UNIT 7: Infectious disease

1 Introduction

Infectious disease

- Extremely common
- Huge impacts on ecological interactions
- A form of exploitation, but doesn't fit well into our previous modeling framework
 - How many people are there?
 - How many influenza viruses are there?
 - How do they find each other?

Disease agents

- Can you name an infectious agent that causes disease in humans?
- Disease agents vary tremendously:
 - Most viruses have just a handful of genes that allow them to hijack a cell and get it to make virus copies

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 Bacteria are independent, free-living cells with hundreds or thousands of chemical pathways

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 Eukaryotic pathogens are nucleated cells who are more closely related to you than they are to bacteria

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Microparasites

- For infections with small pathogens (viruses and bacteria), we don't attempt to count pathogens, but instead divide disease into stages
 - Latently infected
 - Productively infected
 - Recovered

Microparasite models

- We model microparasites by counting the number of hosts in various **states**:
 - Susceptible individuals can become infected
 - **Infectious** individuals are infected and can infect others
 - Resistant individuals are not infected and cannot become infected

• More complicated models might include other states, such as latently infected hosts who are infected with the pathogen but cannot yet infect others

Models as tools

- Models are the tools that we use to connect scales:
 - individuals to populations
 - single actions to trends through time

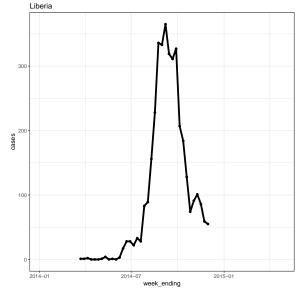
2 Rate of spread

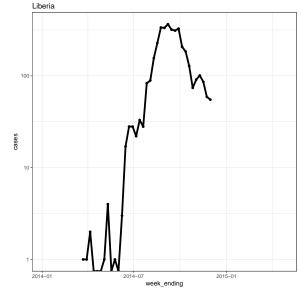
- many diseases, especially new diseases, we can *observe* and $estimate \ r$.
- to know what factors contribute to that, and how it relates to \mathcal{R} .

Basic reproductive number

- ullet People in the disease field love to talk specifically about \mathcal{R}_0
- But they don't always mean the same thing:
 - Actual value of \mathcal{R} before an epidemic
 - Hypothetical value assuming no immunity
 - Hypothetical value assuming no control efforts whatsoever
- Often easier to talk simply about \mathcal{R} .

Example: the West African Ebola epidemic



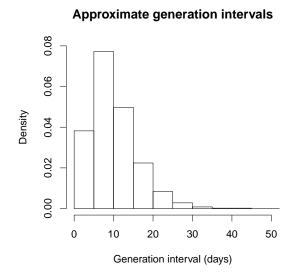


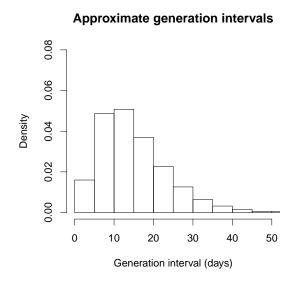
Generation intervals

• Researchers try to estimate the *proportion* of transmission that happens for different **ages of infection**

- How long from the time you are *infected* to the time you *infect* someone else?
- Analogous to a life table
- The effective generation time \hat{G} has units of time

Generation intervals





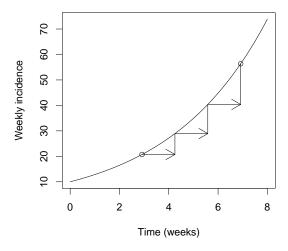
Speed and risk

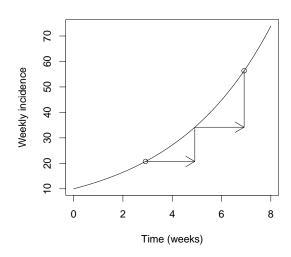
- Which is more dangerous, a fast disease, or a slow disease?
 - How are we measuring speed?
 - How are we measuring danger?
 - What do we already know?

