1. Solve the equation A = B where

$$A = \begin{bmatrix} 1 & -2 \\ 3 & 1 \\ -1 & 2 \end{bmatrix}, \qquad B = \begin{bmatrix} 1 & x \\ y - x & 1 \\ -1 & 2 \end{bmatrix}$$
 for  $x$  and  $y$ .

2. Given that

$$A = \begin{bmatrix} 1 & 2 & -3 \\ -1 & 0 & 4 \end{bmatrix}, \qquad B = \begin{bmatrix} 2 & -1 & 3 \\ 4 & 1 & 2 \end{bmatrix}$$

Find the matrices A + B, A - B, and 2A - 3B.

- 3. Taking 3 appropriate matrices verify the distributive law A(B+C) = AB + AC and the associative law A(BC) = (AB)C
- 4. Show that  $A + A^{T}$  is a symmetric matrix, and that  $A A^{T}$  is skew symmetric. If  $A = \begin{bmatrix} 1 & -1 & 0 \\ 2 & 3 & -2 \\ 1 & -1 & 1 \end{bmatrix}$

If 
$$A = \begin{bmatrix} 1 & -1 & 0 \\ 2 & 3 & -2 \\ 1 & -1 & 1 \end{bmatrix}$$

5. Let

$$A = \begin{bmatrix} 1 & 3 \\ -1 & 2 \\ 0 & 1 \end{bmatrix}$$

Write down  $A^T$ , and find the products  $AA^T$  and  $A^TA$ 

6. Let

$$A = \begin{bmatrix} 1 & 0 & 0 \\ a & -1 & 0 \\ b & c & 1 \end{bmatrix}$$
Find  $A^2$ 

For what relation between a, b and c is  $A^2 = I_3$ ?