MODULE Zab WithFLE -

This is the formal specification for the Zab consensus algorithm, which means Zookeeper Atomic Broadcast.

Reference:

 $FLE: Fast Leader Election. java, \\ Vote. java, \\ Quorum Peer. java \\ \text{in}$

https://github.com/apache/zookeeper.

ZAB: QuorumPeer.java, Learner.java, Follower.java, LearnerHandler.java, Leader.java in https://github.com/apache/zookeeper. https://cwiki.apache.org/confluence/display/ZOOKEEPER/Zab1.0.

EXTENDS FastLeaderElection

The set of requests that can go into history

CONSTANT Value

Zab states

CONSTANTS ELECTION, DISCOVERY, SYNCHRONIZATION, BROADCAST

Message types

CONSTANTS FOLLOWERINFO, LEADERINFO, ACKEPOCH, NEWLEADER, ACKLD, UPTODATE, PR

NOTE: Additional message types used for recovery in synchronization(TRUNC/DIFF/SNAP) are not needed since we abstract this part.(see action RECOVERYSYNC)

NOTE: In production, there is no message type ACKLD. Server judges if counter of ACK is 0 to distinguish one ACK represents ACKLD or not. Here we divide ACK into ACKLD and ACK, to enhance readability of spec.

TODO: Consider in the future replacing the magic atomic synchronization RECOVERYSYNC with DIFF based message passing.

[MaxTimeoutFailures, MaxTransactionNum, MaxEpoch]

CONSTANT Parameters

TODO: Here we can add more constraints to decrease space.

$MAXEPOCH \triangleq 10$

Variables that all servers need to use.

VARIABLES zabState, The current phase of server,

in {ELECTION, DISCOVERY, SYNCHRONIZATION, BROADCAST}.

acceptedEpoch, The epoch number of the last LEADERINFO packet accepted,

namely f.p in paper.

history, The history of servers as the sequence of transactions.

commitIndex Maximum index known to be committed.

Starts from 0, and increases monotonically before restarting.

Equals to 'lastCommitted' in code.

These transactions whose index $\ensuremath{\operatorname{le}}\xspace commitIndex[i]$ can be applied to state machine immediately. So if we have a variable applyIndex, we can suppose that applyIndex[i] = commitIndex[i] when verifying properties. But in phase SYNC, follower will apply all queued proposals to state machine when receiving NEWLEADER. But follower only serves traffic after receiving UPTODATE, so sequential consistency is not violated.

So when we verify properties, we still suppose applyIndex[i] = commitIndex[i], because this is an engineering detail.

Variables only used when state = LEADING.

VARIABLES learners, The set of servers which leader i think are connected wich i.

cepochRecv, The set of followers who has successfully sent FOLLOWERINFO to leader.

Equals to 'connectingFollowers' in code.

ackeRecv, The set of followers who has successfully sent ACK-E to leader.

Equals to 'electingFollowers' in code.

ackldRecv, The set of followers who has successfully sent ACK-LD to leader in leader.

Equals to 'newLeaderProposal' in code.

forwarding, The set of servers which leader i should broadcast PROPOSAL and COMMIT to.

Equals to 'forwardingFollowers' in code.

ackIndex, [i][j]: The latest index that leader i has received from follower j via ACK.

currentCounter, [i]: The count of transactions that clients have requested leader i.

sendCounter, $\setminus *[i]$: The count of transactions that leader i has broadcast via PROPOSAL.

 $\frac{committedIndex, \ \setminus \ *[i]: \ \text{The maximum index of trasactions}}{\text{that leader i has broadcast in $COMMIT$}}.$

committedCounter [i][j]: The latest counter of transaction

that leader i has confirmed that follower j has committed.

Variables only used when state = LEADING & zabState! = BROADCAST.

VARIABLES initialHistory, [i]: The initial history of leader i in epoch acceptedEpoch[i].

tempMaxEpoch the maximum epoch in CEPOCH the prospective leader received from followers.

Variables only used when state = FOLLOWING.

VARIABLES cepochSent, Express whether follower has sent FOLLOWERINFO to leader.

leaderAddr, Express whether follower i has connected or lost connection.

[i]: The leader id of follower i.

synced Express whether follower has completed sync with leader.

Variables about network channel.

VARIABLE msqs Simulates network channel.

msgs[i][j] means the input buffer of server j from server i.

Variables only used in verifying properties.

VARIABLES epochLeader, The set of leaders in every epoch.

proposalMsgsLog, The set of all broadcast messages.

inherent ViolatedCheck whether there are conditions contrary to the facts.

7 varia

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Variable used for recording data to constrain state space.
VARIABLE recorder Consists: members of Parameters and pc.
serverVarsZ \stackrel{\triangle}{=} \langle state, currentEpoch, lastZxid, zabState, acceptedEpoch, history, commitIndex \rangle
election Vars Z \stackrel{\Delta}{=} election Vars  6 variables
leaderVarsZ \triangleq \langle leadingVoteSet, learners, cepochRecv, ackeRecv, ackldRecv, forwarding,
                   ackIndex, currentCounter, committedCounter
                                                                                      9 variables
tempVarsZ \triangleq \langle initialHistory, tempMaxEpoch \rangle
                                                          2 variables
followerVarsZ \triangleq \langle cepochSent, leaderAddr, synced \rangle
                                                                             3 variables
verifyVarsZ \triangleq \langle proposalMsqsLoq, epochLeader, inherentViolated \rangle
                                                                             3 variables
msqVarsZ \triangleq \langle msqs, electionMsqs \rangle
                                                        2 variables
vars \triangleq \langle serverVarsZ, electionVarsZ, leaderVarsZ, tempVarsZ, followerVarsZ, verifyVarsZ, msgVarsZ, idTa
ServersIncNullPoint \triangleq Server \cup \{NullPoint\}
Zxid \triangleq
    Seq(Nat)
     \cup [epoch: Nat, counter: Nat]
HistoryItem \triangleq
     [epoch: Nat,
      counter: Nat,
      value: Value
Proposal \triangleq
    [msource: Server, mtype: \{ \text{"RECOVERYSYNC"} \}, mepoch: Nat, mproposals: Seq(HistoryItem) ] \cup
    [msource: Server, mtype: \{PROPOSAL\}, mepoch: Nat, mproposal: HistoryItem]
Message \triangleq
    [mtype: \{FOLLOWERINFO\}, mepoch: Nat] \cup
    [mtype: \{NEWLEADER\}, mepoch: Nat, mlastZxid: Zxid] \cup
    [mtype: \{ACKLD\}, mepoch: Nat] \cup
     [mtype: \{LEADERINFO\}, mepoch: Nat] \cup
    [mtype: \{ACKEPOCH\}, mepoch: Nat, mlastEpoch: Nat, mlastZxid: Zxid] \cup
    [mtype: \{UPTODATE\}, mepoch: Nat, mcommit: Nat] \cup
    [mtype: \{PROPOSAL\}, mepoch: Nat, mproposal: HistoryItem] \cup
     [mtype: \{ACK\}, mepoch: Nat, mzxid: Zxid] \cup
    [mtype: \{COMMIT\}, mepoch: Nat, mzxid: Zxid]
ElectionState \triangleq \{LOOKING, FOLLOWING, LEADING\}
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Vote \triangleq
    [proposed Leader: Servers Inc Null Point,
    proposedZxid:Zxid.
    proposedEpoch: Nat
Election Vote \triangleq
    [vote: Vote, round: Nat, state: ElectionState, version: Nat]
ElectionMsq \triangleq
    [mtype: \{NOTIFICATION\}, msource: Server, mstate: ElectionState, mround: Nat, mvote: Vote] \cup
    [mtype: \{NONE\}]
TypeOK \triangleq
    \land zabState \in [Server \rightarrow \{ELECTION, DISCOVERY, SYNCHRONIZATION, BROADCAST\}]
         acceptedEpoch \in [Server \rightarrow Nat]
         history \in [Server \rightarrow Seq(HistoryItem)]
         commitIndex \in [Server \rightarrow Nat]
        learners \in [Server \rightarrow SUBSET \ ServersIncNullPoint]
    \wedge
         cepochRecv \in [Server \rightarrow SUBSET \ ServersIncNullPoint]
         ackeRecv \in [Server \rightarrow SUBSET \ ServersIncNullPoint]
         ackldRecv \in [Server \rightarrow SUBSET \ ServersIncNullPoint]
         ackIndex \in [Server \rightarrow [Server \rightarrow Nat]]
          currentCounter \in [Server \rightarrow Nat]
      \land \ sendCounter \in \ [Server \rightarrow Nat]
      \land committedIndex \in [Server \rightarrow Nat]
    \land committedCounter \in [Server \rightarrow [Server \rightarrow Nat]]
    \land forwarding \in [Server \rightarrow SUBSET ServersIncNullPoint]
    \land initialHistory \in [Server \rightarrow Seq(HistoryItem)]
    \land tempMaxEpoch \in [Server \rightarrow Nat]
    \land cepochSent \in [Server \rightarrow BOOLEAN]
    \land leaderAddr \in [Server \rightarrow ServersIncNullPoint]
    \land synced \in [Server \rightarrow BOOLEAN]
    \land proposalMsgsLog \in \text{SUBSET } Proposal
    \land epochLeader \in [1 .. MAXEPOCH \rightarrow SUBSET ServersIncNullPoint]
    \land inherentViolated \in BOOLEAN
    \land forwarding \in [Server \rightarrow SUBSET Server]
    \land msgs \in [Server \rightarrow [Server \rightarrow Seq(Message)]]
     Fast Leader Election
    \land electionMsgs \in [Server \rightarrow [Server \rightarrow Seq(ElectionMsg)]]
    \land recvQueue \in [Server \rightarrow Seq(ElectionMsg)]
    \land leadingVoteSet \in [Server \rightarrow SUBSET Server]
    \land receiveVotes \in [Server \rightarrow [Server \rightarrow ElectionVote]]
    \land currentVote \in [Server \rightarrow Vote]
    \land outOfElection \in [Server \rightarrow [Server \rightarrow ElectionVote]]
    \land lastZxid \in [Server \rightarrow Zxid]
    \land state \in [Server \rightarrow ElectionState]
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Return the maximum value from the set S
Maximum(S) \stackrel{\triangle}{=} \text{ if } S = \{\} \text{ Then } -1
                                          ELSE CHOOSE n \in S : \forall m \in S : n > m
 Return the minimum value from the set S
Minimum(S) \stackrel{\triangle}{=} \text{ IF } S = \{\} \text{ THEN } -1
                                          ELSE CHOOSE n \in S : \forall m \in S : n \leq m
 Check server state
IsLeader(s) \stackrel{\triangle}{=} state[s] = LEADING
IsFollower(s) \triangleq state[s] = FOLLOWING
IsLooking(s) \stackrel{\triangle}{=} state[s] = LOOKING
\begin{array}{ll} \textit{IsMyLearner}(i,j) & \triangleq j \in \textit{learners}[i] \\ \textit{IsMyLeader}(i,j) & \triangleq \textit{leaderAddr}[i] = j \\ \textit{HasNoLeader}(i) & \triangleq \textit{leaderAddr}[i] = \textit{NullPoint} \end{array}
                            \stackrel{\Delta}{=} leaderAddr[i] \neq NullPoint
HasLeader(i)
  Check if s is a quorum
IsQuorum(s) \stackrel{\Delta}{=} s \in Quorums
 Check zxid state
ToZxid(z) \stackrel{\Delta}{=} [epoch \mapsto z[1], counter \mapsto z[2]]
PZxidEqual(p, z) \stackrel{\triangle}{=} p.epoch = z[1] \land p.counter = z[2]
TransactionEqual(t1, t2) \stackrel{\triangle}{=} \land t1.epoch = t2.epoch
                                            \land t1.counter = t2.counter
TransactionPrecede(t1, t2) \triangleq \lor t1.epoch < t2.epoch
                                               \vee \wedge t1.epoch = t2.epoch
                                                   \land t1.counter < t2.counter
  Actions about recorder
GetParameter(p) \stackrel{\Delta}{=} \text{ if } p \in \text{Domain } Parameters \text{ Then } Parameters[p] \text{ else } 0
RecorderGetHelper(m) \stackrel{\triangle}{=} (m:> recorder[m])
RecorderIncHelper(m) \triangleq (m :> recorder[m] + 1)
                                             \stackrel{\triangle}{=} RecorderIncHelper("nTimeout")
RecorderIncTimeout
                                            \triangleq RecorderGetHelper("nTimeout")
Recorder Get Timeout
RecorderSetTransactionNum \stackrel{\triangle}{=} ("nTransaction" :>
                                                           Let s \stackrel{\Delta}{=} \text{ choose } i \in Server :
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 $\land waitNotmsg \in [Server \rightarrow BOOLEAN]$ $\land currentEpoch \in [Server \rightarrow Nat]$ $\land logicalClock \in [Server \rightarrow Nat]$

