

# UNIT 6: Competition

# Outline

## Introduction

### Population model with competition

- Balanced competition

- Unbalanced competition

### Population-level interactions

- Invasion theory

- Colonization and co-existence

### Niches and coexistence

- The competitive exclusion principle

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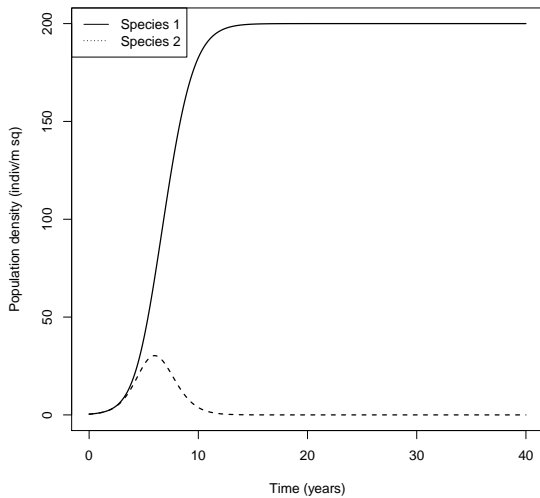
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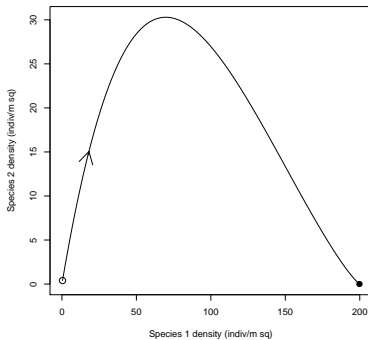
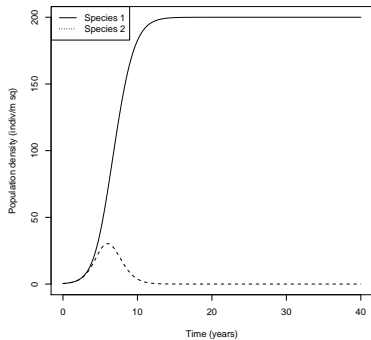
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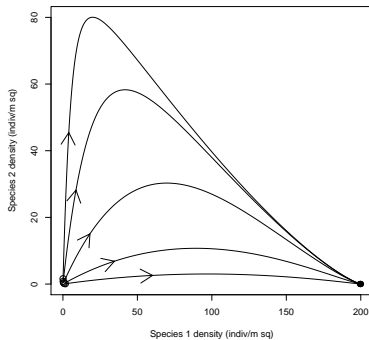
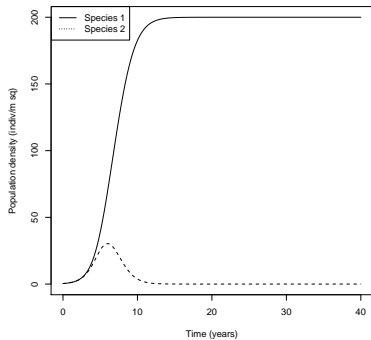
## Dominance time plot



