**BIO3SS3: Population Ecology** 

**UNIT 1: Introduction** 

#### 1 Course overview

#### 1.1 Course structure

#### Communication

- Lecture notes for each section will be available the afternoon before you need them
  - Check Avenue frequently for announcements and new information
  - All info will also be on the course resource page
    - \* http://bio3ss.github.io/
- The professor is Jonathan Dushoff
  - dushoff@mcmaster.ca
  - Office hours will be announced
  - Or ask questions electronically
    - \* We need a forum!

### Expectations of professor

- Start and end on time
- Focus on conceptual understanding
- Make clear what terminology and facts must be learned
- Open to questions both in class (within reason) and at office hours
- Responsive to questions on class forums (to be decided)

### **Expectations of students**

- Start and end on time
- Don't talk while other students are talking, or while I am responding to student questions
- If you must talk at other times, be unobtrusive
- Don't use the internet for non-class activities
- Attend the lecture, and the mandatory tutorials

#### **Texts**

- The primary text for this course is the lecture notes
- You will be given readings, which will be posted to Avenue

### Structure of presentation

- Required material will be clearly outlined in the notes
- Required terminology will be presented in **bold**
- General ideas and approaches presented in class may also be required; you should take notes on these in your own words

#### Taking notes

- You will do best if you take notes
  - You should know by now what works for you
  - Or else that you need to keep working on it
- If a new concept is making sense to you right now, write something that will help you remember
- If there's something specific I think you all need to write down, I will write it for you (or mark it as an answer)

# Polling

- You can obtain extra credit by responding to in-class polls
  - Text from your cell phone, or answer on the web
- Poll: Why are you taking this class?

### 1.2 People

#### Li

- Ex-TA
- Post-doc
- Studies evolution and spread of infectious diseases
  - Rabies, ebola, influenza, ...
  - Statistics, math, theoretical biology, computations, ...
  - Mechanisms and disease control

### Dushoff

- Loves math
- Lived in four countries
- Studies evolution and spread of infectious diseases
  - HIV, rabies, ebola, influenza, ...
  - http://lalashan.mcmaster.ca/theobio/DushoffLab/
  - https://twitter.com/jd\_mathbio

#### TAs

- Steve Cygu
- Zachery Dickson
- Danielle Montocchio

#### **Students**

- Poll: What year are you in?
- Poll: What kind of career are you aiming for?

## 2 Course content

# 2.1 Learning goals

- Ecology and population ecology
- Quantitative thinking
- Dynamical modeling

# **Ecology**

- Poll: What is ecology?
- My answer

\_

### Population ecology

- Poll: What is population ecology?
- My answer

\_

\_

### Dynamical modeling

- Investigates the links between local, short-term processes, and large-scale, long-term outcomes
- Allows us to explore what assumptions we're making, and how assumptions affect the link

#### Math

- Population ecology uses math
  - Math is a critical tool for linking processes to outcomes
  - Math will play a central role in the course
- We will keep it *simple* 
  - But we understand that simple does not always mean easy
- Link: Review the math supplement

### Humans and abstract thought

- People are evolved to be concrete thinkers, not conceptual thinkers
- A goal of this course is to build conceptual thinking skills

### 2.2 Examples

#### Malaria

- A nasty, mosquito-borne disease
- In some places (e.g., the southeastern US), it has been eradicated almost by accident
  - Mosquitoes are still present
- In other places it persists at high levels despite concerted efforts at elimination
- What factors determine when and where malaria spreads?

### Red squirrels

- Red squirrels are rapidly disappearing from England
  - Loss of suitable habitat?
  - Competition from gray squirrels introduced from North America?
  - Diseases carried by gray squirrels?
- http://en.wikipedia.org/wiki/Eastern\_grey\_squirrels\_in\_Europe

#### Cod fisheries

- Is the ocean too big for people to affect?
- What happened to the cod?
- http://en.wikipedia.org/wiki/Collapse\_of\_the\_Atlantic\_northwest\_cod\_fishery

### **Populations**

• Poll: What population of organisms interests you?

#### **Dandelions**

- Start with one dandelion; it produces 100 seeds, of which only 4% survive to reproduce the next year.
  - How many dandelions after 3 years?

\*

\*

# 3 Example populations

#### 3.1 Dandelions

- Start with one dandelion; it produces 100 seeds, of which only 4% survive to reproduce the next year.
- How many dandelions after 3 years?

- Link: See spreadsheet on resource page

• The spreadsheet is an implementation of a dynamical model!