Generation time and risk

- If we know \mathcal{R} , what does the generation time tell us about r?
- If we know r, what does the generation time tell us about \mathbb{R} ?
- $\mathcal{R} = \exp(r\hat{G})$

Generation time and risk





Generation time and risk

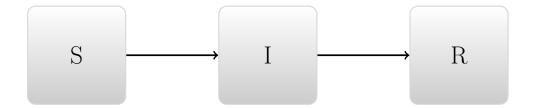
- An intuitive view:
 - Epidemic speed = Generation speed \times Generation strength

• If we know generation speed, then a faster epidemic speed means:

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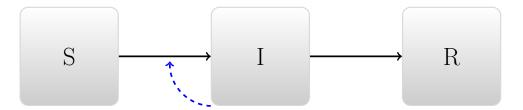
• If we know epidemic speed, a faster generation speed means

3 Single-epidemic model



- Susceptible \rightarrow Infectious \rightarrow Recovered
- ullet We also use N to mean the total population

Transition rates



- What factors govern movement through the boxes?
 - People get better independently
 - People get infected by infectious people

Conceptual modeling

- What happens in the long term if we introduce an infectious individual?

 - ___
 - _

Interpreting

- Why might there not be an epidemic?
- Why doesn't everyone get infected?

Implementing the model

• The simplest way to implement this conceptual model is with differential equations:

$$\frac{dS}{dt} = -\beta \frac{SI}{N}$$

$$\frac{dI}{dt} = \beta \frac{SI}{N} - \gamma I$$

$$\frac{dR}{dt} = \gamma I$$

Quantities

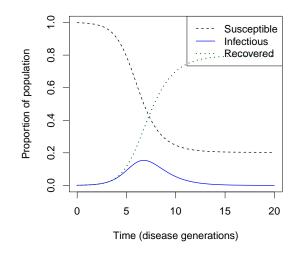
State variables

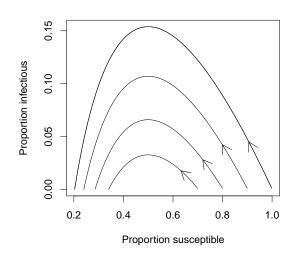
• S, I, R, N: [people] or [people/ha]

Parameters

- Susceptible people have **potentially effective** contacts at rate β (units [1/time])
 - These are contacts that would lead to infection if the person contacted is infectious
 - Total infection rate is $\beta I/N$, because I/N is the proportion of the population infectious
- Infectious people recover at $per\ capita$ rate γ (units [1/time])
 - Total recovery rate is γI
 - Mean time infectious is $D = 1/\gamma$ (units [time])

Simulating the model





Basic reproductive number

• What *unitless* parameter can you make from the model above?

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Basic reproductive number implications

• What happens early in the epidemic if $\mathcal{R}_0 > 1$?

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• What happens early in the epidemic if $\mathcal{R}_0 < 1$?

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Effective reproductive number

• The effective reproductive number gives the number of new infections per infectious individual in a partially susceptible population:

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• Is the disease increasing or decreasing?

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	_
• 1	Why doesn't everyone get infected?
	_
	_
3.1	Epidemic size
•]	In this model, the epidemic always burns out
	 No source of new susceptibles
•]	Epidemic size is determined by:
	_
	_
Ove	rshoot
	Why does more susceptibles at the beginning mean fewer susceptibles at the end?
	_
	_
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Ebola example

- In September, the US CDC predicted "as many as" 1.5 million Ebola cases in Liberia by January
- In fact, their model predicted many *more* cases than that by April
- What happened?

What limits epidemics?

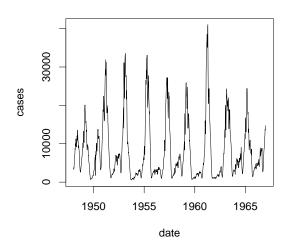
- What limits epidemics in our simple models?
- What else limits epidemics in real life?
- what else limits epidemics in real life:

4 Recurrent epidemic models

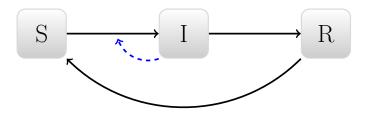
• If epidemics tend to burn out, why do we often see repeated epidemics?

