Pattern Recognition Report3 Chapter3

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1 Question1

In my program of this question, function u1.m compute question(a), u2.m for question(b), u3.m for question(c), u4.m for question(d).

1.1 (a)

According to the maximum likelihood estimation on the Gaussian distribution, we can get :

$$\hat{\mu} = \frac{1}{N} \sigma_{k=1} N x_k \tag{1}$$

$$\hat{\Sigma} = \frac{1}{N} \sum_{k=1}^{N} (x_k - \hat{\mu})(x_k - \hat{\mu})^T$$
(2)

In terms of (1) and (2), we could compute the value of the parameters by the program . The results are as follows:

| feature | $\hat{\mu}$ | $\hat{\sigma}^2$ |
|---------|-------------|------------------|
| x_1 | -0.0709 | 0.9062 |
| x_2 | -0.6047 | 4.2007 |
| x_3 | -0.9110 | 4.5419 |

1.2 (b)

Similar with (1) and (2), we can get the results as follows:

$$\begin{array}{lll} \mu_{12} = (-0.0709, -0.6047)^T & \Sigma_{12} = & \begin{array}{ll} 0.9062 & 0.5678 \\ 0.5678 & 4.2007 \end{array} \\ \mu_{23} = (-0.6047, -0.9110)^T & \Sigma_{23} = & \begin{array}{ll} 4.2007 & 0.7337 \\ 0.7337 & 44.5419 \end{array} \\ \mu_{13} = (-0.0709, -0.9110)^T & \Sigma_{13} = & \begin{array}{ll} 0.9062 & 0.3941 \\ 0.3941 & 4.5419 \end{array} \end{array}$$

1.3 (c)

According to (1) and (2), we get the results as follows:

$$\mu = (-0.0709, -0.6047, -0.9110)^T$$

$$0.9062 \quad 0.5678 \quad -0.9110$$

$$\Sigma = \quad 0.5678 \quad 4.2007 \quad 0.7337$$

4.5419

 $0.3941 \quad 0.7337$

- 1.4 (d)
- 1.5 (e)
- 1.6 (f)