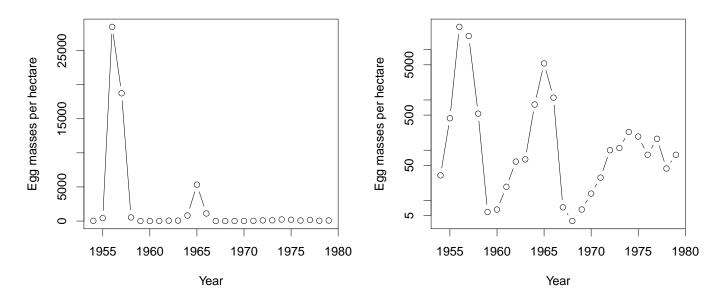
### Dynamical models

- Make rules about how things change on a small scale
- Assumptions should be clear enough to allow you to calculate or simulate populationlevel results
- Challenging and clarifying assumptions is a key advantage of models

## 3.2 Gypsy moths

- A pest species that feeds on deciduous trees
- Introduced to N. America from Europe 150 years ago
- Capable of wide-scale defoliation

## Gypsy moth populations



#### Moth calculation

- Researchers studying a gypsy moth population make the following estimates:
  - The average reproductive female lays 600 eggs
  - 10% of eggs hatch into larvae
  - 10% of larvae mature into pupae
  - -50% of pupae mature into adults
  - 50\% of adults survive to reproduce

- All adults die after reproduction
- What happens if we start with 10 moths?

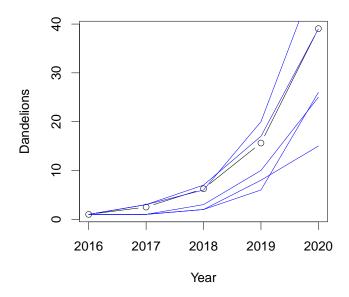
\_

#### Stochastic version

- Obviously, we will not get *exactly* 7.5 moths.
- If we consider moths as individuals, we need a **stochastic** model
- What do we mean by stochastic?

\_

### Stochastic model



- A stochastic model has randomness in the model.
- If we run it again with the same parameters and starting conditions, we get a different answer

#### 3.3 Bacteria

- Imagine we have some bacteria growing in a big tank, constantly dividing and dying:
  - They divide (forming two bacteria from one) at a rate of 0.04/hr
  - They wash out of the tank at a rate of 0.02/hr

- They die at a rate of 0.01/hr
- Rates are **per capita** (i.e., per individual) and **instaneous** (they describe what is happening at each moment of time)
- We start with 10 bacteria/ml
  - How many do we have after 1 hr?
  - What about after 1 day?

### Bacteria, rescaled

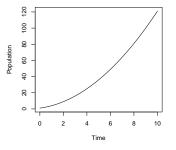
- Imagine we have some bacteria growing in a big tank:
  - They divide (forming two bacteria from one) at a rate of 0.96/day
  - They wash out of the tank at a rate of 0.48/day
  - They die at a rate of 0.24/day
- If we start with 10 bacteria/ml, how many do we have after 1 day?

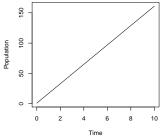
#### Units

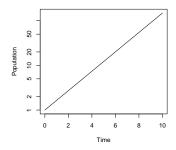
- When we attach units to a quantity, the meaning is concrete
  - -0.24/day must mean exactly the same thing as 0.01/hr
  - The two questions above *must* have the same answer

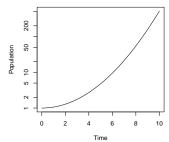
# 4 Exponential growth

- What is exponential growth?
- Which of these is an example?









# Types of growth

- $\bullet$ arithmetic/linear:
  - \_
- $\bullet \ \ geometric/exponential:$ 
  - \_
  - \_
- other:
  - Many possibilities, we may discuss some later

# Exponential decline?

- Poll: What is exponential decline?
  - \_

# Terminology

- Sometimes people distinguish
  - arithmetic from linear growth, or
  - **geometric** from **exponential** growth
- Based on:

\_

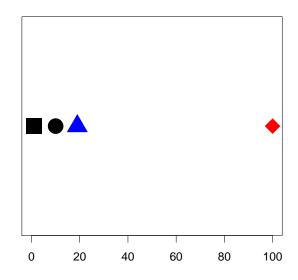
• We won't worry much about this.

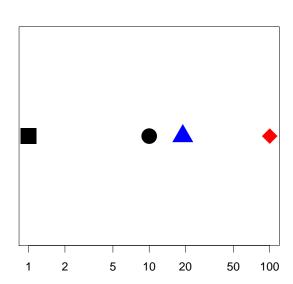
# 4.1 Log and linear scales

# Scales of comparison

• Poll: 1 is to 10 as 10 is to what?

# Scales of display



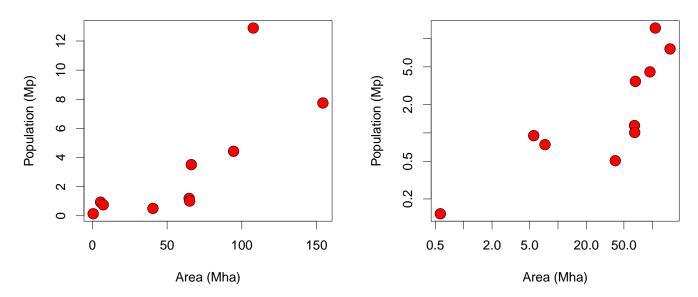


There is only one log scale; it doesn't matter which base you use!

