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1  |----- MODULE MinMax2H -----|
   | This module defines SpecH to be a specification obtained by adding a history variable h to the |
   | specification Spec of module MinMax2. It then shows that SpecH implements specification Spec |
   | of module MinMax1 under the refinement mapping  $y \leftarrow h$ . |
8  | EXTENDS MinMax2 |
10 | VARIABLE h |
11 |  $varsH \triangleq \langle vars, h \rangle$  |
   | |
   | InitH is the initial predicate of SpecH and NextH is its next-state action, obtained by adding the |
   | history variable h to the subactions InputNum and Respond of the obvious disjunctive represen- |
   | tation of Next. (Disjunctive representations are explained in Section 3.2 of the paper “Auxiliary |
   | Variables in TLA+”.) |
20 |  $InitH \triangleq Init \quad \wedge (h = \{\})$  |
22 |  $InputNumH \triangleq \quad \wedge InputNum$  |
23 |  $\quad \wedge h' = h$  |
25 |  $RespondH \triangleq \quad \wedge Respond$  |
26 |  $\quad \wedge h' = h \cup \{x\}$  |
28 |  $NextH \triangleq InputNumH \vee RespondH$  |
30 |  $SpecH \triangleq InitH \wedge \Box[NextH]_{varsH}$  |
31 |-----|
   | The following statement and theorem assert that SpecH implements specification Spec of module |
   | MinMax1 under the refinement mapping  $y \leftarrow h$ . |
37 |  $M \triangleq \text{INSTANCE } MinMax1 \text{ WITH } y \leftarrow h$  |
39 | THEOREM  $SpecH \Rightarrow M!Spec$  |
40 |-----|
   | * Modification History |
   | * Last modified Fri Oct 21 23:59:25 PDT 2016 by lamport |
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