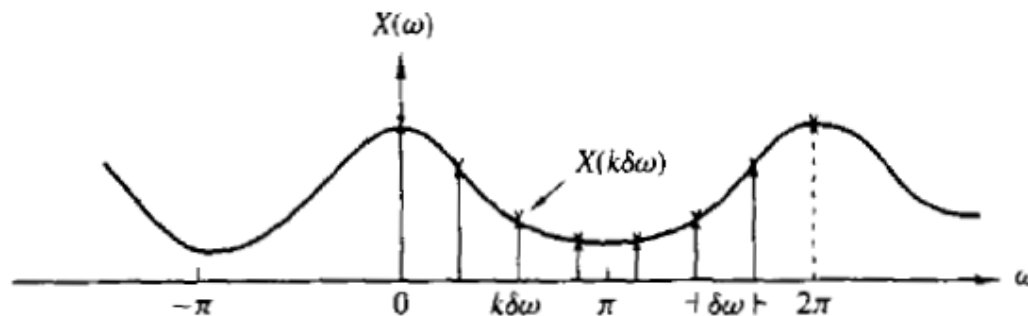


# **The Discrete Fourier Transforms**

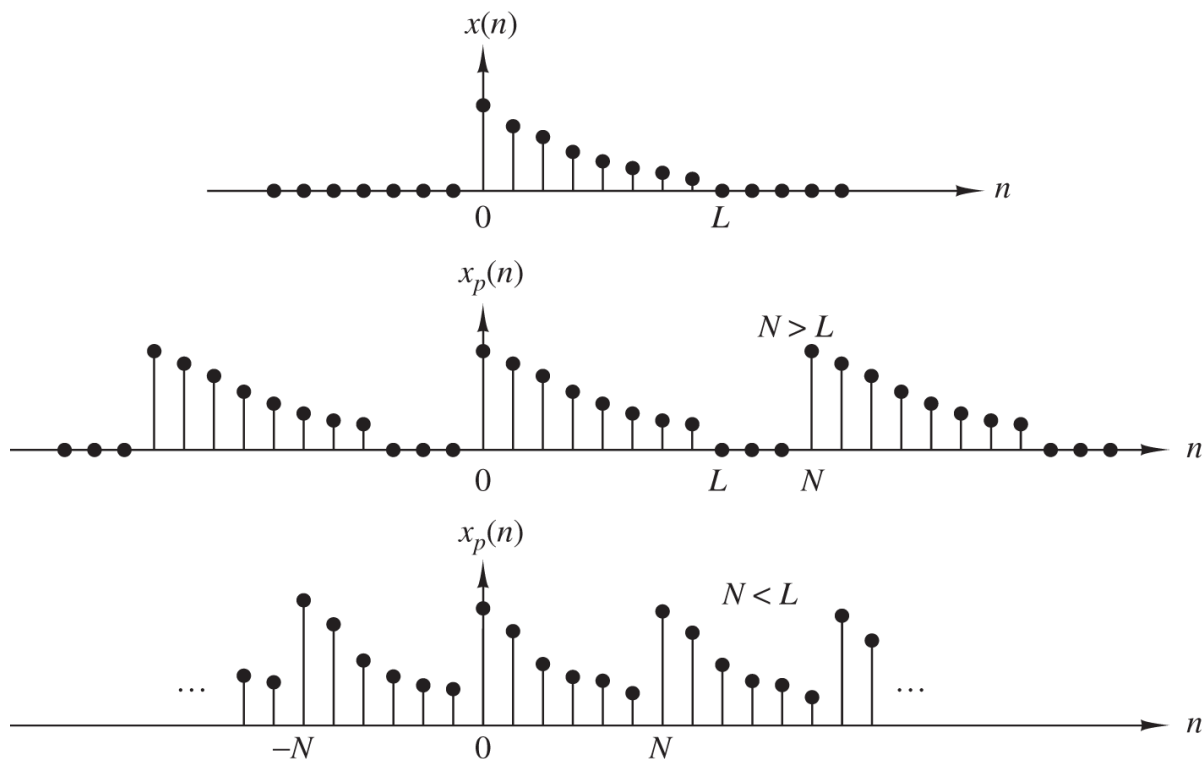
Phan Duy Hùng

What is the objective of DFT ?

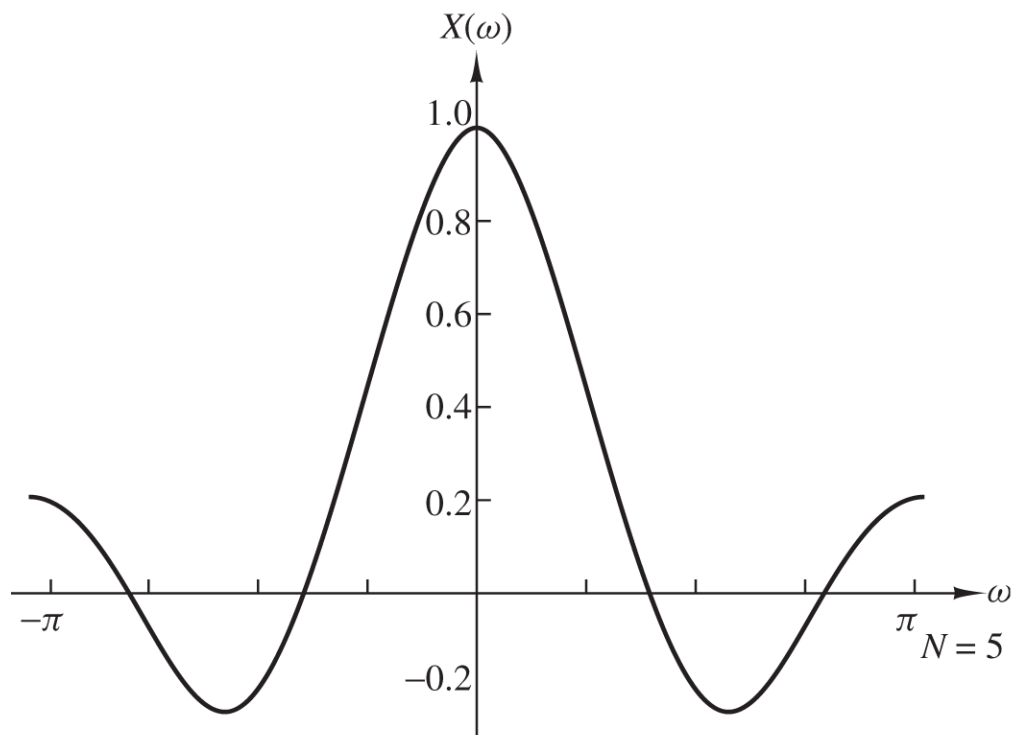
# Frequency-Domain Sampling and Reconstruction of Discrete-Time Signals



