

UNIT 7: Exploitation

Outline

Introduction

- Balance and equilibrium

- Tendency to oscillate

A simple model

- Dynamics

- Reciprocal control

Adding details

- Dynamics

- Equilibria

Who controls whom?

Introduction

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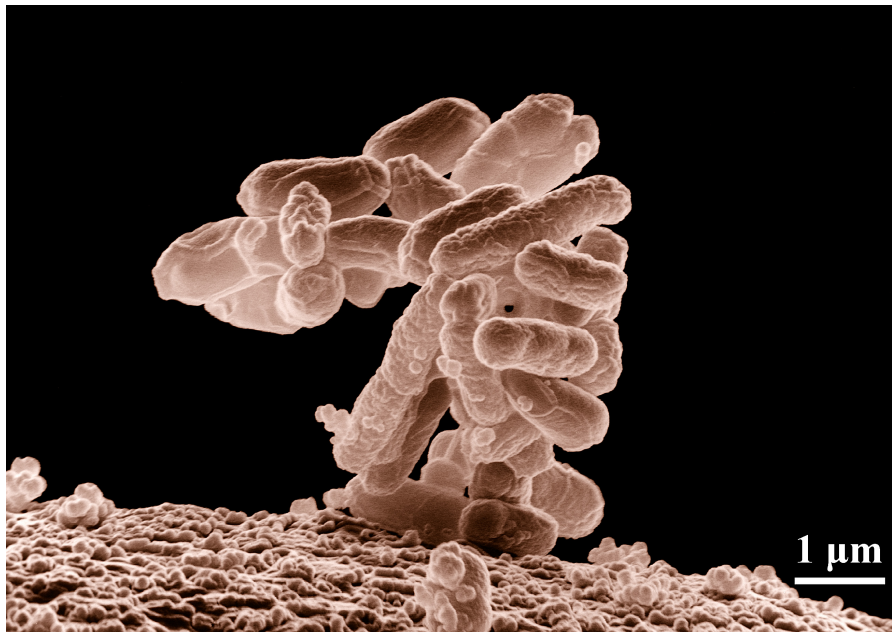
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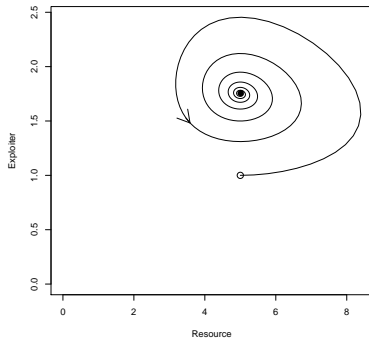
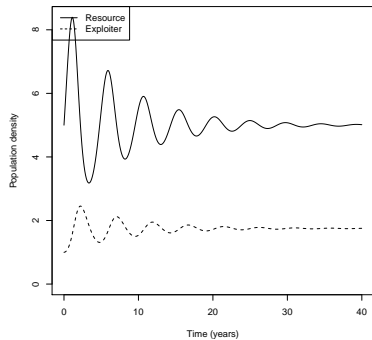
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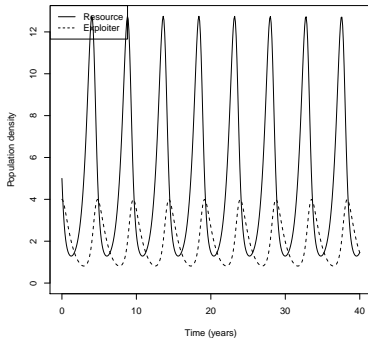
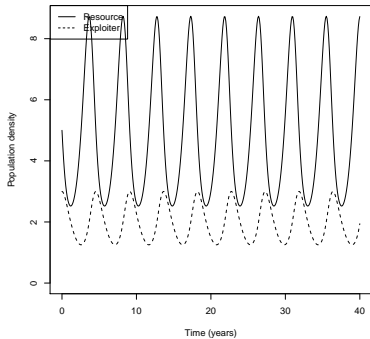
