



泛亚汽车技术中心

阶段性报告

地图模块

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摘要：本文讨论了地图模块的接口设计和主要的功能模块以及车辆和目标在地理坐标系下的定位....

关键词：地图；RTK；数据融合；路径规划；微波雷达；SRR, ESR.

## **HD Map implementation by RTK deployment for Path Planning with Vehicle and Object localization**

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**Abstract:** This document has discussed the implementation of HD Map and the vehicle and objects localization in geographic coordinate system with RTK.

**Key words:** HD Map; RTK; Sensor Fusion; isomorphism; Fourier transform.

## 1 项目假设

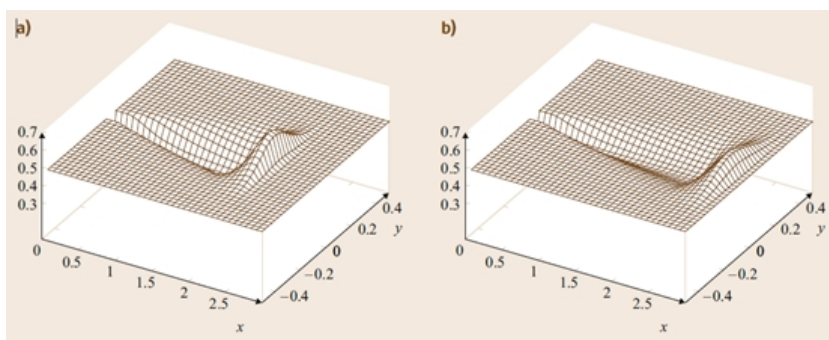
RTK, 高精度地图, 4 个 SRR, 1 个 ESR; 若干地标物 (landmark, beacon, 交通标示) 道路模型 (局部地图) 需要处理未知, 占据和非占据信息。接口静态的占据栅格图 OGM+ 动态的目标列表。根据静态地标占据栅格图用来更新本车姿态, 叠加动态的障碍物, 局部地图: 障碍物列表, 车道, 静态地标, RTK 车辆定位--> 路径规划。



## 2 2D 世界模型

2D 占据栅格图

$$p(m|x_{1:t}, z_{1:t}) = \prod_{l=1}^L p(m_l|x_{1:t}, z_{1:t}) \quad (1)$$



## 3 追踪列表 (动态)

```
1 int main() {
2     printf("hello, world");
3     return 0;
4 }

1 typedef struct{
2     int id;
```

```

3 // set to 1 in the very first cycle onl that an object is output, 0 in all other cycles.
4 bool newObj;
5 //one of GCS (WGS84/UTM), LCS, CCS, VCS, SCS, ACS, ENUM tbd
6 int coordinate_system;
7 PatObjState objState;
8 PatObjSize objSize;
9 // Pedestrian/vehicle_car/vehicle_truck/unknown/... ---> ENUM tbd.
10 int objClass;
11 //1 if the object is moving;0 if it's still;
12 bool moving;
13 //tracking when the object is seen by which exteroceptive sensor;
14 PatTime lastSeenBySensor[NUM_SENSOR_EXTEROCEPTIVE];
15 //0 for invalid; 1 for valid;
16 float existenceProbability;
17 }PatObject;
18
19 //maximally 256 tracked objects by all sensors around the vehicle;
20 PatObject object_list[128];

```

## 4 SLAM（同时定位与生成地图）

本车姿态（车辆位置，航向）和被观测目标的位置相关（地图, 此处只考虑静态的地标），应该同时求解。当特征（地标）较少，使用基于EKF的SLAM. (fastSLAM/DP-SLAM 适用于其他场合)

### 4.1 运动模型

$$x_{k+1} = x_k + D_k \cdot \cos \theta_{k+1} \quad (2)$$

$$y_{k+1} = y_k + D_k \cdot \sin \theta_{k+1} \quad (3)$$

$$\theta_{k+1} = \theta_k + \Delta \theta_k \quad (4)$$

$$D_k = v_{t,k} \cdot T \quad (5)$$

$$\Delta \theta_k = \omega_k \cdot T \quad (6)$$

$$v_{t,k} = \frac{v_{L,k} + v_{R,k}}{2} = \frac{\omega_{L,k}R + \omega_{R,k}R}{2} \quad (7)$$

$$\omega_k = \frac{v_{R,k} - v_{L,k}}{b} = \frac{\omega_{R,k}R - \omega_{L,k}R}{b} \quad (8)$$

标定

$$v_{t,k} = \frac{k_1 \cdot v_{L,k} + k_2 \cdot v_{R,k}}{2} \quad (9)$$

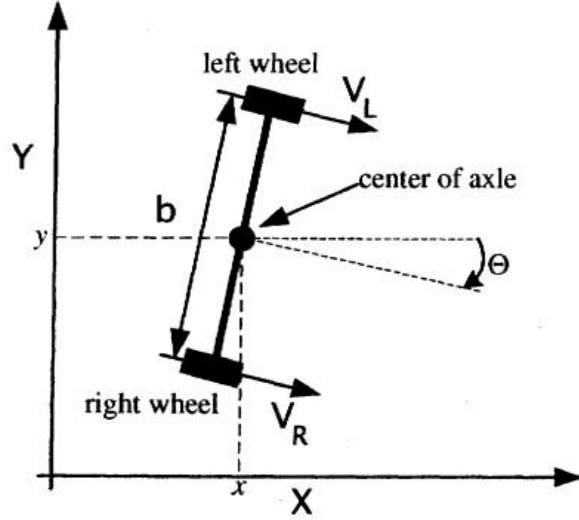
$$\omega_k = \frac{k_2 \cdot v_{R,k} - k_1 \cdot v_{L,k}}{k_3 \cdot b} \quad (10)$$

$$u_k = (v_k, \omega_k)^T$$

预测

$$x_{k+1} = f(x_k, u_k, v_k) \quad (11)$$

$$f(x_k, u_k, v_k) = \begin{cases} x_k + (D_k + v_{1,k} \cdot \cos(\theta_k + \Delta\theta_k + v_{2,k})) \\ y_k + (D_k + v_{1,k} \cdot \sin(\theta_k + \Delta\theta_k + v_{2,k})) \\ \theta_k + \Delta\theta_k + v_{2,k} \end{cases} \quad (12)$$



