# Supplement for: countfitteR: efficient selection of count distributions to assess DNA damage

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**Abstract**: Count data, one of the most common data types in many fields. In personalized medicine and pharmacology, the analysis is relevant for numerous applications, such as cancer and ageing research and in the evaluation of drug efficacy [1-5]. By default it is assumed to follow the Poisson distribution. This assumption, however, may lead to biased results and faulty conclusions in data bodies with excess zero values (zero-inflation [6,7]), a variance larger than the mean (overdispersion), or both. In such cases, the standard assumption of a Poisson distribution would skew the estimation of mean and variance, and other models like the negative binomial (NB), zero-inflated Poisson or zero-inflated NB distributions should be employed. The model chosen has an influence on the parameter estimation (mean value and confidence interval). Yet the choice of the most suitable distribution model is not trivial. To support and simplify this process, we have implemented the countfitteR software, which is provided as an R package and a web server. We show the application of our software based on examples of count data from phenotypic imaging as used in radiomics and precision medicine: DNA double-strand breaks (DSBs) [8]. DSBs are a highly specific and sensitive molecular biomarker for monitoring DNA damage in cancer, aging research and the evaluation of drug efficacy, and are detected and quantified by foci formation in fluorescence microscopy. In analyzing a large number of datasets of a molecular pharmacological markers (phosphorylated Histone H2AX and p53 binding protein [9,10]), countfitteR demonstrated an equal or superior statistical performance compared to the usually employed two-step procedure, with an overall power of up to 98 %. In addition, it still gave information in cases with no result at all from the two-step procedure. In our data sample we found that the NB distribution was the most frequent, with the Poisson distribution taking second place. Originally

designed for the analysis of foci in biomedical image data, countfitteR can be used in a variety of areas where non-Poisson distributed counting data is prevalent. —

# 1 General information about the countfitteR graphical user interface

#### 1.1 Charts

Each chart may be saved in the .svg (Scalable Vector Graphic) format. A download button is always located at the top of a chart.

#### 1.2 Tables

Tables may be downloaded in a specified format or printed using the buttons at the top of the table.

#### 1.3 Data upload

The data format suitable for upload is the .csv file, where a single column corresponds to a single count (Note: example files are included in the package). Use raw counts instead a pivot table! If your document does not have headers, specify it using the "Header" checkbox. In this case, countfitteR will automatically name your counts with the index number of a count prefixed by 'C'.

#### 1.4 Count data

This panel contains descriptive statistics and summaries of the input data. It consists of three subpanels:

- 1. Count table: the input dataset in the tabular format allowing sanity checks and manual modification. 2. Summary: summary statistics of the input data (respectively mean, standard deviation, median, median absolute deviate, minimum, maximum, number of elements).
- 3. Distribution: a bar chart of the counts distribution followed by a pivot table.

#### 1.5 Fitted models

- 1. Mean value estimates: the estimated value of mean  $(\lambda)$  and its confidence intervals. The BIC indicates the most appropriate distribution.
- 2. Coefficients: coefficients of fitted models.
- 3. Decision: the most appropriate model and the strength of the evidence [11].

#### 1.6 Compare distributions

The bar charts represent theoretical counts depending on the chosen distribution. Red dots describe the real number of counts. The visualized data is also available in the tabular format.

#### 1.7 Settings

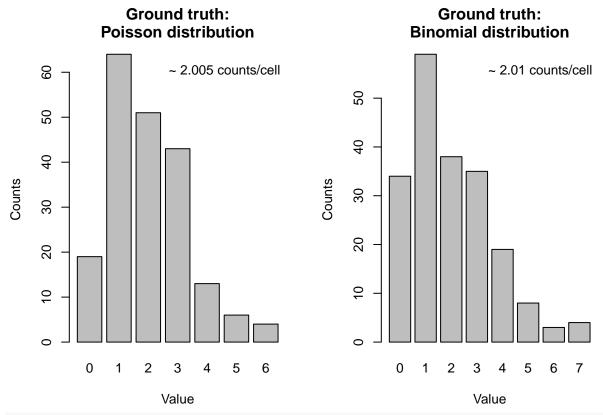
**Separate experiments**: if this checkbox is marked, the **countfitteR** assumes that experiments are separate and fits the distribution to each individually and independently. Otherwise, all counts are simultaneously fitted to a single model. It is more appropriate for situations, where there is assumption that all samples may be describe by the same distribution, for example in case of technical replicates.

Confidence level: the confidence level of confidence intervals.

Count distributions: count distributions fitted to data: Poisson, Negative Binomial, Zero-Inflated Poisson, Zero-Inflated Negative Binomial. Possible distributions are described further in the manual.

## 2 Usage of the countfitteR software via the R console

```
# Below is an example of how to work with the countfitteR software in the
# R environment. For a simple example data was simulated.
# Generate poisson (Poisson data) and negative binomial (nBinomial data)
# distributed count data in silico. Here 200 random integer numbers
# (= 200 cells) were generated for both distributions.
# The simulation was set to mimic data with a low number of counts (low number
# of foci per cell in average).
set.seed(007)
df <- data.frame(Poisson_data = rpois(200, 1.85),</pre>
                 nBinomial_data = rnbinom(200, 8.5, 0.8))
# Inspect the first 10 and last 10 data points via the head() and tail()
# functions, respectively.
head(df, n = 10)
##
      Poisson_data nBinomial_data
## 1
                 6
## 2
                 1
                                 0
## 3
                 0
                                 0
## 4
                 0
                                 3
                                2
## 5
                 1
## 6
                 3
                                2
## 7
                 1
                                 1
## 8
                 5
                                1
                                7
## 9
## 10
                                 1
tail(df, n = 10)
       Poisson_data nBinomial_data
## 191
                  1
                                  3
## 192
                  2
                                  1
## 193
                  3
                                  1
## 194
                  2
                                  0
                                  2
## 195
                  Λ
## 196
                                  2
                                 3
## 197
                  1
## 198
                  4
                                  1
## 199
                  1
                                  0
## 200
                  1
# Visualize the count data after tabulation of the frequencies of both data sets.
# The red vertical lines indicate the arithmetic means of the data samples.
par(mfrow = c(1,2), cex = 0.8)
# Plot for the data with a Poisson distribution
barplot(table(df[, "Poisson_data"]), main = "Ground truth:\nPoisson distribution",
        xlab = "Value", ylab = "Counts")
legend("topright", paste("~", mean(df[, "Poisson_data"]), "counts/cell"), bty = "n")
```



# Note the arithmetic means (Mean  $\sim$  2) and median (Median  $\sim$  2) of the samples # are very similar, as determined by the summary() function.