**Figure 7.1.1** Frequency-domain sampling of the Fourier transform

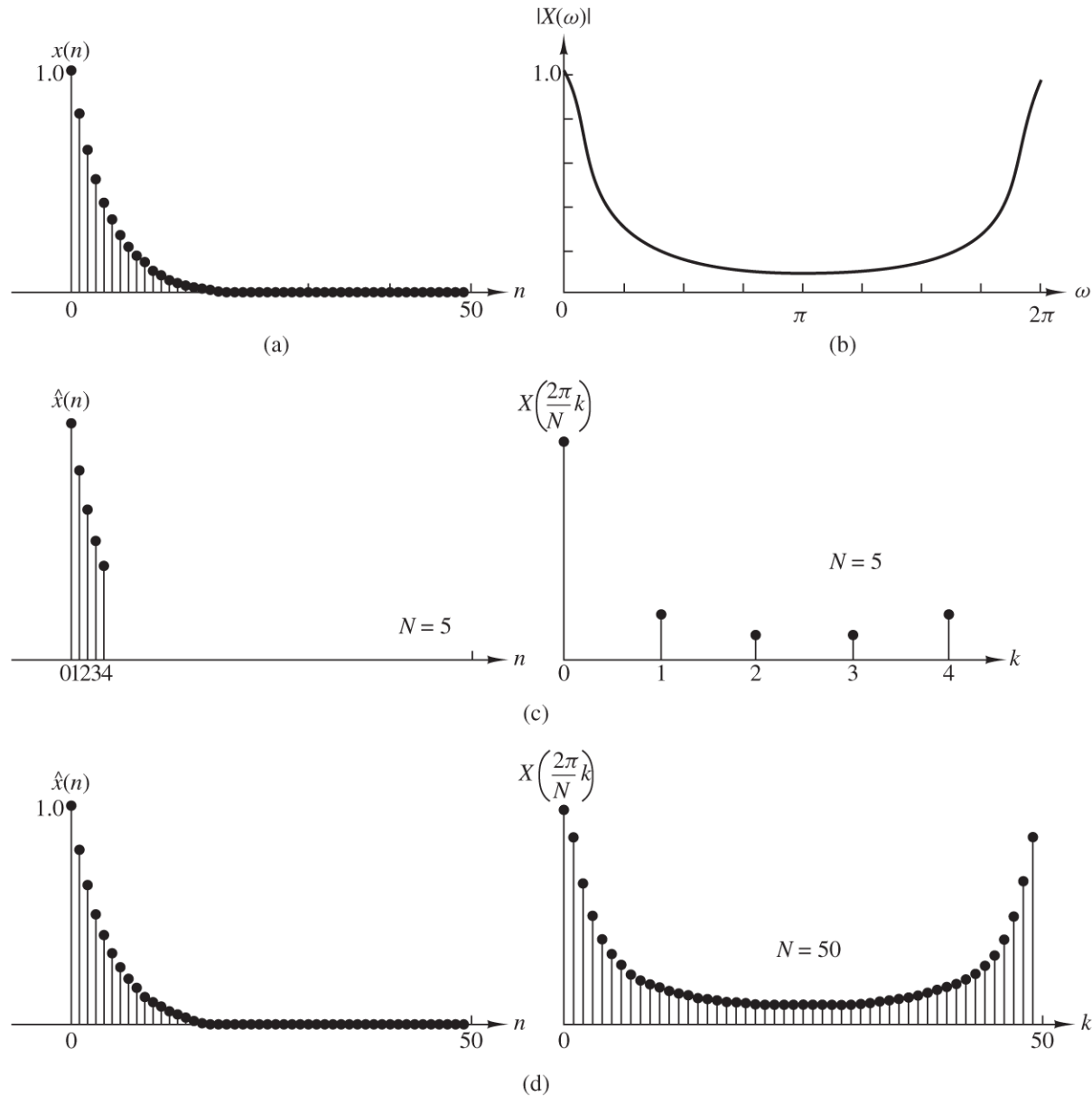


**Figure 7.1.2** Aperiodic sequence  $x(n)$  of length  $L$  and its periodic extension for  $N \geq L$  (no aliasing) and  $N < L$  (aliasing).

