) = max $\begin{cases} C(i-1,j-1) + \emptyset(Q(i),P(j)) \\ C(i-1,j) + \emptyset(Q(i),-) \\ C(i,j-1) + \emptyset(-,P(j)) \end{cases}$

C

C

-7

	-	0	-1	-2	-3	-4	
	٦	-1					
$\emptyset(a,b) = \begin{cases} 1 & \text{if } a = b \\ -1 & \text{if } a \neq b \\ -1 & \text{if } a = gap \\ -1 & \text{if } b = gap \end{cases}$	С	-2					
$ \begin{cases} -1 & \text{if } a = gap \\ -1 & \text{if } b = gap \end{cases} $	А	-3					
(, , , , , , , , , , , , , , , , , , ,							

• 2. Recursive calculation C(i,j) = max $\begin{cases} C(i-1,j-1) + \emptyset(Q(i),P(j)) \\ C(i-1,j) + \emptyset(Q(i),-) \\ C(i,j-1) + \emptyset(-,P(j)) \end{cases}$

C

C

-7

	-	0	-1	-2	-3	-4	-!
	Т	-1					
$\emptyset(a,b) = \begin{cases} 1 & \text{if } a = b \\ -1 & \text{if } a \neq b \\ -1 & \text{if } a = gap \\ -1 & \text{if } b = gap \end{cases}$	С	-2					
$ \begin{cases} -1 & \text{if } a = gap \\ -1 & \text{if } b = gap \end{cases} $	А	-3					
(, 3 ,							

• 2. Recursive calculation C(i,j) = max $\begin{cases} C(i-1,j-1) + \emptyset(Q(i),P(j)) \\ C(i-1,j) + \emptyset(Q(i),-) \\ C(i,j-1) + \emptyset(-,P(j)) \end{cases}$

C

C

-7

	-	0	-1 -1	-2	-3	-4	-5
	Т	-1	1				
$\emptyset(a,b) = \begin{cases} 1 & \text{if } a = b \\ -1 & \text{if } a \neq b \\ -1 & \text{if } a = gap \\ -1 & \text{if } b = gap \end{cases}$	С	-2		•			
$ \begin{pmatrix} \phi(a,b) = \\ -1 & \text{if } a = gap \\ -1 & \text{if } b = gap \end{pmatrix} $	А	-3					
(, , , , , , , , , , , , , , , , , , ,							

• 2. Recursive calculation C(i,j) = max $\begin{cases} C(i-1,j-1) + \emptyset(Q(i),P(j)) \\ C(i-1,j) + \emptyset(Q(i),-) \\ C(i,j-1) + \emptyset(-,P(j)) \end{cases}$

$$\emptyset(a,b) = \begin{cases} 1 & \text{if } a = b \\ -1 & \text{if } a \neq b \\ -1 & \text{if } a = gap \\ -1 & \text{if } b = gap \end{cases}$$

_	Q								
		-	Т	С	А	Т	G	G	С
	-	0	-1 -1 >	-2 1 ₋₁ 1	-3 -11 Q	-4 -11	-5 -11	-6 -1	-7 -1
	Т	-1	1 -1 1	1.0 -	-1-1 -1-1	-1 1	L3 ⁻	L -4-	1 -5 -1
-	С	-2 -	1 0 =	1 2 -	1 1 -1 1 -1	0-1	-1-	1 -2 -	1,3
	А	-3 <mark></mark>	-1 -1	1,1 =	1 3 -	1, 2 -1 -1	1 -1 1	1.0 =	L-1
	Т	-4-	1,-2 = 1 -1 \	1. ₂ -	1 0 =	1 ₄ =	1 3 = 1	L 2 = 1	1 -1
	С	-5 <mark>-</mark>	1 -3 -	1, 1	→-1 -	1-3-1	+ 3 -	1, 2 -	3

• 3. Traceback

Check which operation obtained the current alignment score.

