```
- module \mathit{Op} -
 1 [
    Model checking basic operations on strings (i.e., list of characters).
   EXTENDS Naturals, Sequences, Additional Sequence Operators
 7 |
    CONSTANTS
                        Char,
                        MaxPos.
 9
                        MaxPr
10
     ASSUME \land MaxPos \in Nat \setminus \{0\} WARNING: index from 1
12
                 \wedge MaxPr \in Nat \setminus \{0\}
13
    List \triangleq Seq(Char)
                                  The set of all lists.
15
    The set of all operations. In this specification, we will focus on "Ins" and "Del".
     Op \stackrel{\triangle}{=} [type : \{ \text{"Rd"} \}] \cup \text{ a read specifies no arguments}
               [type: {"Del"}, pos: MaxPos] \cup a deletion specifies a position (from 1)
22
               [type: {"Ins"}, pos: MaxPos, ch: Char, pr: MaxPr] an insertion specifies a position (from 1), a character, as
23
    Nop \stackrel{\Delta}{=} CHOOSE \ v : v \notin Op \quad Nop: an operation representing "doing nothing"
24
25
    Some operations for test.
    Del1 \stackrel{\triangle}{=} [type \mapsto "Del", pos \mapsto 1]
    Del2 \triangleq [type \mapsto "Del", pos \mapsto 2]
     Del3 \triangleq [type \mapsto "Del", pos \mapsto 3]
    Del4 \triangleq [type \mapsto "Del", pos \mapsto 4]
    Ins1 \stackrel{\triangle}{=} [type \mapsto "Ins", pos \mapsto 1, ch \mapsto "a", pr \mapsto 1]
    Ins2 \stackrel{\triangle}{=} [type \mapsto "Ins", pos \mapsto 2, ch \mapsto "b", pr \mapsto 2]
    Ins3 \stackrel{\triangle}{=} [type \mapsto "Ins", pos \mapsto 3, ch \mapsto "c", pr \mapsto 3]
    Ops \stackrel{\Delta}{=} \langle Ins2, Del3, Ins1, Del2, Ins3, Del1 \rangle
37 F
    The "Apply" operator which applies an operation op on the list l.
    Apply(op, l) \triangleq
41
         LET len \stackrel{\triangle}{=} Len(l)
42
                pos \stackrel{\triangle}{=} op.pos
43
                Case op = Nop \rightarrow l
44
                        op.type = "Del" \rightarrow SubSeq(l, 1, pos - 1) \circ SubSeq(l, pos + 1, len)
45
                        op.type = "Ins" \rightarrow Append(SubSeq(l, 1, pos - 1), op.ch) \circ SubSeq(l, pos, len)
46
    The "ApplyOps" operator which applies an operation sequence ops on the list l.
    RECURSIVE ApplyOps(\_, \_)
52
    ApplyOps(ops, l) \triangleq
53
         IF ops = \langle \rangle
54
           THEN l
55
56
           ELSE Apply(Last(ops), ApplyOps(AllButLast(ops), l))
```

**\\*** Modification History