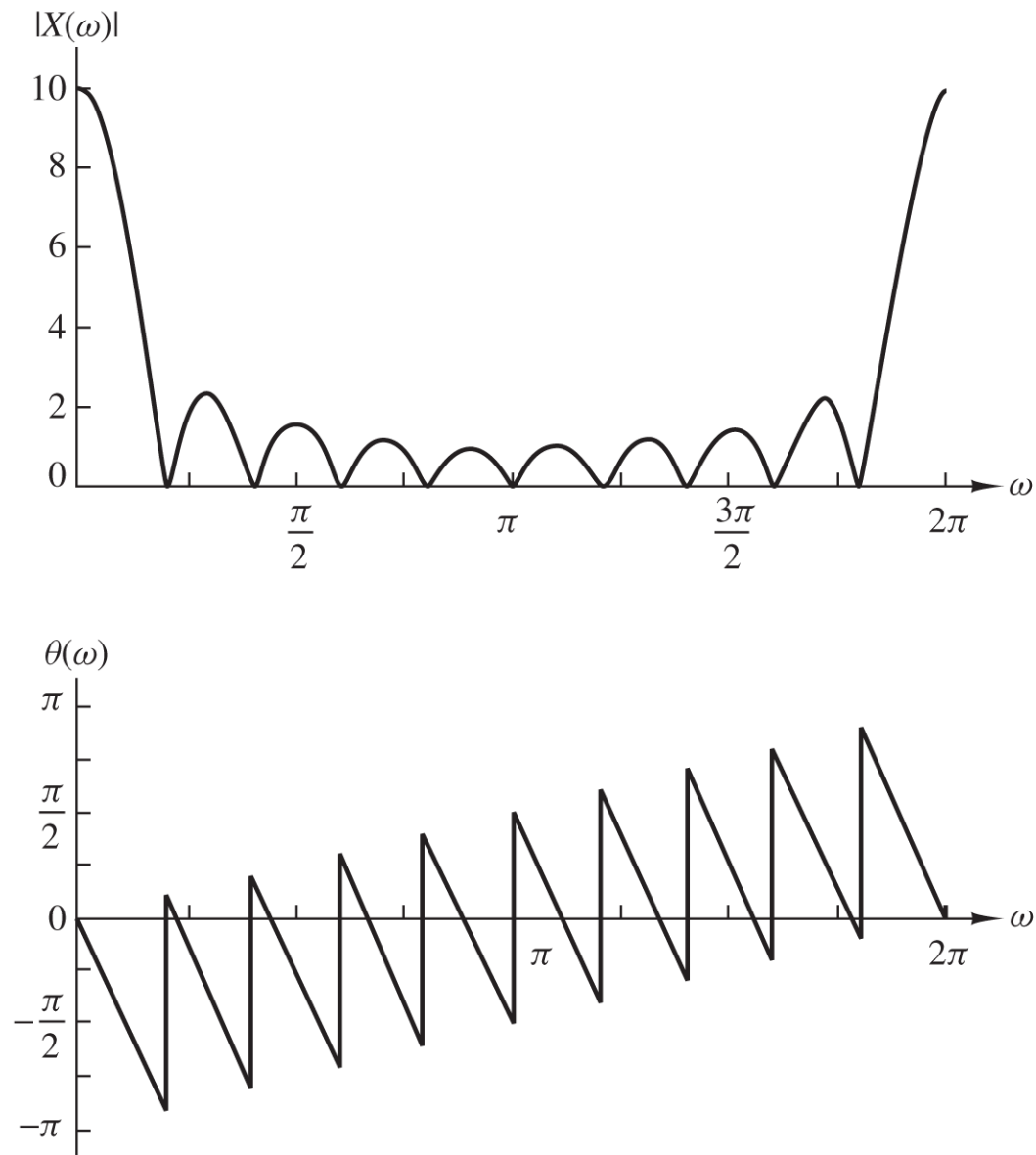


**Figure 7.1.3** Plot of the function  $[\sin(\omega N/2)]/[N \sin(\omega/2)]$ .

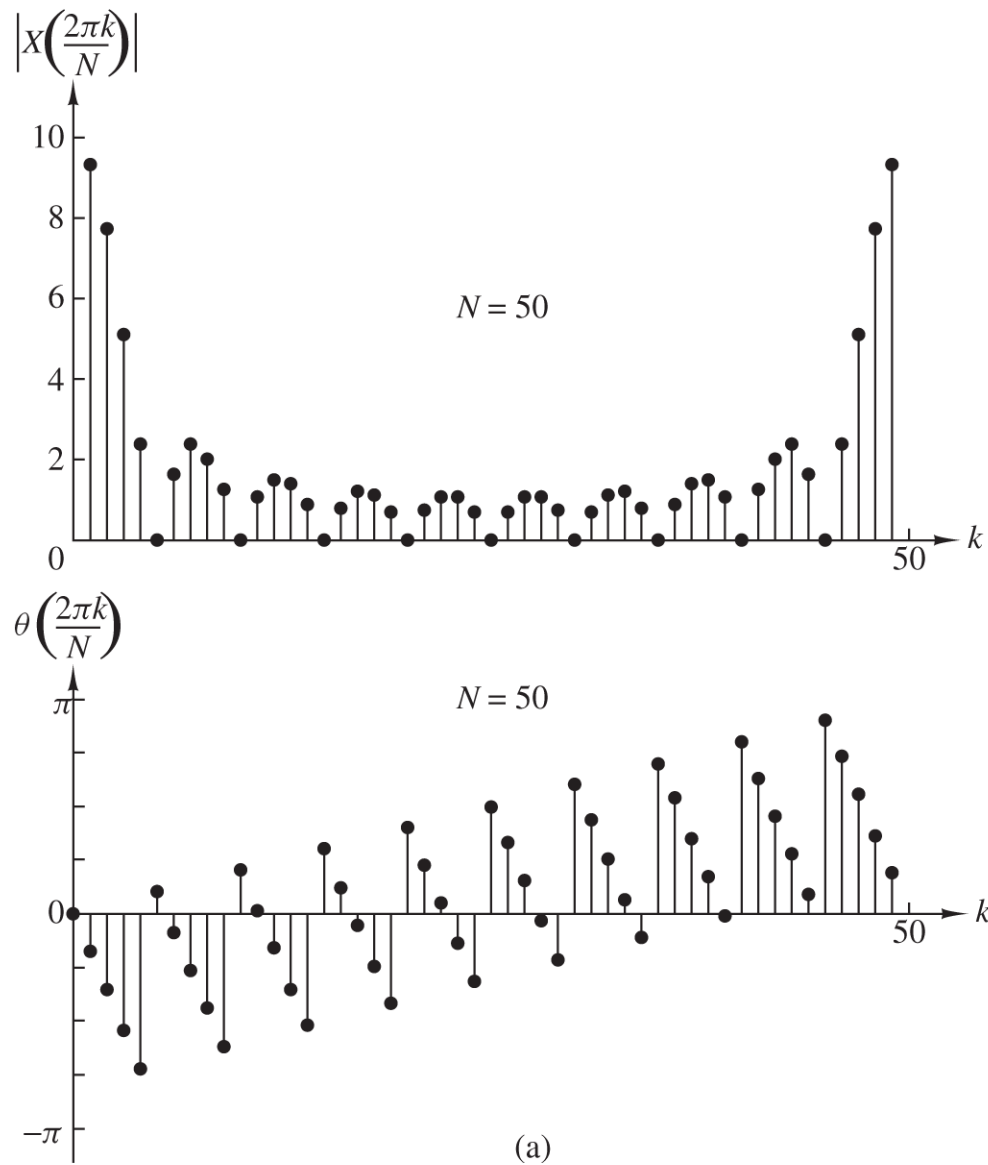
# The Discrete Fourier Transform (DFT)



**Figure 7.1.4** (a) Plot of sequence  $x(n) = (0.8)^n u(n)$ ; (b) its Fourier transform (magnitude only); (c) effect of aliasing with  $N = 5$ ; (d) reduced effect of aliasing with  $N = 50$ .



**Figure 7.1.5** Magnitude and phase characteristics of the Fourier transform for signal in Example 7.1.2.



**Figure 7.1.6** Magnitude and phase of an  $N$ -point DFT in Example 7.1.2;  
 (a)  $L = 10$ ,  $N = 50$ ; (b)  $L = 10$ ,  $N = 100$ .