# summary(df)

```
##
    Poisson_data
                   nBinomial_data
##
   Min.
          :0.000
                   Min.
                          :0.00
   1st Qu.:1.000
                   1st Qu.:1.00
##
  Median :2.000
                   Median:2.00
##
         :2.005
## Mean
                   Mean :2.01
  3rd Qu.:3.000
                   3rd Qu.:3.00
##
## Max.
          :6.000
                   Max.
                          :7.00
```

# For the analysis the countfitteR package is loaded

#### library(countfitteR)

```
\# Next we use the fit_counts() function to fit counts to distributions. In our \# case the data are fitted to the Poisson, Negative Binomial (NB), Zero-Inflated \# Poisson (ZIP) and the Zero-Inflated Negative Binomial (ZINB) distributions.
```

```
fc <- fit_counts(df, model = "all")
summ <- summary_fitlist(fc)</pre>
```

```
# distribution for the count data in the html-friendly format.
# Note: the decide() function gives a verbal output for the decision
# stating how substantial a model fit is.

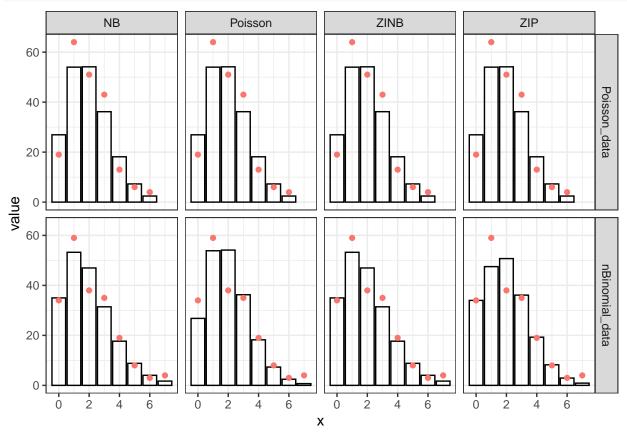
decide(summ, separate = TRUE)

## [1] "Count name: nBinomial_data<br/>The most appropriate model (model with the lowest BIC value): NB
# Next, the empirical distribution of counts with the distribution defined by
# the model fitted to counts are compared. The bar charts represent theoretical
# counts depending on the chosen distribution. Red dots describe the real number
# of counts.

fitcmp <- compare_fit(df, fitlist = fit_counts(df, model = "all"))</pre>
```

# Next, the decide() function is used to select the most appropriate

plot\_fitcmp(fitcmp)



```
# Finally, the counts are fitted to model(s) using the count name as the
# explanatory variable. Estimates are presented in the table below along with the
# BIC values of their models from the summary_fitlist() function. Estimated
# coefficients of models (lambda for all distributions, theta for NB and ZINB,
# r for ZIP and ZINB).

results <- summary_fitlist(fc)
# Sort the dataset according to their BIC values and print them as table.</pre>
```

knitr::kable(results[order (results[["BIC"]]),])

	count	lambda	lower	upper	BIC	theta	r	model
1	Poisson_data	2.005000	1.818057	2.211166	666.8974	NA	NA	Poisson
3	Poisson_data	2.005010	1.818064	2.211179	672.1961	NA	0.0000034	ZIP
5	Poisson_data	2.005000	1.818050	2.211174	672.1975	2.715018e + 04	NA	NB
7	Poisson_data	2.004999	1.818052	2.211171	677.4951	2.836674e + 05	0.0000078	ZINB
6	$nBinomial\_data$	2.010000	1.796391	2.249009	728.5517	6.261040e+00	NA	NB
2	$nBinomial\_data$	2.010000	1.822812	2.216410	731.1431	NA	NA	Poisson
4	$nBinomial\_data$	2.135487	1.902169	2.397424	733.3299	NA	0.0587695	ZIP
8	$nBinomial\_data$	2.010036	1.796331	2.249165	733.8502	6.261978e + 00	0.0000182	ZINB

# 3 Sample records of counting data

The countfitteRsoftware contains sample data sets of counting data. These were obtained from measurements on human cells. Further information about the data can be found in the documentation of the countfitteR-package.

- case\_study: Short version of the 'case\_study\_FITC' for the biomarker phosphorylated Histone H2AX
- case\_study\_all: Case study with two fluorescent dyes (biomarker phosphorylated Histone H2AX & biomarker p53 binding protein)
- case\_study\_APC: Case study for APC dye for the biomarker p53 binding protein
- case\_study\_FITC: Case study for FITC dye for the biomarker phosphorylated Histone H2AX

```
# Output the first five columns and rows measured values of the dataset
# `case_study_FITC`. Each measuring point of a data series corresponds to the
# number of gamma H2AX foci per cell (~> 0 = no foci per cell).
countfitteR::case_study_FITC[1:5, 1:5]
```

```
L3_AF_DMSO_B_10_FITC L3_AF_100_ETP_11_FITC L3_AF_100_ETP_12_FITC
##
## 1
                          0
                                                  0
## 2
                          0
                                                  0
                                                                          19
## 3
                          0
                                                  0
                                                                          0
## 4
                                                  1
                                                                          12
## 5
                                                                           4
     L3_AF_Med_C_13_FITC L3_AF_Med_C_14_FITC
##
## 1
## 2
                         0
                                               0
                         0
## 3
                                               0
## 4
                         0
                                               0
## 5
```

# 4 Overdispersion of count data

One of the important features of the Poisson distribution is the equality of variance and expected value. Although count data is commonly assumed to be Poisson-distributed, we often encounter overdispersed datasets, when the variance is bigger than the mean. Three distributions included in **countfitteR**: Zero-Inflated Poisson (ZIP), Negative Binomial (NB) and Zero-negative Binomial (ZINB) model overdispersed counts.

Overdispersion may be caused by the increased variability of counts, for example when a counting algorithm under- and overcounts. In such situation the data might have the NB distribution. The other cause of

overdispersion is called zero-inflation and occurs in datasets, where some factor introduced faulty zeros. That means that some counts, regardless of their real state, are treated as zeros. In this case, data has the ZIP distribution. If both faulty zeros and increased variance affect the data, the ZINB distribution is the most appropriate.

#### 4.1 Overdispersed count data distribution

Poisson and Negative Binomial distributions have the same expected value. In case of ZIP and ZINB, the expected value is smaller than the real average number of foci per cell.

**Table S1**: Expected value and variance of Poisson, ZIP, NB and ZINB distributions.  $\lambda$ : Poisson parameter (number of occurrences, e.g., average number of foci per cell). r: zero inflation (fraction of occurrences treated as zeros, e.g., fraction of cells treated by system as having no foci regardless of their real state).  $\theta$ : dispersion parameter.