## 4.2 观测模型

基于距离变换  $DT$

$$DT(x) = \min_{v_j \in V} |x - v_j|$$

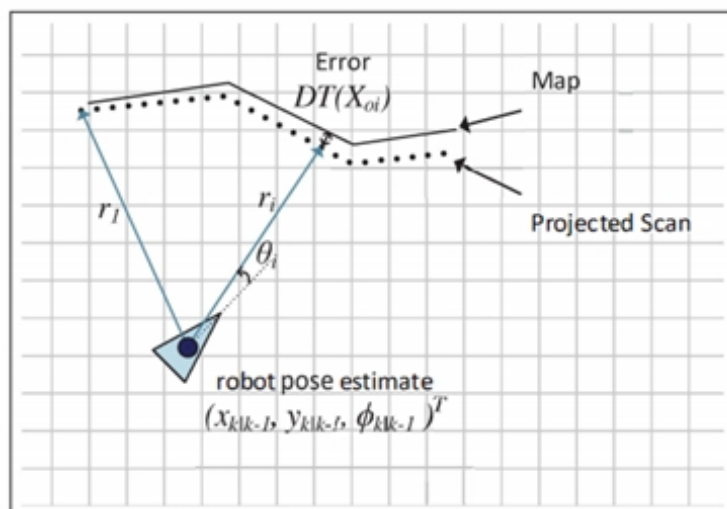
Chamfer distance  $CD$

$$h(X, z) = \frac{1}{n} \sum_{i=0}^{n-1} DT(X_{O_i}) = CD$$

$$X_{O_i} = \begin{cases} x_{O_i} \\ y_{O_i} \end{cases} = \begin{cases} x_{k|k-1} + r_i \cos(\theta_i + \phi_{k|k-1}) \\ y_{k|k-1} + r_i \sin(\theta_i + \phi_{k|k-1}) \end{cases}$$

隐式观测模型

$$h(X, z)$$



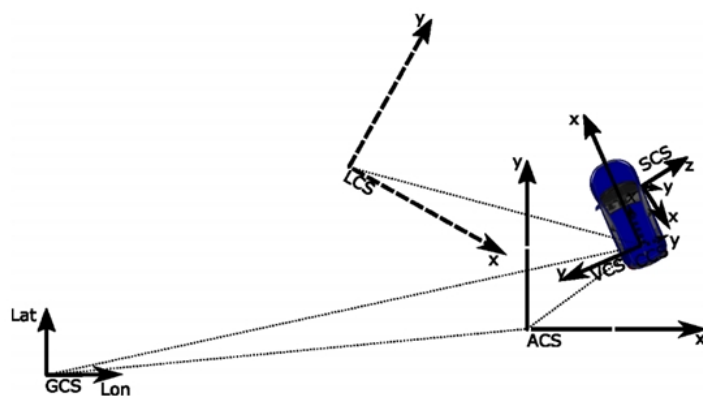
### 4.3 更新

$$K = P_{k|k-1} \nabla h_X^T (\nabla h_X P_{k|k-1} \nabla h_X^T + \nabla h_z^T \Sigma_z \nabla h_z)^{-1} \quad (13)$$