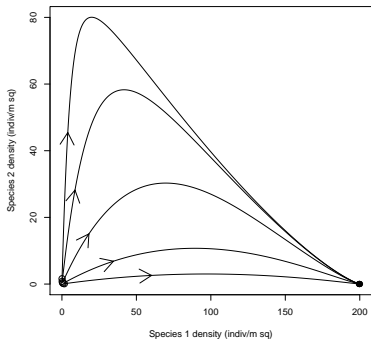
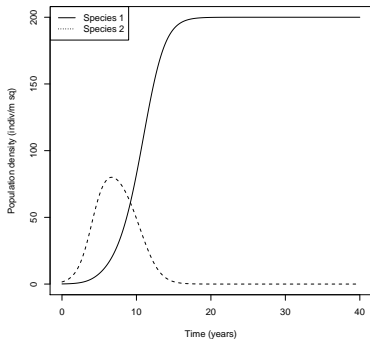
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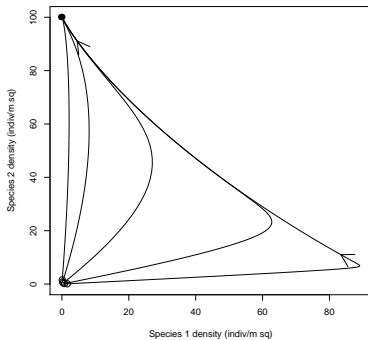
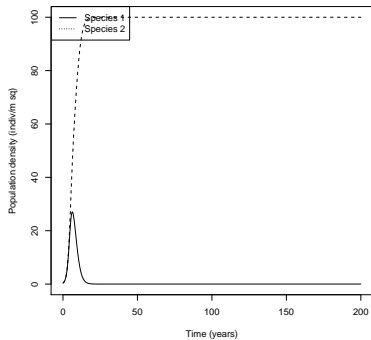
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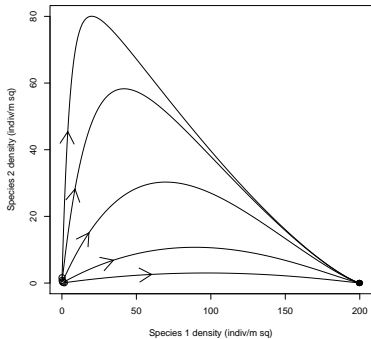
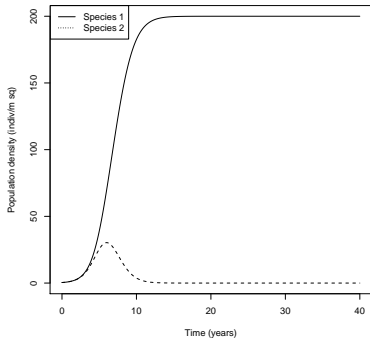
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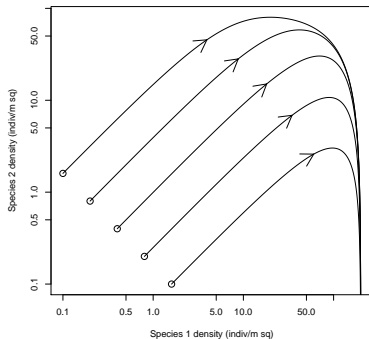
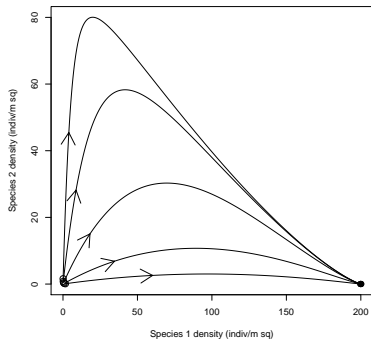
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# Outline

## Introduction

## Population model with competition

- Balanced competition

- Unbalanced competition

## Population-level interactions

- Invasion theory

- Colonization and co-existence

## Niches and coexistence

- The competitive exclusion principle

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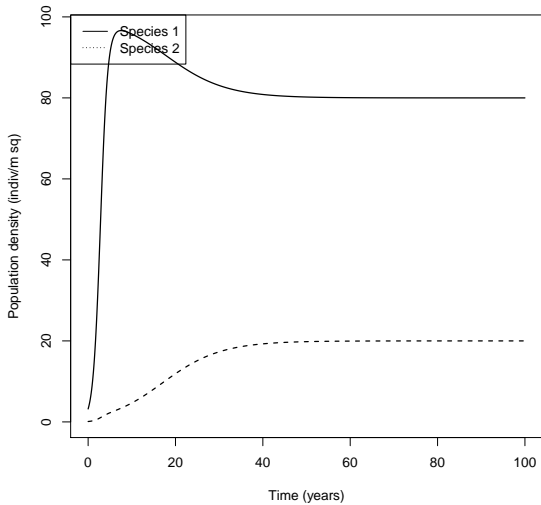
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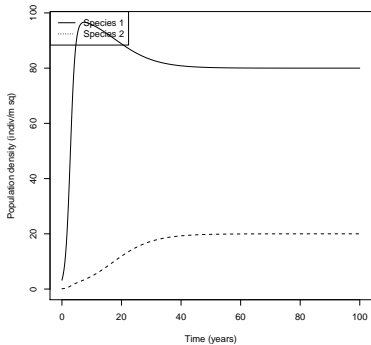
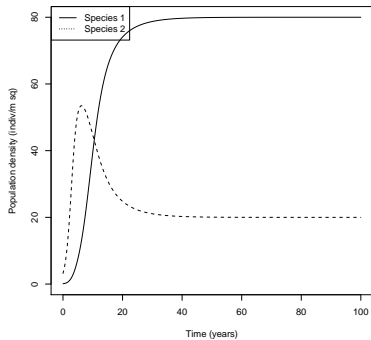