Distribution name	Expected value	Variance
Poisson	$E(X) = \lambda$	$var(X) = \lambda$
ZIP	$E(X) = (1 - r)\lambda$	$var(X) = \lambda(1-r)(1+\lambda r)$
NB	$E(X) = \lambda$	$var(X) = \lambda + \frac{\lambda^2}{\theta}$
ZINB	$E(X) = (1 - r)\lambda$	$var(X) = (1 - r)\lambda \left(1 + r\lambda + \frac{1}{\theta}\right)$

Depending on the value of r the variance of ZIP and ZINB may be smaller or bigger than the variance of Poisson distribution. In case of the NB distribution, the variance is always bigger than for the Poisson distribution, although the difference becomes negligible, when the  $\theta$  is much bigger than  $\lambda^2$ .

#### Parameters:

- $\lambda$  Poisson parameter (average number of foci per cell).
- r zero inflation (fraction of cells treated by system as having no foci regardless of their real state).
- $\theta$  dispersion parameter.

Usually the NB distribution is parameterized using  $\mu$  and  $\theta$ , but to make comparison clearer, we use  $\lambda$  instead of  $\mu$ . In this parameterization, NB and ZINB are treated as the mixture of Poisson and Gamma ( $\Gamma$ ) distributions.

**Table S2**: Probability mass functions of Poisson, ZIP, NB and ZINB distributions.  $\lambda$ : Poisson parameter (number of occurrences, e.g., average number of foci per cell). r: zero inflation (fraction of occurrences treated as zeros, e.g., fraction of cells treated by system as having no foci regardless of their real state).  $\theta$ : dispersion parameter.

Distribution name pmf

Poisson

$$P\{X = k\} = \frac{\lambda^k \exp^{-\lambda}}{k!}$$

Zero-inflated Poisson

$$P\{X = k\} = \begin{cases} r + (1 - r) \exp^{-\lambda}, & \text{if } k = 0 \\ r \frac{\lambda^k \exp^{-\lambda}}{k!}, & \text{if } k = 1, 2, \dots \end{cases}$$

Negative Binomial

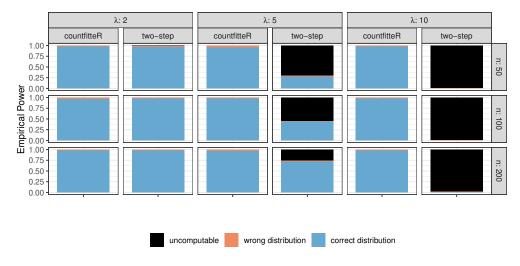
$$P\{X = k\} = \frac{\Gamma(\theta + k)}{\Gamma(\theta)k!} \left( \left( \frac{\theta}{\theta + \lambda} \right)^{\theta} \left( \frac{\lambda}{\theta + \lambda} \right) \right)^{k}$$

Zero-inflated Negative Binomial

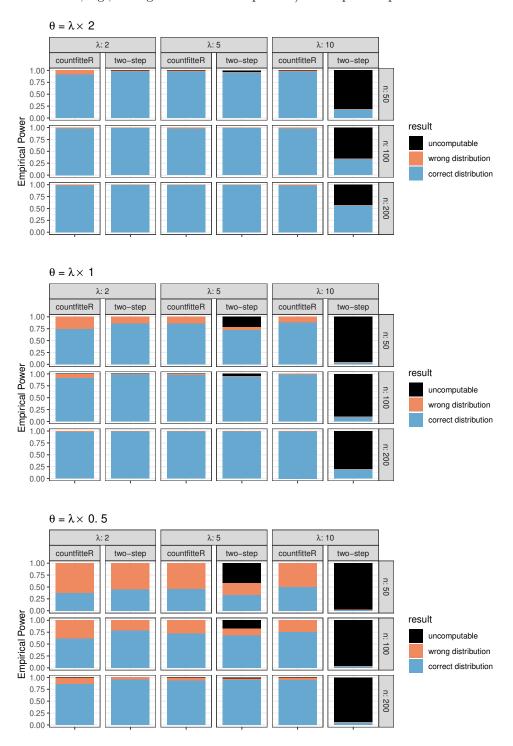
$$P\{X = k\} = \begin{cases} r + (1 - r) \left(\frac{\theta}{\theta + \lambda}\right)^{\theta}, & \text{if } k = 0\\ (1 - r) \frac{\Gamma(\theta + k)}{\Gamma(\theta) k!} \left(\left(\frac{\theta}{\theta + \lambda}\right)^{\theta} \left(\frac{\lambda}{\theta + \lambda}\right)\right)^{k}, & \text{if } k = 1, 2 \end{cases}$$

#### 4.2 Results of the simulation

Figure S1: Empirical power of count fitteR and two-step test for Poisson distribution. n: number of counts in the sample.  $\lambda$ : Poisson parameter (number of occurrences, e.g., average number of foci per cell).



**Figure S2**: Empirical power of countfitteR and two-step test for NB distribution.  $\lambda$ : Poisson parameter (number of occurrences, e.g., average number of foci per cell).  $\theta$ : dispersion parameter.



**Table S3**: Comparison of count fitteR empirical power with two-step procedure for Poisson distribution with three possible sample sizes (n = 50, 100, 200) and three possible means ( $\lambda$  = 2, 5, 10).

model	method	n	lambda	pow_mean	pow_sd	uncomputable
pois	count fitte R	50	2	0.9780000	0.1467567	0
pois	count fitte R	100	2	0.9760000	0.1531256	0
pois	count fitte R	200	2	0.9850000	0.1216133	0
pois	count fitte R	50	5	0.9600000	0.1960572	0
pois	count fitte R	100	5	0.9770000	0.1499783	0
pois	count fitte R	200	5	0.9720000	0.1650553	0
pois	count fitte R	50	10	0.9840000	0.1255379	0
pois	count fitte R	100	10	0.9880000	0.1089397	0
pois	count fitte R	200	10	0.9800000	0.1400701	0
pois	two-step	50	2	0.9808468	0.1371326	8
pois	two-step	100	2	0.9880000	0.1089397	0
pois	two-step	200	2	0.9800000	0.1400701	0
pois	two-step	50	5	0.9595960	0.1972373	703
pois	two-step	100	5	0.9759825	0.1532707	542
pois	two-step	200	5	0.9690860	0.1732011	256
pois	two-step	50	10	1.0000000	0.0000000	998
pois	two-step	100	10	0.3333333	0.5773503	997
pois	two-step	200	10	0.8571429	0.3631365	986

**Table S4**: Comparison of countfitteR and two-step procedure empirical power for ZIP distribution with three possible sample sizes (n = 50, 100, 200), three possible means ( $\lambda$  = 2, 5, 10), and dispersion parameter r ranging from 0.1 to 0.9.