$$X_{k|k} = X_{k|k-1} + K(-h((X)_{k|k-1}, z)) \quad (14)$$

$$P_{k|k} = (I - K \nabla h_X) P_{k|k-1} \quad (15)$$

### 4.4 参考坐标系



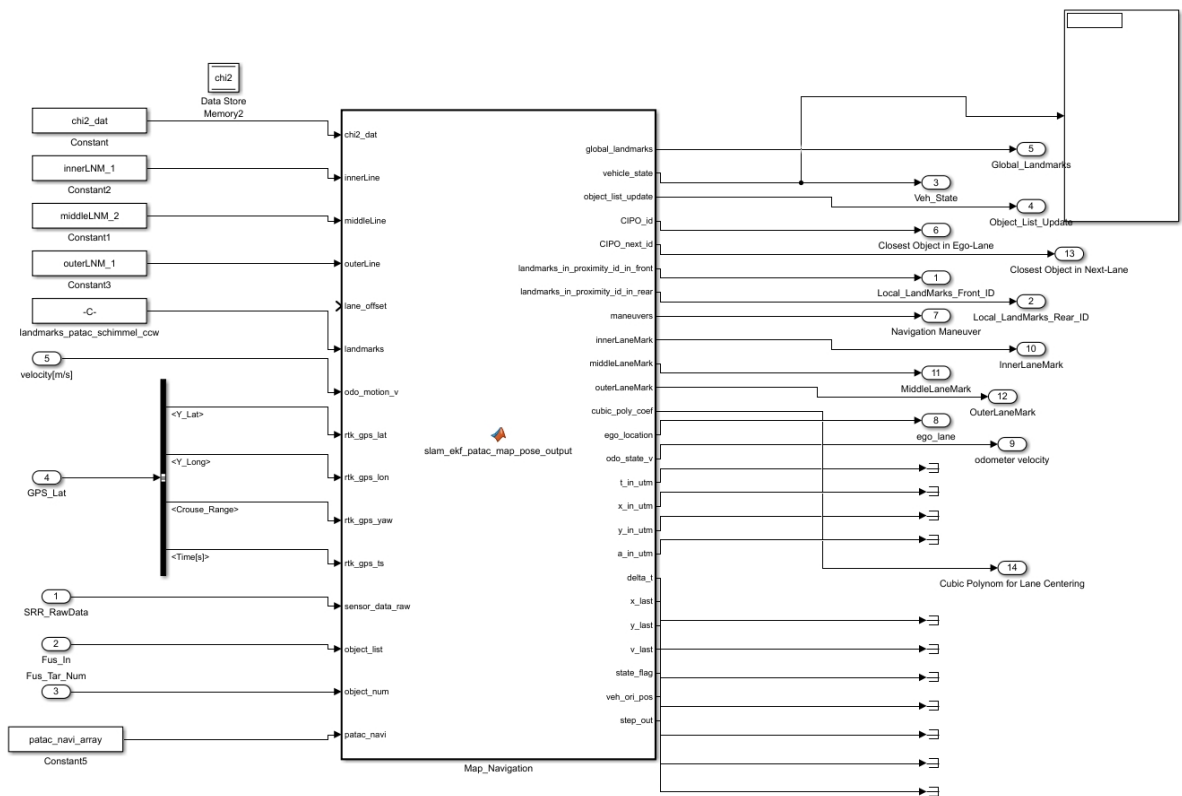
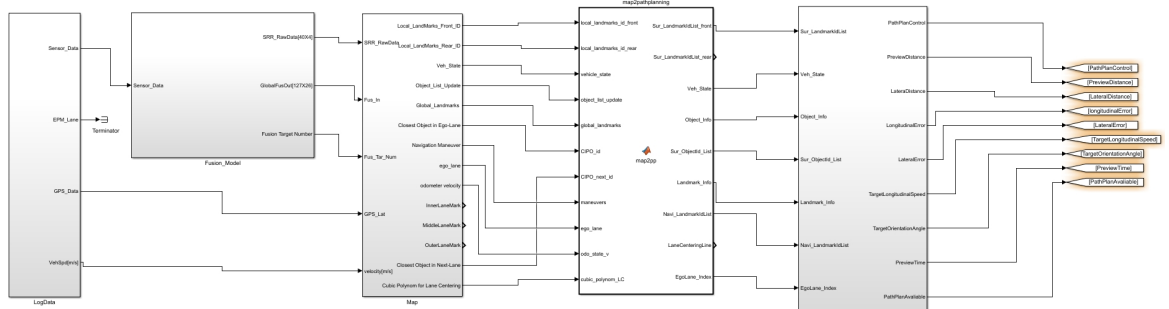
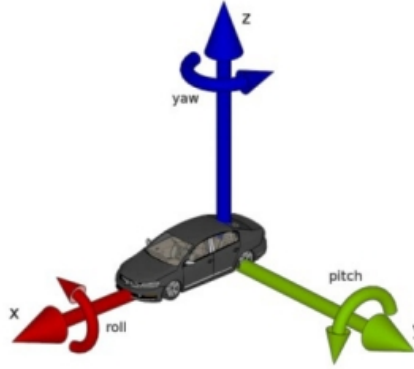
## 5 附录

### 5.1 主控模型 m 函数

```

1 function [veh_pose, veh_vel] = slam_ekf_patac (innerLine, middleLine, outerLine,...
2         landmarks, ...
3         odom_motion_x, odom_motion_y, odom_motion_yaw, ...
4         rtk_gps_lat, rtk_gps_lon, rtk_gps_yaw, rtk_gps_ts,...

```



```

5         sensor_data_raw,...
6         proximity)
7     coder.extrinsic('EKF_prediction');
8     coder.extrinsic('draw_ellipse');

```

```

9  rng;%randn('state', 0);
10
11 % determines execution and display modes
12 coder.inline('never');
13 %global configuration sensor;
14
15 persistent sensor configuration step veh_origin_pose map ground; %step = 0;
16 %chi2 = chi2inv(configuration.alpha,1:1000);
17 persistent rtk_gps_lat_last rtk_gps_lon_last rtk_gps_ts_last;
18
19 if isempty(step)
20     %adapt to applied sensors (SRR)!
21     step = 1;
22
23 configuration = struct('ellipses',true,'tags',false,'odometry',true, ...
24                       'noise',true,'alpha',0.99,'step_by_step',false,...
25                       'people',false,'ground',1,'map',2,'observations',3,...
26                       'compatibility',4,'ground_hypothesis',5,'hypothesis',6,...
27                       'tables',7);
28
29 sensor.range = 5;
30 sensor.minangle = -pi/2;
31 sensor.maxangle = pi/2;
32 sensor.srho = 0.01;
33 sensor.stita = 0.125*pi/180;
34
35 rtk_gps_lat_last = rtk_gps_lat;
36 rtk_gps_lon_last = rtk_gps_lon;
37 rtk_gps_yaw_last = rtk_gps_yaw;
38 rtk_gps_ts_last = rtk_gps_ts;
39 % generate the ground data from hdmap and RTK
40 ground = generate_rtk_ground(innerLine, middleLine, outerLine);
41
42 % start with a fresh map
43 [map, ground] = new_map(ground);
44
45 % plot ground
46 draw_ground(ground,landmarks, configuration);
47 %%pause