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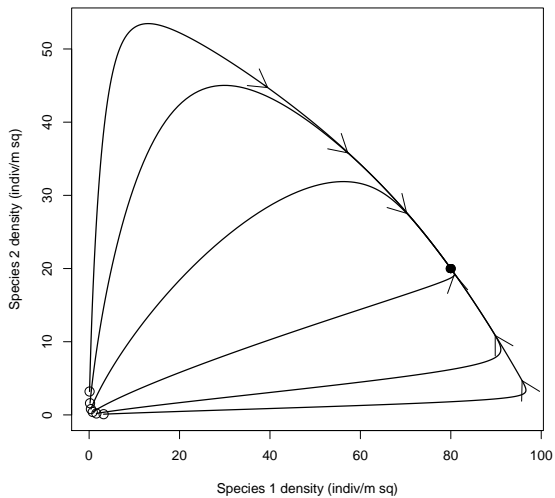




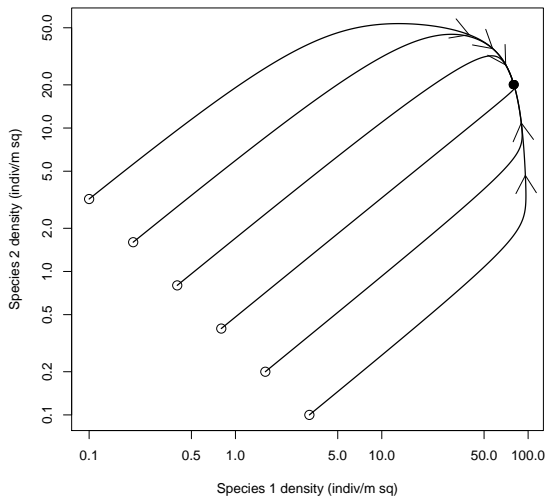
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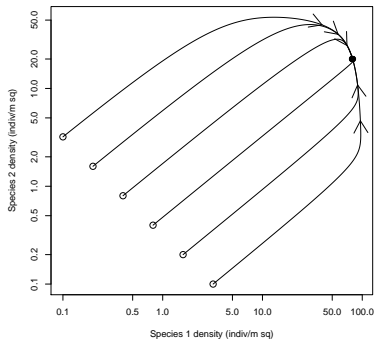
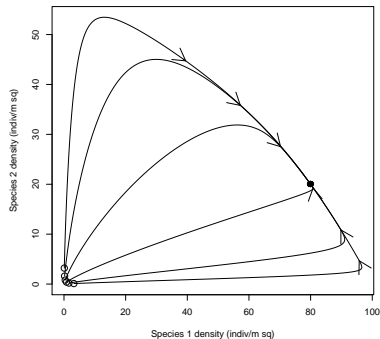
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# Coexistence phase plot (log scale)