nb         countfitteR         50         2         1.0         0.9150000         0.2790212           nb         countfitteR         100         2         1.0         0.9800000         0.1400701           nb         countfitteR         200         2         1.0         0.9890000         0.1043546           nb         countfitteR         50         2         2.0         0.7410000         0.4383048           nb         countfitteR         100         2         2.0         0.9210000         0.2698737           nb         countfitteR         200         2         2.0         0.9820000         0.1330176           nb         countfitteR         50         2         4.0         0.3760000         0.4846224	0 0 0 0 0 0 0 0 0 0
nb         countfitteR         200         2         1.0         0.9890000         0.1043546           nb         countfitteR         50         2         2.0         0.7410000         0.4383048           nb         countfitteR         100         2         2.0         0.9210000         0.2698737           nb         countfitteR         200         2         2.0         0.9820000         0.1330176	0 0 0 0 0 0 0 0
nb     countfitteR     50     2     2.0     0.7410000     0.4383048       nb     countfitteR     100     2     2.0     0.9210000     0.2698737       nb     countfitteR     200     2     2.0     0.9820000     0.1330176	0 0 0 0 0 0 0
nb     countfitteR     100     2     2.0     0.9210000     0.2698737       nb     countfitteR     200     2     2.0     0.9820000     0.1330176	0 0 0 0 0 0
nb countfitteR 200 2 2.0 0.9820000 0.1330176	0 0 0 0 0
	0 0 0 0
ph countfitteB 50 9 4.0 0.2760000 0.4846224	0 0 0 0
nb countfitteR 50 2 4.0 0.3760000 0.4846224	0 0 0
nb countfitteR 100 2 4.0 0.6200000 0.4856293	0
nb countfitteR 200 2 4.0 0.8650000 0.3418946	0
nb countfitteR 50 5 2.5 0.9790000 0.1434558	
nb countfitteR 100 5 2.5 0.9850000 0.1216133	Ω
nb countfitteR 200 5 2.5 0.9920000 0.0891288	U
nb countfitteR 50 5 5.0 0.8590000 0.3481957	0
nb countfitteR 100 5 5.0 0.9800000 0.1400701	0
nb countfitteR 200 5 5.0 0.9930000 0.0834144	0
nb countfitteR 50 5 10.0 0.4610000 0.4987261	0
nb countfitteR 100 5 10.0 0.7240000 0.4472405	0
nb countfitteR 200 5 10.0 0.9410000 0.2357426	0
nb countfitteR 50 10 5.0 0.9840000 0.1255379	0
nb countfitteR 100 10 5.0 0.9860000 0.1175492	0
nb countfitteR 200 10 5.0 0.9890000 0.1043546	0
nb countfitteR 50 10 10.0 0.8840000 0.3203852	0
nb countfitteR 100 10 10.0 0.9880000 0.1089397	0
nb countfitteR 200 10 10.0 0.9900000 0.0995485	0
nb countfitteR 50 10 20.0 0.4980000 0.5002462	0
nb countfitteR 100 10 20.0 0.7520000 0.4320679	0
nb countfitteR 200 10 20.0 0.9490000 0.2201078	0
nb two-step 50 2 1.0 0.9870000 0.1133307	0
nb two-step 100 2 1.0 0.9980000 0.0446990	0
nb two-step 200 2 1.0 1.0000000 0.0000000	0
nb two-step 50 2 2.0 0.8610000 0.3461196	0
nb two-step 100 2 2.0 0.9900000 0.0995485	0
nb two-step 200 2 2.0 0.9990000 0.0316228	0
nb two-step 50 2 4.0 0.4490000 0.4976411	0
nb two-step 100 2 4.0 0.7820000 0.4130940	0
nb two-step 200 2 4.0 0.9550000 0.2074079	0
nb two-step 50 5 2.5 0.9968944 0.0556700	34
nb two-step 100 5 2.5 0.9990000 0.0316228	0
nb two-step 200 5 2.5 1.0000000 0.0000000	0
-	215
nb two-step 100 5 5.0 0.9958159 0.0645829	44
nb two-step 200 5 5.0 1.0000000 0.0000000	3
	416
-	171
nb two-step 200 5 10.0 0.9753846 0.1550294	25
<u>.</u>	811
<u>.</u>	657
·	438
<u>.</u>	959

model	method	n	lambda	size	pow_mean	pow_sd	uncomputable
nb	two-step	100	10	10.0	1.0000000	0.0000000	899
nb	two-step	200	10	10.0	1.0000000	0.0000000	801
nb	two-step	50	10	20.0	0.7000000	0.4701623	980
nb	two-step	100	10	20.0	0.8666667	0.3457459	970
nb	two-step	200	10	20.0	0.9833333	0.1290994	940

**Table S5**: Comparison of count fitteR empirical and two-step procedure empirical power for NB distribution with three possible sample sizes (n = 50, 100, 200), three possible means ( $\lambda$  = 2, 5, 10), and three possible sizes ( $\theta = \frac{\lambda}{2}, \lambda, 2\lambda$ ).