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\forall j \in Server : Len(history'[i]) \ge Len(history'[j])
                                                  IN Len(history'[s])
                                      \stackrel{\Delta}{=} ("maxEpoch":>
RecorderSetMaxEpoch
                                                  Let s \stackrel{\triangle}{=} \text{Choose } i \in Server :
                                                       \forall j \in Server : acceptedEpoch'[i] \geq acceptedEpoch'[j]
                                                  IN acceptedEpoch'[s])
                                      \stackrel{\Delta}{=} ("pc":> pc)
RecorderSetPc(pc)
                                      \stackrel{\triangle}{=} CASE pc[1] = "Timeout"
RecorderSetFailure(pc)
                                                                                 \rightarrow RecorderIncTimeout
                                                 pc[1] = \text{``LeaderTimeout''} \rightarrow RecorderIncTimeout'
                                                 pc[1] = "FollowerTimout" \rightarrow RecorderIncTimeout
                                          OTHER
                                                                                  \rightarrow RecorderGetTimeout
UpdateRecorder(pc) \stackrel{\triangle}{=} recorder' = RecorderSetFailure(pc) @@ RecorderSetTransactionNum
                                              @@ RecorderSetMaxEpoch @@ RecorderSetPc(pc) @@ recorder
UnchangeRecorder \triangleq UnchangeD recorder
CheckParameterHelper(n, p, Comp(\_, \_)) \stackrel{\triangle}{=} IF p \in DOMAIN Parameters
                                                           THEN Comp(n, Parameters[p])
                                                           ELSE TRUE
CheckParameterLimit(n, p) \stackrel{\triangle}{=} CheckParameterHelper(n, p, LAMBDA i, j : i < j)
                              \stackrel{\triangle}{=} CheckParameterLimit(recorder.nTimeout,
CheckTimeout
                                                                                              "MaxTimeoutFailures")
CheckTransactionNum \triangleq CheckParameterLimit(recorder.nTransaction, "MaxTransactionNum")
CheckEpoch
                              \stackrel{\triangle}{=} CheckParameterLimit(recorder.maxEpoch,
                                                                                              "MaxEpoch")
CheckStateConstraints \triangleq CheckTimeout \land CheckTransactionNum \land CheckEpoch
 Actions about network
PendingFOLLOWERINFO(i, j) \stackrel{\Delta}{=} \land msgs[j][i] \neq \langle \rangle
                                               \land \mathit{msgs}[j][i][1].\mathit{mtype} = \mathit{FOLLOWERINFO}
                                          \stackrel{\Delta}{=} \wedge msgs[j][i] \neq \langle \rangle
PendingLEADERINFO(i, j)
                                               \land msgs[j][i][1].mtype = LEADERINFO
                                          \stackrel{\Delta}{=} \wedge msgs[j][i] \neq \langle \rangle
PendingACKEPOCH(i, j)
                                               \land \mathit{msgs}[j][i][1].\mathit{mtype} = \mathit{ACKEPOCH}
PendingNEWLEADER(i, j)
                                              \land msgs[j][i] \neq \langle \rangle
                                               \land \, msgs[j][i][1].mtype = NEWLEADER
                                           \stackrel{\Delta}{=} \wedge msgs[j][i] \neq \langle \rangle
PendingACKLD(i, j)
                                               \land msgs[j][i][1].mtype = ACKLD
                                           \stackrel{\Delta}{=} \wedge msgs[j][i] \neq \langle \rangle
PendingUPTODATE(i, j)
                                               \land \ msgs[j][i][1].mtype = \mathit{UPTODATE}
                                          \stackrel{\Delta}{=} \land msgs[j][i] \neq \langle \rangle
PendingPROPOSAL(i, j)
                                               \land \ msgs[j][i][1].mtype = PROPOSAL
PendingACK(i, j)
                                               \land msgs[j][i] \neq \langle \rangle
                                               \land msgs[j][i][1].mtype = ACK
                                          \stackrel{\Delta}{=} \wedge msgs[j][i] \neq \langle \rangle
PendingCOMMIT(i, j)
                                               \land msgs[j][i][1].mtype = COMMIT
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Add a message to msgs – add a message m to msgs.
Send(i, j, m) \stackrel{\triangle}{=} msgs' = [msgs \ \text{EXCEPT} \ ![i][j] = Append(msgs[i][j], m)]
 Remove a message from msgs — discard head of msgs.
Discard(i, j) \stackrel{\triangle}{=} msgs' = \text{IF } msgs[i][j] \neq \langle \rangle \text{ THEN } [msgs \text{ except } ![i][j] = Tail(msgs[i][j])]
                                                         ELSE msqs
 Leader broadcasts a message(PROPOSAL/COMMIT) to all other servers in forwardingFollowers.
Broadcast(i, m) \stackrel{\triangle}{=} msgs' = [msgs \ \text{EXCEPT} \ ![i] = [v \in Server \mapsto \text{IF} \ \land v \in forwarding[i]]
                                                                                          \wedge v \neq i
                                                                                      THEN Append(msqs[i][v], m)
                                                                                      ELSE msgs[i][v]]
Broadcast(i, m) \stackrel{\Delta}{=} msgs' = [msgs \ \text{except } ![i] = [v \in Server \mapsto \text{if } \land v \in forwarding[i]]
                                                   \land \lor \land m.mtype = PROPOSAL
                                                        \land \ ackIndex[i][v] < \ Len(initialHistory[i]) +
                                                       m.mproposal.counter
                                                     \lor \land m.mtype = COMMIT
                                                       \land committedCounter[i][v] < m.mzxid[2]
                                                  THEN Append(msgs[i][v], m)
                                                  ELSE msgs[i][v]]
DiscardAndBroadcast(i, j, m) \triangleq
          msgs' = [msgs \ EXCEPT \ ![j][i] = Tail(msgs[j][i]),
                                         ![i] = [v \in Server \mapsto IF \land v \in forwarding[i]]
                                                                        \wedge v \neq i
                                                                      THEN Append(msgs[i][v], m)
                                                                      ELSE msgs[i][v]]
 Leader broadcasts LEADERINFO to all other servers in connectingFollowers.
BroadcastLEADERINFO(i, m) \stackrel{\Delta}{=} msgs' = [msgs \ \text{EXCEPT} \ ![i] = [v \in Server \mapsto \text{IF} \land v \in cepochRecv[i]]
                                                                                                              \land v \in learners[i]
                                                                                                              \land v \neq i \text{ THEN } Append(m_i)
                                                                                                                        ELSE msgs[i][v]]
 Leader broadcasts UPTODATE to all other servers in newLeaderProposal.
BroadcastUPTODATE(i, m) \triangleq msgs' = [msgs \ \text{EXCEPT} \ ![i] = [v \in Server \mapsto \text{IF} \ \land v \in ackldRecv[i]]
                                                                                                           \land v \in learners[i]
                                                                                                          \land v \neq i \text{ THEN } Append(msgs
                                                                                                                     ELSE msgs[i][v]]]
 Combination of Send and Discard — discard head of msgs[j][i] and add m into msgs.
Reply(i, j, m) \stackrel{\triangle}{=} msgs' = [msgs \ \text{EXCEPT} \ ![j][i] = Tail(msgs[j][i]),
                                                       ![i][j] = Append(msgs[i][j], m)
 Shuffle the input buffer from server j(i) in server i(j).
Clean(i, j) \triangleq msgs' = [msgs \ \text{EXCEPT} \ ![j][i] = \langle \rangle, \ ![i][j] = \langle \rangle]
```

Define initial values for all variables

 $InitServerVarsZ \triangleq \land InitServerVars \\ \land zabState = [s \in Server \mapsto ELECTION]$

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\land acceptedEpoch = [s \in Server \mapsto 0]
                                           = [s \in Server \mapsto \langle \rangle]
                            \land history
                            \land commitIndex = [s \in Server \mapsto 0]
InitLeaderVarsZ \triangleq \land InitLeaderVars
                           \land learners
                                                     = [s \in Server \mapsto \{\}]
                           \land \ ackldRecv
                                                   = [s \in Server \mapsto \{\}]
                            \land \ ackIndex
                                                     = [s \in Server \mapsto [v \in Server \mapsto 0]]
                            \land currentCounter = [s \in Server \mapsto 0]
                             \land \ sendCounter \qquad = \ [s \in Server \mapsto 0]
                             \land committedIndex = [s \in Server \mapsto 0]
                            \land committedCounter = [s \in Server \mapsto [v \in Server \mapsto 0]]
                                                     = [s \in Server \mapsto \{\}]
                            \land forwarding
InitElectionVarsZ \triangleq InitElectionVars
InitTempVarsZ \stackrel{\triangle}{=} \land initialHistory = [s \in Server \mapsto \langle \rangle]
                          \land tempMaxEpoch = [s \in Server \mapsto 0]
InitFollowerVarsZ \stackrel{\Delta}{=} \land cepochSent = [s \in Server \mapsto FALSE]
                              \land leaderAddr = [s \in Server \mapsto NullPoint]
                                              = [s \in Server \mapsto FALSE]
                              \land synced
InitVerifyVarsZ \stackrel{\triangle}{=} \land proposalMsgsLog = \{\}
                           \land epochLeader = [i \in 1 .. MAXEPOCH \mapsto \{\}]
                           \land inherentViolated = False
InitMsgVarsZ \stackrel{\Delta}{=} \land msgs \qquad = [s \in Server \mapsto [v \in Server \mapsto \langle \rangle]]
                        \land electionMsgs = [s \in Server \mapsto [v \in Server \mapsto \langle \rangle]]
InitRecorder \stackrel{\triangle}{=} recorder = [nTimeout]
                                       nTransaction \mapsto 0,
                                       maxEpoch
                                                          \mapsto 0,
                                                          \mapsto \langle \text{"InitZ"} \rangle
InitZ \triangleq \land InitServerVarsZ
             \wedge InitLeaderVarsZ
             \land InitElectionVarsZ
             \wedge InitTempVarsZ