# Coexistence phase plots



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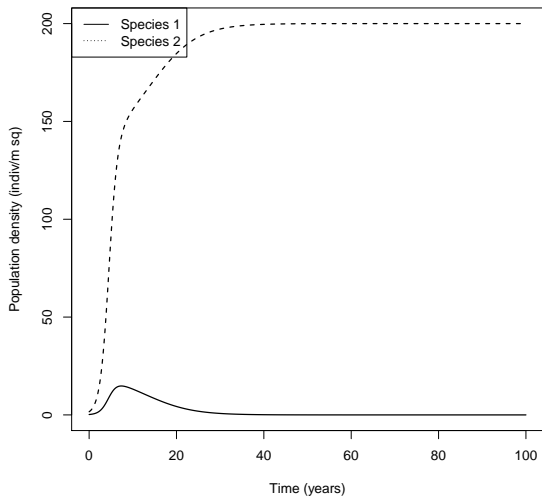


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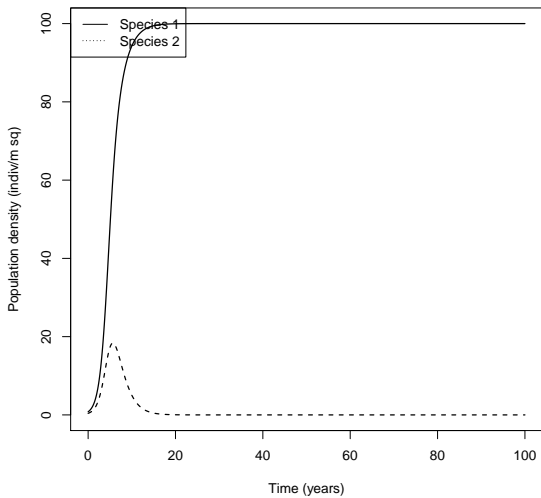


*Changing the environment*

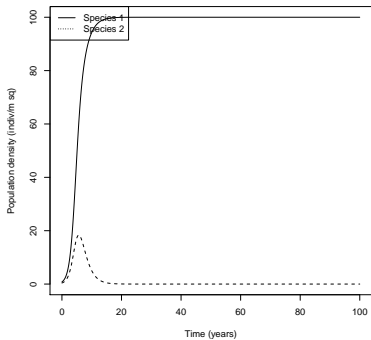
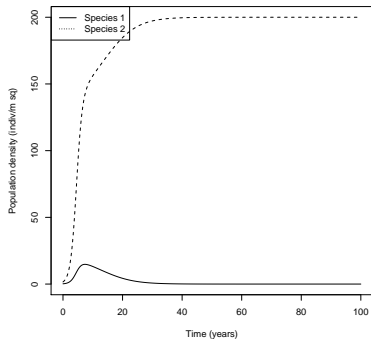
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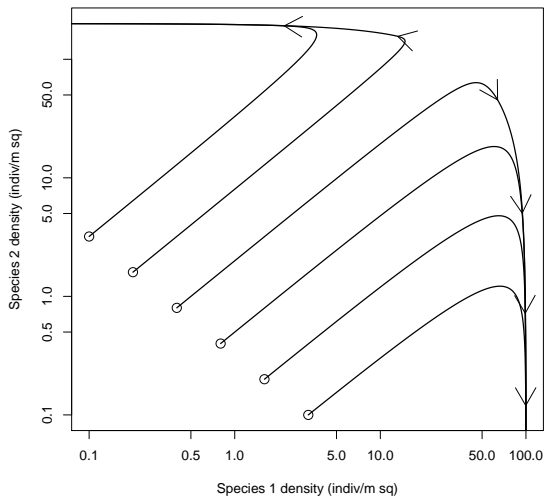


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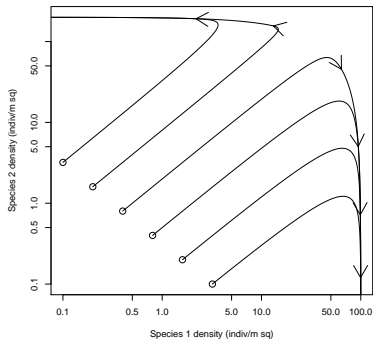
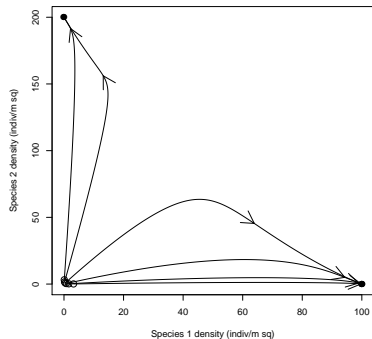