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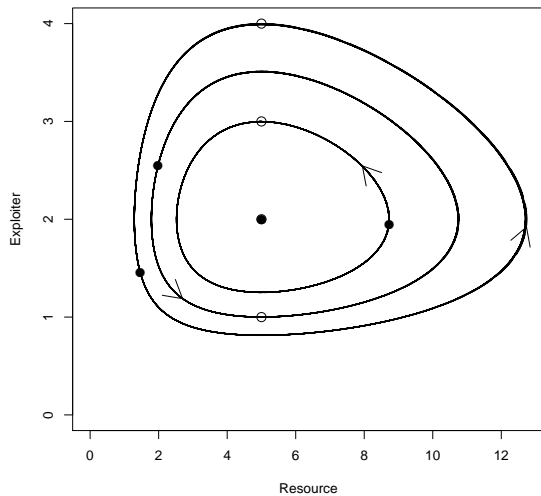
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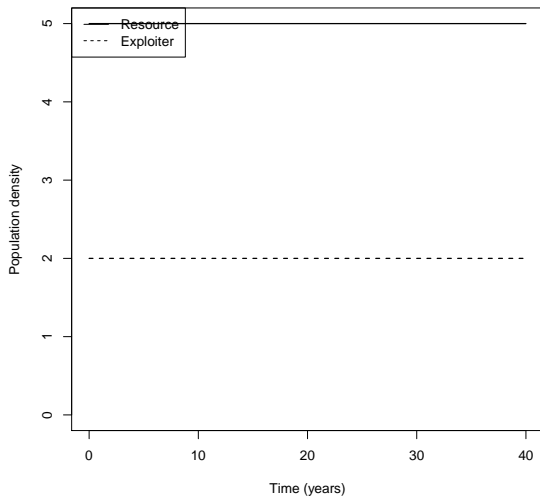
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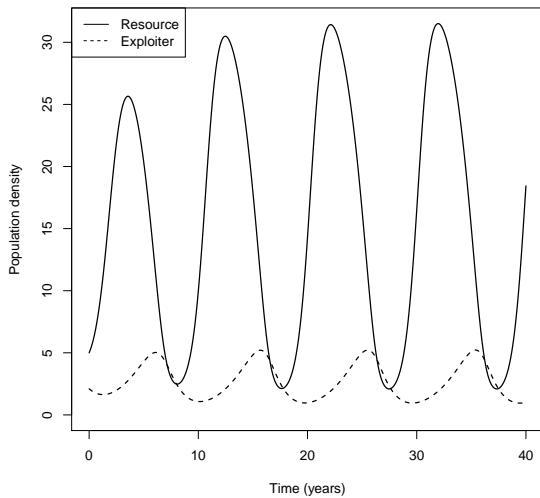
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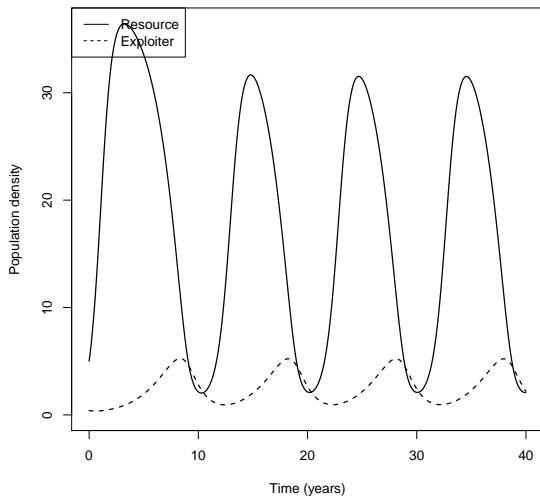
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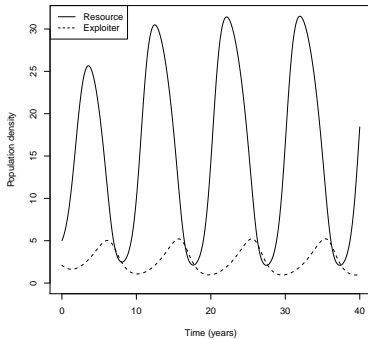
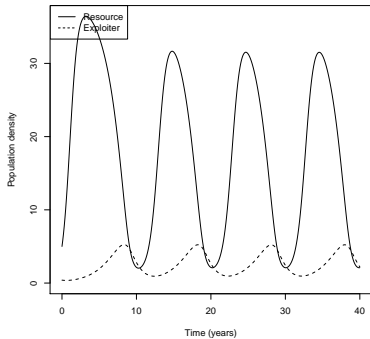
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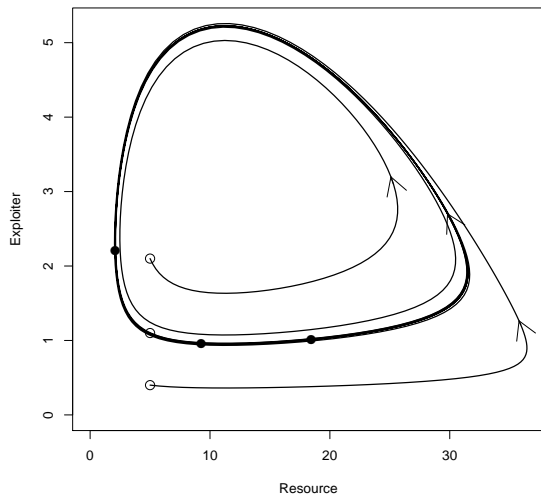