             \land InitFollowerVarsZ
             \wedge InitVerifyVarsZ
             \land InitMsgVarsZ
             \wedge idTable = InitializeIdTable(Server)
             \land \ InitRecorder
```

```
ZabTurnToLeading(i) \triangleq
         \land zabState'
                              = [zabState \ EXCEPT ![i] = DISCOVERY]
         \land learners'
                              = [learners \quad EXCEPT \ ![i] = \{i\}]
                              = [cepochRecv EXCEPT ![i] = \{i\}]
         \land cepochRecv'
         \land ackeRecv'
                              = [ackeRecv \quad EXCEPT \ ![i] = \{i\}]
         \land \ ackldRecv'
                              = [ackldRecv \ EXCEPT \ ![i] = \{i\}]
         \land forwarding'
                              = [forwarding \ EXCEPT \ ![i] = \{\}]
                              = [ackIndex \quad \text{EXCEPT } ![i] = [v \in Server \mapsto \text{IF } v = i \text{ THEN } Len(history[i])]
         \land ackIndex'
                                                                                              ELSE 0]]
                                 = [currentCounter \quad \text{EXCEPT } ![i] = 0]
         \land currentCounter'
         \land commitIndex'
                                 = [commitIndex]
                                                          EXCEPT ![i] = 0
                                                    EXCEPT ![i] = 0
          \land sendCounter'
                             = [sendCounter]
          \land committedIndex' = [committedIndex \ \ \texttt{EXCEPT} \ ![i] = 0]
         \land committedCounter' = [committedCounter except ![i] = [v \in Server \mapstructure IF v = i then Len(history)]
                                                                                                           ELSE 0]]
         \land initialHistory' = [initialHistory \ EXCEPT \ ![i]]
                                                                      = history[i]
         \land tempMaxEpoch' = [tempMaxEpoch \ EXCEPT \ ![i] = acceptedEpoch[i]]
ZabTurnToFollowing(i) \triangleq
         \land zabState'
                            = [zabState \ EXCEPT \ ![i] = DISCOVERY]
         \land cepochSent'
                            = [cepochSent EXCEPT ![i] = FALSE]
         \land synced'
                            =[synced]
                                            EXCEPT ![i] = FALSE
         \land commitIndex' = [commitIndex]
                                                     EXCEPT ![i] = 0
 Fast Leader Election
FLEReceiveNotmsg(i, j) \triangleq
         \land ReceiveNotmsq(i, j)
         \land UNCHANGED \langle zabState, acceptedEpoch, history, commitIndex, learners, cepochRecv,
                            ackeRecv, ackldRecv, forwarding, ackIndex, currentCounter,
                            committedCounter,\ temp\ Vars\ Z,\ follower\ Vars\ Z,\ verify\ Vars\ Z,\ msgs 
angle
         \land UpdateRecorder(\langle "FLEReceiveNotmsg", i, j \rangle)
FLENotmsgTimeout(i) \stackrel{\Delta}{=}
         \land NotmsgTimeout(i)
         \land UNCHANGED \langle zabState, acceptedEpoch, history, commitIndex, learners, cepochRecv, ackeRecv, ackle
                            forwarding, ackIndex, currentCounter, committedCounter,
                            tempVarsZ, followerVarsZ, verifyVarsZ, msgs
         \land UpdateRecorder(\langle "FLENotmsgTimeout", i \rangle)
FLEHandleNotmsg(i) \triangleq
          \land \  \, HandleNotmsg(i) \\ \land \  \, \text{let} \  \, newState \ \stackrel{\triangle}{=} \  \, state'[i] 
            \lor \land newState = LEADING
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 $\wedge ZabTurnToLeading(i)$

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\land UNCHANGED \langle cepochSent, synced \rangle
           \lor \land newState = FOLLOWING
             \wedge ZabTurnToFollowing(i)
             ∧ UNCHANGED ⟨learners, cepochRecv, ackeRecv, ackldRecv, forwarding, ackIndex, currentCounter
                                 committedCounter, tempVarsZ
           \lor \land newState = LOOKING
             \land UNCHANGED \langle zabState, learners, cepochRecv, ackeRecv, ackldRecv, forwarding, ackIndex,
                                currentCounter, commitIndex,
                                committedCounter, tempVarsZ, cepochSent, synced
        \land UNCHANGED \langle acceptedEpoch, history, leaderAddr, verifyVarsZ, msgs <math>\rangle
        \land UpdateRecorder(\langle \text{"FLEHandleNotmsg"}, i \rangle)
On the premise that ReceiveVotes.HasQuorums = TRUE, corresponding to logic in line 1050 - 1055 in LFE.java.
FLEWaitNewNotmsq(i) \stackrel{\Delta}{=}
        \land WaitNewNotmsg(i)
        \land UNCHANGED \langle zabState, acceptedEpoch, history, commitIndex, learners, cepochRecv, ackeRecv,
                          ackldRecv, forwarding, ackIndex, currentCounter,
                          committedCounter, tempVarsZ, followerVarsZ, verifyVarsZ, msgs
        \land UpdateRecorder(\langle "FLEWaitNewNotmsg", i \rangle)
On the premise that Receive Votes. Has Quorums = TRUE, corresponding to logic in line 1061 - 1066 in LFE. java.
FLEWaitNewNotmsqEnd(i) \triangleq
        \land \ WaitNewNotmsgEnd(i)
        \land LET newState \stackrel{\triangle}{=} state'[i]
           \lor \land newState = LEADING
             \land ZabTurnToLeading(i)
             \land UNCHANGED \langle cepochSent, synced \rangle
           \lor \land newState = FOLLOWING
             \wedge ZabTurnToFollowing(i)
             ∧ UNCHANGED ⟨learners, cepochRecv, ackeRecv, ackldRecv, forwarding, ackIndex, currentCounter
                                 committedCounter, tempVarsZ\rangle
           \lor \land newState = LOOKING
             ∧ PrintT ("New state is LOOKING in FLEWaitNewNotmsgEnd, which should not happen.")
             \land UNCHANGED \langle zabState, learners, cepochRecv, ackeRecv, ackldRecv, forwarding, ackIndex,
                                currentCounter, commitIndex,
                                committedCounter, tempVarsZ, cepochSent, synced
        \land UNCHANGED \langle acceptedEpoch, history, leaderAddr, verifyVarsZ, msgs <math>\rangle
        \land UpdateRecorder(\langle "FLEWaitNewNotmsgEnd", i \rangle)
 Describe how a server transitions from LEADING/FOLLOWING to LOOKING.
FollowerShutdown(i) \triangleq
        \wedge ZabTimeout(i)
        \land zabState' = [zabState \ EXCEPT ![i] = ELECTION]
        \land leaderAddr' = [leaderAddr \ EXCEPT \ ![i] = NullPoint]
```

```
LeaderShutdown(i) \stackrel{\Delta}{=}
        \wedge ZabTimeout(i)
                       = [zabState \quad EXCEPT \ ![i] = ELECTION]
        \land leaderAddr' = [s \in Server \mapsto \text{if } s \in learners[i] \text{ Then } NullPoint \text{ else } leaderAddr[s]]
        \land learners' = [learners \ EXCEPT \ ![i] = \{\}]
        \land forwarding' = [forwarding \ EXCEPT \ ![i] = \{\}]
                       = [s \in Server \mapsto [v \in Server \mapsto \texttt{IF} \ v \in learners[i] \lor s \in learners[i]
        \land msgs'
                                                            THEN \langle \rangle ELSE msgs[s][v]]
RemoverLearner(i, j) \triangleq
        \land learners' = [learners \ EXCEPT \ ![i] = learners[i] \setminus \{j\}]
        \land forwarding' = [forwarding except ![i] = if j \in forwarding[i] then forwarding[i] \setminus \{j\} else forwarding
        \land cepochRecv' = [cepochRecv except ![i] = if j \in cepochRecv[i] then cepochRecv[i] \{j} else cepoch
        \wedge \ ackIndex' = [ackIndex \ EXCEPT \ ![i][j] = 0]
        \land committedCounter' = [committedCounter \ \texttt{EXCEPT} \ ![i][j] = 0]
FollowerTimout(i) \triangleq
        \land IsFollower(i)
        \land HasNoLeader(i)
        \land FollowerShutdown(i)
        \land msgs' = [s \in Server \mapsto [v \in Server \mapsto if v = i \text{ Then } \langle \rangle \text{ else } msgs[s][v]]]
        \land UNCHANGED \(\alpha\) accepted Epoch, history, commitIndex, learners, cepoch Recv, acke Recv, ackld Recv,
                          forwarding, ackIndex, currentCounter, committedCounter,
                          tempVarsZ, cepochSent, synced, verifyVarsZ
        \land \ UpdateRecorder(\langle \, \text{``FollowerTimout''}, \ i \rangle)
LeaderTimeout(i) \triangleq
        \wedge IsLeader(i)
        \land \neg IsQuorum(learners[i])
        \wedge LeaderShutdown(i)
        \land UNCHANGED \land acceptedEpoch, history, commitIndex, cepochRecv, ackeRecv, ackldRecv, ackIndex, cu
                          committedCounter, tempVarsZ, cepochSent, synced, verifyVarsZ\rangle
        \land UpdateRecorder(\langle "LeaderTimeout", i \rangle)
  Establish connection between leader i and follower j. It means i creates a learner Handler for
  communicating with j, and j finds i's address.
EstablishConnection(i, j) \triangleq
        \wedge IsLeader(i)
        \wedge IsFollower(j)
        \wedge \neg IsMyLearner(i, j)
        \land HasNoLeader(i)
        \land currentVote[j].proposedLeader = i
        \land learners' = [learners \ EXCEPT \ ![i] = learners[i] \cup \{j\}] Leader: 'addLearnerHandler(peer)'
        \wedge leaderAddr' = [leaderAddr \ EXCEPT \ ![j] = i]
                                                                            Follower: 'connectToLeader(addr, hostname)'
```

```
\land UNCHANGED \langle serverVarsZ, electionVarsZ, leadingVoteSet, cepochRecv, ackeRecv, ackldRecv, forwarder for a contract of the server varsZ acker for a contract of the contract of the server varsZ acker for a contract of the contract of t
                                                       ackIndex, currentCounter, committedCounter, tempVarsZ,
                                                       cepochSent, synced, verifyVarsZ, msgVarsZ, idTable
                 \land UpdateRecorder(\langle "EstablishConnection", i, j \rangle)
 The leader i finds timeout and TCP connection between i and j closes.
Timeout(i, j) \triangleq
                      \wedge IsLeader(i)
                     \land IsFollower(j)
                     \land IsMyLearner(i, j)
                      \wedge IsMyLeader(j, i)
                       The action of leader i.(corresponding\ to\ function'remove Learner Handler(peer)'.)
                      \land RemoverLearner(i, j)
                       The action of follower j.
                      \land FollowerShutdown(j)
                       Clean channel between i and j.
                      \wedge Clean(i, j)
                      \land UNCHANGED \langle acceptedEpoch, history, commitIndex, currentCounter,
                                                            tempVarsZ, cepochSent, synced, verifyVarsZ
                     \land UpdateRecorder(\langle "Timeout", i, j \rangle)
  Follower sends f.p to leader via FOLLOWERINFO(CEPOCH).
FollowerSendFOLLOWERINFO(i) \triangleq
                 \land IsFollower(i)
                 \land zabState[i] = DISCOVERY
                 \wedge HasLeader(i)
                 \land \neg cepochSent[i]
                 \land Send(i, leaderAddr[i], [mtype \mapsto FOLLOWERINFO,
                                                                            mepoch \mapsto acceptedEpoch[i])