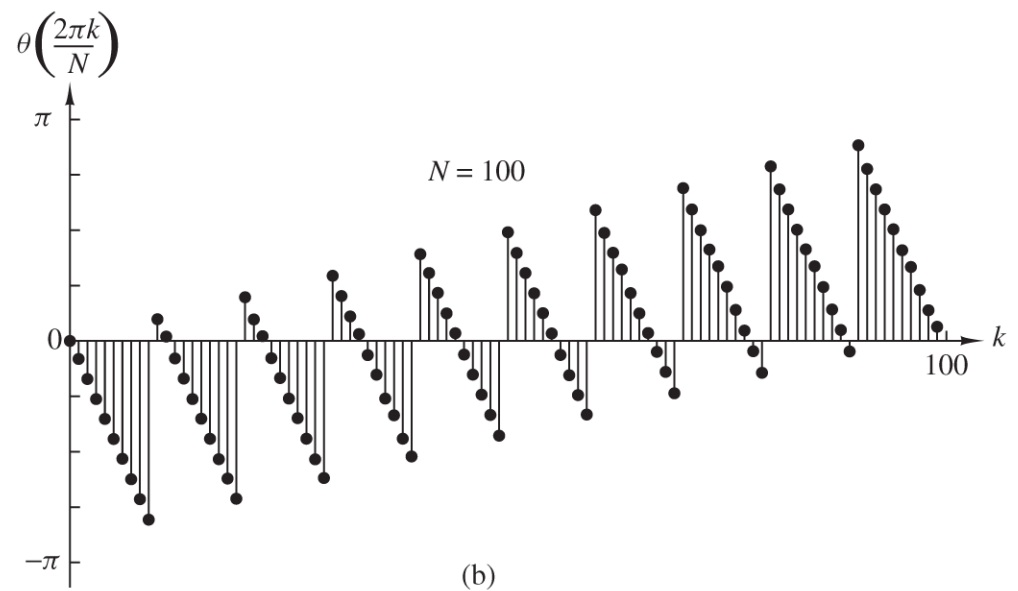
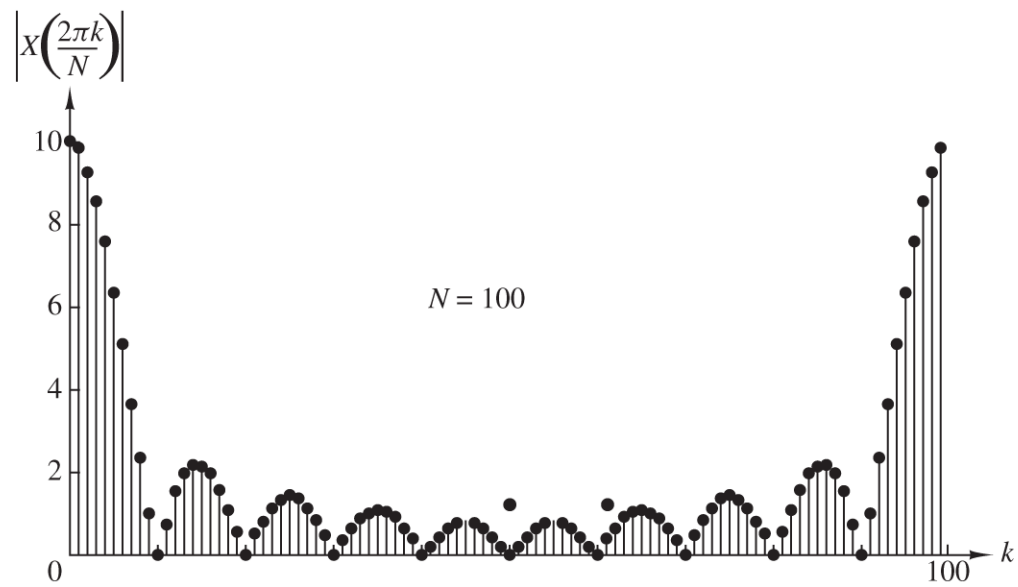
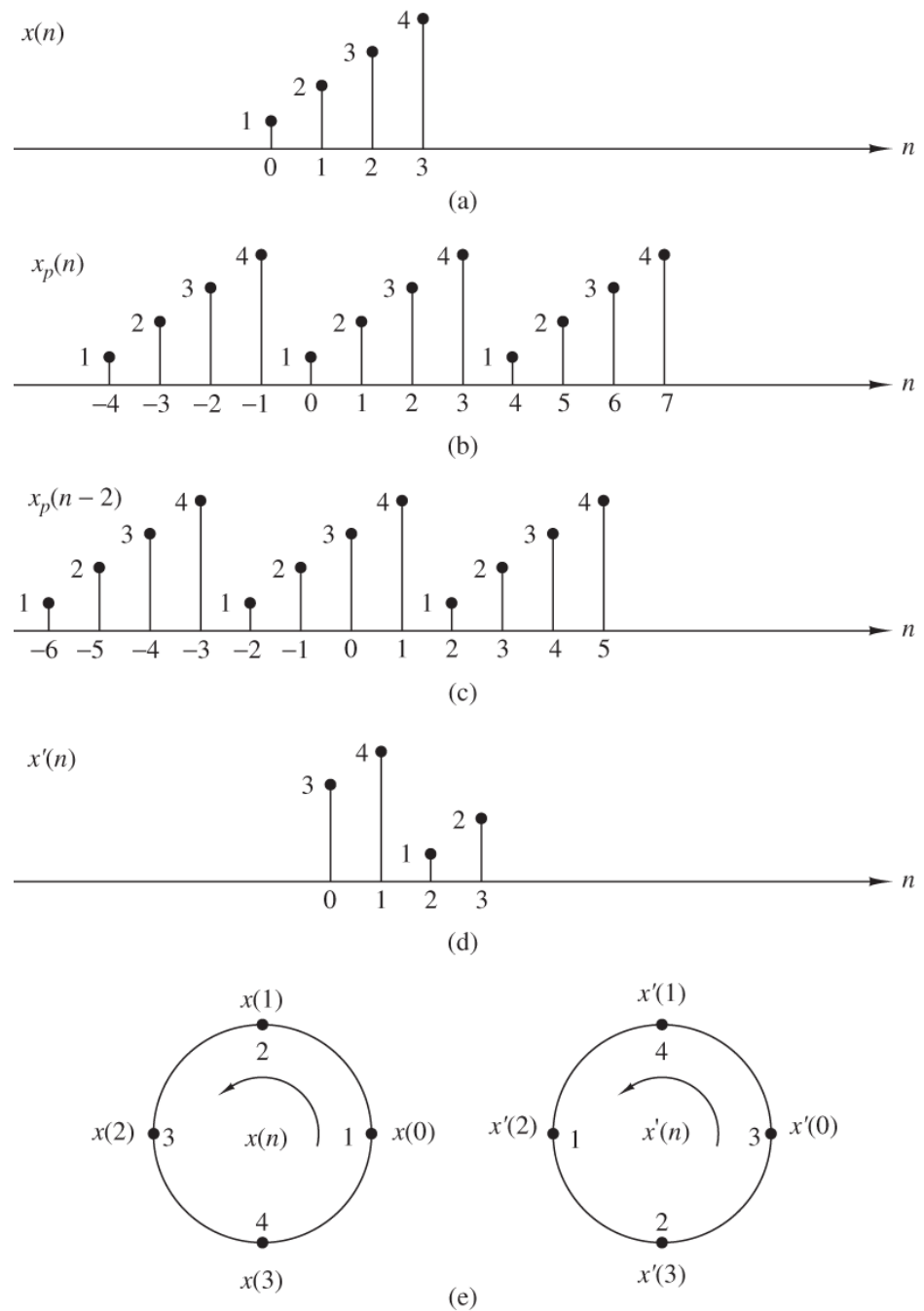


Figure 7.1.6 Figure continued



# Properties of DFT

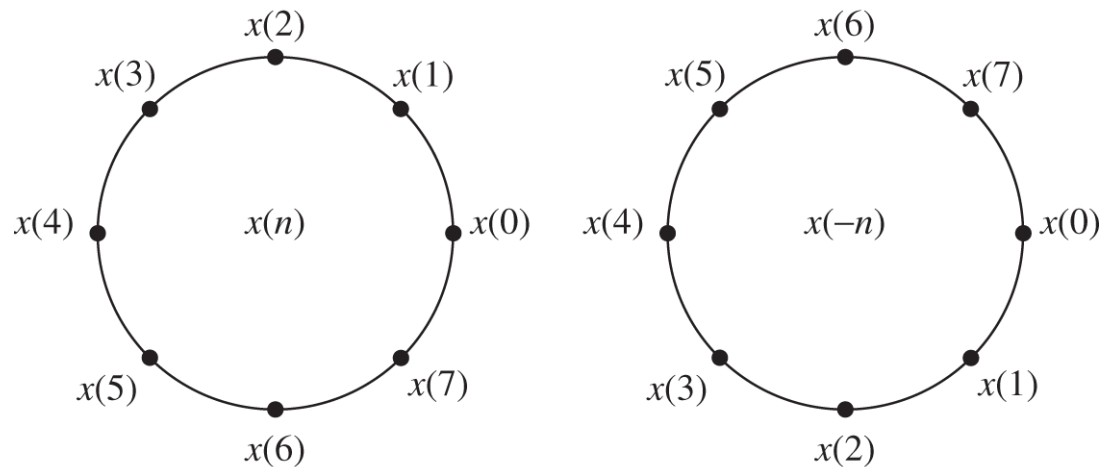
- Periodicity
- Linearity
- Circular Symmetries



