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1 MODULE *ABSpec*

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2 EXTENDS *Integers*

4 CONSTANT *Data*    The set of all possible data values.

6 VARIABLES *AVar*,    The last  $\langle \textit{value}, \textit{bit} \rangle$  pair A decided to send.  
7                *BVar*    The last  $\langle \textit{value}, \textit{bit} \rangle$  pair B received.

Type correctness means that *AVar* and *BVar* are tuples  $\langle d, i \rangle$  where  $d \in \textit{Data}$  and  $i \in \{0, 1\}$ .

13  $\textit{TypeOK} \triangleq \wedge \textit{AVar} \in \textit{Data} \times \{0, 1\}$   
14                 $\wedge \textit{BVar} \in \textit{Data} \times \{0, 1\}$

It's useful to define *vars* to be the tuple of all variables, for example so we can write  $[\textit{Next}]_{\textit{vars}}$  instead of  $[\textit{Next}]_{\langle \dots \rangle}$

20  $\textit{vars} \triangleq \langle \textit{AVar}, \textit{BVar} \rangle$

Initially *AVar* can equal  $\langle d, 1 \rangle$  for any *Data* value *d*, and *BVar* equals *AVar*.

27  $\textit{Init} \triangleq \wedge \textit{AVar} \in \textit{Data} \times \{1\}$   
28                 $\wedge \textit{BVar} = \textit{AVar}$

When  $\textit{AVar} = \textit{BVar}$ , the sender can “send” an arbitrary data *d* item by setting  $\textit{AVar}[1]$  to *d* and complementing  $\textit{AVar}[2]$ . It then waits until the receiver “receives” the message by setting *BVar* to *AVar* before it can send its next message. Sending is described by action A and receiving by action B.

37  $A \triangleq \wedge \textit{AVar} = \textit{BVar}$   
38                 $\wedge \exists d \in \textit{Data} : \textit{AVar}' = \langle d, 1 - \textit{AVar}[2] \rangle$   
39                 $\wedge \textit{BVar}' = \textit{BVar}$

41  $B \triangleq \wedge \textit{AVar} \neq \textit{BVar}$   
42                 $\wedge \textit{BVar}' = \textit{AVar}$   
43                 $\wedge \textit{AVar}' = \textit{AVar}$

45  $\textit{Next} \triangleq A \vee B$

47  $\textit{Spec} \triangleq \textit{Init} \wedge \Box [\textit{Next}]_{\textit{vars}}$

For understanding the spec, it's useful to define formulas that should be invariants and check that they are invariant. The following invariant *Inv* asserts that, if *AVar* and *BVar* have equal second components, then they are equal (which by the invariance of *TypeOK* implies that they have equal first components).

56  $\textit{Inv} \triangleq (\textit{AVar}[2] = \textit{BVar}[2]) \Rightarrow (\textit{AVar} = \textit{BVar})$

58  $\textit{DeliveryLiveness} \triangleq \forall v \in \textit{Data} \times \{0, 1\} : (\textit{AVar} = v) \leadsto (\textit{BVar} = v)$

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*FairSpec* is *Spec* with the addition requirement that it keeps taking steps.

64  $\textit{FairSpec} \triangleq \textit{Spec} \wedge \text{WF}_{\textit{vars}}(\textit{Next})$

*FairABSpec* is *Spec* with the additional requirement that both A and B keep taking steps.

70  $FairABSpec \triangleq Spec \wedge WF_{vars}(A) \wedge WF_{vars}(B)$

*FairBSpec* is *Spec* with the additional requirement that every sent value to be received, but allows the sender to stop sending.

76  $FairBSpec \triangleq Spec \wedge WF_{vars}(B)$

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\ \* Modification History

\ \* Last modified Sat Aug 11 22:07:13 CST 2018 by *hengxin*

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