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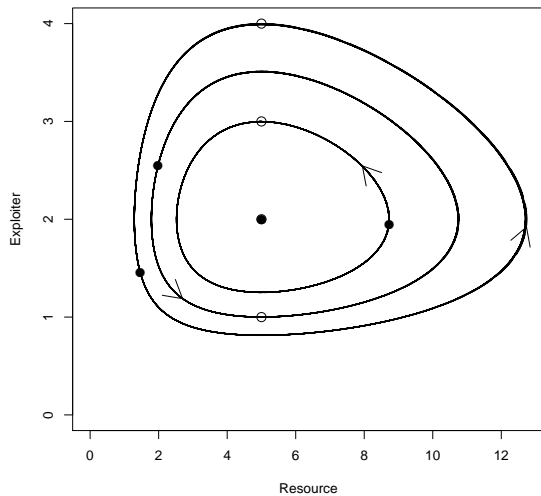
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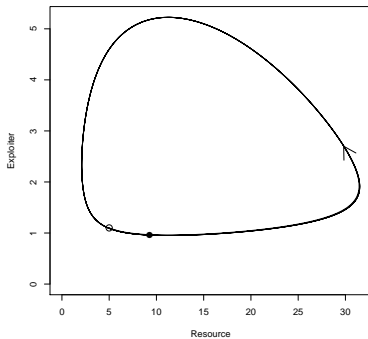
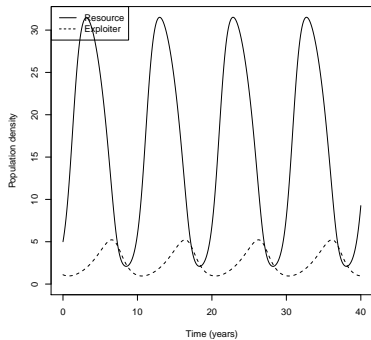
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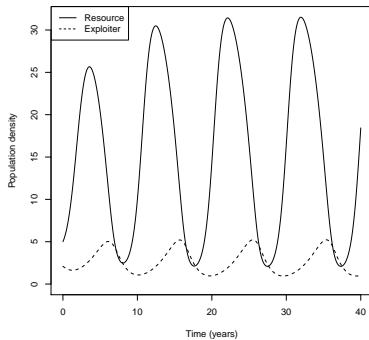
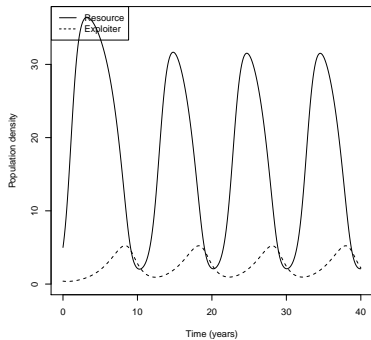
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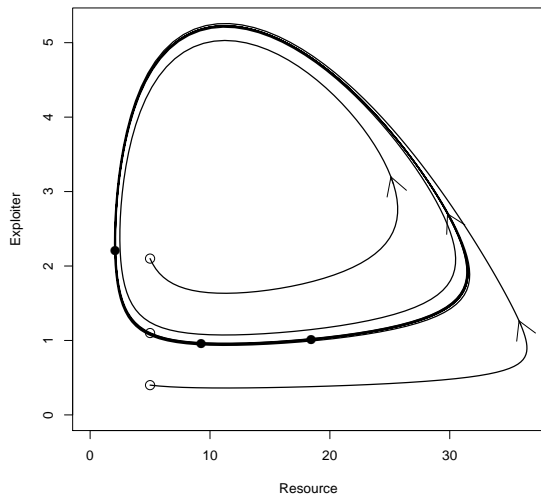
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Adding details