```



```

48
49 % ok, here we go
50
51 %%observations = get_observations(ground, sensor, step);
52 [x1,y1,utmzone,utmhemi] = wgs2utm(rtk_gps_lat,rtk_gps_lon,51,'N');
53 veh_origin_pose.x = x1;
54 veh_origin_pose.y = y1;
55 veh_origin_pose.yaw = rtk_gps_yaw;
56 veh_origin_pose.ts = rtk_gps_ts;
57 veh_pose = veh_origin_pose;
58 veh_vel = [0; 0]; % Start point with 0 velocity.
59 observations = get_observations (ground, landmarks, veh_pose, ...
60                               sensor_data_raw, sensor, proximity);
61 draw_observations (observations, configuration, step);
62
63 % GT = zeros(1, size(sensor_data_raw,1));
64 % H = zeros(1, size(sensor_data_raw,1));
65
66 map = add_features(map, observations);
67 % plot map
68 draw_map (map, ground,configuration,step);
69
70 % steps = length(ground.motion);
71 else
72
73 step = step+1;
74 disp('-----');
75 % disp(sprintf('Step: %d', step));
76
77 % EKF prediction step
78 odometry.x = [odo_motion_x, odo_motion_y,odo_motion_yaw]';;%odo_motion.x;
79 odometry.P = diag([0.25 0.1 5*pi/180].^2);
80
81
82 map = EKF_prediction (map, odometry);
83
84 % sense
85 [x1,y1,utmzone,utmhemi] = wgs2utm(rtk_gps_lat,rtk_gps_lon,51,'N');
86 veh_pose.x = x1;

```

```

87     veh_pose.y = y1;
88     veh_pose.yaw = rtk_gps_yaw;
89     veh_pose.ts = rtk_gps_ts;
90
91     [x2,y2,utmzone,utmhemi] = wgs2utm(rtk_gps_lat_last,rtk_gps_lon_last,51,'N');
92     veh_vel = [x1-x2; y1-y2]/(rtk_gps_ts - rtk_gps_ts_last)/1000;%ms-->s
93
94     rtk_gps_lat_last = rtk_gps_lat;
95     rtk_gps_lon_last = rtk_gps_lon;
96     rtk_gps_ts_last = rtk_gps_ts;
97
98
99     motion.x = [x1 y1 rtk_gps_yaw]';
100     motion.P = diag([0.02 0.02 2*pi/180].^2); % expectation of std of RTK
101     ground = move_vehicle (ground, motion, step);
102
103     observations = get_observations(ground, landmarks, veh_pose, ...
104                                     sensor_data_raw, sensor, proximity);
105
106     % individual compatibility
107     prediction = predict_observations (map, ground);
108     compatibility = compute_compatibility (prediction, observations);
109
110     disp(compatibility.HS);
111     disp(compatibility.AL);
112
113     disp(' ');
114
115     % ground truth
116     % your algorithm here!
117     % 1. Try NN
118     % 2. Complete SINGLES and try it
119     % 3. Include people and try SINGLES5
120     % 4. Try JCBB
121
122     H = NN (prediction, observations, compatibility,configuration);
123
124     draw_map (map, ground,configuration, step);
125     draw_observations (observations, configuration, step);

```

```

126
127
128     draw_compatibility (prediction, observations, compatibility,configuration);
129
130     disp(' ');
131
132     draw_hypothesis (prediction, observations, H, 'NN:', 'b-',configuration);
133
134     % update EKF step
135     map = EKF_update (map, prediction, observations, H, step);
136
137
138     % only new features with no neighbours
139     new = find((H == 0) & (compatibility.AL == 0));
140
141     if nnz(new)
142         map = add_features(map, observations, new);
143     end
144
145     draw_map (map, ground, configuration, step);
146 end
147 veh_pose = map.x(1:3);

```

## 5.2 目标定位模块 m 函数

```

1 function object_list_update = object_localization(object_list, object_num,...
2     innerLine_coordinate, innerLine_Vertex_index, ...
3     middleLine_coordinate, middleLine_Vertex_index,...
4     outerLine_coordinate, outerLine_Vertex_index, lane_offset,...
5     option)
6
7 object_list_update = object_list;
8 % distance      = zeros(size(object_list,1),3);
9 side_direction  = zeros(size(object_list,1),3);
10 % nearestIndex  = zeros(size(object_list,1),3);
11
12 for i = 1:object_num
13     if(object_list(i,1)~=0)
14         p = [object_list(i,2),object_list(i,4)];%2nd and 4th column are range x and range y
15         side_direction(i,1) = point_inside_lane(p,innerLine_coordinate, innerLine_Vertex_index);

```

```

16     side_direction(i,2) = point_inside_lane(p,middleLine_coordinate,middleLine_VerTEX_index);
17 %     side_direction(i,3) = point_inside_lane(p,outerLine_coordinate, outerLine_VerTEX_index);
18     side_direction(i,3) = point_inside_lane_offset(p,outerLine_coordinate, outerLine_VerTEX_index);
19 end
20 end
21
22 for i = 1:object_num
23     if(object_list(i,1)~=0)
24         if(option.clockWise == 0)%counter-clockwise
25             switch(sum(side_direction(i,:)))
26                 case 3 %( 1 1 1) outside outer ring
27                     object_list_update(i,9) = 3;
28                 case 1 %( 1 1 -1)
29                     object_list_update(i,9) = 2; %outer lane
30                 case -1 %( 1 -1 -1)
31                     object_list_update(i,9) = 1; %inner lane
32                 case -3 %(-1 -1 -1)
33                     object_list_update(i,9) = 0; %inside inner ring
34                 otherwise
35                     object_list_update(i,9) = 5;%warning('Unexpected location!')
36             end
37         else%clockwise
38             switch(sum(side_direction(i,:)))%counterclockwise
39                 case -3 %(-1 -1 -1)
40                     object_list_update(i,9) = 3;
41                 case -1 %(-1 -1 1)
42                     object_list_update(i,9) = 2; %outer lane
43                 case 1 %(-1 1 1)
44                     object_list_update(i,9) = 1; %inner lane
45                 case 3 %( 1 1 1)
46                     object_list_update(i,9) = 0; %inside inner ring
47                 otherwise
48                     object_list_update(i,9) = 5;%warning('Unexpected location!')
49             end
50         end
51     end
52 end