Zip	model	method	n	lambda	r	pow mean	pow_sd	uncomputable
zip         countfitteR         100         2         0.1         0.8830000         0.3215811         0           zip         countfitteR         200         2         0.1         0.9370000         0.2430845         0           zip         countfitteR         100         5         0.1         0.9870000         0.1133307         0           zip         countfitteR         200         5         0.1         0.9990000         0.0995485         0           zip         countfitteR         100         0.1         0.9950000         0.07075690         0           zip         countfitteR         100         0.1         0.9950000         0.0631505         0           zip         countfitteR         100         1.0         1.0         0.9950000         0.031505         0           zip         countfitteR         100         2.0         0.2         0.9930000         0.034144         0           zip         countfitteR         100         2.0         2.0         0.9850000         0.1760881         0           zip         countfitteR         50         5         0.2         0.9950000         0.0705690         0           zip         countf	zip	countfitteR.	50	2	0.1	0.7970000		
zip         countfitteR         200         2         0.1         0.9370000         0.2430845         0           zip         countfitteR         50         5         0.1         0.9610000         0.1930918         0           zip         countfitteR         100         5         0.1         0.9870000         0.1333307         0           zip         countfitteR         50         10         0.1         0.9930000         0.0834144         0           zip         countfitteR         100         10         0.1         0.9930000         0.0631505         0           zip         countfitteR         50         2         0.2         0.8590000         0.0631505         0           zip         countfitteR         50         2         0.2         0.8990000         0.0631505         0           zip         countfitteR         50         2         0.2         0.9580000         0.1760881         0           zip         countfitteR         50         5         0.2         0.9930000         0.0831444         0           zip         countfitteR         50         5         0.2         0.9930000         0.0831288         0 <t< td=""><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></t<>								
zip         countfitteR         50         5         0.1         0.9610000         0.136918         0           zip         countfitteR         100         5         0.1         0.9870000         0.1333307         0           zip         countfitteR         50         0.1         0.9990000         0.0995485         0           zip         countfitteR         100         0.1         0.9950000         0.0705690         0           zip         countfitteR         100         1.0         0.1         0.9950000         0.0631505         0           zip         countfitteR         100         2         0.2         0.8550000         0.3481957         0           zip         countfitteR         100         2         0.2         0.9280000         0.2586173         0           zip         countfitteR         100         5         0.2         0.9930000         0.1760881         0           zip         countfitteR         100         5         0.2         0.9930000         0.0705690         0           zip         countfitteR         100         5         0.2         0.9920000         0.0891288         0           zip         countfitteR								
zip         countfitteR         100         5         0.1         0.9870000         0.1133307         0           zip         countfitteR         200         5         0.1         0.9900000         0.0995485         0           zip         countfitteR         100         10         0.1         0.9930000         0.0834144         0           zip         countfitteR         200         10         0.1         0.9950000         0.0705690         0           zip         countfitteR         50         2         0.2         0.8590000         0.3481957         0           zip         countfitteR         100         2         0.2         0.9280000         0.2586173         0           zip         countfitteR         50         5         0.2         0.9980000         0.1760881         0           zip         countfitteR         50         5         0.2         0.9980000         0.0776690         0           zip         countfitteR         100         5         0.2         0.9980000         0.0776690         0           zip         countfitteR         50         10         0.2         0.99920000         0.0891288         0								
zip         countfitteR         200         5         0.1         0.9900000         0.0995485         0           zip         countfitteR         50         10         0.1         0.9930000         0.0834144         0           zip         countfitteR         100         10         0.1         0.9950000         0.0705690         0           zip         countfitteR         50         2         0.2         0.8590000         0.3481957         0           zip         countfitteR         100         2         0.2         0.9280000         0.2586173         0           zip         countfitteR         200         2         0.2         0.9280000         0.160881         0           zip         countfitteR         100         5         0.2         0.9980000         0.0705690         0           zip         countfitteR         100         5         0.2         0.9990000         0.0891288         0           zip         countfitteR         200         10         0.2         0.9920000         0.0891288         0           zip         countfitteR         100         10         0.2         0.9920000         0.0831288         0								
zip         countfitteR         50         10         0.1         0.9930000         0.0834144         0           zip         countfitteR         100         10         0.1         0.9950000         0.0705690         0           zip         countfitteR         50         2         0.2         0.8590000         0.3481957         0           zip         countfitteR         100         2         0.2         0.9280000         0.2586173         0           zip         countfitteR         200         2         0.2         0.9980000         0.2586173         0           zip         countfitteR         50         5         0.2         0.9980000         0.76690         0           zip         countfitteR         100         5         0.2         0.9950000         0.0705690         0           zip         countfitteR         200         5         0.2         0.9950000         0.0891288         0           zip         countfitteR         100         10         0.2         0.9920000         0.0891288         0           zip         countfitteR         100         10         0.2         0.9920000         0.081555         0								
zip         countfitteR         100         10         0.1         0.9950000         0.0705690         0           zip         countfitteR         200         10         0.1         0.9960000         0.0631505         0           zip         countfitteR         100         2         0.2         0.8590000         0.2886173         0           zip         countfitteR         100         2         0.2         0.9280000         0.2886173         0           zip         countfitteR         50         5         0.2         0.9980000         0.0705690         0           zip         countfitteR         100         5         0.2         0.9950000         0.0705690         0           zip         countfitteR         200         5         0.2         0.9950000         0.0891288         0           zip         countfitteR         100         10         0.2         0.9920000         0.0891288         0           zip         countfitteR         100         10         0.2         0.9920000         0.0891288         0           zip         countfitteR         100         10         0.2         0.9940000         0.0772656         0								
zip         countfitteR         200         10         0.1         0.9960000         0.0631505         0           zip         countfitteR         50         2         0.2         0.8590000         0.3481957         0           zip         countfitteR         100         2         0.2         0.9280000         0.2586173         0           zip         countfitteR         200         2         0.2         0.9860000         0.1760881         0           zip         countfitteR         100         5         0.2         0.9930000         0.0834144         0           zip         countfitteR         200         5         0.2         0.9920000         0.0891288         0           zip         countfitteR         50         10         0.2         0.9990000         0.0631505         0								
zip         countfitteR         50         2         0.2         0.8590000         0.3481957         0           zip         countfitteR         100         2         0.2         0.9280000         0.2586173         0           zip         countfitteR         50         5         0.2         0.9930000         0.1760881         0           zip         countfitteR         100         5         0.2         0.9930000         0.0705690         0           zip         countfitteR         200         5         0.2         0.9920000         0.0891288         0           zip         countfitteR         100         10         0.2         0.9920000         0.0891288         0           zip         countfitteR         100         2         0.3         0.9920000         0.03105357         0								
zip         countfitteR         100         2         0.2         0.9280000         0.2586173         0           zip         countfitteR         200         2         0.2         0.9860000         0.1760881         0           zip         countfitteR         50         5         0.2         0.9930000         0.0705690         0           zip         countfitteR         100         5         0.2         0.9920000         0.0831444         0           zip         countfitteR         50         10         0.2         0.9920000         0.0891288         0           zip         countfitteR         100         10         0.2         0.9940000         0.0631505         0           zip         countfitteR         50         10         0.2         0.9940000         0.0772656         0           zip         countfitteR         50         2         0.3         0.8920000         0.3105357         0           zip         countfitteR         50         2         0.3         0.9390000         0.1400701         0           zip         countfitteR         200         2         0.3         0.980000         0.1255379         0								
zip         countfitteR         200         2         0.2         0.9680000         0.1760881         0           zip         countfitteR         50         5         0.2         0.9930000         0.0834144         0           zip         countfitteR         100         5         0.2         0.9950000         0.0705690         0           zip         countfitteR         50         10         0.2         0.9920000         0.0891288         0           zip         countfitteR         100         10         0.2         0.9920000         0.0891288         0           zip         countfitteR         100         10         0.2         0.9920000         0.0631505         0           zip         countfitteR         100         10         0.2         0.994000         0.07772656         0           zip         countfitteR         100         2         0.3         0.9920000         0.3105357         0           zip         countfitteR         100         2         0.3         0.9820000         0.1400701         0           zip         countfitteR         50         5         0.3         0.9820000         0.140701         0								
zip         countfitteR         50         5         0.2         0.9930000         0.0834144         0           zip         countfitteR         100         5         0.2         0.9950000         0.0705690         0           zip         countfitteR         200         5         0.2         0.9920000         0.0891288         0           zip         countfitteR         100         10         0.2         0.9920000         0.0631505         0           zip         countfitteR         100         10         0.2         0.9940000         0.0631505         0           zip         countfitteR         50         2         0.3         0.9940000         0.0631505         0           zip         countfitteR         50         2         0.3         0.9940000         0.0772656         0           zip         countfitteR         100         2         0.9940000         0.0772656         0           zip         countfitteR         100         2         0.3         0.990000         0.1407701         0           zip         countfitteR         200         5         0.3         0.9820000         0.1333077         0           zip								
zip         countfitteR         100         5         0.2         0.9950000         0.0705690         0           zip         countfitteR         200         5         0.2         0.9920000         0.0891288         0           zip         countfitteR         50         10         0.2         0.9920000         0.0891288         0           zip         countfitteR         100         10         0.2         0.9960000         0.0631505         0           zip         countfitteR         200         10         0.2         0.9960000         0.0772656         0           zip         countfitteR         100         2         0.3         0.9920000         0.3105357         0           zip         countfitteR         100         2         0.3         0.9390000         0.2394501         0           zip         countfitteR         50         5         0.3         0.980000         0.1330176         0           zip         countfitteR         50         5         0.3         0.980000         0.1255379         0           zip         countfitteR         50         10         0.3         0.9950000         0.123307         0								
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zip         countfitteR         50         10         0.2         0.9920000         0.0891288         0           zip         countfitteR         100         10         0.2         0.9960000         0.0631505         0           zip         countfitteR         200         10         0.2         0.9940000         0.0772656         0           zip         countfitteR         50         2         0.3         0.8920000         0.3105357         0           zip         countfitteR         100         2         0.3         0.9390000         0.2394501         0           zip         countfitteR         200         2         0.3         0.980000         0.1400701         0           zip         countfitteR         100         5         0.3         0.980000         0.1330176         0           zip         countfitteR         100         5         0.3         0.9820000         0.1255379         0           zip         countfitteR         100         10         0.3         0.9870000         0.1043546         0           zip         countfitteR         100         10         0.3         0.9890000         0.1043546         0								
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zip         countfitteR         50         5         0.3         0.9820000         0.1330176         0           zip         countfitteR         100         5         0.3         0.9840000         0.1255379         0           zip         countfitteR         200         5         0.3         0.9900000         0.0995485         0           zip         countfitteR         50         10         0.3         0.9870000         0.1133307         0           zip         countfitteR         100         10         0.3         0.9890000         0.1043546         0           zip         countfitteR         200         10         0.3         0.9950000         0.0705690         0           zip         countfitteR         50         2         0.4         0.9900000         0.3001501         0           zip         countfitteR         100         2         0.4         0.9900000         0.3001501         0           zip         countfitteR         200         2         0.4         0.9900000         0.2241456         0           zip         countfitteR         50         5         0.4         0.9920000         0.133307         0								
zip         countfitteR         100         5         0.3         0.9840000         0.1255379         0           zip         countfitteR         200         5         0.3         0.9900000         0.0995485         0           zip         countfitteR         50         10         0.3         0.9870000         0.1133307         0           zip         countfitteR         100         10         0.3         0.9890000         0.1043546         0           zip         countfitteR         50         2         0.4         0.9900000         0.0705690         0           zip         countfitteR         50         2         0.4         0.9900000         0.3001501         0           zip         countfitteR         100         2         0.4         0.9900000         0.3001501         0           zip         countfitteR         100         2         0.4         0.9900000         0.2241456         0           zip         countfitteR         50         5         0.4         0.9900000         0.0133307         0           zip         countfitteR         100         5         0.4         0.9920000         0.1043546         0								
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$\begin{array}{cccccccccccccccccccccccccccccccccccc$		count fitte R	200	10	0.3	0.9950000	0.0705690	0
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		count fitte R	50	2	0.4	0.9000000	0.3001501	0
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		count fitte R	100	2	0.4	0.9470000	0.2241456	0
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		count fitte R	200	2	0.4	0.9900000	0.0995485	0
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		count fitte R	50	5	0.4	0.9870000	0.1133307	0
zip         countfitteR         200         5         0.4         0.9890000         0.1043546         0           zip         countfitteR         50         10         0.4         0.9930000         0.0834144         0           zip         countfitteR         100         10         0.4         0.9950000         0.0705690         0           zip         countfitteR         200         10         0.4         0.9900000         0.0995485         0           zip         countfitteR         50         2         0.5         0.9230000         0.2667248         0           zip         countfitteR         100         2         0.5         0.9230000         0.1787259         0           zip         countfitteR         200         2         0.5         0.9860000         0.1175492         0           zip         countfitteR         50         5         0.5         0.9840000         0.1255379         0           zip         countfitteR         100         5         0.5         0.9830000         0.1293357         0           zip         countfitteR         50         10         0.5         0.9980000         0.1043546         0		count fitte R	100	5	0.4	0.9920000	0.0891288	0
zip         countfitteR         50         10         0.4         0.9930000         0.0834144         0           zip         countfitteR         100         10         0.4         0.9950000         0.0705690         0           zip         countfitteR         200         10         0.4         0.9900000         0.0995485         0           zip         countfitteR         50         2         0.5         0.9230000         0.2667248         0           zip         countfitteR         100         2         0.5         0.9670000         0.1787259         0           zip         countfitteR         200         2         0.5         0.9860000         0.1175492         0           zip         countfitteR         50         5         0.5         0.9840000         0.1255379         0           zip         countfitteR         100         5         0.5         0.9830000         0.1293357         0           zip         countfitteR         50         10         0.5         0.9980000         0.0446990         0           zip         countfitteR         100         10         0.5         0.9980000         0.1043546         0		count fitte R	200	5	0.4	0.9890000	0.1043546	0
zip         countfitteR         100         10         0.4         0.9950000         0.0705690         0           zip         countfitteR         200         10         0.4         0.9900000         0.0995485         0           zip         countfitteR         50         2         0.5         0.9230000         0.2667248         0           zip         countfitteR         100         2         0.5         0.9670000         0.1787259         0           zip         countfitteR         200         2         0.5         0.9860000         0.1175492         0           zip         countfitteR         50         5         0.5         0.9840000         0.1255379         0           zip         countfitteR         100         5         0.5         0.9830000         0.1293357         0           zip         countfitteR         200         5         0.5         0.9980000         0.0446990         0           zip         countfitteR         100         10         0.5         0.9980000         0.0631505         0           zip         countfitteR         200         10         0.5         0.9930000         0.0834144         0		count fitte R	50	10	0.4	0.9930000	0.0834144	0
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		count fitte R	100	10	0.4	0.9950000	0.0705690	0
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		count fitte R	200	10	0.4	0.9900000	0.0995485	0
zip         countfitteR         200         2         0.5         0.9860000         0.1175492         0           zip         countfitteR         50         5         0.5         0.9840000         0.1255379         0           zip         countfitteR         100         5         0.5         0.9830000         0.1293357         0           zip         countfitteR         200         5         0.5         0.9980000         0.0446990         0           zip         countfitteR         50         10         0.5         0.9890000         0.1043546         0           zip         countfitteR         100         10         0.5         0.9960000         0.0631505         0           zip         countfitteR         200         10         0.5         0.9930000         0.0834144         0           zip         countfitteR         50         2         0.6         0.8750000         0.3308844         0           zip         countfitteR         100         2         0.6         0.9470000         0.2241456         0		count fitte R	50	2	0.5	0.9230000	0.2667248	0
zip         countfitteR         50         5         0.5         0.9840000         0.1255379         0           zip         countfitteR         100         5         0.5         0.9830000         0.1293357         0           zip         countfitteR         200         5         0.5         0.9980000         0.0446990         0           zip         countfitteR         50         10         0.5         0.9890000         0.1043546         0           zip         countfitteR         100         10         0.5         0.9960000         0.0631505         0           zip         countfitteR         200         10         0.5         0.9930000         0.0834144         0           zip         countfitteR         50         2         0.6         0.8750000         0.3308844         0           zip         countfitteR         100         2         0.6         0.9470000         0.2241456         0	zip	count fitte R	100	2	0.5	0.9670000	0.1787259	0
zip         countfitteR         100         5         0.5         0.9830000         0.1293357         0           zip         countfitteR         200         5         0.5         0.9980000         0.0446990         0           zip         countfitteR         50         10         0.5         0.9890000         0.1043546         0           zip         countfitteR         100         10         0.5         0.9960000         0.0631505         0           zip         countfitteR         200         10         0.5         0.9930000         0.0834144         0           zip         countfitteR         50         2         0.6         0.8750000         0.3308844         0           zip         countfitteR         100         2         0.6         0.9470000         0.2241456         0	zip	count fitte R	200	2	0.5	0.9860000	0.1175492	0
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	zip	count fitte R	50	5	0.5	0.9840000	0.1255379	0
zip         countfitteR         50         10         0.5         0.9890000         0.1043546         0           zip         countfitteR         100         10         0.5         0.9960000         0.0631505         0           zip         countfitteR         200         10         0.5         0.9930000         0.0834144         0           zip         countfitteR         50         2         0.6         0.8750000         0.3308844         0           zip         countfitteR         100         2         0.6         0.9470000         0.2241456         0	zip	count fitte R	100	5	0.5	0.9830000	0.1293357	0
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	zip	count fitte R	200	5	0.5	0.9980000	0.0446990	0
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$\begin{array}{cccccccccccccccccccccccccccccccccccc$		count fitte R	100	10	0.5	0.9960000	0.0631505	0
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	zip	count fitte R	200	10	0.5	0.9930000	0.0834144	0
•	zip	count fitte R	50		0.6	0.8750000	0.3308844	0
zip countfitteR 200 2 $0.6$ $0.9880000$ $0.1089397$ 0	zip	count fitte R	100		0.6	0.9470000	0.2241456	0
	zip	count fitte R	200	2	0.6	0.9880000	0.1089397	0