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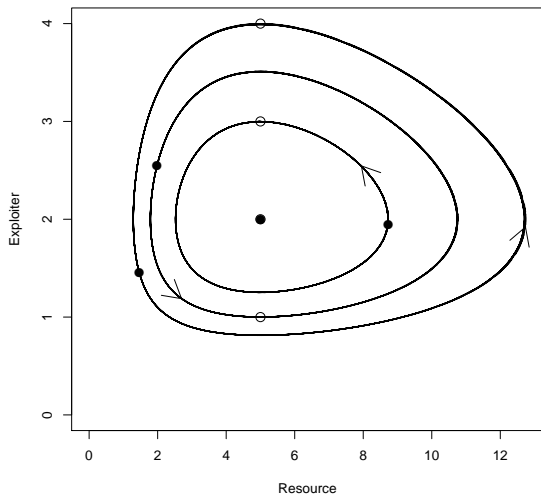
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People and the ocean



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- Balance and equilibrium

- Tendency to oscillate

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- Dynamics

- Reciprocal control

Adding details

- Dynamics

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Who controls whom?

How do populations affect their own growth rates?



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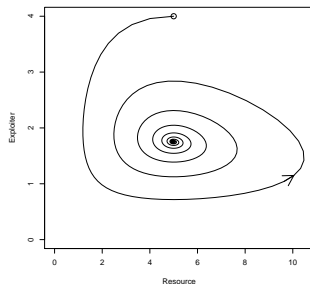
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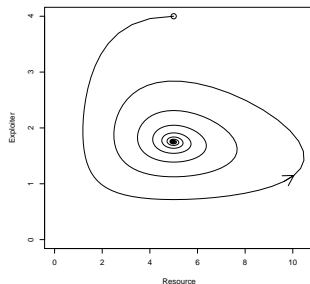
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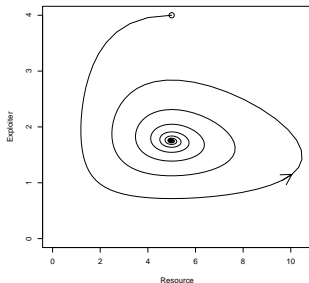
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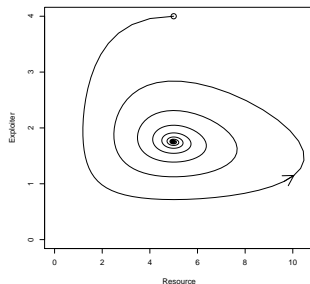
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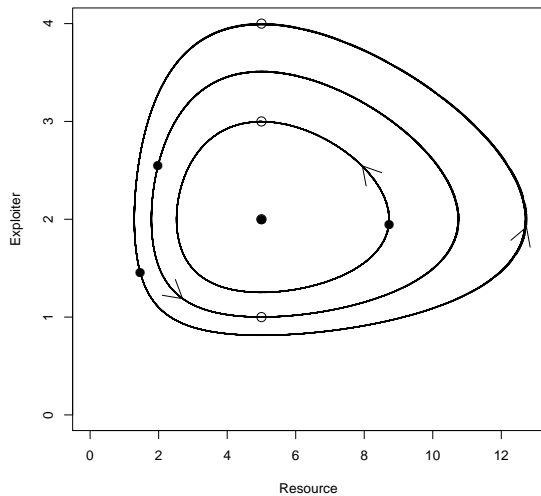


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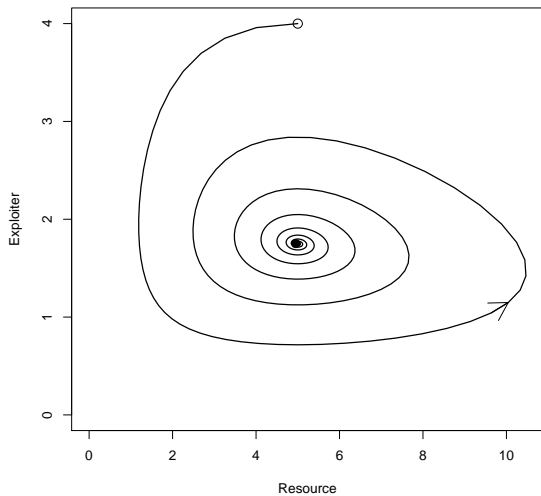
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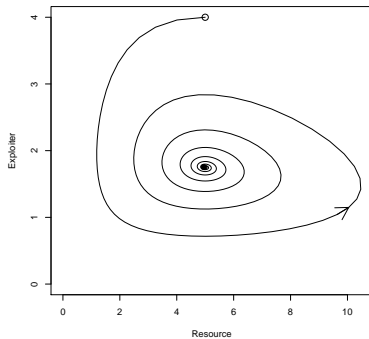
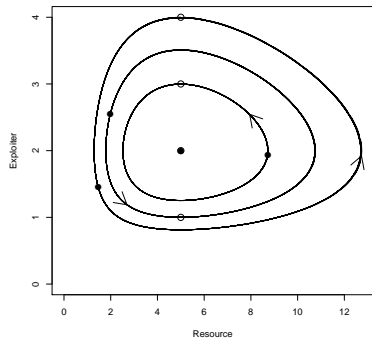
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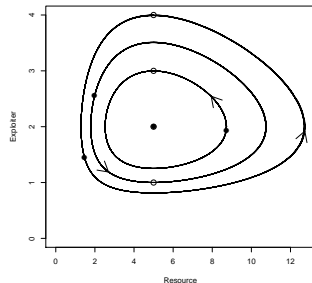