# Canadian provinces

- How many people know the Canadian provinces song?
- Poll: Which Canadian province is the most unusual in terms of area?
- Poll: Which Canadian province is the most unusual in terms of population?

# Canadian provinces



# Predation comparison

- A 300 lb lion is attacking a 600 lb buffalo!
- Poll: This is analogous to a 15 lb red fox attacking: a beaver, an elk
  - A 30 lb beaver (twice as heavy)?
  - A 315 lb elk (300 lbs heavier)?

### Different scales

- The log scale and linear scale provide different ways of looking at the same data
- Equally valid
- What are some advantages of each?

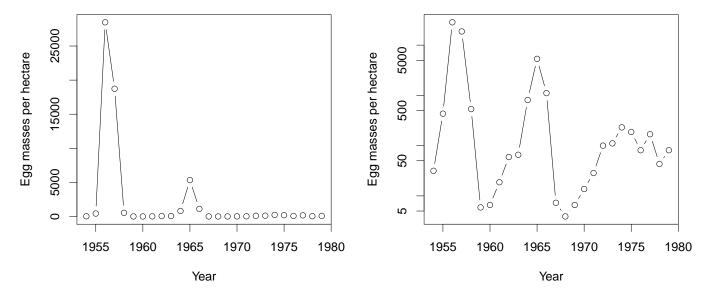
# Advantages of arithmetic view

- ullet
  - \_
- •
- •

# Advantages of geometric view

- •
- •

### Gypsy-moth example



# Scales in population biology

- The linear scale looks at differences at the population scale
- The log scale looks at differences at the individual scale (per capita)

#### 4.2 Time scales

#### Characteristic times

- If something is declining exponentially, the rate of change (units [widgets/time]) is always proportional to the size of the thing ([widgets]).
- The constant ratio between the rate of change and the thing that is changing is:
  - the **characteristic time** (something/change), or
  - the rate of exponential decline (change/something)

#### **Bacteriostasis**

- What if we add an agent to the tank that makes the birth and death rates nearly zero?
- Now the bacteria are merely washing out at the rate of 0.02/hr
- If we start with 10 bacteria/ml, how many do we have after:
  - Poll: 1 hr?
  - Poll: 1 wk?

#### Bacteriostasis answers

• Bacteria wash out at the rate of 0.02/hr

• Start with 10 bacteria/ml:

### Bacteriostasis analysis

- Rate of exponential decline is  $r = 0.02/\,\mathrm{hr}$
- Characteristic time is  $T_c = 1/r = 50 \,\mathrm{hr}$
- If experiment time  $t \ll T_c$ , then proportional decline  $\approx t/T_c$
- The answer makes sense for short times and for long times

#### Euler's e

- $\bullet$  The reason mathematicians like e is that it makes this link between instantaneous change and long-term behaviour
- If I drive for an hour, how much closer do I get to the ideal town of Speed?

- e or 1/e is the approximate answer to a lot of questions like this one
  - If I compound 1\%/year interest for 100 years, how much does my money grow?
  - If two people go deal out two decks of cards simultaneously, what is the probability they will never match cards?
  - If everyone picks up a backpack at random after a test, what's the probability nobody gets the right backpack?

### Exponential growth

- We can think about exponential growth the same way as exponential decline:
  - Things are always changing at a rate that would take a fixed amount of time to get (back) to zero
  - This is the characteristic time
  - Exponential growth follows  $N = N_0 \exp(rt) = N_0 \exp(t/T_c)$

### Half life

- Some people prefer to think about half lives.
- Half life is similar to characteristic time, but doesn't have the direct link to the instantaneous change.
  - It takes  $T_c$  time to decrease by a factor of e
  - It takes  $\log_e(2)T_c \approx 0.69T_c$  to decrease by a factor of 2
  - We can write  $T_h = \log_e(2)T_c$
- You should be able to do this calculation

$$-\exp(-rT_h) = 1/2$$

$$-rT_h = log_e(1/2) = -\log_e(2)$$

$$-T_h = \log_e(2)/r$$

$$- T_h = \log_e(2)T_c$$

### Doubling time

- The doubling time plays the same role for exponential growth as the half life does for exponential decline:
  - $T_h = \log_e(2)T_c$
  - It takes  $T_c$  time for a declining population to decrease by a factor of e
  - It takes  $\log_e(2)T_c \approx 0.69T_c$  to decrease by a factor of 2
  - We can write  $T_h = \log_e(2)T_c$

### Summary

- Exponential growth is a specific thing
  - At least in math and science
- Often tied to a specific mechanism
  - \_
- Units can help us think clearly
  - or notice our mistakes