$\overline{\text{model}}$	method	n	lambda	r	pow_mean	pow_sd	uncomputable
zip	countfitteR	50	5	0.6	0.9870000	0.1133307	0
zip	count fitte R	100	5	0.6	0.9880000	0.1089397	0
zip	count fitte R	200	5	0.6	0.9880000	0.1089397	0
zip	count fitte R	50	10	0.6	0.9830000	0.1293357	0
zip	count fitte R	100	10	0.6	0.9910000	0.0944877	0
zip	count fitte R	200	10	0.6	0.9940000	0.0772656	0
zip	count fitte R	50	2	0.7	0.7820000	0.4130940	0
zip	count fitte R	100	2	0.7	0.9260000	0.2619019	0
zip	count fitte R	200	2	0.7	0.9810000	0.1365930	0
zip	count fitte R	50	5	0.7	0.9850000	0.1216133	0
zip	count fitte R	100	5	0.7	0.9880000	0.1089397	0
zip	count fitte R	200	5	0.7	0.9920000	0.0891288	0
zip	count fitte R	50	10	0.7	0.9900000	0.0995485	0
zip	count fitte R	100	10	0.7	0.9870000	0.1133307	0
zip	count fitte R	200	10	0.7	0.9920000	0.0891288	0
zip	count fitte R	50	2	0.8	0.5350000	0.4990231	0
zip	count fitte R	100	2	0.8	0.8000000	0.4002002	0
zip	count fitte R	200	2	0.8	0.9480000	0.2221381	0
zip	count fitte R	50	5	0.8	0.9820000	0.1330176	0
zip	count fitte R	100	5	0.8	0.9890000	0.1043546	0
zip	count fitte R	200	5	0.8	0.9860000	0.1175492	0
zip	count fitte R	50	10	0.8	0.9880000	0.1089397	0
zip	count fitte R	100	10	0.8	0.9870000	0.1133307	0
zip	count fitte R	200	10	0.8	0.9940000	0.0772656	0
zip	count fitte R	50	2	0.9	0.2030000	0.4024338	0
zip	count fitte R	100	2	0.9	0.3130000	0.4639464	0
zip	count fitte R	200	2	0.9	0.5480000	0.4979397	0
zip	count fitte R	50	5	0.9	0.8980000	0.3027997	0
zip	count fitte R	100	5	0.9	0.9840000	0.1255379	0
zip	count fitte R	200	5	0.9	0.9940000	0.0772656	0
zip	count fitte R	50	10	0.9	0.9770000	0.1499783	0
zip	count fitte R	100	10	0.9	0.9860000	0.1175492	0
zip	count fitte R	200	10	0.9	0.9920000	0.0891288	0
zip	two-step	50	2	0.1	0.0000000	0.0000000	545
zip	two-step	100	2	0.1	0.0000000	0.0000000	660
zip	two-step	200	2	0.1	0.0000000	0.0000000	701
zip	two-step	50	5	0.1	0.0000000	0.0000000	907
zip	two-step	100	5	0.1	0.0000000	0.0000000	921
zip	two-step	200	5	0.1	0.0000000	0.0000000	998
zip	two-step	50	10	0.1	NaN	NA	1000
zip	two-step	100	10	0.1	NaN	NA	1000
zip	two-step	200	10	0.1	NaN	NA	1000
zip	two-step	50	2	0.2	0.0000000	0.0000000	208
zip	two-step	100	2	0.2	0.0000000	0.0000000	0
zip	two-step	200	2	0.2	0.0000000	0.0000000	0
zip	two-step	50	5	0.2	0.0870000	0.2819761	0
$\overset{ ext{zip}}{\cdot}$	two-step	100	5	0.2	0.1540000	0.3611294	0
$\overset{ ext{zip}}{\cdot}$	two-step	200	5	0.2	0.6920000	0.4618976	0
$\overset{ ext{zip}}{\cdot}$	two-step	50	10	0.2	0.2900000	0.4539891	0
$\overset{ ext{zip}}{\cdot}$	two-step	100	10	0.2	0.6990000	0.4589222	0
$\overset{ ext{zip}}{\cdot}$	two-step	200	10	0.2	0.9990000	0.0316228	0
zip	two-step	50	2	0.3	0.0000000	0.0000000	0