**Figure 7.2.1** Circular shift of a sequence.

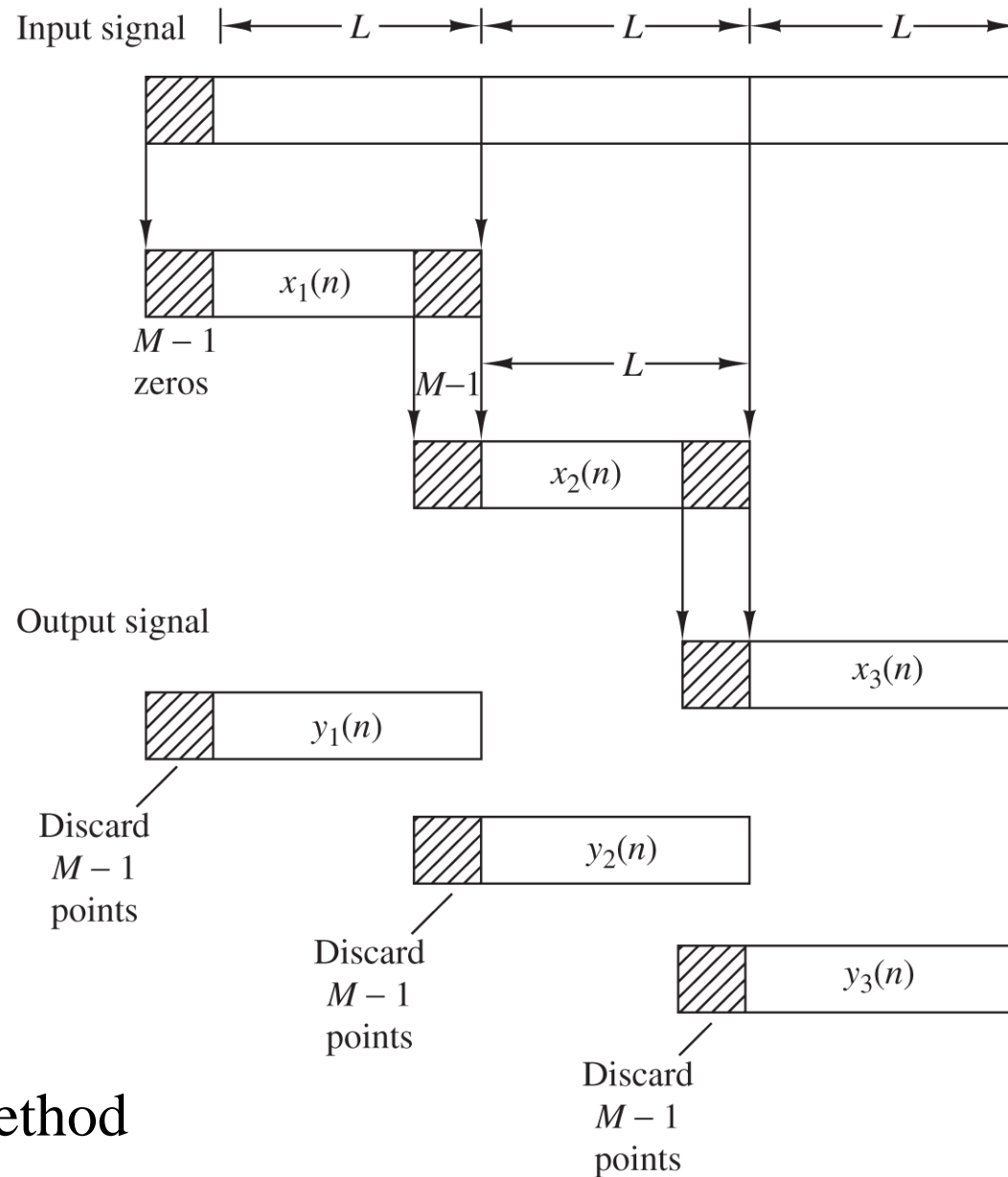
## *Additional DFT Properties*

- Time reversal of a sequence
- Circular time shift of a sequence
- Circular frequency shift
- Complex-conjugate properties
- Circular correlation
- Multiplication of two sequences
- Parseval's Theorem