 \mathbf{Q}

P

	-	Т	С	А	Т	G	G	С
-	0	-1	-2	-3	-4	-5	-6	-7
Т	-1	1	0	-1	-2	-3	-4	-5
С	-2	0	2	1	0	-1	-2	-3
А	-3	-1	1	3	2	1	0	-1
Т	-4	-2	-2	0	4	- 3 ←	-2	1
С	-5	-3	-1	-1	3	3	2	3

- Best local alignment
 - Have maximal alignment score with a subset of bases in two sequences
 - Assume we have two sequences: **P** and **Q**
 - **P** = TCATGGC
 - **Q** = TCATC
 - Score functions

$$\emptyset(a,b) = \begin{cases} 1 & \text{if } a = b \\ -1 & \text{if } a \neq b \\ -1 & \text{if } a = gap \\ -1 & \text{if } b = gap \end{cases}$$

- 1. Tabular arrangement
 - C(0,j) = 0
 - C(i, 0) = 0

 $\emptyset(a,b) = \begin{cases} 1 & \text{if } a = b \\ -1 & \text{if } a \neq b \\ -1 & \text{if } a = gap \\ -1 & \text{if } b = gap \end{cases}$

Q

	-	Т	С	А	Т	G	G	С
-	0	0	0	0	0	0	0	0
Т	0							
С	0							
А	0							
Т	0							
С	0							

• 2. Tabular arrangement(*i*, *j*) =

•
$$max$$

$$\begin{cases}
C(i-1,j-1) + \emptyset(Q(i),P(j)) \\
C(i-1,j) + \emptyset(Q(i),-) \\
C(i,j-1) + \emptyset(-,P(j)) & \mathbf{Q} \\
0 & \mathbf{P}
\end{cases}$$

$$\emptyset(a,b) = \begin{cases} 1 & \text{if } a = b \\ -1 & \text{if } a \neq b \\ -1 & \text{if } a = gap \\ -1 & \text{if } b = gap \end{cases}$$

			4					
	-	Т	С	Α	Т	G	G	С
-	0	0 -1	0	0	0	0	0	0 1 1
Т	0 =	111	1,0 - -1	0 -	1 -1 -1 1	0	l → 0 = - 11 ×	0 -1
С	0 -1	1 0 <u>-</u>	1 2 =	1 1 1 1 -1	0-1	- 0 =	1 0 =	1 1 1
А	0 -	0 1	1 ₋₁ -	1, ₃ - 1 -1	1 2 -1 -1	\1 →1 -1\1	1 0 = -1 \ 1	L 0 -1
Т	0 =	1 0 = 1 1 1	1 0 <u>-</u>	1.0 -	1 4 - L -1 1	1 3 - -1	L 2 <u>-</u>	1 1 -1
С	0 -	1.0 -	1.0-	0 -	1,3-1	+ 3 -	1 2 -1	+ 3

- 3. Traceback
 - 1. Find a best score recursively
 - 2. Check which operation is used to obtain the current alignment score.
 - 3. Stop when an alignment is 0



<u>Q</u>

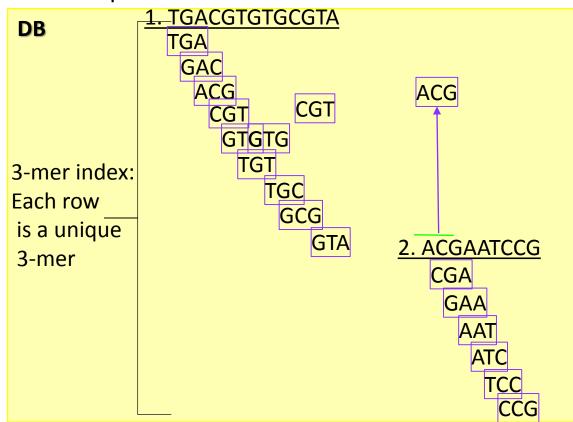
	1	Т	С	А	T	G	G	С
-	0	0	0	0	0	0	0	0
Т	0	1	0	0	1	0	0	0
С	0	0	2	1	0	0	0	1
А	0	0	1	3	2	1	0	0
Т	0	0	0	0	4	3	2	1
С	0	0	0	0	3	3	2	3