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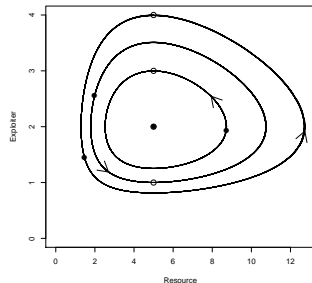
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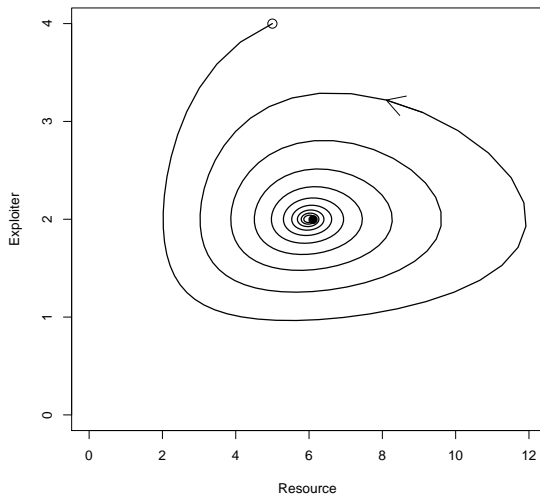


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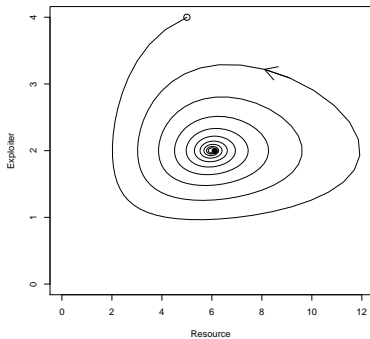
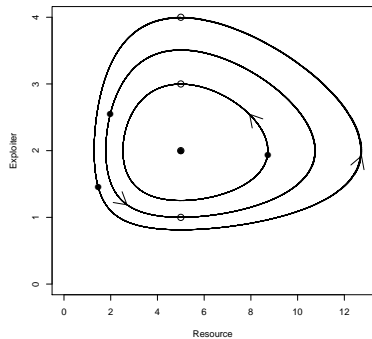
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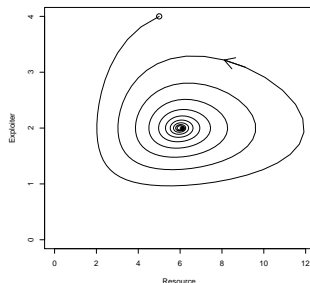