**Figure 7.2.3** Time reversal of a sequence.

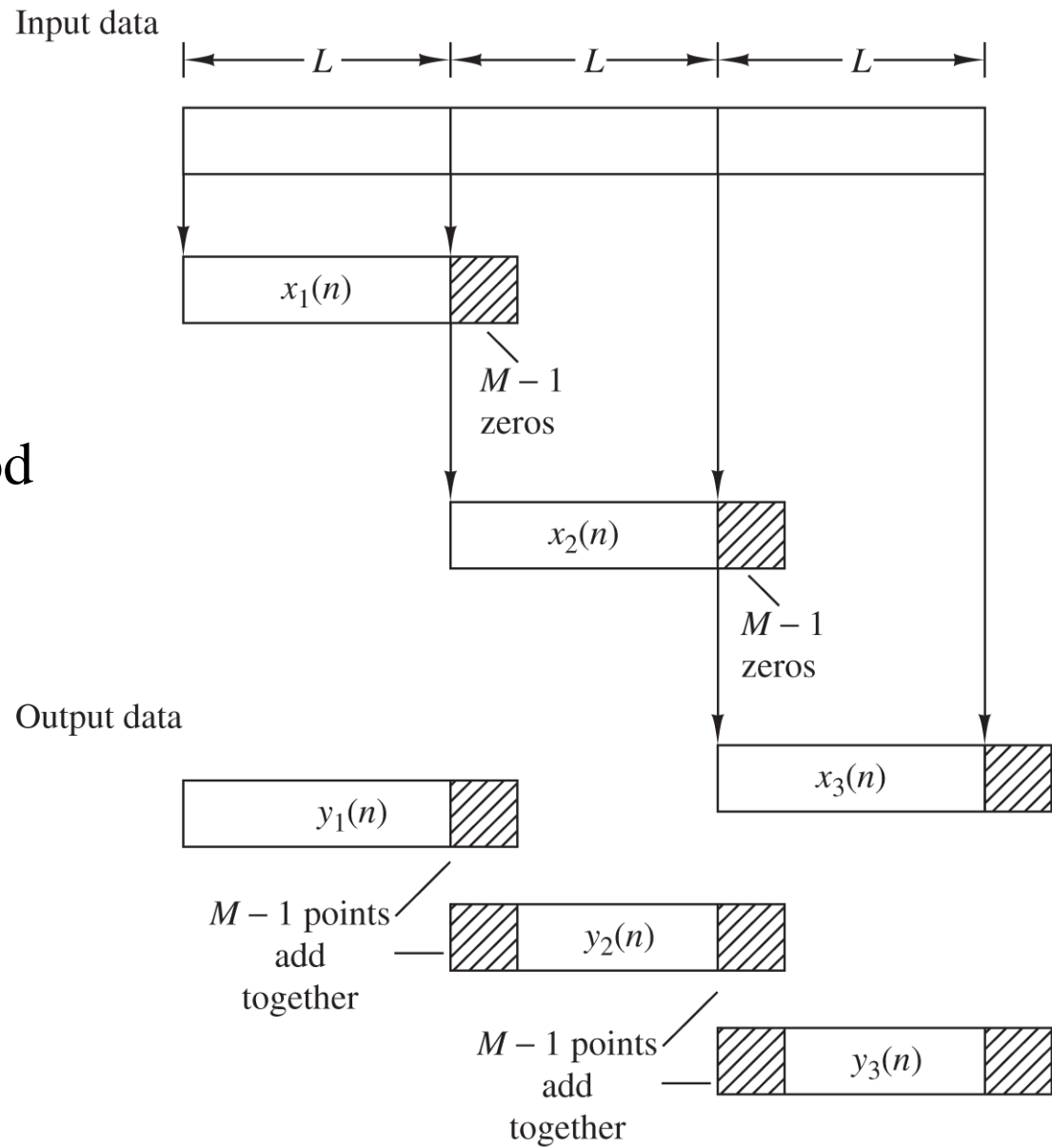
# Filtering of Long Data Sequences



## Overlap-save method

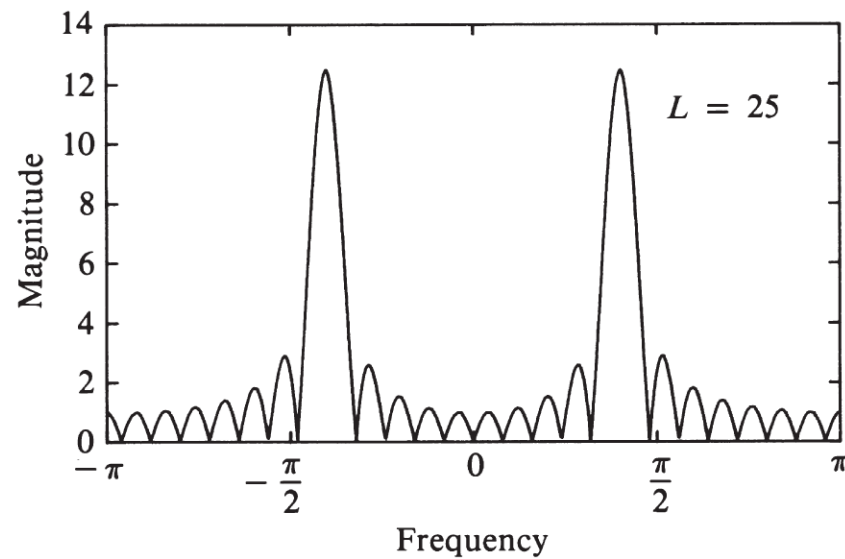
**Figure 7.3.1** Linear FIR filtering by the overlap-save method.

## Overlap-add method

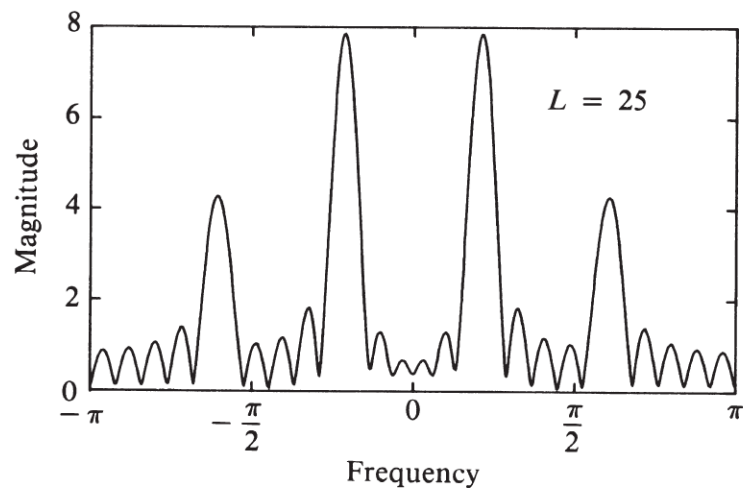


**Figure 7.3.2** Linear FIR filtering by the overlap-add method.

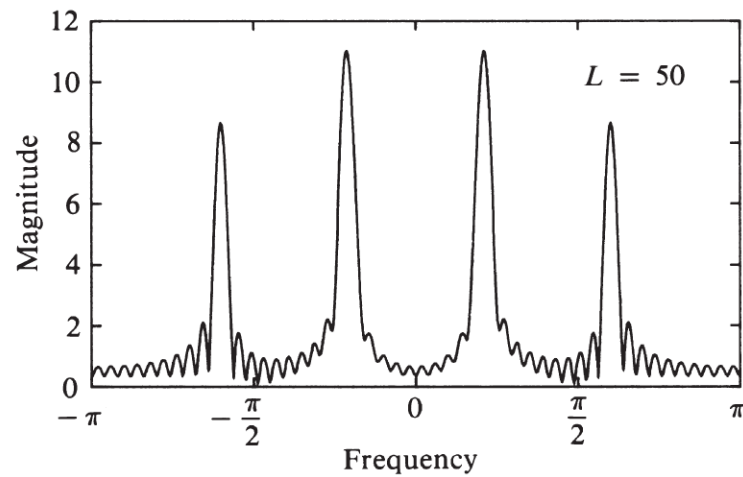
# *Frequency Analysis of Signals Using the DFT*



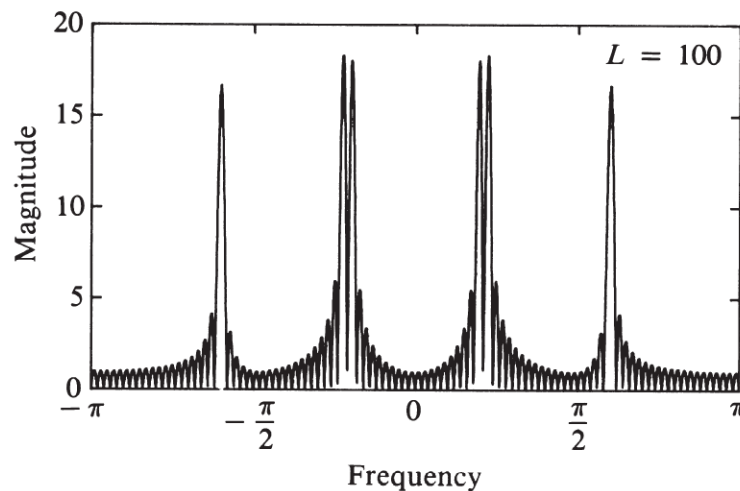
**Figure 7.4.1** Magnitude spectrum for  $L = 25$  and  $N = 2048$ , illustrating the occurrence of leakage.