	•	T	A	T	c	T	T	A	A	C	G	С	$\overline{\mathbf{c}}$
-	0	0	0	0	0	0	0	0	0	0	0	0	0
G	0	0	0	0	0	0	0	0	0	0	1	0	0
A	0	0	1	0	0	0	0	1	1	0	0	0	0
T	0	1	0	2	1	1	1	0	0	0	0	0	0
C	0	0	0	1	3	2	1	0	0	1	0	1	1
A	0	0	1	0	2	2	1	2	1	0	0	0	0
A	0	0	1	0	1	1	1	2	3	2	1	0	0
T	0	1	0	2	1	2	2	1	2	2	1	0	0
T	0	1	0	1	1	2	3	2	1_	1	1	0	0
C	0	0	0	0	2	1	2	2	1	2	1	2	1
G	0	0	0	0	1	1	1	1	1	1	3	2	1
C	0	0	0	0	1	0	0	0	0	2	2 {	4	3
A	0	0	1	0	0	0	0	1	1_	1	1	3	3

- BLAST is used for sequence similarity search, and much faster than Smith-Waterman method
- Compare a query sequence against a database of sequences.
- BLAST is a collection of algorithms
 - BLASTN: nucleotide sequence against nucleotide database
 - BLASTP: protein sequence against protein database
 - BLASTX: translated nucleotide sequence against protein database
 - TBLASTX: six-frame translations of a nucleotide query sequence against the six-frame translations of a nucleotide sequence database
 - TBLASTN: protein sequence against translated nucleotide databases

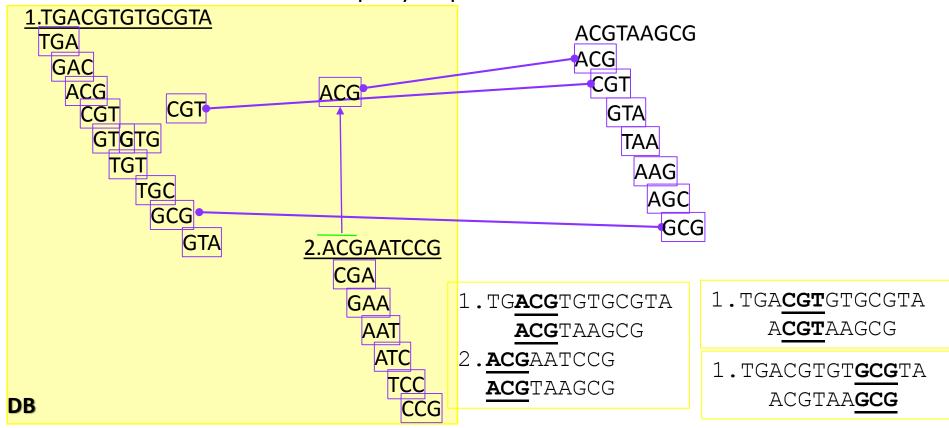
- Process: The seed-index-map-extend-merge strategy
 - Seed and index:
 - Construct common words (k-mers) for sequences in a database
 - Assume the database has two sequences and k=3
 - 1. TGACGTGTGCGTA
 - 2. ACGAATCCG

- Assume all 3-mers are high-score words
 - BLAST needs a threshold to determine high-score words.