                 \land cepochSent' = [cepochSent \ EXCEPT \ ![i] = TRUE]
                 ∧ UNCHANGED \(\serverVarsZ\), \(\leftlef{leaderVarsZ}\), \(\leftlef{leaderVarsZ}\), \(\text{tempVarsZ}\), \(\text{tempVarsZ}\), \(\text{leaderAddr}\), \(\symma\)
                                                       verifyVarsZ, electionMsgs, idTable
                 \land UpdateRecorder(\langle "FollowerSendFOLLOWERINFO", i \rangle)
   Leader waits for receiving FOLLOWERINFO from a quorum, and then chooses a new epoch
   e' as its own epoch and broadcasts LEADERINFO.
LeaderHandleFOLLOWERINFO(i, j) \triangleq
                 \wedge IsLeader(i)
                 \land PendingFOLLOWERINFO(i, j)
                 \wedge \text{ LET } msq \stackrel{\triangle}{=} msqs[j][i][1]
                                 \lor 1. has not broadcast LEADERINFO - modify tempMaxEpoch
                                        \land NullPoint \notin cepochRecv[i]
                                        \land LET newEpoch \stackrel{\triangle}{=} Maximum(\{tempMaxEpoch[i], msg.mepoch\})
                                                       tempMaxEpoch' = [tempMaxEpoch Except ! [i] = newEpoch]
                                        \wedge Discard(i, i)
```

```
2. has broadcast LEADERINFO — no need to handle the msg, just send LEADERINFO to corresponding
                                       \land NullPoint \in cepochRecv[i]
                                       \land Reply(i, j, [mtype \mapsto LEADERINFO,
                                                                       mepoch \mapsto acceptedEpoch[i])
                                       \land UNCHANGED tempMaxEpoch
                 \land cepochRecv' = [cepochRecv \ Except \ ![i] = \text{if} \ j \in cepochRecv[i] \ \text{then} \ cepochRecv[i]
                                                                                                                                                                   ELSE cepochRecv[i] \cup \{j\}]
                 \land UNCHANGED \land server \lor ars Z, follower \lor ars Z, election \lor ars Z, initial \lor is the initial \lor becomes \lor and \lor are \lor 
                                                      ackeRecv, ackldRecv, forwarding, ackIndex, currentCounter,
                                                      committedCounter,\ verifyVarsZ,\ electionMsgs,\ idTable 
angle
                 \land UpdateRecorder(\langle "LeaderHandleFOLLOWERINFO", i, j \rangle)
LeaderBroadcastLEADERINFO(i) \triangleq
                \land IsLeader(i)
                 \land zabState[i] = DISCOVERY
                \land IsQuorum(cepochRecv[i])
                 \land acceptedEpoch' = [acceptedEpoch \ EXCEPT \ ![i] = tempMaxEpoch[i] + 1]
                 \land cepochRecv' = [cepochRecv]
                                                                                            EXCEPT ![i] = cepochRecv[i] \cup \{NullPoint\}]
                 \land BroadcastLEADERINFO(i, [mtype \mapsto LEADERINFO,
                                                                                      mepoch \mapsto acceptedEpoch'[i])
                 \land UNCHANGED \langle state, currentEpoch, lastZxid, zabState, history, commitIndex, electionVarsZ,
                                                     leadingVoteSet,\ learners,\ ackeRecv,\ ackldRecv,\ forwarding,\ ackIndex,\ currentCounter
                                                     committedCounter, tempVarsZ, followerVarsZ, verifyVarsZ,
                                                      electionMsqs, idTable
                 \land UpdateRecorder(\langle "LeaderBroadcastLEADERINFO", i \rangle)
   In phase f12, follower receives NEWEPOCH. If e' > f.p, then follower sends ACK-E back, and
   ACK-E contains f.a and lastZxid to let leader judge whether it is the latest. After handling
   NEWEPOCH, follower's zabState turns to SYNCHRONIZATION.
FollowerHandleLEADERINFO(i, j) \stackrel{\Delta}{=}
                 \land IsFollower(i)
                 \land PendingLEADERINFO(i, j)
                                                     \stackrel{\triangle}{=} msgs[j][i][1]
                 \wedge LET msq
                                infoOk \triangleq IsMyLeader(i, j)
                                epochOk \triangleq \land infoOk
                                                             \land msg.mepoch \ge acceptedEpoch[i]
                                                    \triangleq \land epochOk
                                correct
                                                             \land zabState[i] = DISCOVERY
                                \wedge infoOk
                                 ∧ ∨ 1. Normal case
                                            \land epochOk
                                            \land \lor \land correct
                                                        \land acceptedEpoch' = [acceptedEpoch EXCEPT ! [i] = msq.mepoch]
                                                                                                                 \mapsto ACKEPOCH,
                                                        \land Reply(i, j, [mtype])
                                                                                                                 \mapsto msq.mepoch,
                                                                                       meroch
                                                                                       mlastEpoch \mapsto currentEpoch[i],
```

```
\wedge Discard(j, i)
                                                                             \land UNCHANGED \langle acceptedEpoch, cepochSent \rangle
                                                              \land zabState' = [zabState \ \ \text{except} \ ![i] = \ \text{if} \ zabState[i] = DISCOVERY \ \ \text{then} \ SYNCHRONGED
                                                                                                                                                                                                                                                                                      ELSE zabState[i]
                                                             \land UNCHANGED \langle varsL, leaderAddr \rangle
                                                      V 2. Abnormal case - go back to election
                                                              \land \neg epochOk
                                                              \land FollowerShutdown(i)
                                                              \wedge Clean(i, j)
                                                              \land UNCHANGED \langle acceptedEpoch, cepochSent, inherentViolated <math>\rangle
                        \land UNCHANGED \langle history, commitIndex, learners, cepochRecv, ackeRecv, ackldRecv, forwarding, ackInd
                                                                           current Counter, committed Counter, temp Vars Z, synced, proposal Msqs Loq, epoch Lead
                        \land UpdateRecorder(\langle "FollowerHandleLEADERINFO", i, j \rangle)
   Abstraction of actions making follower synced with leader before leader sending NEWLEADER.
SubRECOVERYSYNC(i, j) \triangleq
                      LET canSync \triangleq \land IsLeader(i) \land zabState[i] \neq DISCOVERY
                                                                                                                                                                                                                                                      \land IsMyLearner(i, j)
                                                                             \land IsFollower(j) \land zabState[j] = SYNCHRONIZATION \land IsMyLeader(j, i)
                                                                             \land synced[j] = FALSE
                      IN
                        \lor \land canSync
                                \land history'
                                                                           = [history]
                                                                                                                       EXCEPT ![j] = history[i]
                                \wedge lastZxid'
                                                                           = [lastZxid]
                                                                                                                   EXCEPT ![j] = lastZxid[i]]
                                \land \ \mathit{UpdateProposal}(j, \ \mathit{leaderAddr}[j], \ \mathit{lastZxid'}[j], \ \mathit{currentEpoch}[j])
                                \land commitIndex' = [commitIndex \ EXCEPT \ ![j] = commitIndex[i]]
                                                                                 = [synced]
                                                                                                                               EXCEPT ![j] = TRUE
                                \land synced'
                                \land forwarding'
                                                                                 = [forwarding \ EXCEPT \ ![i] = forwarding[i] \cup \{j\}]
                                                                                                                                                                                                                                                            j will join traffic, and receive P
                                                                                 = [ackIndex \quad \text{EXCEPT } ![i][j] = Len(history[i])]
                                \land ackIndex'
                                \land committedCounter' = [committedCounter \ \ \texttt{EXCEPT} \ ![i][j] = Maximum(\{commitIndex[i] - Len(inter(i))\}) + (committedCounter') 
                                \land LET ms \triangleq [msource \mapsto i, mtype \mapsto "RECOVERYSYNC", mepoch <math>\mapsto acceptedEpoch[i], mproposalset is a constant.
                                      in proposalMsgsLog' = \text{if } ms \in proposalMsgsLog \text{ then } proposalMsgsLog
                                                                                                                                                                                                    ELSE proposalMsgsLog \cup \{ms\}
                                \land UNCHANGED inherentViolated
                        \vee \wedge \neg canSync
                                \land PrintT( "Exception: Leader wants to sync with follower while the condition doesn't allow.")
                                \wedge inherent Violated' = TRUE
                                \land UNCHANGED \langle history, lastZxid, currentVote, commitIndex, synced, forwarding, ackIndex, ack
     Leader waits for receiving ACKEPOPCH from a quorum, and check whether it has the latest
     history and epoch from them. If so, leader's zabState turns to SYNCHRONIZATION.
```

