## MTH 9831 Assignment 3 (09/16 - 09/23).

Read Lecture 3. Some additional references for this material are:

- 1. S. Shreve, Stochastic Calculus for Finance II, Sections 4.2, 4.3.
- 2. A. Etheridge, A Course in Financial Calculus, Section 4.2.
- (1) (Imitation of the technique which precedes the exercise) Exercise 1 from Lecture 3.
- (2) (The difference between Ito and Stratonovich integrals) Exercise 3 from Lecture 3.
- (3) (Stochastic integral of an elementary process is a martingale) Exercise 4 from Lecture 3.
- (4) (General education problem) Let  $(B(t))_{t\geq 0}$  be a standard Brownian motion. Show that  $E((B(t))^{2n}) = t^n(2n-1)!!$  Steps: (a) **use scaling** to reduce the problem to computing  $E(Z^{2n})$ , where Z is a standard normal; (b) use integration by parts and induction (or any other elementary method you like) to get the answer.
- (5) Exercise 4.2 from the textbook.
- (6) Exercise 4.3 from the textbook.
- (7) (Review of Brownian motion and basic calculus) Use properties of Brownian motion to find the expectation and variance of  $\int_0^t B^2(s) ds$ . Hint: write the square of the integral as a double integral and only then take the expectation.