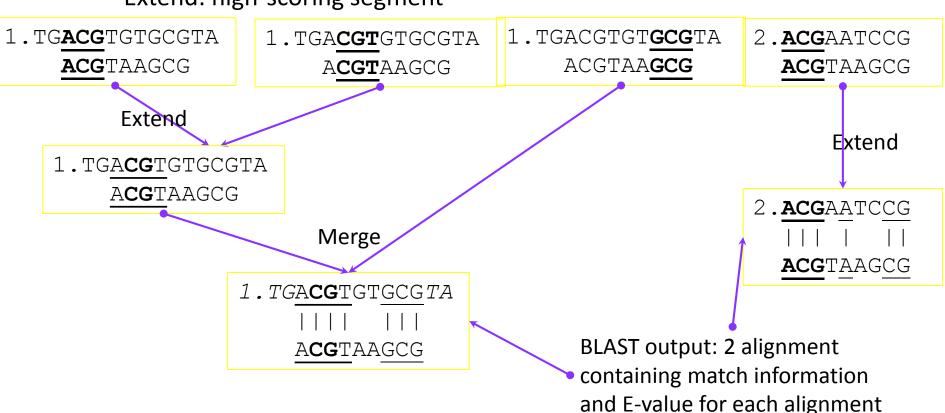


- Process: The seed-index-map-extend-merge strategy
 - Seed-map with high-score words

Obtain words from a query sequence



- Process: The seed-index-map-extend-merge strategy
 - Extend-merge
 - Extend: high-scoring segment



Statistical significance of alignment

- How to assess the significance of a high-scoring hit to the database?
 - E is the number of alignments expected by chance during a database search
 - E is a function of the size of the search space (mn), the normalized score (λ S), and a constant (K).
- Karlin-Altschul equation: $E = Kmne^{-\lambda S}$
 - Score (S) from scoring matrix
 - K and λ are two constants
 - *m*: the length of a query sequence
 - n: the sum of bases of all sequences in database
 - The lower E value indicates more significant alignment.

Statistical significance of alignment

- How to assess the P-value of finding a high-scoring pair (HSP)?
 - The number of random HSPs with score >= S is described by a Poisson distribution
 - the probability of finding exactly k HSPs with score >=S is given by $e^{-E} * E^k/k!$
 - Specifically the chance of finding zero HSPs with score >=S is e^{-E}, so the probability of finding at least one such HSP is P=1-e^{-E}
 - Conversely, $E = -\ln(1 P)$
 - When E and P are very small, they are almost identical

Bowtie/BWA

- Ultrafast, memory-efficient alignment programs for aligning short DNA sequence reads to large genome
- Burrows–Wheeler transform (BWT)
 - Invented by Burrows and Wheeler, 1994
 - Is a block-sorting compression algorithm for many repeated characters
 - BWA and Bowtie are the most famous implementations of BWT in sequence alignment

Burrows–Wheeler transform (BWT)

- BWT is an invertible transformation of a string S of length n into another string S' of length n
- BWT can organize the genome string into a sequence of suffixes of the original genome string
- Given a string S, BWT
 - Add \$ and assume \$<any alphabet
 - Obtains a suffix array of all cyclic rotations
 - Transform into a new string S'

- Given a string S = "TCATC", BWT
 - Adds \$ and assume \$<any alphabet
 - Obtains a suffix array of all cyclic rotations

Transformation								
1. Input	2. Cyclic rotations	3. Sorting	4. Last column	5. BWT output				
TCATC\$								

- Cyclic rotation:
 - Obtains a suffix array of all cyclic rotations
 - Keeps an index of the rotated strings in the array
 - Creates Circular Permutation Table (CPT)

Transformation								
1. Input	2. Cyclic rotations	3. Sorting	4. Last column	5. BWT output				
TCATC\$	0 TCATC\$ 1 CATC\$T 2 ATC\$TC 3 TC\$TCA 4 C\$TCAT 5 \$TCATC							

- Sorting:
 - Sorts the Circular Permutation Table (CPT) alphabetically
 - Keep the index with the strings

Transformation								
1. Input	2. Cyclic rotations	3. Sorting	4. Last column	5. BWT output				
TCATC\$	0 TCATC\$ 1 CATC\$T 2 ATC\$TC 3 TC\$TCA 4 C\$TCAT 5 \$TCATC	5 \$TCATC 2 ATC\$TC 4 C\$TCAT 1 CATC\$T 3 TC\$TCA 0 TCATC\$						