 $mlastZxid \mapsto lastZxid[i]])$ $\land cepochSent' = [cepochSent \ \texttt{EXCEPT} \ ![i] = \texttt{TRUE}]$

 $\land PrintT$ ("Exception: Follower receives LEADERINFO while its ZabState is not DISCO"

∧ UNCHANGED inherent Violated

 \wedge inherent Violated' = TRUE

 $\vee \wedge \neg correct$

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```
LeaderHandleACKEPOCH(i, j) \triangleq
         \land IsLeader(i)
         \land PendingACKEPOCH(i, j)
         \wedge LET msg \stackrel{\triangle}{=} msgs[j][i][1]
                 infoOk \triangleq \land IsMyLearner(i, j)
                               \land acceptedEpoch[i] = msg.mepoch
                 logOk
                               logOk represents whether leader is more up-to-date than follower
                               \wedge infoOk
                               \land \lor currentEpoch[i] > msq.mlastEpoch
                                  \lor \land currentEpoch[i] = msg.mlastEpoch
                                     \land \lor lastZxid[i][1] > msg.mlastZxid[1]
                                        \lor \land lastZxid[i][1] = msg.mlastZxid[1]
                                           \land lastZxid[i][2] \ge msg.mlastZxid[2]
                 replyOk \triangleq \land infoOk
                                \land NullPoint \in ackeRecv[i]
                 \wedge infoOk
                  \land \lor \land replyOk
                        \land SubRECOVERYSYNC(i, j)
                        \land ackeRecv' = [ackeRecv \ Except \ ![i] = \text{if} \ j \notin ackeRecv[i] \ \text{then} \ ackeRecv[i] \cup \{j\}
                                                                                               ELSE ackeRecv[i]
                        \land Reply(i, j, [mtype])
                                                     \mapsto NEWLEADER,
                                         mepoch
                                                     \mapsto acceptedEpoch[i],
                                         mlastZxid \mapsto lastZxid[i]
                        \land UNCHANGED \langle state, currentEpoch, logicalClock, receiveVotes, outOfElection, recvQueue
                                           leadingVoteSet, electionMsgs, idTable, zabState, leaderAddr, learners
                     \lor \land \neg replyOk
                        ∧ ∨ normal case
                              \wedge logOk
                              \land ackeRecv' = [ackeRecv \ EXCEPT \ ![i] = IF \ j \notin ackeRecv[i] \ THEN \ ackeRecv[i] \cup \{j\}
                                                                                                     ELSE ackeRecv[i]
                              \wedge Discard(j, i)
                              \land UNCHANGED \langle varsL, zabState, leaderAddr, learners, forwarding <math>\rangle
                           V go back to election since there exists follower more up-to-date than leader
                              \wedge \neg logOk
                              \wedge LeaderShutdown(i)
                              \land UNCHANGED ackeRecv
                        \land UNCHANGED \langle history, commitIndex, synced, forwarding, ackIndex,
                                            committedCounter, proposalMsgsLog, inherentViolated \rangle
         \land UNCHANGED \langle acceptedEpoch, cepochRecv, ackldRecv, currentCounter,
                             tempVarsZ, cepochSent, epochLeader
         \land UpdateRecorder(\langle \text{"LeaderHandleACKEPOCH"}, i, j \rangle)
LeaderTransitionToSynchronization(i) \stackrel{\Delta}{=}
         \wedge IsLeader(i)
         \land zabState[i] = DISCOVERY
```

```
\land IsQuorum(ackeRecv[i])
        \land zabState'
                           = [zabState]
                                               EXCEPT ![i] = SYNCHRONIZATION]
        \land \ currentEpoch' \ = [currentEpoch \ \ Except \ ![i] \ = \ acceptedEpoch[i]]
        \land initialHistory' = [initialHistory \ EXCEPT \ ![i] = history[i]]
                                                EXCEPT ![i] = ackeRecv[i] \cup \{NullPoint\}]
        \land ackeRecv'
                            = [ackeRecv]
        \land ackIndex'
                           = [ackIndex]
                                                EXCEPT ![i][i] = Len(history[i])]
        \land UpdateProposal(i, i, lastZxid[i], currentEpoch'[i])
        \wedge LET epoch \stackrel{\triangle}{=} acceptedEpoch[i]
          IN epochLeader' = [epochLeader \ EXCEPT \ ! [epoch] = epochLeader[epoch] \cup \{i\}]
        \land UNCHANGED \langle state, lastZxid, acceptedEpoch, history, commitIndex, logicalClock, receiveVotes, outC
                          recvQueue, waitNotmsg, leadingVoteSet, learners, cepochRecv, ackldRecv, forwarding
                          committedCounter, tempMaxEpoch, followerVarsZ, proposalMsgsLog,
                          inherent Violated, msg Vars Z, id Table \rangle
        \land UpdateRecorder(\langle "LeaderTransitionToSynchronization", i \rangle)
 Note: Set cepochRecv,
                           ackeRecv,
                                         ackldRecv to \{NullPoint\} in
        three actions to make sure that the prospective leader will not broadcast
        NEWEPOCH/NEWLEADER/COMMITLD twice.
RECOVERYSYNC(i, j) \triangleq
                     canSync \stackrel{\triangle}{=} \land IsLeader(i) \land zabState[i] \neq DISCOVERY
                                                                                                 \land IsMyLearner(i, j)
                                   \land IsFollower(j) \land zabState[j] = SYNCHRONIZATION \land IsMyLeader(j, i)
       IN
        \land\ canSync
        \land SubRECOVERYSYNC(i, j)
                                  \mapsto NEWLEADER,
        \land Send(i, j, [mtype])
                       mepoch
                                  \mapsto acceptedEpoch[i],
                       mlastZxid \mapsto lastZxid[i]
        \land UNCHANGED \langle state, zabState, acceptedEpoch, currentEpoch, logicalClock, receiveVotes, outOfElectio
                          leading VoteSet, learners, cepochRecv, ackeRecv, ackldRecv, currentCounter,
                          tempVarsZ, cepochSent, leaderAddr, epochLeader, electionMsgs, idTable
        \land UpdateRecorder(\langle "RECOVERYSYNC", i, j \rangle)
 Follower receives NEWLEADER. The follower updates its epoch and history, and sends back
 ACK-LD to leader.
FollowerHandleNEWLEADER(i, j) \stackrel{\Delta}{=}
        \land IsFollower(i)
        \land PendingNEWLEADER(i, j)
                         \triangleq msgs[j][i][1]
        \wedge LET msg
                        \triangleq \land IsMyLeader(i, j)
                infoOk
                             \land acceptedEpoch[i] = msg.mepoch
                correct \triangleq \land infoOk
                             \land zabState[i] = SYNCHRONIZATION
                              \land synced[i]
                              \land ZxidEqual(lastZxid[i], msg.mlastZxid)
```

 $\wedge infoOk$

IN

```
\land UpdateProposal(i, j, lastZxid[i], currentEpoch'[i])
                 \land \lor \land correct
                       \land Reply(i, j, [mtype \mapsto ACKLD,
                                       mepoch \mapsto msg.mepoch)
                       \land \ \mathtt{UNCHANGED} \ \ inherent Violated
                    \lor \land \neg correct
                       \land PrintT ("Exception: Follower receives NEWLEADER while it has not completed sync with
                       \wedge inherent Violated' = TRUE
                       \wedge Discard(j, i)
         \land UNCHANGED \langle state, lastZxid, zabState, acceptedEpoch, history, commitIndex, logicalClock, receiveV
                            outOfElection, recvQueue, waitNotmsg, leaderVarsZ, tempVarsZ, followerVarsZ, pro
                            epochLeader, electionMsgs, idTable
         \land UpdateRecorder(\langle "FollowerHandleNEWLEADER", i, j \rangle)
 Leader receives ACK-LD from a quorum of followers, and sends COMMIT-LD (UPTODATE) to followers.
LeaderHandleACKLD(i, j) \triangleq
         \land IsLeader(i)
        \land PendingACKLD(i, j)
                          \stackrel{\Delta}{=} msgs[j][i][1]
         \wedge LET msq
                 infoOk \stackrel{\triangle}{=} \land acceptedEpoch[i] = msg.mepoch
                               \land IsMyLearner(i, j)
                 replyOk \triangleq \land infoOk
                               \land NullPoint \in ackldRecv[i]
                \wedge infoOk
                 \wedge V leader has broadcast UPTODATE – just reply
                       \land replyOk
                                                  \mapsto UPTODATE,
                       \land Reply(i, j, [mtype])
                                       mepoch \mapsto acceptedEpoch[i],
                                       mcommit \mapsto commitIndex[i])
                       \land committedCounter' = [committedCounter \ Except \ ![i][j] = Maximum(\{commitIndex[i]\})
                       leader still waits for a quorum's ACKLD to broadcast UPTODATE
                       \land \neg replyOk
                       \wedge Discard(j, i)
                       \land UNCHANGED committedCounter
                 \land ackldRecv' = [ackldRecv \ EXCEPT \ ![i] = IF \ j \notin ackldRecv[i] \ THEN \ ackldRecv[i] \cup \{j\}
                                                                                        ELSE ackldRecv[i]
         \land UNCHANGED \langle serverVarsZ, electionVarsZ, leadingVoteSet, learners, cepochRecv, ackeRecv, forward
                            ackIndex, currentCounter, tempVarsZ, followerVarsZ, verifyVarsZ, electionMsgs, id
         \land UpdateRecorder(\langle "LeaderHandleACKLD", i, j \rangle)
LeaderTransitionToBroadcast(i) \stackrel{\Delta}{=}
         \land IsLeader(i)
         \land \ zabState[i] = SYNCHRONIZATION
```

 $\land currentEpoch' = [currentEpoch \ EXCEPT \ ![i] = msg.mepoch]$

 $\land IsQuorum(ackldRecv[i])$