```

### 5.3 地标搜索模块 m 函数

```

1 function [landmarks_in_proximity_id_in_front, landmarks_in_proximity_id_in_rear] = quest_m
2     configuration,option)
3
4 % landmarks_in_proximity = zeros(size(landmarks));
5 %Landmarks
6 x1 = (double(landmarks(:,1))+double(landmarks(:,3)))/2 - ones(size(landmarks,1),1)*x_in_lcs;%lan
7 y1 = (double(landmarks(:,2))+double(landmarks(:,4)))/2 - ones(size(landmarks,1),1)*y_in_lcs;
8 % visible = find( (abs(x1) <= roi.x) & (abs(y1) <= roi.y) );
9 % distance2ego = (x1.^2 + y1.^2);
10 % [min_dist, ind] = min(distance2ego);
11 visible = find( (x1.^2 + y1.^2) <= configuration.proximity*configuration.proximity);
12
13
14
15 %%%%%%%%%%%%%%
16
17 if(size(visible,1)~=0)
18     p = [x_in_lcs,y_in_lcs];
19     [~,~,nearestIndex_Ego] = calDistance(p,middleLine_coordinate,middleLine_Verex_index,option
20
21     landmarks_in_proximity = landmarks(visible,:);
22     lat_distance_ldm        = zeros(size(visible,1),1);
23     side_direction_ldm      = zeros(size(visible,1),1);
24     nearestIndex_ldm        = zeros(size(visible,1),1);
25
26     %Initialize search
27     % p = (landmarks_in_proximity(1,1:2)+ landmarks_in_proximity(1,3:4))/2; %
28     % [lat_distance_ldm(1),side_direction_ldm(1),nearestIndex_ldm(1)] = calDistance(p,middleLine
29     % ldm_closest_in_path_ID_Index = nearestIndex_ldm(1);
30     ldm_closest_in_path_ID = -1;
31     ldm_closest_in_path_ID_Index = nearestIndex_Ego;
32
33     %Find the closest landmark in front
34     for i = 1:size(visible,1)
35         p = (landmarks_in_proximity(i,1:2)+ landmarks_in_proximity(i,3:4))/2; %
36         [lat_distance_ldm(i),side_direction_ldm(i),nearestIndex_ldm(i)]=calDistance(p,middleLine_
37         if(option.clockWise == 0) %counter-clockwise

```

```

38         if (nearestIndex_ldm(i) >= nearestIndex_Ego && ...%middleLine Index-->(2);in front of t
39             (nearestIndex_ldm(i) < ldm_closest_in_path_ID_Index...
40             || ldm_closest_in_path_ID < 0 )...
41         )%nearer than the closest so far
42         ldm_closest_in_path_ID = i;
43         ldm_closest_in_path_ID_Index = nearestIndex_ldm(i);
44     end
45 else %clockwise
46     if (nearestIndex_ldm(i) <= nearestIndex_Ego && ...%middleLine Index-->(2);in front of t
47         (nearestIndex_ldm(i) > ldm_closest_in_path_ID_Index...
48         || ldm_closest_in_path_ID < 0)...
49     )%nearer than the closest so far, clockwise is greater Index --> ">"
50     ldm_closest_in_path_ID = i;
51     ldm_closest_in_path_ID_Index = nearestIndex_ldm(i);
52 end
53 end
54 end
55
56 landmarks_in_proximity_id_in_front = zeros(size(landmarks,1),1);
57 landmarks_in_proximity_id_in_rear = zeros(size(landmarks,1),1);
58 if(ldm_closest_in_path_ID<0)%no front landmarks all are behind the ego vehicle.
59     if(option.clockWise == 0) %counter-clockwise
60         landmarks_in_proximity_id_in_rear(1:size(visible,1)) = flipud(visible);
61     else%clockwise
62         landmarks_in_proximity_id_in_rear(1:size(visible,1)) = visible;
63     end
64 elseif(abs(ldm_closest_in_path_ID-1)<1e-3)
65     if(option.clockWise == 0) % counter-clockwise
66         if(middleLine_Vertex_index(1,1)<nearestIndex_Ego && nearestIndex_Ego<middleLine_V
67             ldm_ID = visible(ldm_closest_in_path_ID);
68             if(nearestIndex_Ego>2)
69                 front_cyclic_1 = find(visible<=79);
70                 front_cyclic_2 = find(visible>=ldm_ID);
71                 if isempty(front_cyclic_1)
72                     front_cyclic_1=zeros(0,1);
73                 end
74                 if isempty(front_cyclic_2)
75                     front_cyclic_2=zeros(0,1);
76                 end

```

```

77     front_cyclic = intersect(front_cyclic_1,front_cyclic_2);
78     rear_cyclic_1 = find(visible>79);
79     rear_cyclic_2 = find(visible<ldm_ID);
80     rear_size_1 = size(rear_cyclic_1,1);
81     rear_size_2 = size(rear_cyclic_2,1);
82     %     rear_cyclic = union(rear_cyclic_1,rear_cyclic_2);
83     front_size = size(front_cyclic,1);
84     %     rear_size = size(rear_cyclic,1);
85     if(front_size~=0)
86         landmarks_in_proximity_id_in_front(1:front_size) = visible(front_cyclic);
87     end
88     if(rear_size_2~=0)
89         landmarks_in_proximity_id_in_rear(1:rear_size_2)= flipud(visible(rear_cyclic_2));
90     end
91     if(rear_size_1~=0)
92         landmarks_in_proximity_id_in_rear(rear_size_2+1:rear_size_2+rear_size_1)=
93         visible(rear_cyclic_1);
94     end
95     else %if(nearestIndex_Ego==2
96         front_cyclic_1 = find(visible<=79);
97         front_cyclic_2_1 = find(nearestIndex_ldm==2);
98         front_cyclic_2_2 = find(visible>79);
99         if isempty(front_cyclic_2_1)
100             front_cyclic_2_1=zeros(0,1);
101         end
102         if isempty(front_cyclic_2_2)
103             front_cyclic_2_2=zeros(0,1);
104         end
105         front_cyclic_2 = intersect(front_cyclic_2_1,front_cyclic_2_2);
106         front_size_1 = size(front_cyclic_1,1);
107         front_size_2 = size(front_cyclic_2,1);
108         %     front_cyclic = union(front_cyclic_1,front_cyclic_2);
109         %     front_size = size(front_cyclic,1);
110         rear_cyclic_1 = find(visible>79);
111         rear_cyclic_2 = find(nearestIndex_ldm~=2);
112         if isempty(rear_cyclic_1)
113             rear_cyclic_1=zeros(0,1);
114         end
115         if isempty(rear_cyclic_2)
116             rear_cyclic_2=zeros(0,1);