$\overline{\text{model}}$	method	n	lambda	r	pow_mean	pow_sd	uncomputable
zip	two-step	100	2	0.3	0.0000000	0.0000000	0
zip	two-step	200	2	0.3	0.0000000	0.0000000	0
zip	two-step	50	5	0.3	0.0880000	0.2834367	0
zip	two-step	100	5	0.3	0.4500000	0.4977427	0
zip	two-step	200	5	0.3	0.6060000	0.4888793	0
zip	two-step	50	10	0.3	0.7590000	0.4279043	0
zip	two-step	100	10	0.3	0.9950000	0.0705690	0
zip	two-step	200	10	0.3	1.0000000	0.0000000	0
zip	two-step	50	2	0.4	0.0010000	0.0316228	0
zip	two-step	100	2	0.4	0.0000000	0.0000000	0
zip	two-step	200	2	0.4	0.0000000	0.0000000	0
zip	two-step	50	5	0.4	0.0650000	0.2466492	0
zip	two-step	100	5	0.4	0.3620000	0.4808193	0
zip	two-step	200	5	0.4	0.2910000	0.4544508	0
zip	two-step	50	10	0.4	0.9410000	0.2357426	0
zip	two-step	100	10	0.4	1.0000000	0.0000000	0
zip	two-step	200	10	0.4	1.0000000	0.0000000	0
zip	two-step	50	2	0.5	0.0060000	0.0772656	0
zip	two-step	100	2	0.5	0.0000000	0.0000000	0
zip	two-step	200	2	0.5	0.0000000	0.0000000	0
zip	two-step	50	5	0.5	0.0180000	0.1330176	0
zip	two-step	100	5	0.5	0.1060000	0.3079917	0
zip	two-step	200	5	0.5	0.0470000	0.2117447	0
zip	two-step	50	10	0.5	0.6480000	0.4778329	0
zip	two-step	100	10	0.5	0.9990000	0.0316228	0
zip	two-step	200	10	0.5	1.0000000	0.0000000	0
zip	two-step	50	2	0.6	0.0100000	0.0995485	0
zip	two-step	100	2	0.6	0.0010000	0.0316228	0
zip	two-step	200	2	0.6	0.0000000	0.0000000	0
zip	two-step	50	5	0.6	0.0000000	0.0000000	0
zip	two-step	100	5	0.6	0.0080000	0.0891288	0
zip	two-step	200	5	0.6	0.0010000	0.0316228	0
zip	two-step	50	10	0.6	0.1860000	0.3893014	0
zip	two-step	100	10	0.6	0.8428428	0.3641312	1
zip	two-step	200	10	0.6	1.0000000	0.0000000	1
zip	two-step	50	2	0.7	0.0300000	0.1706726	0
zip	two-step	100	2	0.7	0.0070000	0.0834144	0
zip	two-step	200	2	0.7	0.0000000	0.0000000	0
zip	two-step	50	5	0.7	0.0000000	0.0000000	0
zip	two-step	100	5	0.7	0.0000000	0.0000000	0
zip	two-step	200	5	0.7	0.0000000	0.0000000	0
zip	two-step	50	10	0.7	0.0270000	0.1621644	0
zip	two-step	100	10	0.7	0.1251251	0.3310265	1
zip	two-step	200	10	0.7	0.9660000	0.1813198	0
zip	two-step	50	2	0.8	0.0130000	0.1133307	0
zip	two-step	100	2	0.8	0.0360000	0.1863833	0
zip	two-step	200	2	0.8	0.0150000	0.1216133	0
zip	two-step	50	5	0.8	0.0160000	0.1255379	0
zip	two-step	100	5	0.8	0.0030000	0.0547174	0
zip	two-step	200	5	0.8	0.0000000	0.0000000	0
zip	two-step	50	10	0.8	0.0560000	0.2300368	0
zip	two-step	100	10	0.8	0.0000000	0.0000000	0

