

$$\text{let } \underline{X} = \begin{bmatrix} x_{11} & x_{12} & \dots & x_{1p} \\ x_{21} & x_{22} & \dots & x_{2p} \\ \vdots & \vdots & & \vdots \\ x_{n1} & x_{n2} & & x_{np} \end{bmatrix}$$

data matrix w/ variables in columns

$$\underline{S} = \text{cov}(\underline{X})$$

$(p \times p)$

$$\underline{V} = \begin{bmatrix} \vec{v}_1 & \vec{v}_2 & \dots & \vec{v}_p \end{bmatrix}$$

$(p \times p)$

matrix w/ eigenvectors of S columns

$$\underline{l} = [l_1 \quad l_2 \quad \dots \quad l_p]$$

eigenvalues of S

Variance summarized by k^{th} PC: $\sqrt{l_k}$

$$\text{PC Scores matrix: } \underline{W} = \underline{X} \underline{V}$$

$$\text{PC loadings matrix: } \underline{V} \underline{L}^{-\frac{1}{2}}$$

$$\text{where } \underline{L}^{-\frac{1}{2}} = \begin{bmatrix} \sqrt{l_1} & & 0 \\ & \sqrt{l_2} & \\ 0 & & \ddots \\ & & & \sqrt{l_p} \end{bmatrix}$$