```
EXCEPT ![i] = Len(history[i])]
                        \land commitIndex'
                                                                                    = [commitIndex]
                        \land zabState'
                                                                                   = [zabState]
                                                                                                                                           EXCEPT ![i] = BROADCAST]
                        \land \ currentCounter' = [currentCounter \ \texttt{EXCEPT} \ ![i] = 0]
                          \land sendCounter' = [sendCounter \ Except \ ![i] = 0]
                          \land committedIndex' = [committedIndex \ \ \texttt{EXCEPT} \ ![i] = Len(history[i])]
                        \land ackldRecv'
                                                                                = [ackldRecv]
                                                                                                                                         EXCEPT ![i] = ackldRecv[i] \cup \{NullPoint\}]
                        \land BroadcastUPTODATE(i, [mtype])
                                                                                                                                                 \mapsto UPTODATE,
                                                                                                                                                \mapsto acceptedEpoch[i],
                                                                                                                  mepoch
                                                                                                                  mcommit \mapsto Len(history[i]) In actual UPTODATE doesn't carry this info
                        \land UNCHANGED \langle state, currentEpoch, lastZxid, acceptedEpoch, history, electionVarsZ, leadingVoteSet,
                                                                           cepochRecv, ackeRecv, forwarding, ackIndex, committedCounter, tempVarsZ, followe
                                                                            electionMsgs, idTable\rangle
                        \land UpdateRecorder(\langle "LeaderTransitionToBroadcast", i \rangle)
FollowerHandleUPTODATE(i, j) \triangleq
                        \land IsFollower(i)
                        \land PendingUPTODATE(i, j)
                       \land Let msg \stackrel{\triangle}{=} msgs[j][i][1]
                                             infoOk \triangleq \land IsMyLeader(i, j)
                                                                                 \land acceptedEpoch[i] = msg.mepoch
                                             correct \triangleq \land infoOk
                                                                                 \land zabState[i] = SYNCHRONIZATION
                                                                                  \land currentEpoch[i] = msg.mepoch
                                             \wedge infoOk
                              IN
                                              \land \lor \land correct
                                                               \land commitIndex' = [commitIndex \ EXCEPT \ ![i] = Maximum(\{commitIndex[i], msg.mcommitIndex[i], msg.mcommitIndex[i
                                                               \wedge zabState'
                                                                                                                 = [zabState]
                                                                                                                                                                EXCEPT ![i] = BROADCAST]
                                                               \land UNCHANGED inherentViolated
                                                      \vee \wedge \neg correct

∧ PrintT("Exception: Follower receives UPTODATE while its ZabState is not SYNCHRONIZ
                                                               \wedge inherent Violated' = TRUE
                                                               \land UNCHANGED \langle commitIndex, zabState \rangle
                        \wedge Discard(j, i)
                        \land UNCHANGED \langle state, currentEpoch, lastZxid, acceptedEpoch, history, electionVarsZ, leaderVarsZ, teaterVarsZ, teaterVa
                                                                           proposalMsgsLog, epochLeader, electionMsgs, idTable
                        \land UpdateRecorder(\langle "FollowerHandleUPTODATE", i, j \rangle)
   Leader receives client request and broadcasts PROPOSAL.
    Note1: In production, any server in traffic can receive requests and forward it to leader if neces-
                        sary. We choose to let leader be the sole one who can receive requests, to simplify spec
                        and keep correctness at the same time.
    Note2: To compress state space, we now choose to merge action client request and action leader
```

broadcasts proposal into one action.

```
ClientRequestAndLeaderBroadcastProposal(i, v) \stackrel{\Delta}{=}
         \wedge IsLeader(i)
         \land zabState[i] = BROADCAST
```

```
\land currentCounter' = [currentCounter \ Except \ ![i] = currentCounter[i] + 1]
          \land LET newTransaction \stackrel{\triangle}{=} [epoch \mapsto acceptedEpoch[i],
                                            counter \mapsto currentCounter'[i],
                                            value \mapsto v
                 \land history' = [history \ EXCEPT \ ![i] = Append(history[i], newTransaction)]
                   \land lastZxid' = [lastZxid \ EXCEPT \ ![i] = \langle acceptedEpoch[i], \ currentCounter'[i] \rangle]
                   \land ackIndex' = [ackIndex \ EXCEPT \ ![i][i] = Len(history'[i])]
                   \land UpdateProposal(i, i, lastZxid'[i], currentEpoch[i])
                   \land Broadcast(i, [mtype])
                                                    \mapsto PROPOSAL,
                                       mepoch
                                                   \mapsto acceptedEpoch[i],
                                       mproposal \mapsto newTransaction)
                   \land LET m \stackrel{\triangle}{=} [msource \mapsto i, mepoch \mapsto acceptedEpoch[i], mtype \mapsto PROPOSAL, mproposal \mapsto i
                     IN proposalMsgsLog' = proposalMsgsLog \cup \{m\}
          \land UNCHANGED \langle state, currentEpoch, zabState, acceptedEpoch, commitIndex, logicalClock, receiveVotes
                               recvQueue, waitNotmsg, leadingVoteSet, learners, cepochRecv, ackeRecv, ackldRecv,
                              committedCounter, tempVarsZ, followerVarsZ, epochLeader, inherentViolated,
                               electionMsgs, idTable\rangle
          \land UpdateRecorder(\langle "ClientRequestAndLeaderBroadcastProposal", i, v \rangle)
LeaderBroadcastProposal(i) \stackrel{\Delta}{=}
      \land IsLeader(i)
      \land zabState[i] = BROADCAST
      \land sendCounter[i] < currentCounter[i]
      \land LET toBeSentCounter \stackrel{\Delta}{=} sendCounter[i] + 1
          toBeSentIndex \stackrel{\triangle}{=} Len(initialHistory[i]) + toBeSentCounter

toBeSentEntry \stackrel{\triangle}{=} history[i][toBeSentIndex]
       IN \land Broadcast(i, [mtype \mapsto PROPOSAL,
                      mepoch \mapsto acceptedEpoch[i],
                      mproposal \mapsto toBeSentEntry])
          \land sendCounter' = [sendCounter except ![i] = toBeSentCounter]
           \wedge LET m \stackrel{\Delta}{=} [msource \mapsto i, mepoch \mapsto acceptedEpoch[i], mtype \mapsto PROPOSAL,
          mproposal \mapsto toBeSentEntry
            IN proposalMsgsLog' = proposalMsgsLog \cup \{m\}
      \land UpdateRecorder(\langle "LeaderBroadcastProposal", i \rangle)
      \land UNCHANGED \langle server Vars Z, election Vars Z, leading Vote Set, learners, cepoch Recv., acked Recv., forwarding,
                ackIndex, currentCounter, committedCounter, tempVarsZ, followerVarsZ, epochLeader,
                inherent Violated, election Msqs, id Table
 Follower accepts proposal and append it to history.
FollowerHandlePROPOSAL(i, j) \triangleq
          \land IsFollower(i)
          \land PendingPROPOSAL(i, j)
          \wedge \text{ LET } msg \qquad \stackrel{\triangle}{=} \ msgs[j][i][1]
                  infoOk \triangleq \land IsMyLeader(i, j)
                                 \land acceptedEpoch[i] = msg.mepoch
                  correct \triangleq \land infoOk
```

```
\land synced[i]
                 logOk \stackrel{\triangle}{=} the first PROPOSAL in this epoch
                              \lor \land msg.mproposal.counter = 1
                                 \wedge \vee Len(history[i]) = 0
                                    \lor \land Len(history[i]) > 0
                                       \land history[i][Len(history[i])].epoch < msg.mepoch
                               not the first PROPOSAL in this epoch
                              \lor \land msg.mproposal.counter > 1
                                 \wedge Len(history[i]) > 0
                                 \land history[i][Len(history[i])].epoch = msg.mepoch
                                 \land history[i][Len(history[i])].counter = msg.mproposal.counter - 1
                \wedge infoOk
                 \land \lor \land correct
                       \land \lor \land logOk
                             \land history' = [history \ EXCEPT \ ![i] = Append(history[i], msg.mproposal)]
                             \land lastZxid' = [lastZxid \ EXCEPT \ ![i] = \langle msg.mepoch, msg.mproposal.counter \rangle]
                             \land UpdateProposal(i, j, lastZxid'[i], currentEpoch[i])
                             \land Reply(i, j, [mtype \mapsto ACK,
                                              mepoch \mapsto acceptedEpoch[i],
                                              mzxid \mapsto \langle msg.mepoch, msg.mproposal.counter \rangle \rangle
                             ∧ UNCHANGED inherent Violated
                          \vee \wedge \neg logOk
                             \land PrintT( "Exception: Follower receives PROPOSAL while the transaction is not the next
                             \wedge inherent Violated' = TRUE
                             \wedge Discard(i, i)
                             \land UNCHANGED \langle history, lastZxid, currentVote \rangle
                    \vee \wedge \neg correct
                       ∧ PrintT("Exception: Follower receives PROPOSAL while it has not completed sync with lea
                       \land inherentViolated' = TRUE
                       \wedge Discard(j, i)
                       \land UNCHANGED \langle history, lastZxid, currentVote \rangle
         \land UNCHANGED \langle state, currentEpoch, zabState, acceptedEpoch, commitIndex, logicalClock, receiveVotes
                            outOfElection, recvQueue, waitNotmsg, leaderVarsZ, tempVarsZ, followerVarsZ, pro
                            epochLeader, electionMsgs, idTable
         \land UpdateRecorder(\langle "FollowerHandlePROPOSAL", i, j \rangle)
 Create a commit packet and send it to all the members of the quorum.
LeaderCommit(s, source, index, zxid) \stackrel{\Delta}{=}
         \land commitIndex' = [commitIndex \ EXCEPT \ ![s] = index]
         \land DiscardAndBroadcast(s, source, [mtype \mapsto COMMIT,
                                                  mepoch \mapsto acceptedEpoch[s],
                                                  mzxid \mapsto \langle zxid.epoch, zxid.counter \rangle])
```

 $\land zabState[i] \neq DISCOVERY$