Recurrent epidemics

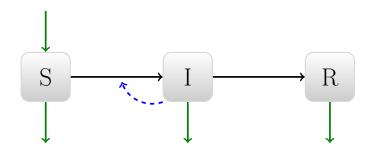
Measles reports from England and Wales



Closing the circle



Closing the circle



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Births and deaths

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$$\frac{dS}{dt} = bN - \beta \frac{SI}{N} - dS$$

•

$$\frac{dI}{dt} = \beta \frac{SI}{N} - \gamma I - dI$$

•

$$\frac{dR}{dt} = \gamma I - dR$$

• We often assume b = d

population is constant

Equilibrium

- At equilibrium, we know that $\mathcal{R}_e = 1$
 - One case per case
 - Number of susceptibles at equilibrium determined by the number required to keep infection in balance

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$$S/N = 1/\mathcal{R}_0$$

- Number of infectious individuals determined by number required to keep susceptibles in balance.
- As susceptibles go up, what happens?
 - Per capita replenishment goes down
 - Infections required goes down

Reciprocal control

 \bullet What happens if we protect susceptibles (move them to R class)?

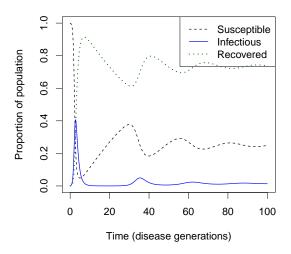
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•	What	else	could	happen
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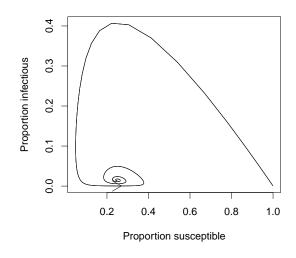
Reciprocal control

• What happens if we remove infectious individuals at a constant rate (find them and cure them or isolate them)?

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Tendency to oscillate





Tendency to oscillate

- "Closed-loop" SIR models (ie., with births or loss of immunity):
 - Tend to oscillate
 - Oscillations tend to be damped
 - * System reaches an **endemic** equilibrium disease persists

Source of oscillations

- Similar to predator-prey systems
- What happens if we start with too many susceptibles?

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Persistent oscillations

• If oscillations tend to be damped in simple models, why do they persist in real life?

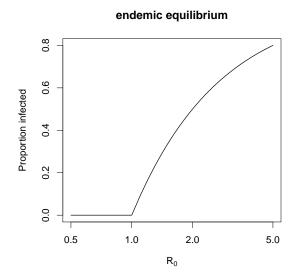
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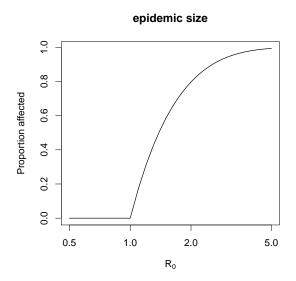
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5 Reproductive numbers and risk

- At equilibrium, the proportion of people who are susceptible to disease should be approximately $S/N = 1/\mathcal{R}_0$
- Proportion "affected" (infectious or immune) should be approximately $V/N = 1 1/\mathcal{R}_0$
- If you have a single, fast epidemic, the size is also predicted by \mathcal{R}_0 .

Reproductive numbers and risk





Examples

- Ronald Ross predicted 100 years ago that reducing mosquito densities by a factor of 5 or so would *eliminate* malaria
- Gradual disappearance of polio, typhoid, etc., without risk factors going to zero
- Eradication of smallpox!

Threshold for elimination

• What proportion of the population should be vaccinated to eliminate a disease?

Examples:

- Polio has an \mathcal{R}_0 of about 5.
- What proportion of the population should be vaccinated to eliminate polio?

• Measles has an \mathcal{R}_0 of about 20. What proportion of the population should be vaccinated to eliminate measles?

Persistence of infectious disease

- Why have infectious diseases persisted?
 - The pathogens evolve
 - Human populations are heterogeneous
 - * People differ in: nutrition, exposure, access to care
 - Information and misinformation
 - * Vaccine scares, trust in health care in general

Heterogeneity and persistence

- Heterogeneity increases \mathcal{R}_0
 - When disease is rare, it is concentrated in the most vulnerable populations
 - * Cases per case is high
 - * Elimination is harder
- Marginal populations
 - Heterogeneity could make it easier to concentrate on the most vulnerable populations and eliminate disease
 - Humans rarely do this, however: the populations that need the most support typically have the least access

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