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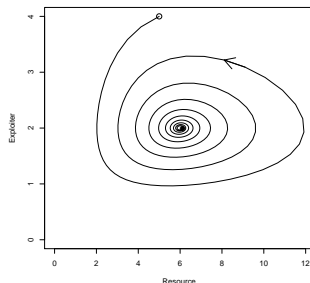
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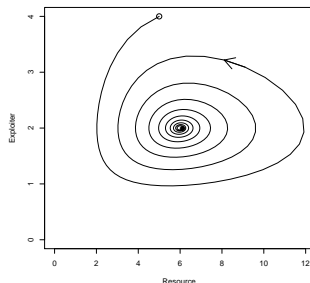
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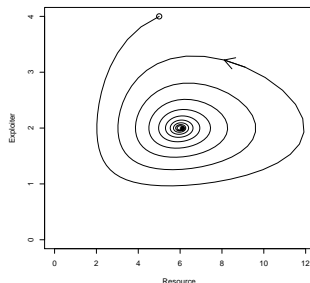
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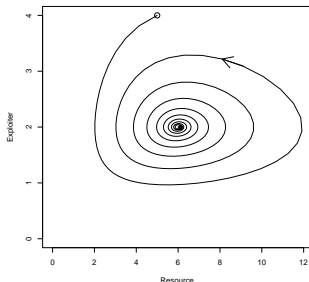
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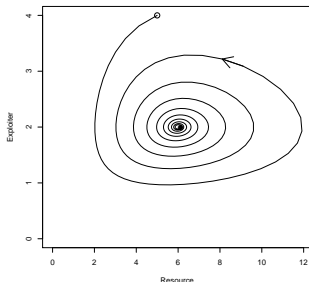
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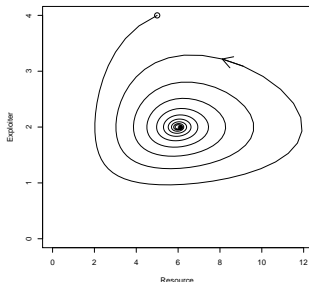
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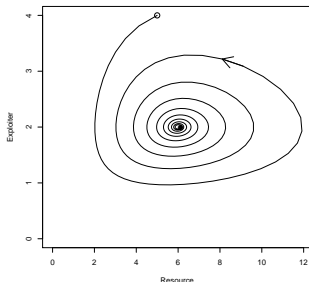
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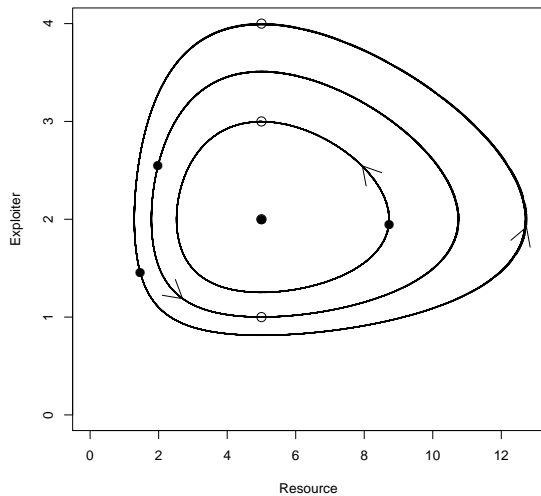