```
LeaderTryToCommit(s, zxid, follower) \stackrel{\triangle}{=} \\ \stackrel{\triangle}{=} Len(initialHistory[s]) + zxid.counter
                 Only when all proposals before zxid all committed, this proposal can be permitted to be committed.
                allProposalsBeforeCommitted \stackrel{\Delta}{=} \lor zxid.counter = 1
                                                           \vee \wedge zxid.counter > 1
                                                               \land commitIndex[s] \ge pindex - 1
                 In order to be committed, a proposal must be accepted by a quorum.
                                                      \stackrel{\triangle}{=} \{s\} \cup \{k \in (Server \setminus \{s\}) : ackIndex'[s][k] \ge pindex\}
                agreeSet
                                                      \triangleq IsQuorum(agreeSet)
                has All Quorums
                 Commit proposals in order.
                                                   \stackrel{\triangle}{=} commitIndex[s] + 1 = pindex
                ordered
                \lor \land \lor \neg all Proposals Before Committed
         IN
                       \vee \neg hasAllQuorums
                   \land Discard(follower, s)
                   \land UNCHANGED \langle inherentViolated, commitIndex \rangle
                \lor \land all Proposals Before Committed
                   \land hasAllQuorums
                   \land \lor \land \neg ordered
                          \land PrintT( "Exception: Committing zxid" \circ zxid \circ "not first.")
                          \wedge inherent Violated' = TRUE
                       \lor \land ordered
                          ∧ UNCHANGED inherent Violated
                   \land LeaderCommit(s, follower, pindex, zxid)
 Keep a count of acks that are received by the leader for a particular
 proposal, and commit the proposal.
LeaderProcessACK(i, j) \triangleq
          \wedge IsLeader(i)
          \land PendingACK(i, j)
          \wedge \text{ LET } msg \stackrel{\triangle}{=} msgs[j][i][1]
                   infoOk \stackrel{\triangle}{=} \land j \in forwarding[i]
                                  \land acceptedEpoch[i] = msg.mepoch
                   correct \triangleq \land infoOk
                                  \land zabState[i] = BROADCAST
                                  \land currentCounter[i]
                                                               \geq msg.mzxid[2]
                   noOutstanding \triangleq commitIndex[i] = Len(history[i])
                                    outstanding Proposals: proposals in <math>history[commitIndex + 1: Len(history)]
                   hasCommitted \stackrel{\Delta}{=} commitIndex[i] \ge Len(initialHistory[i]) + msg.mzxid[2]
                                    namely, lastCommitted \ge zxid
                   logOk \triangleq \land infoOk
                                \land ackIndex[i][j] + 1 = Len(initialHistory[i]) + msg.mzxid[2]
                                      everytime, ackIndex should just increase by 1
                   \wedge infoOk
                   \land \lor \land correct
                          \land logOk
```

```
\land \lor \land \lor noOutstanding
                                                                \lor hasCommitted
                                                          \wedge PrintT ("Note: outstanding is 0 / proposal has already been committed.")
                                                          \wedge Discard(j, i)
                                                          \land UNCHANGED \langle ackIndex, commitIndex, inherentViolated \rangle
                                                    \lor \land \neg noOutstanding
                                                          \land \neg hasCommitted
                                                          \land ackIndex' = [ackIndex \ EXCEPT \ ![i][j] = Len(initialHistory[i]) + msg.mzxid[2]]
                                                          \land LeaderTryToCommit(i, ToZxid(msq.mzxid), j)
                                        \lor \land \lor \neg correct
                                                    \vee \neg logOk
                                               \land PrintT( "Exception: ackIndex doesn't increase monotonically.")
                                               \wedge inherent Violated' = TRUE
                                               \wedge Discard(j, i)
                                               \land UNCHANGED \langle ackIndex, commitIndex \rangle
                  \land UNCHANGED \langle state, currentEpoch, lastZxid, zabState, acceptedEpoch, history, electionVarsZ,
                                                        leadingVoteSet, learners, cepochRecv, ackeRecv, ackldRecv,
                                                        forwarding, currentCounter, committedCounter, tempVarsZ,
                                                        followerVarsZ, proposalMsgsLog, epochLeader, electionMsgs, idTable
                  \land UpdateRecorder(\langle "LeaderProcessACK", i, j \rangle)
LeaderAdvanceCommit(i) \stackrel{\Delta}{=}
           \wedge IsLeader(i)
           \land \ zabState[i] = BROADCAST
           \land commitIndex[i] < Len(history[i])
            \land \text{ LET } Agree(index) \stackrel{\Delta}{=} \{i\} \cup \{k \in (Server \setminus \{i\}) : ackIndex[i][k] \ge index\} 
 agreeIndexes \stackrel{\Delta}{=} \{index \in (commitIndex[i] + 1) \dots Let
                    agreeIndexes
                                                                        \{index \in (commitIndex[i] + 1) \dots Len(history[i])\}
                    Agree(index) \in Quorums
                    newCommitIndex \stackrel{\Delta}{=} \text{IF} \quad agreeIndexes \neq \{\} \text{ THEN } Maximum(agreeIndexes)
                                                                          ELSE commitIndex[i]
              IN commitIndex' = [commitIndex \ EXCEPT \ ![i] = newCommitIndex]
           \land UpdateRecorder(\langle "LeaderAdvanceCommit", i \rangle)
           \land \texttt{UNCHANGED} \ \langle state, \ current Epoch, \ last Zxid, \ zab State, \ accepted Epoch, \ history, \ election Vars Z, \ leader Vars Z, \ electron Vars Z, \ leader Vars Z, \ electron V
                               tempVarsZ, followerVarsZ, verifyVarsZ, msgVarsZ, idTable
LeaderBroadcastCommit(i) \stackrel{\Delta}{=}
           \land IsLeader(i)
           \land zabState[i] = BROADCAST
           \land committedIndex[i] < commitIndex[i]
           \land Len(initialHistory[i]) + sendCounter[i] > committedIndex[i]
           \land LET newCommittedIndex \stackrel{\triangle}{=} committedIndex[i] + 1
              IN \land Broadcast(i, [mtype \mapsto COMMIT,
                                         mepoch \mapsto acceptedEpoch[i],
                                         mzxid \mapsto \langle history[i][newCommittedIndex].epoch, history[i][newCommittedIndex].counter \rangle])
                   \land committedIndex' = [committedIndex \ Except \ ![i] = committedIndex[i] + 1]
                    \land committedCounter' = [committedCounter EXCEPT ![i] = [v \in Server \dots IF \lambda
                   v \in forwarding[i]
```

```
\land \quad committedCounter[i][v]
                                                            history[i][newCommittedIndex].counter
                                                           THEN history[i][newCommittedIndex].counter
                                                           ELSE committedCounter[i][v]]
     \land UpdateRecorder(\langle "LeaderBroadcastCommit", i \rangle)
     AUNCHANGED (server Vars Z, election Vars Z, leading Vote Set, learners, cepoch Recv, acke Recv, ackel Recv,
               forwarding, ackIndex, currentCounter, sendCounter, tempVarsZ, followerVarsZ, verifyVarsZ,
               electionMsgs, idTable\rangle
 Follower receives COMMIT and commits transaction.
FollowerHandleCOMMIT(i, j) \triangleq
         \land IsFollower(i)
         \land PendingCOMMIT(i, j)
                         \triangleq msgs[j][i][1]
         \wedge LET msg
                 infoOk \triangleq \land IsMyLeader(i, j)
                              \land acceptedEpoch[i] = msg.mepoch
                 correct \triangleq \land infoOk
                              \land zabState[i] \neq DISCOVERY
                              \land synced[i]
                 mindex \stackrel{\Delta}{=} \text{ IF } Len(history[i]) = 0 \text{ THEN } -1
                               ELSE IF \exists idx \in 1.. Len(history[i]) : PZxidEqual(history[i][idx], msg.mzxid)
                                        THEN CHOOSE idx \in 1.. Len(history[i]) : PZxidEqual(history[i][idx], msg.r
                                        ELSE -1
                           \stackrel{\triangle}{=} mindex > 0
                 logOk
                          \stackrel{\triangle}{=} commitIndex[i] + 1 = mindex
                 latest
                 \wedge infoOk
                 \land \lor \land correct
                       \land \lor \land logOk
                             \land \lor \land latest
                                   \land commitIndex' = [commitIndex \ EXCEPT \ ![i] = commitIndex[i] + 1]
                                   \land UNCHANGED inherentViolated
                                \vee \wedge \neg latest
                                   ∧ PrintT("Note: Follower receives COMMIT while the index is not the next comm
                                   \land inherentViolated' = TRUE
                                   \land UNCHANGED commitIndex
                          \vee \wedge \neg logOk
                             ∧ PrintT("Exception: Follower receives COMMIT while the transaction has not been sa
                             \wedge inherent Violated' = TRUE
                             ∧ UNCHANGED commitIndex
                    \lor \land \neg correct

∧ PrintT("Exception: Follower receives COMMIT while it has not completed sync with leade

                       \wedge inherent Violated' = TRUE
                       ∧ UNCHANGED commitIndex
```