```

```

116         end
117         rear_cyclic = intersect(rear_cyclic_1,rear_cyclic_2);
118         rear_size = size(rear_cyclic,1);
119         %         front_cyclic = find(visible<=79 || visible>=ldm_ID);
120         %         rear_cyclic = find( visible>79 && visible<ldm_ID);
121         %         front_size = size(front_cyclic,1);
122         %         rear_size = size(rear_cyclic,1);
123         if(front_size_2~=0)
124             landmarks_in_proximity_id_in_front(1:front_size_2) = visible(front_cyclic_2);
125         end
126         if(front_size_1~=0)
127             landmarks_in_proximity_id_in_front(front_size_2+1:front_size_2+front_size_1) = visible(front_cyclic_1);
128         end
129         if(rear_size~=0)
130             landmarks_in_proximity_id_in_rear(1:rear_size)= flipud(visible(rear_cyclic));
131         end
132     end
133 elseif(middleLine_Vertex_index(4,1)<nearestIndex_Ego && nearestIndex_Ego<middleLine_Vertex_index(4,1))
134     ldm_ID = visible(ldm_closest_in_path_ID);
135     front_cyclic_1 = find(visible <= 21);
136     front_cyclic_2 = find(visible>=ldm_ID);
137     %     front_cyclic = union(front_cyclic_1,front_cyclic_2);
138     rear_cyclic_1 = find(visible > 21);
139     rear_cyclic_2 = find(visible < ldm_ID);
140     if isempty(rear_cyclic_1)
141         rear_cyclic_1=zeros(0,1);
142     end
143     if isempty(rear_cyclic_2)
144         rear_cyclic_2=zeros(0,1);
145     end
146     rear_cyclic = intersect(rear_cyclic_1,rear_cyclic_2);
147     %     front_size = size(front_cyclic,1);
148     rear_size = size(rear_cyclic,1);
149
150     front_size_1 = size(front_cyclic_1,1);
151     front_size_2 = size(front_cyclic_2,1);
152     %     rear_size_1 = size(rear_cyclic_1,1);
153     %     rear_size_2 = size(rear_cyclic_2,1);
154     if(front_size_2~=0)

```



```

155         landmarks_in_proximity_id_in_front(1:front_size_2) = visible(front_cyclic_2);
156     end
157     if(front_size_1~=0)
158         landmarks_in_proximity_id_in_front(front_size_2+1:(front_size_1+front_size_2)
159     end
160     if(rear_size~=0)
161         landmarks_in_proximity_id_in_rear(1:rear_size)= flipud(visible(rear_cyclic));
162     end
163 else
164     landmarks_in_proximity_id_in_front(1:size(visible,1)) = visible;
165 end
166 end
167 else% (ldm_closest_in_path_ID>1)
168     if(option.clockWise == 0) % counter-clockwise
169         if(middleLine_Vertex_index(1,1)<nearestIndex_Ego && nearestIndex_Ego<middleLine_V
170             ldm_ID = visible(ldm_closest_in_path_ID);
171             if(nearestIndex_Ego>2)
172                 front_cyclic_1 = find(visible<=79);
173                 front_cyclic_2 = find(visible>=ldm_ID);
174                 if isempty(front_cyclic_1)
175                     front_cyclic_1=zeros(0,1);
176                 end
177                 if isempty(front_cyclic_2)
178                     front_cyclic_2=zeros(0,1);
179                 end
180                 front_cyclic = intersect(front_cyclic_1,front_cyclic_2);
181                 rear_cyclic_1 = find(visible>79);
182                 rear_cyclic_2 = find(visible<ldm_ID);
183                 rear_size_1 = size(rear_cyclic_1,1);
184                 rear_size_2 = size(rear_cyclic_2,1);
185                 %         rear_cyclic = union(rear_cyclic_1,rear_cyclic_2);
186                 front_size = size(front_cyclic,1);
187                 %         rear_size = size(rear_cyclic,1);
188                 if(front_size~=0)
189                     landmarks_in_proximity_id_in_front(1:front_size) = visible(front_cyclic);
190                 end
191                 if(rear_size_2~=0)
192                     landmarks_in_proximity_id_in_rear(1:rear_size_2)= flipud(visible(rear_cyclic_
193                 end