Taking the last column from the sorted array

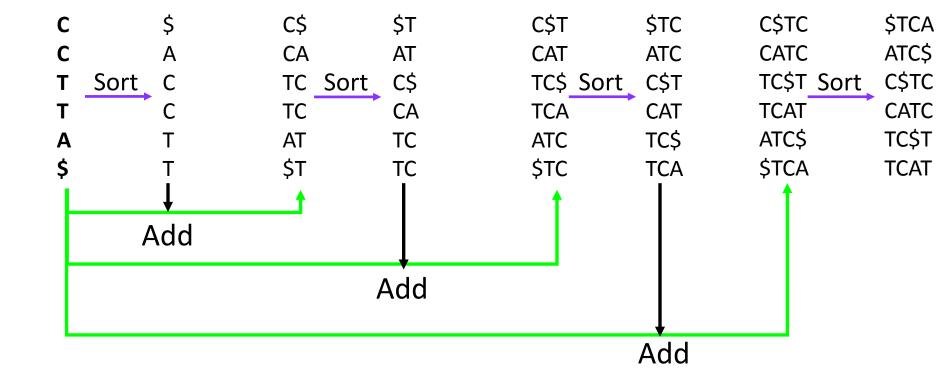
Transformation								
1. Input	2. Cyclic rotations	3. Sorting	4. Last column	5. BWT output				
TCATC\$	0 TCATC\$ 1 CATC\$T 2 ATC\$TC 3 TC\$TCA 4 C\$TCAT 5 \$TCATC	5 \$TCATC 2 ATC\$TC 4 C\$TCAT 1 CATC\$T 3 TC\$TCA 0 TCATC\$	5 \$TCATC 2 ATC\$TC 4 C\$TCAT 1 CATC\$T 3 TC\$TCA 0 TCATC\$					

- BWT output:
 - The last column represents the transformed string

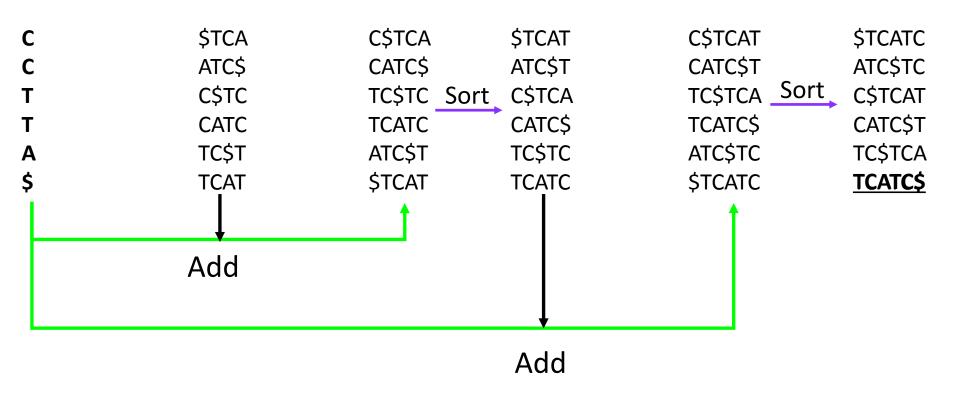
Transformation							
1. Input	2. Cyclic rotations	3. Sorting	4. Last column	5. BWT output			
TCATC\$	0 TCATC\$ 1 CATC\$T 2 ATC\$TC 3 TC\$TCA 4 C\$TCAT 5 \$TCATC	5 \$TCATC 2 ATC\$TC 4 C\$TCAT 1 CATC\$T 3 TC\$TCA 0 TCATC\$	5 \$TCATC 2 ATC\$TC 4 C\$TCAT 1 CATC\$T 3 TC\$TCA 0 TCATC\$	CCTTA\$			

BWT reverse transformation

- Transform back to the original string
 - With a suffix array, it is easy to recover the original string S
 - Input: CCTTA\$ for TCATC\$

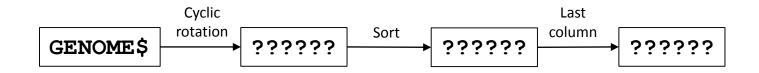


BWT reverse transformation



What's the BWT for GENOME?