```
\wedge Discard(j, i)
         \land UNCHANGED \langle state, currentEpoch, lastZxid, zabState, acceptedEpoch, history, electionVarsZ, leader
                             tempVarsZ, followerVarsZ, proposalMsqsLoq, epochLeader, electionMsqs, idTable
         \land UpdateRecorder(\langle "FollowerHandleCOMMIT", i, j \rangle)
 Used to discard some messages which should not exist in actual. This action should not be
 triggered.
FilterNonexistentMessage(i) \triangleq
          \land \exists j \in Server \, \backslash \, \{i\} : \land msgs[j][i] \neq \langle \rangle \\ \land \text{let } msg \ \stackrel{\triangle}{=} \ msgs[j][i][1] 
                                           \vee \wedge IsLeader(i)
                                              \land LET infoOk \stackrel{\triangle}{=} \land j \in learners[i]
                                                                    \land acceptedEpoch[i] = msg.mepoch
                                                 \lor \mathit{msg.mtype} = \mathit{LEADERINFO}
                                                 \lor msg.mtype = NEWLEADER
                                                 \lor msg.mtype = UPTODATE
                                                 \lor \mathit{msg.mtype} = \mathit{PROPOSAL}
                                                 \lor msg.mtype = COMMIT
                                                 \vee \wedge j \notin learners[i]
                                                    \land msg.mtype = FOLLOWERINFO
                                                 \vee \wedge \neg infoOk
                                                    \land \lor msg.mtype = ACKEPOCH
                                                       \lor msg.mtype = ACKLD
                                                       \vee msq.mtype = ACK
                                           \vee \wedge IsFollower(i)
                                              \wedge \text{ LET } infoOk \stackrel{\triangle}{=} \wedge j = leaderAddr[i]
                                                                    \land acceptedEpoch[i] = msg.mepoch
                                                 \lor msg.mtype = FOLLOWERINFO
                                                 \lor msg.mtype = ACKEPOCH
                                                 \lor msg.mtype = ACKLD
                                                 \lor msg.mtype = ACK
                                                 \lor \land j \neq leaderAddr[i]
                                                    \land \ msg.mtype = LEADERINFO
                                                 \lor \land \neg infoOk
                                                    \land \lor msg.mtype = NEWLEADER
                                                       \lor msg.mtype = UPTODATE
                                                       \lor msg.mtype = PROPOSAL
                                                       \lor msg.mtype = COMMIT
                                           \vee IsLooking(i)
                                    \wedge Discard(j, i)
         \wedge inherent Violated' = TRUE
         \land UnchangeRecorder
```

 $\land \ \, \text{UNCHANGED} \ \, \langle serverVarsZ, \ electionVarsZ, \ leaderVarsZ, \ tempVarsZ, \ followerVarsZ, \ proposalMsgsLepochLeader, \ electionMsgs, \ idTable \rangle$

```
Defines how the variables may transition.
NextZ \triangleq
           FLE modlue
              \vee \exists i, j \in Server : FLEReceiveNotmsq(i, j)
                                  FLENotmsgTimeout(i)
              \vee \exists i \in Server :
              \vee \exists i \in Server :
                                  FLEHandleNotmsq(i)
              \lor \exists i \in Server : FLEWaitNewNotmsq(i)
              \vee \exists i \in Server :
                                    FLEWaitNewNotmsgEnd(i)
           Some conditions like failure, network delay
              \vee \exists i \in Server : FollowerTimout(i)
              \vee \exists i \in Server :
                                     LeaderTimeout(i)
              \vee \exists i, j \in Server : Timeout(i, j)
           Zab module - Discovery and Synchronization part
              \vee \exists i, j \in Server : Establish Connection(i, j)
                                    FollowerSendFOLLOWERINFO(i)
              \vee \exists i \in Server:
              \vee \exists i, j \in Server : LeaderHandleFOLLOWERINFO(i, j)
              \vee \exists i \in Server : LeaderBroadcastLEADERINFO(i)
              \vee \exists i, j \in Server : FollowerHandleLEADERINFO(i, j)
              \vee \exists i, j \in Server : LeaderHandleACKEPOCH(i, j)
              \vee \exists i \in Server : LeaderTransitionToSynchronization(i)
              \forall \exists i, j \in Server : RECOVERYSYNC(i, j)
              \vee \exists i, j \in Server : FollowerHandleNEWLEADER(i, j)
              \vee \exists i, j \in Server : LeaderHandleACKLD(i, j)
              \lor \exists i \in Server : LeaderTransitionToBroadcast(i)
              \vee \exists i, j \in Server : FollowerHandleUPTODATE(i, j)
           Zab module -Broadcast part
              \forall \exists i \in Server, v \in Value : ClientRequestAndLeaderBroadcastProposal(i, v)
               \vee \exists i \in Server, v \in Value: ClientRequest(i, v)
                \lor \exists i \in Server: LeaderBroadcastProposal(i)
              \forall \exists i, j \in Server : FollowerHandlePROPOSAL(i, j)
              \vee \exists i, j \in Server : LeaderProcessACK(i, j)
                \vee \exists i \in Server: LeaderAdvanceCommit(i)
                \lor \exists i \in Server: LeaderBroadcastCommit(i)
              \vee \exists i, j \in Server : FollowerHandleCOMMIT(i, j)
           An action used to judge whether there are redundant messages in network
              \vee \exists i \in Server : FilterNonexistentMessage(i)
SpecZ \triangleq InitZ \wedge \Box [NextZ]_{vars}
```

Define safety properties of $Zab\ 1.0$ protocol.

```
ShouldNotBeTriggered \triangleq inherentViolated = False
There is most one established leader for a certain epoch.
Leadership1 \triangleq \forall i, j \in Server:
                       \land IsLeader(i) \land zabState[i] \in {SYNCHRONIZATION, BROADCAST}
                       \land IsLeader(j) \land zabState[j] \in {SYNCHRONIZATION, BROADCAST}
                       \land acceptedEpoch[i] = acceptedEpoch[j]
Leadership2 \stackrel{\triangle}{=} \forall epoch \in 1 ... MAXEPOCH : Cardinality(epochLeader[epoch]) < 2
PrefixConsistency: The prefix that have been committed in history in any process is the same.
PrefixConsistency \triangleq \forall i, j \in Server :
                             LET smaller \triangleq Minimum(\{commitIndex[i], commitIndex[j]\})
                                   \vee smaller = 0
                                   \vee \wedge smaller > 0
                                      \land \forall index \in 1 ... smaller : TransactionEqual(history[i][index], history[j][index]
 Integrity: If some follower delivers one transaction, then some primary has broadcast it.
Integrity \stackrel{\triangle}{=} \forall i \in Server :
                  \land IsFollower(i)
                  \wedge \; commitIndex[i] > 0
                  \Rightarrow \forall index \in 1 ... commitIndex[i] : \exists msg \in proposalMsgsLog :
                        \lor \land msg.mtype = PROPOSAL
                           \land TransactionEqual(msg.mproposal, history[i][index])
                       \lor \land msg.mtype = "RECOVERYSYNC"
                                           \in 1... Len(msq.mproposals): TransactionEqual(msq.mproposals[tindex], holds:
                           \wedge \exists tindex
 Agreement: If some follower f delivers transaction a and some follower f' delivers transaction b,
then f' delivers a or f delivers b. 
 Agreement \stackrel{\triangle}{=} \forall i, j \in Server:
                    \land IsFollower(i) \land commitIndex[i] > 0
                    \land IsFollower(j) \land commitIndex[j] > 0
                    \forall index 1 \in 1 ... commitIndex[i], index 2 \in 1 ... commitIndex[j] :
                        \vee \exists index j \in 1 ... commitIndex[j] :
                            TransactionEqual(history[j][indexj], history[i][index1])
                        \vee \exists indexi \in 1 ... commitIndex[i] :
                            TransactionEqual(history[i][indexi], history[j][index2])
 Total order: If some follower delivers a before b, then any process that delivers b
          must also deliver a and deliver a before b.
TotalOrder \stackrel{\Delta}{=} \forall i, j \in Server : commitIndex[i] \geq 2 \land commitIndex[j] \geq 2
                      \Rightarrow \forall indexi1 \in 1.. (commitIndex[i] - 1) : \forall indexi2 \in (indexi1 + 1).. commitIndex[i] :
                          LET logOk \triangleq \exists index \in 1 ... commitIndex[j] : TransactionEqual(history[i][indexi2], hist
```

 $\vee \neg logOk$ $\vee \wedge logOk$

```
\land \exists indexj2 \in 1 .. commitIndex[j] :
                                                             \land \ TransactionEqual(history[i][indexi2], \ history[j][indexj2])
                                                             \land \exists indexj1 \in 1 ... (indexj2-1) : TransactionEqual(history[i][interpretation])
 Local primary order: If a primary broadcasts a before it broadcasts b, then a follower that
                 delivers b must also deliver a before b.
Local Primary Order \stackrel{\triangle}{=} LET \ mset(i, e) \stackrel{\triangle}{=} \{ msq \in proposal MsqsLoq : \land msq.mtype = PROPOSAL \}
                                                                                             \land msq.msource = i
                                                                                             \land msg.mepoch = e
                                     mentries(i, e) \stackrel{\Delta}{=} \{msg.mproposal : msg \in mset(i, e)\}
                                    \forall i \in Server : \forall e \in 1 ... currentEpoch[i] :
                                       \vee Cardinality(mentries(i, e)) < 2
                                       \lor \land Cardinality(mentries(i, e)) \ge 2
                                           \land \exists tsc1, tsc2 \in mentries(i, e) :
                                            \vee TransactionEqual(tsc1, tsc2)
                                            \lor \land \neg TransactionEqual(tsc1, tsc2)
                                               \land Let tscPre \stackrel{\triangle}{=} if TransactionPrecede(tsc1, tsc2) then tsc1 else tsc2 tscNext \stackrel{\triangle}{=} if TransactionPrecede(tsc1, tsc2) then tsc2 else tsc3
                                                  IN \forall j \in Server : \land commitIndex[j] \ge 2
                                                                            \land \exists index \in 1 ... commitIndex[j] : TransactionEqual(
                                                    \Rightarrow \exists index 2 \in 1 ... commitIndex[j] :
                                                             \land TransactionEqual(history[j][index2], tscNext)
                                                             \land index2 > 1
                                                             \land \exists index1 \in 1 .. (index2 - 1) : TransactionEqual(history[j])[index1]
 Global primary order: A follower f delivers both a with epoch e and b with epoch e', and e < e',
                  then f must deliver a before b.
GlobalPrimaryOrder \stackrel{\Delta}{=} \forall i \in Server : commitIndex[i] \geq 2
                                   \Rightarrow \forall idx1, idx2 \in 1... commitIndex[i]: \forall history[i][idx1].epoch \geq history[i][idx2].epoch
                                                                                         \lor \land history[i][idx1].epoch < history[i][idx2]
                                                                                            \wedge idx1 < idx2
 Primary integrity: If primary p broadcasts a and some follower f delivers b such that b has epoch
               smaller than epoch of p, then p must deliver b before it broadcasts a.
PrimaryIntegrity \stackrel{\Delta}{=} \forall i, j \in Server : \land IsLeader(i)
                                                   \land \ commitIndex[j] \ge 1
                                \Rightarrow \forall index \in 1 ... commitIndex[j] : \forall history[j][index].epoch \geq currentEpoch[i]
                                                                               \lor \land history[j][index].epoch < currentEpoch[i]
                                                                                  \wedge \exists idx \in 1 ... commitIndex[i] : TransactionEquation
```

^{*} Last modified Sat Oct 09 11:05:52 CST 2021 by Dell

^{\ *} Created Tue Jun 29 22:13:02 CST 2021 by Dell