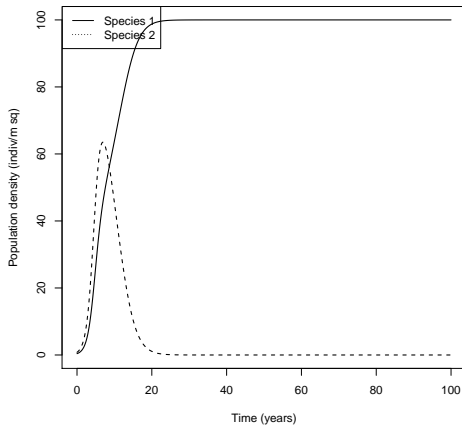
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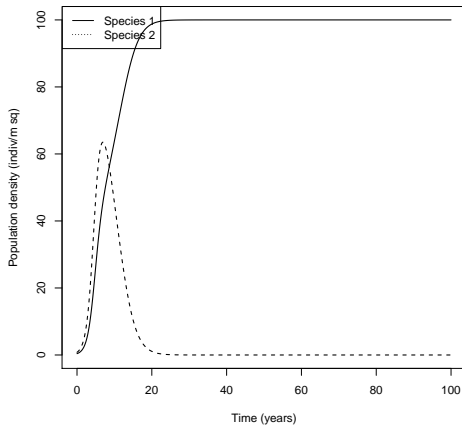
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- Balanced competition