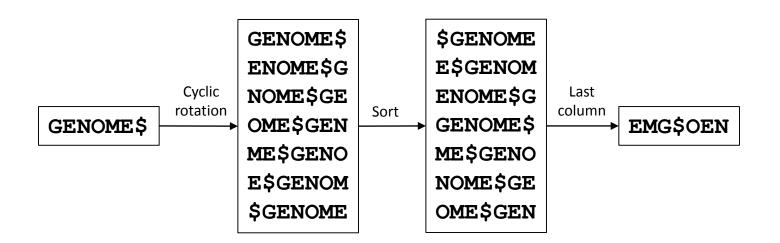
BWT (GENOME\$) =
$$?$$



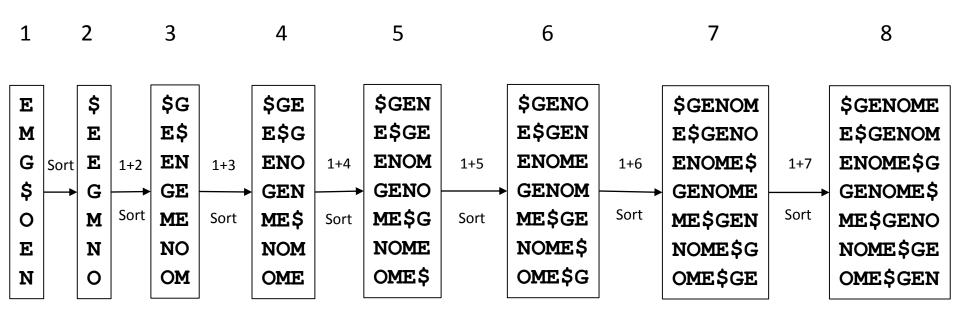
After class exercise: reproduce the BWT transformation above

What's the BWT for GENOME?

BWT (GENOME\$) = EMG\$OEN



BWT reverse transformation



After class exercise: reproduce the reverse transformation above

- Match process:
 - Given a query string, we want to find where is the matched sub-string in original string: TCATC\$
 - We do this search through the use of LF functions on the BWT of the original string
 - ៤₹ (last to first) functions:
 - Purpose: find the same base in the first column corresponding to a specific base in the last column of BWT matrix

LF property

- LF is a function mapping from the last column of the BWT matrix to the first column
- The ith occurrence of the character X in the last column of BWT matrix corresponds to the ith occurrence of X in the first column.

• Examples:

- The 1st occurrence of C in the last column is the same C as the 1st occurrence of C in the first column
- The 2nd occurrence of T in the last column is the same T as the 2nd occurrence of T in the first column

\$TCATC ATC\$TC C\$TCAT CATC\$T TC\$TCA TCATC\$

LF calculation

- LF (pos, na) = C(na) + prg_na(pos, na)
 - pos: position in the output CCTTA\$
 - na: a base
 - C(na): the number of bases smaller than na in BWT first column
 - prg_na(pos, na): the number of base na before the position of pos (not included).
- For TCATC (see right side), the $\mathbb{C}()$ for \$, A, C, T are 0, 1, 2, 4, respectively. This is pre-computed.
- For example, ៤f (3, 'T')
 - C(T') = 4, $prg_na(3, T') = 1$
 - Then: $\mathbb{L}f(3, T') = 4+1 = 5$
 - The two underlined T in bold (one in the last column and one in the first column) as the same T in the original string.