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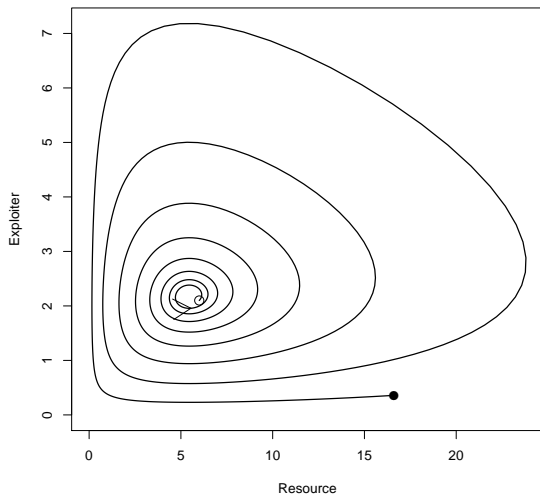
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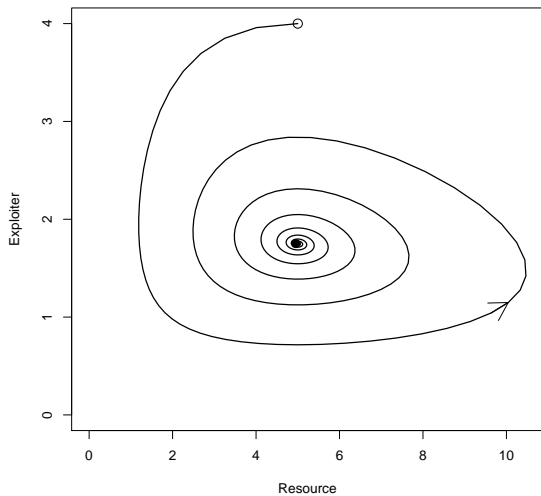
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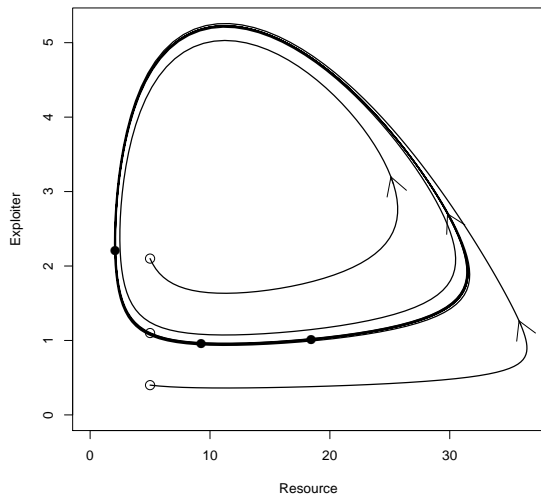
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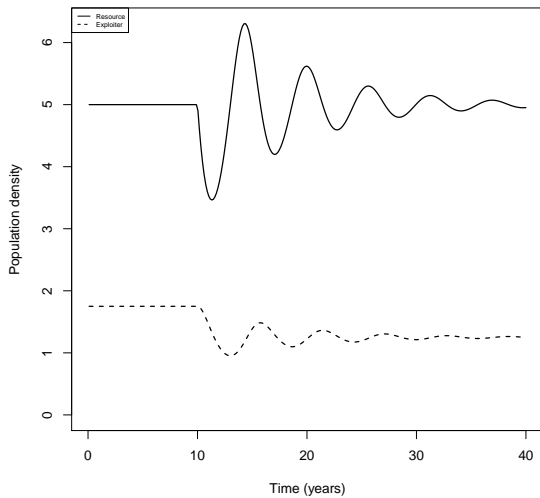
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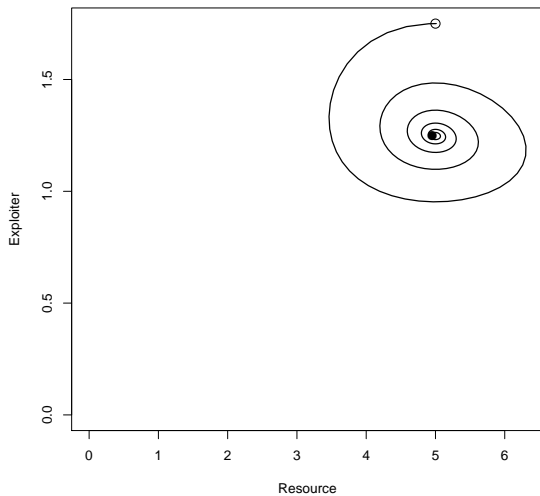
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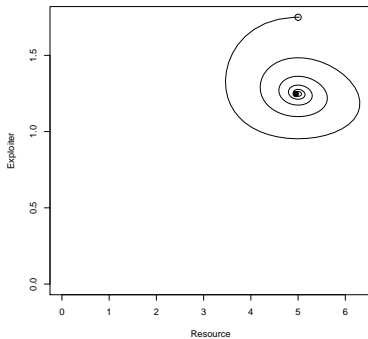
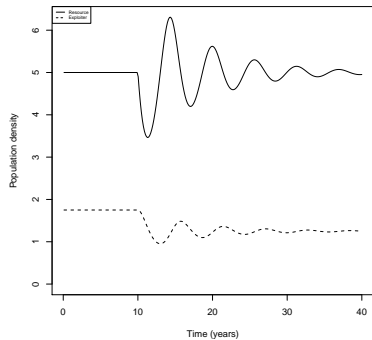
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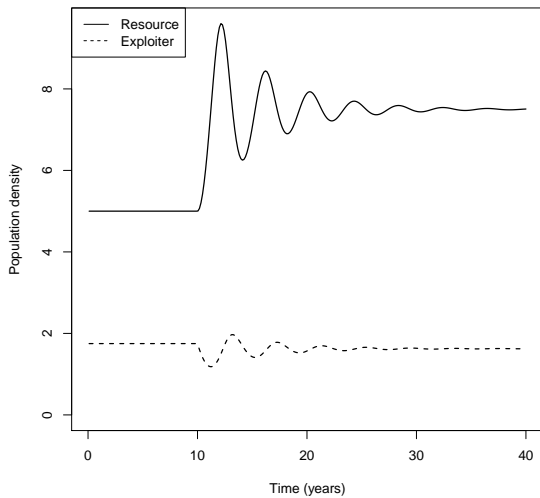