- Unbalanced competition

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- Invasion theory

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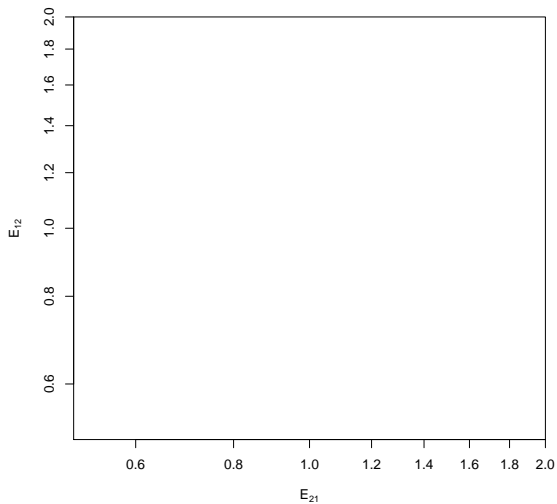
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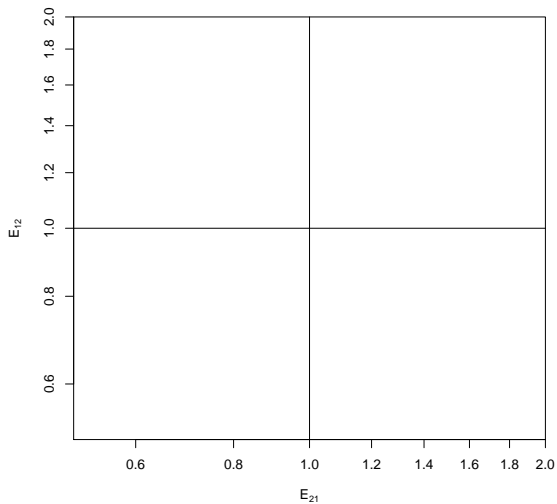
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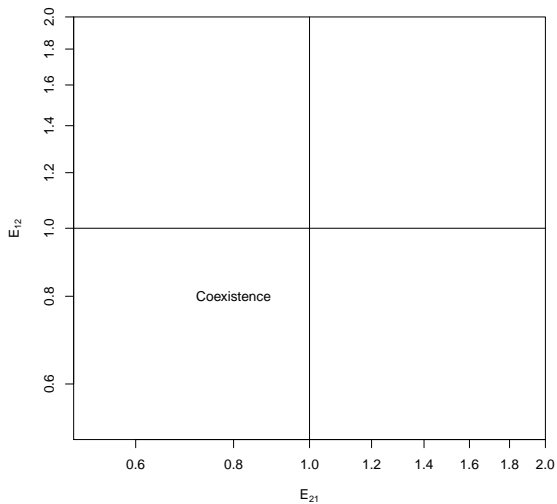
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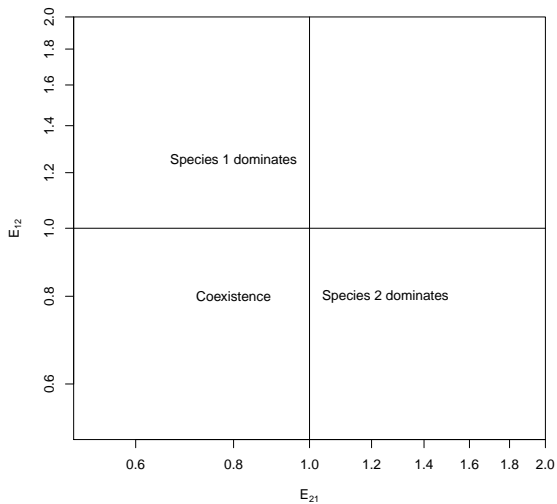
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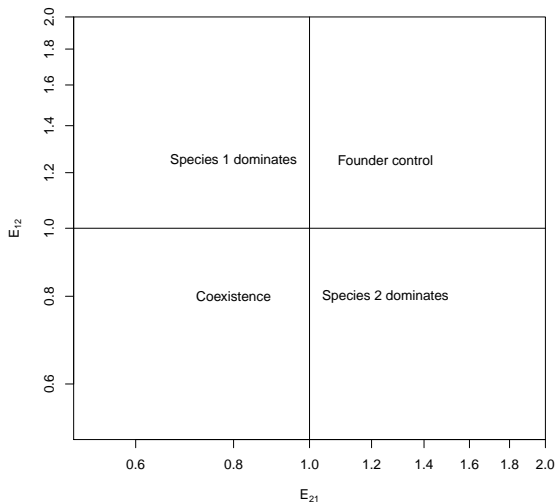
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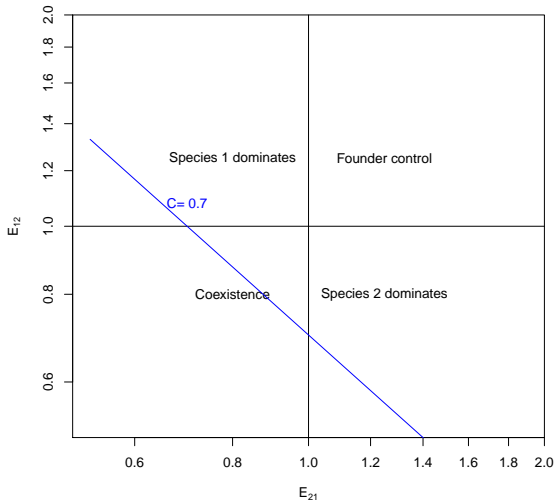
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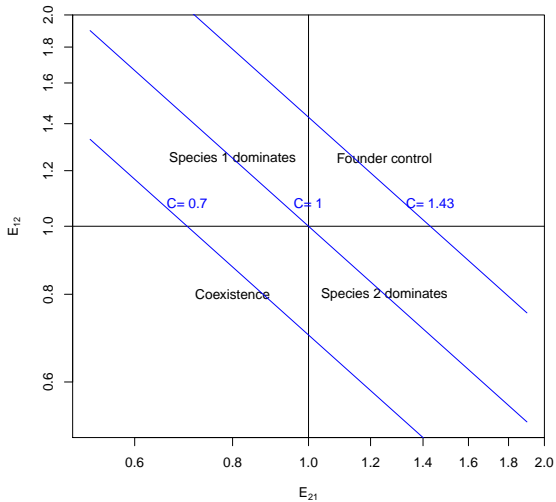