(a)

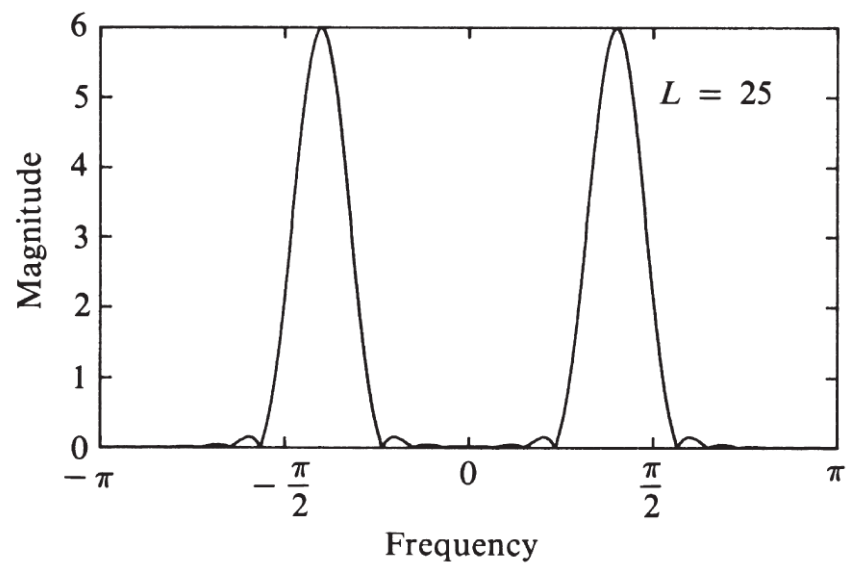


(b)

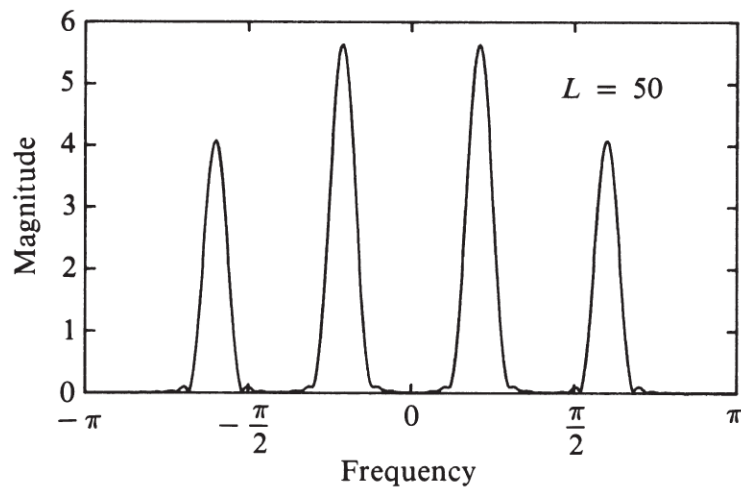


(c)

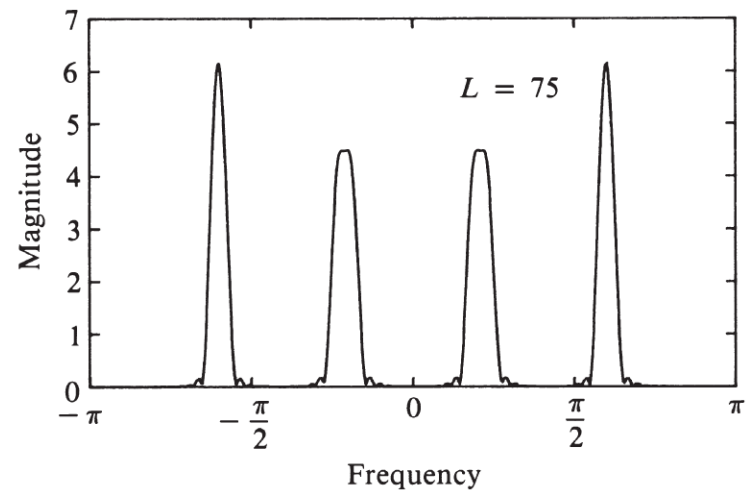
**Figure 7.4.2** Magnitude spectrum for the signal given by (7.4.8), as observed through a rectangular window.



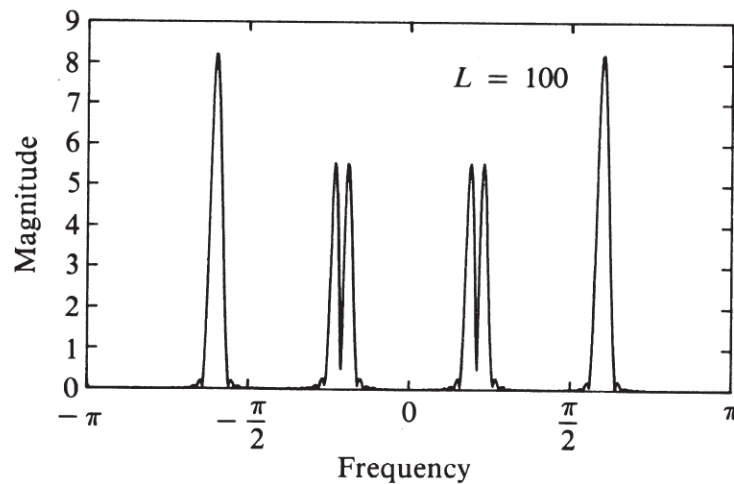
**Figure 7.4.3** Magnitude spectrum of the Hanning window.



(a)



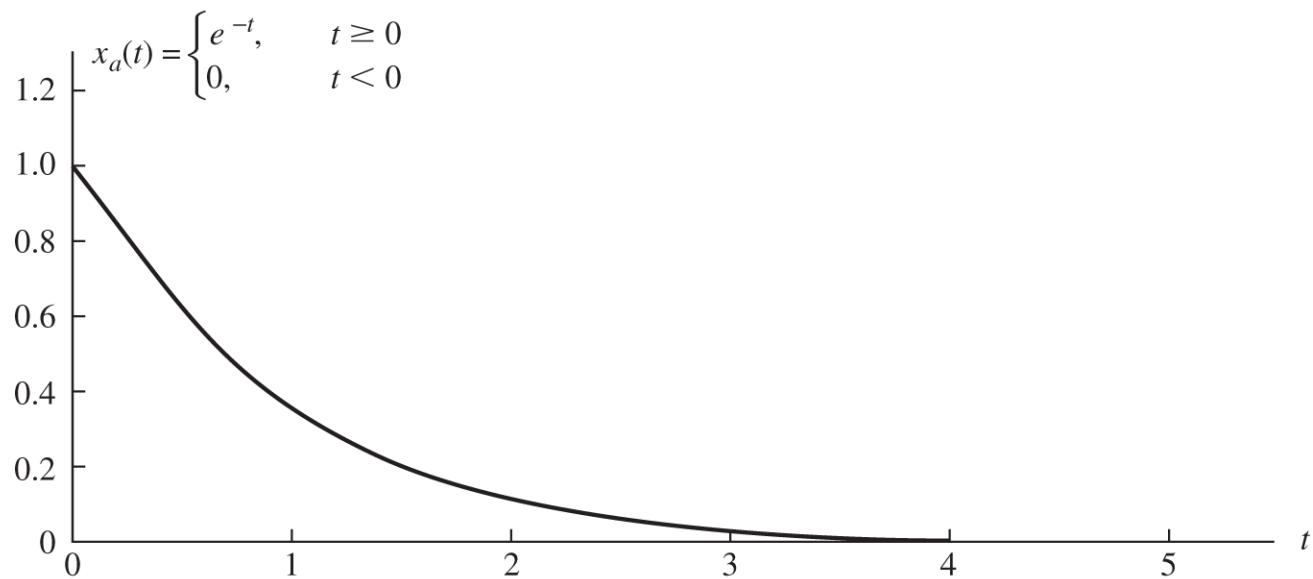
(b)