 \underline{T} in the last column pos =3 is the same \underline{T} in first column pos =5

Now, we can do the exercise on the C in the last column pos = 1

- 0 \$TCATC
- 1 ATC\$TC
- 2 C\$TCAT
- 3 CATC\$**T**
- 4 TC\$TCA
- 5 **T**CATC\$

How LF recovers original string

 Suppose we only know first/last column of BWT, what is the original string?

\$????E

E33333W

E????G

G????\$

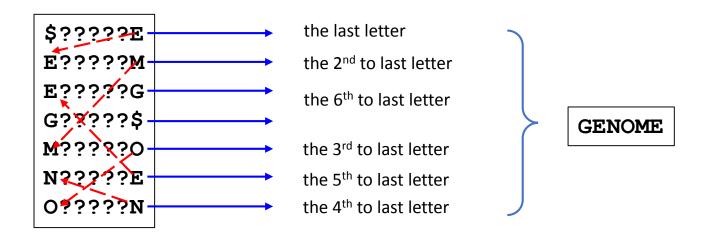
W333330

N?????E

O33333N

How LF recovers original string

 Suppose we only know first/last column of BWT, what is the original string?



- Purpose: search a specific pattern (query) in the BWT matrix, and recover the index in original database sequence
 - Example: search "AT" within the database sequence "TCATC" (the index of "AT" is 2)

```
0 1 2 3 4 5
T C A T C $
```

- Next we define the lower and upper bound of search recursively (from last to first base of query)
 - L(W): lowest index in BWT matrix where W is prefix
 - U(W): highest index in BWT matrix where W is prefix
 - The L() and U() for A, C, G, T can be pre-calculated from the BWT matrix
 - For a new prefix p in front of W, we will have:
 - L(pW) = Lof (L(W), p)
 - U(pW) = LF(U(W)+1, p)-1

- Goal:
 - Original string: TCATC\$; BWT: CCTTA\$
 - Query: AT (find it in original string using BWT matrix)

\$TCATC

ATC\$TC

C\$TCAT

CATC\$T

TC\$TCA

TCATC\$

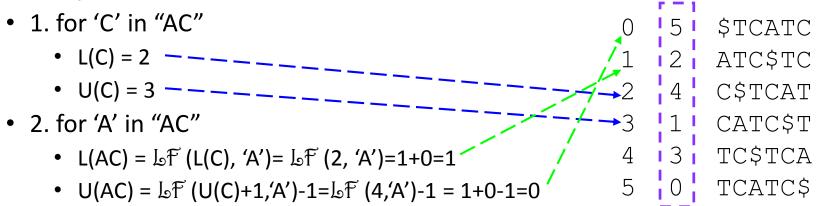
- Search procedure:
 - 1. for 'T' in "AT"
 - L(T) = 4
 - U(T) = 5
 - 2. for 'A' in "AT"
 - L(AT) = ៤₹ (L(T),'A')=៤₹ (4, 'A')=1+0=1
 - U(AT) = ៤₹ (U(T)+1,'A')-1= ៤₹ (6,'A')-1=1+1-1=1
 - The matched row is: 1
 - The index in original string is 2

- Goal:
 - Original string: TCATC\$; BWT: CCTTA\$
 - Query: TC (find it in original string using BWT matrix)
- Search procedure:

 - The matched row is: 4 and 5.
 - The index in original string is 0 and 3.

```
0 1 2 3 4 5
T C A T C $
```

- Goal:
 - Original string: TCATC\$; BWT: CCTTA\$
 - Query: AC (find it in original string using BWT matrix)
- Search procedure:



- The matched row is None.
 - "AC" is not in "TCATC"

- Goal:
 - Original string: TCATC\$; BWT: CCTTA\$
 - Query: ATC (find it in original string using BWT matrix)
- Search procedure:
 - 1. for 'C' in "ATC"
 - L(C) = 2
 - U(C) = 3 -
 - 2. for 'T' in "ATC"
 - L(TC) = ៤f (L(C), 'T')=៤f (2,'T')=4+0=4
 - U(TC) = LF (U(C)+1,'T')-1=LF (4,'T')-1=4+2-1=5 4
 - 3. for "A" in "ATC"
 - L(ATC) = L₹ (4, 'A') = 1 + 0 = 1*
 - U(ATC) = LF (6, 'A')-1 =1+1-1 = 1
 - The matched row is 1
 - The original index is 2
- 0 1 2 3 4 5 T C A T C \$