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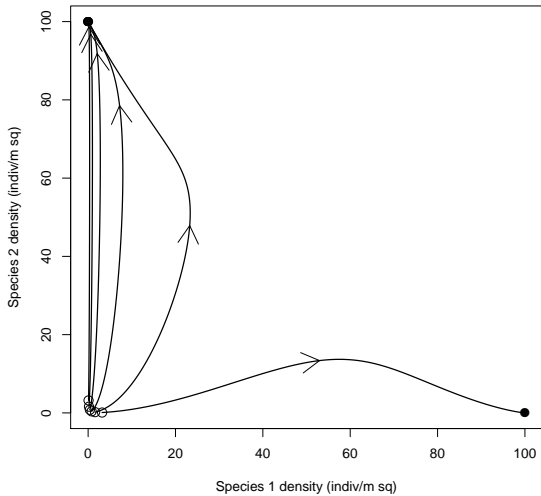
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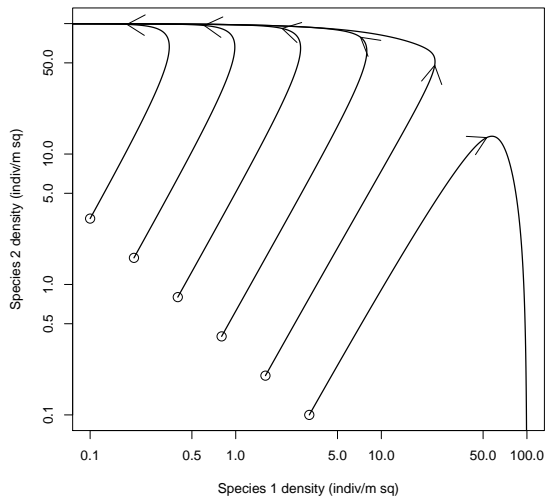
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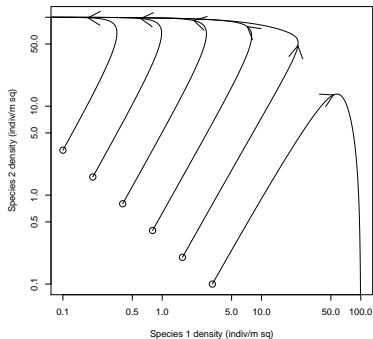
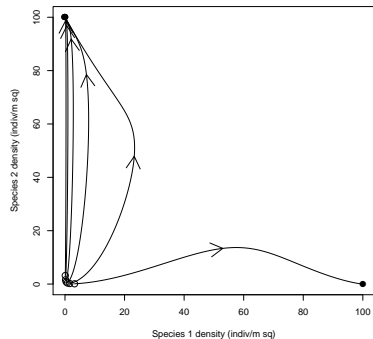
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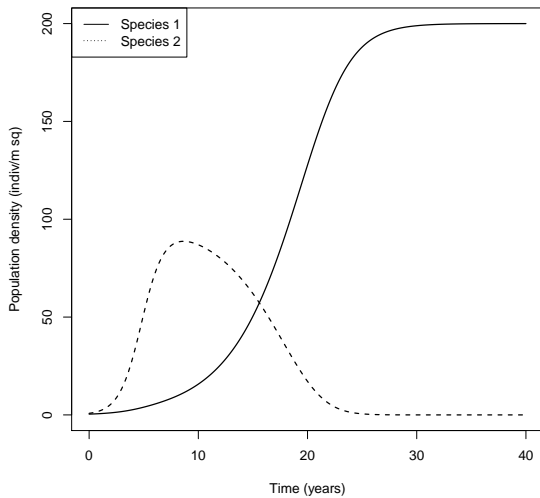
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Ka Hana 'Iani Nā'auao - A Science Careers Curriculum Resource Go to: [www.sds.kapiti.edu.nz/keha](http://www.sds.kapiti.edu.nz/keha)

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