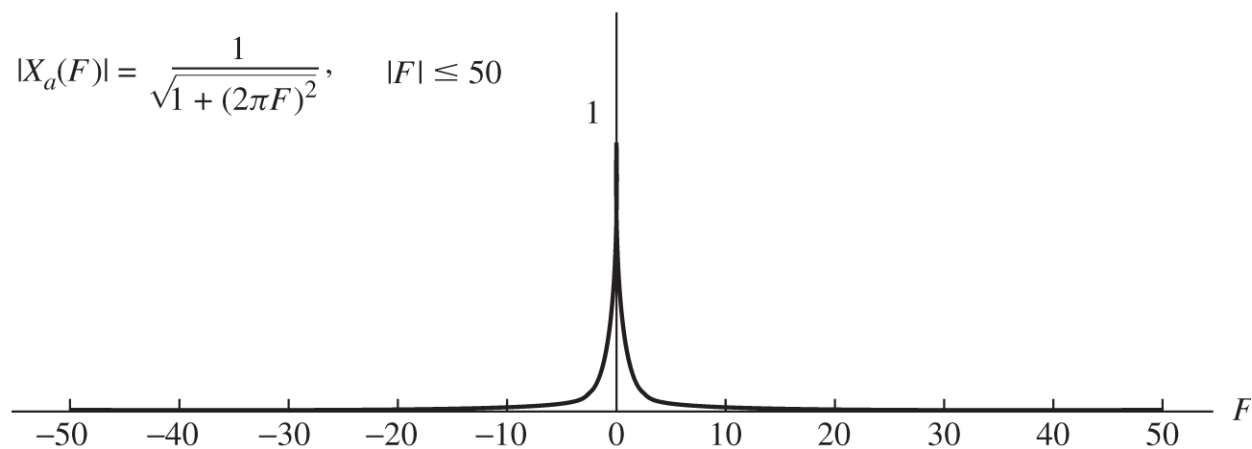
(c)

**Figure 7.4.4** Magnitude spectrum of the signal in (7.4.8) as observed through a Hanning window.



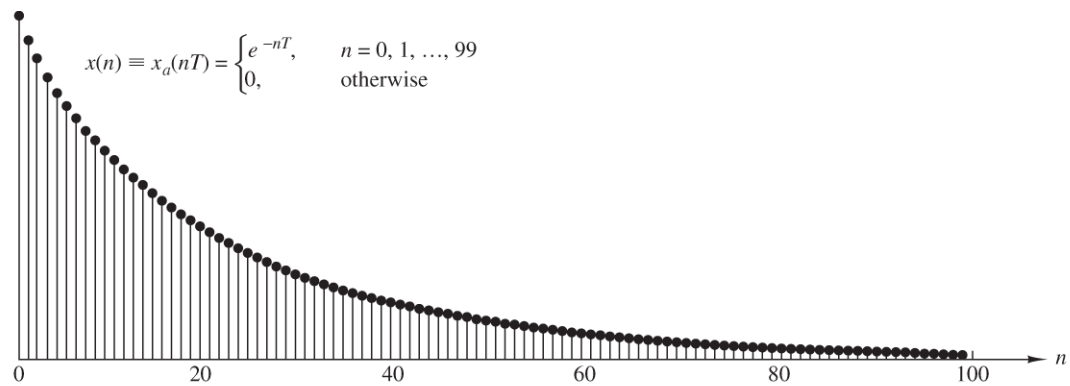


(a)

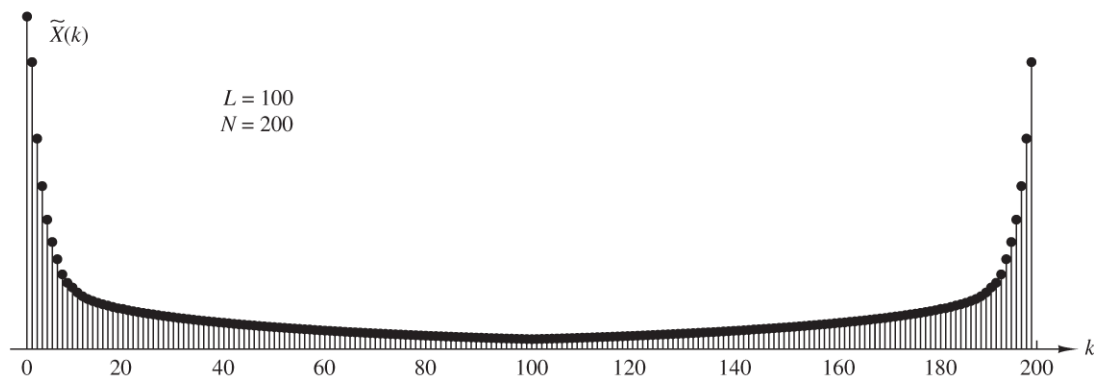


(b)

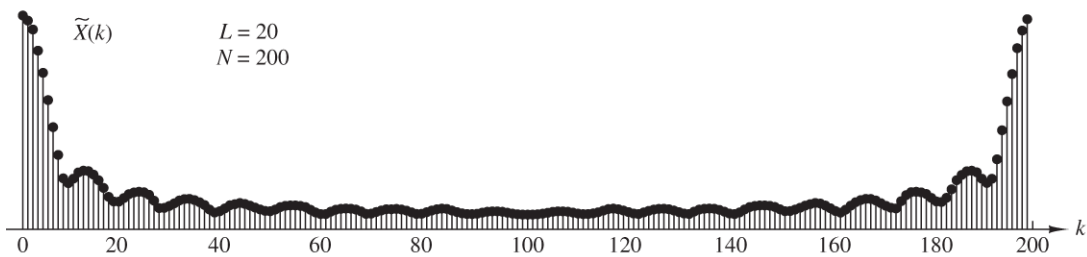
**Figure 7.4.5** Effect of windowing (truncating) the sampled version of the analog signal in Example 7.4.1



(c)



(d)



(e)

Figure 7.4.5 Continued