```

```

194         if(rear_size_1~=0)
195             landmarks_in_proximity_id_in_rear(rear_size_2+1:rear_size_2+rear_size_1)=
196             end
197     else %if(nearestIndex_Ego
198         front_cyclic_1 = find(visible<=79);
199         front_cyclic_2_1 = find(nearestIndex_ldm==2);
200         front_cyclic_2_2 = find(visible>79);
201         if isempty(front_cyclic_2_1))
202             front_cyclic_2_1=zeros(0,1);
203         end
204         if isempty(front_cyclic_2_2))
205             front_cyclic_2_2=zeros(0,1);
206         end
207         front_cyclic_2 = intersect(front_cyclic_2_1,front_cyclic_2_2);
208         front_size_1 = size(front_cyclic_1,1);
209         front_size_2 = size(front_cyclic_2,1);
210         rear_cyclic_1 = find(visible>79);
211         rear_cyclic_2 = find(nearestIndex_ldm~=2);
212         if isempty(rear_cyclic_1))
213             rear_cyclic_1=zeros(0,1);
214         end
215         if isempty(rear_cyclic_2))
216             rear_cyclic_2=zeros(0,1);
217         end
218         rear_cyclic = intersect(rear_cyclic_1,rear_cyclic_2);
219         rear_size = size(rear_cyclic,1);
220
221         if(front_size_2~=0)
222             landmarks_in_proximity_id_in_front(1:front_size_2) = visible(front_cyclic_2);
223         end
224         if(front_size_1~=0)
225             landmarks_in_proximity_id_in_front(front_size_2+1:front_size_2+front_size_1)=
226             end
227         if(rear_size~=0)
228             landmarks_in_proximity_id_in_rear(1:rear_size)= flipud(visible(rear_cyclic));
229         end
230     end
231 elseif(middleLine_Vertex_index(4,1)<nearestIndex_Ego && nearestIndex_Ego<middleLine_Vertex_index(4,1))
232     ldm_ID = visible(ldm_closest_in_path_ID);

```

```

233     front_cyclic_1 = find(visible <= 21);
234     front_cyclic_2 = find(visible>=ldm_ID);
235     rear_cyclic_1 = find(visible > 21);
236     rear_cyclic_2 = find(visible < ldm_ID);
237     if isempty(rear_cyclic_1)
238         rear_cyclic_1=zeros(0,1);
239     end
240     if isempty(rear_cyclic_2)
241         rear_cyclic_2=zeros(0,1);
242     end
243     rear_cyclic = intersect(rear_cyclic_1,rear_cyclic_2);
244     rear_size = size(rear_cyclic,1);
245
246     front_size_1 = size(front_cyclic_1,1);
247     front_size_2 = size(front_cyclic_2,1);
248     if (front_size_2~=0)
249         landmarks_in_proximity_id_in_front(1:front_size_2) = visible(front_cyclic_2);
250     end
251     if (front_size_1~=0)
252         landmarks_in_proximity_id_in_front(front_size_2+1:(front_size_1+front_size_2)) = visible(front_cyclic_1);
253     end
254     if (rear_size~=0)
255         landmarks_in_proximity_id_in_rear(1:rear_size)= flipud(visible(rear_cyclic));
256     end
257 else
258     front_size = size(visible,1) - ldm_closest_in_path_ID+1;
259     rear_size = ldm_closest_in_path_ID-1;
260     landmarks_in_proximity_id_in_front(1:front_size) = visible(ldm_closest_in_path_ID+1:ldm_ID);
261     landmarks_in_proximity_id_in_rear(1:rear_size)= flipud(visible(1:ldm_closest_in_path_ID));
262 end
263 else%clockwise
264     front_size = ldm_closest_in_path_ID;
265     rear_size = size(visible,1) - ldm_closest_in_path_ID;
266     landmarks_in_proximity_id_in_front(1:front_size) = flipud(visible(1:ldm_closest_in_path_ID));
267     landmarks_in_proximity_id_in_rear(1:rear_size)= visible(ldm_closest_in_path_ID+1:ldm_ID);
268 end
269 end
270 else
271     landmarks_in_proximity_id_in_front = zeros(size(landmarks,1),1);

```

```

272 landmarks_in_proximity_id_in_rear = zeros(size(landmarks,1),1);
273 end
274 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

```

#### 5.4 目标定位模块 m 函数

```

1 function object_list_update = object_localization(object_list, object_num,...
2     innerLine_coordinate, innerLine_Vertex_index, ...
3     middleLine_coordinate, middleLine_Vertex_index,...
4     outerLine_coordinate, outerLine_Vertex_index, lane_offset,...
5     option)
6
7 object_list_update = object_list;
8 side_direction      = zeros(size(object_list,1),3);
9
10 for i = 1:object_num
11     if(object_list(i,1)~=0)
12         p = [object_list(i,2),object_list(i,4)];%2nd and 4th column are range x and range y
13         side_direction(i,1) = point_inside_lane(p,innerLine_coordinate, innerLine_Vertex_index);
14         side_direction(i,2) = point_inside_lane(p,middleLine_coordinate,middleLine_Vertex_index);
15         side_direction(i,3) = point_inside_lane_offset(p,outerLine_coordinate, outerLine_Vertex_index, lane_offset);
16     end
17 end
18
19 for i = 1:object_num
20     if(object_list(i,1)~=0)
21         if(option.clockWise == 0)%counter-clockwise
22             switch(sum(side_direction(i,:)))
23                 case 3 %( 1 1 1) outside outer ring
24                     object_list_update(i,9) = 3;
25                 case 1 %( 1 1 -1)
26                     object_list_update(i,9) = 2; %outer lane
27                 case -1 %( 1 -1 -1)
28                     object_list_update(i,9) = 1; %inner lane
29                 case -3 %(-1 -1 -1)
30                     object_list_update(i,9) = 0; %inside inner ring
31                 otherwise
32                     object_list_update(i,9) = 5;%warning('Unexpected location!')
33             end
34         else%clockwise

```

```

35     switch(sum(side_direction(i,:)))%counterclockwise
36         case -3 %(-1 -1 -1)
37             object_list_update(i,9) = 3;
38         case -1 %(-1 -1 1)
39             object_list_update(i,9) = 2; %outer lane
40         case 1 %(-1 1 1)
41             object_list_update(i,9) = 1; %inner lane
42         case 3 %(1 1 1)
43             object_list_update(i,9) = 0; %inside inner ring
44         otherwise
45             object_list_update(i,9) = 5;%warning('Unexpected location!')
46     end
47 end
48 end
49 end