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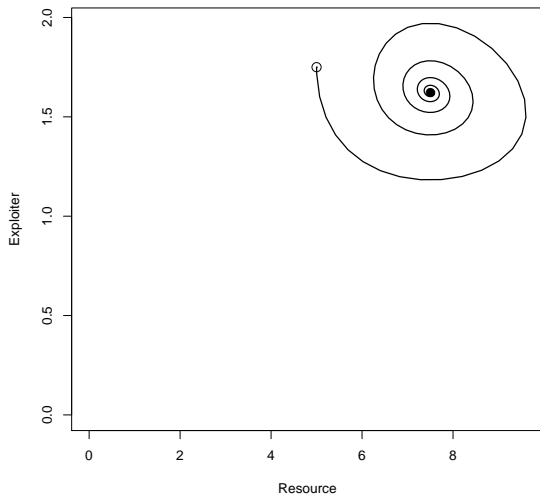
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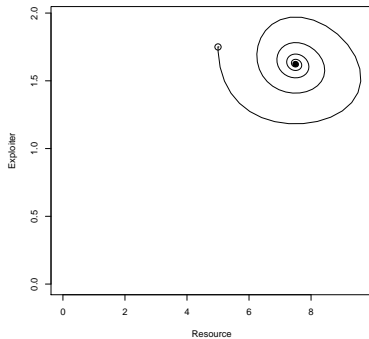
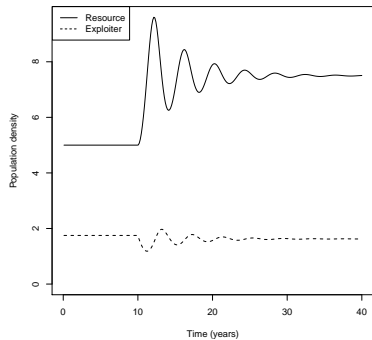
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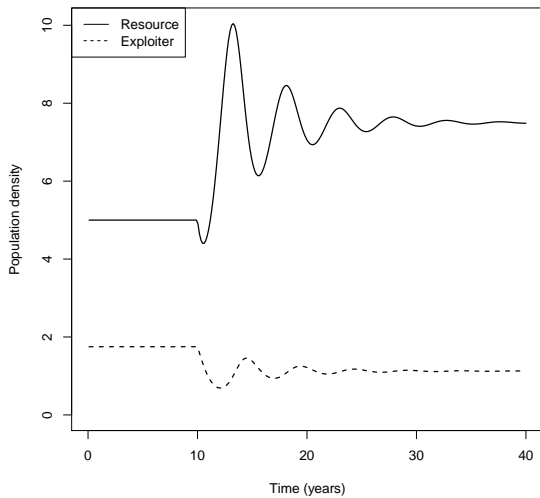
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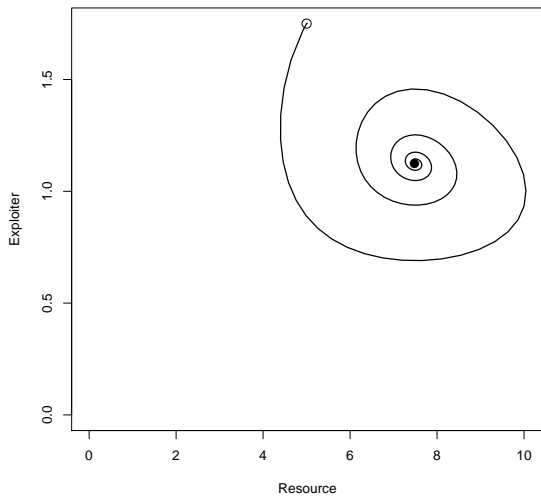
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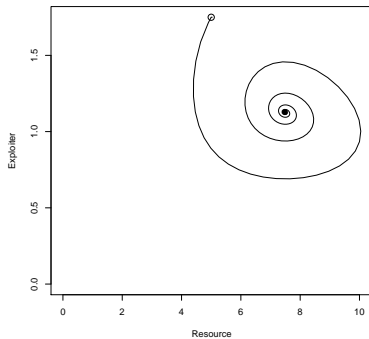
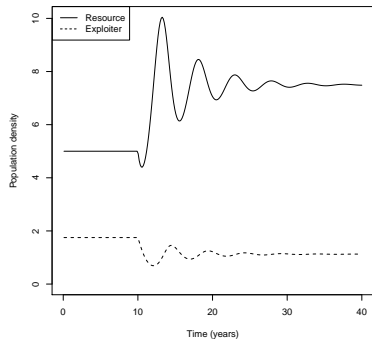
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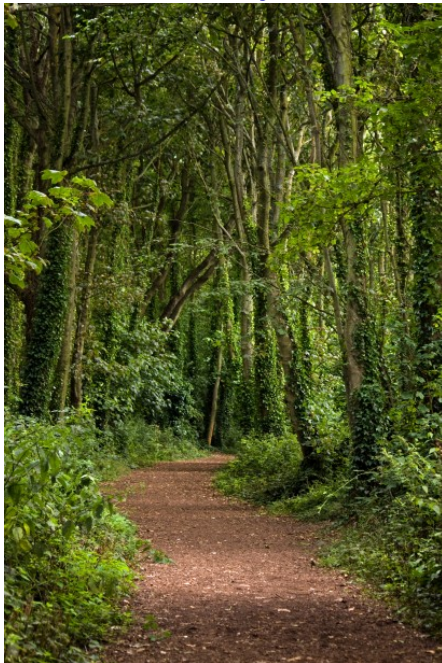
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