\$TCATC

ATC\$TC

C\$TCAT

CATC\$T

TC\$TCA

TCATC\$

- Fast and accurate aligner for whole genome sequencing data against a reference genome
 - Can work with both short reads and noisy long reads
 - A typical seed-chain-alignment strategy
 - 1. Collect minimizers of reference sequence
 - 2. Index in a hash table
 - 3. Get minimizers from query sequences
 - 4. Find exact match as anchors
 - 5. Find collinear anchors
 - 6. Extend or close gaps by dynamic programming

- K-mer based sequence similarity
 - BLAST:
 - Get k-mer, generate hash value and store in a hash table
 - Find k-mer match between reference sequence and query sequence
 - DALIGNER(Myers. WABI 2014; 8701:52-67):
 - Generate k-mer for each of two sets of reads
 - Sort k-mers and merge them for potential match
 - MHAP(Berlin et al. Nat. Biotechnol. 2015;33:623-630):
 - m k-mer hash functions
 - For each hash functions, find minimum hash value for all k-mers in a sequence
 - Two sequences are similar to each other if they have many overlaps of minimum hash value
- Minimap used hash functions, hash table, and sorting

The concept of minimizer

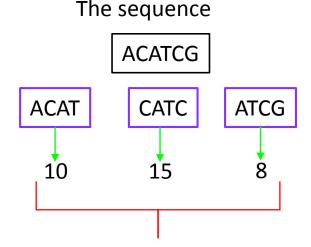
- Chooses a representative k-mer from a group of adjacent k-mers, so different strings Ti and Tj choose the same representative if they share a long enough subsequence.
- Only a small fraction of k-mers, called 'minimizers', needs to be stored.

Position	1	2	3	4	5	6	7	1	2	3	4	5	6	7	8	9	10	11	12
Sequence	2	3	1	0	3	4	3	4	2	6	4	7	2	8	1	4	7	5	1
k-mers	2	3	1					4	2	6	4	7	2	8					
with		3	1	0					2	6	4	7	2	8	1				
minimizer			1	0	3					6	4	7	2	8	1	4			
in				0	3	4					4	7	2	8	1	4	7		
bold					3	4	3					7	2	8	1	4	7	5	
	(a)							(b)					2	8	1	4	7	5	1

- 1. Collect minimizers of reference sequence
 - Minimizer:
 - A smallest k-mer of w consecutive k-mers in a sequence with w+k bases
 - Minimap2: *k*=15 and *w*=5
 - Example:
 - Assume *w*=3 and *k*=4

three k-mer (4-mer)

hash value

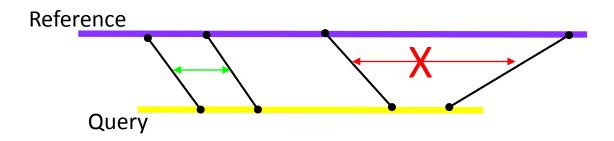


The minimizer of ACATCG is 8

- Given a sequence with >w+k bases
 - A set of minimizers were generated

- 2. Index in a hash table
 - Key: a hash value of a minimizer
 - Values: list of locations of minimizer in the reference genome
- 3. Get minimizers from query sequences
 - Used the same hash function to obtain a set of minimizers for query sequence
- 4. Find exact match as anchors
 - Match minimizers between reference and query sequence
 - The matched sub-sequence of reference and subsequence of query: anchors

- 5. Find collinear anchors
 - Two anchors are collinear
 - Their distance in a sequence is less than a threshold.
 - Forward and reverse strands are considered individually
 - Cluster close anchors.



 6. Extend or close gaps between anchors by dynamic programming