```

## 5.5 地标搜索模块 m 函数

```

1 function [obj_closest_in_path_ID, obj_closest_in_next_path_ID, ego_location] = objects_of_in
2     x_in_lcs, y_in_lcs, ...
3     innerLine_coordinate, innerLine_Vertex_index, ...
4     middleLine_coordinate, middleLine_Vertex_index,...
5     outerLine_coordinate, outerLine_Vertex_index,...
6     option)
7
8     inside = zeros(1,3);
9     p = [x_in_lcs,y_in_lcs];
10    inside(1) = point_inside_lane(p,innerLine_coordinate, innerLine_Vertex_index);
11    inside(2) = point_inside_lane(p,middleLine_coordinate, middleLine_Vertex_index);
12    inside(3) = point_inside_lane(p,outerLine_coordinate, outerLine_Vertex_index);
13
14    if(option.clockWise == 0)%counter-clockwise
15        switch(sum(inside))
16            case 3 %(1 1 1) outside outer ring
17                ego_location = 3;
18            case 1 %(1 1 -1)
19                ego_location = 2; %outer lane
20            case -1 %(1 -1 -1)
21                ego_location = 1; %inner lane

```

```

22     case -3 %(-1 -1 -1)
23         ego_location = 0; %inside inner ring
24     otherwise
25         ego_location = 5;%warning('Unexpected location!')
26     end
27 else%clockwise
28     switch(sum(inside))%counterclockwise
29         case -3 %(-1 -1 -1)
30             ego_location = 3;
31         case -1 %(-1 -1 1)
32             ego_location = 2; %outer lane
33         case 1 %(-1 1 1)
34             ego_location = 1; %inner lane
35         case 3 %( 1 1 1)
36             ego_location = 0; %inside inner ring
37         otherwise
38             ego_location = 5;%warning('Unexpected location!')
39         end
40     end
41
42     if( ~(ego_location==2 || ego_location==1) )
43         obj_closest_in_path_ID = 0;
44         obj_closest_in_next_path_ID = 0;
45         return;
46     end
47     if(ego_location == 1)
48         next_lane = 2;
49     else
50         next_lane = 1;
51     end
52
53
54     [projection_dist,~]=point_dist2lane(p,outerLine_coordinate,outerLine_Vertex_index);
55     [~,sideIndex]=min(projection_dist);
56
57     %find the projected point of vehicle on the outer lane mark and its distance to the 1st corner.
58     corner_1=outerLine_coordinate(outerLine_Vertex_index(sideIndex,1),:);
59     corner_2=outerLine_coordinate(outerLine_Vertex_index(sideIndex,2),:);
60     [~, dist2StartCorner_veh] = point_projection2LNM(p, corner_1, corner_2);

```

```

61
62
63 %find object in ego lane and next lane
64 object_list_lane_loc = object_list(1:object_num,9) ;
65
66 objects_in_ego_lane_id = find(object_list_lane_loc == ego_location);
67 objects_in_next_lane_id = find( object_list_lane_loc == next_lane);
68
69 % objects_in_ego_lane_id(1:size(objects_in_next_lane_id_temp,1))=objects_in_ego_lane_id_t
70 max_len = max(size(objects_in_ego_lane_id,1),size(objects_in_next_lane_id,1));
71 dist2StartCorner_obj = zeros(max_len,2);
72
73 if(size(objects_in_ego_lane_id,1)~=0)
74     objects_in_ego_lane = [object_list(objects_in_ego_lane_id,2),object_list(objects_in_ego_la
75     obj_closest_in_path_ID_dist = dist2StartCorner_veh+500;
76     obj_closest_in_path_ID = 0;
77     %Find the closest in-path object (CIPO)
78     for i = 1:size(objects_in_ego_lane,1)
79         p = objects_in_ego_lane(i,:);
80         [~,dist2StartCorner_obj(i,1)]=point_projection2LNM(p, corner_1, corner_2); % projection on
81
82         if (dist2StartCorner_obj(i,1) >= dist2StartCorner_veh && ...
83             dist2StartCorner_obj(i,1) <= obj_closest_in_path_ID_dist)
84             obj_closest_in_path_ID = objects_in_ego_lane_id(i);
85             obj_closest_in_path_ID_dist = dist2StartCorner_obj(i,1);
86         end
87     end
88 else
89     obj_closest_in_path_ID = 0;
90 end
91
92 % obj_closest_in_next_path_ID =0;
93 if(size(objects_in_next_lane_id,1)~=0)
94     objects_in_next_lane = [object_list(objects_in_next_lane_id,2),object_list(objects_in_next
95     obj_closest_in_path_ID_dist = dist2StartCorner_veh+500;
96     obj_closest_in_next_path_ID = 0;
97
98     %Find the closest Next Lane object
99     for i = 1:size(objects_in_next_lane,1)

```

```

100     p = objects_in_next_lane(i,:);
101     [~, dist2StartCorner_obj(i,2)] = point_projection2LNM(p, corner_1, corner_2);
102     if (dist2StartCorner_obj(i,2) > dist2StartCorner_veh && ...
103         dist2StartCorner_obj(i,2) < obj_closest_in_path_ID_dist)
104         obj_closest_in_next_path_ID = objects_in_next_lane_id(i);
105         obj_closest_in_path_ID_dist = dist2StartCorner_obj(i,2);
106     end
107 end
108 else
109     obj_closest_in_next_path_ID = 0;
110 end
111 %Sort objects in ego and next lane in driving direction and in the proximity sequence of ego vehicle.

```



## References

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