model	method	n	lambda	r	pow_mean	pow_sd	uncomputable
zip	two-step	200	10	0.8	0.0670000	0.2501471	0
zip	two-step	50	2	0.9	0.0050000	0.0705690	0
zip	two-step	100	2	0.9	0.0100000	0.0995485	0
zip	two-step	200	2	0.9	0.0300000	0.1706726	0
zip	two-step	50	5	0.9	0.0370741	0.1890383	2
zip	two-step	100	5	0.9	0.0730000	0.2602667	0
zip	two-step	200	5	0.9	0.0180000	0.1330176	0
zip	two-step	50	10	0.9	0.0050251	0.0707453	5
zip	two-step	100	10	0.9	0.0080000	0.0891288	0
zip	two-step	200	10	0.9	0.0000000	0.0000000	0

**Table S6**: Comparison of countfitteR and two-step 2 procedure empirical power for ZINB distribution with three possible sample sizes (n = 50, 100, 200), three possible means ( $\lambda$  = 2, 5, 10), three possible sizes ( $\theta$  =  $\frac{\lambda}{2}$ ,  $\lambda$ ,  $2\lambda$ ), and dispersion parameter r ranging from 0.1 to 0.9.

$\overline{\text{model}}$	method	n	lambda	size	r	pow_mean	pow_sd	uncomputable
zinb	countfitteR	50	2	1.0	0.1	0.0010000	0.0316228	0
zinb	count fitte R	100	2	1.0	0.1	0.0010000	0.0316228	0
zinb	count fitte R	200	2	1.0	0.1	0.0040000	0.0631505	0
zinb	count fitte R	50	2	2.0	0.1	0.0000000	0.0000000	0
zinb	count fitte R	100	2	2.0	0.1	0.0010000	0.0316228	0
zinb	count fitte R	200	2	2.0	0.1	0.0010000	0.0316228	0
zinb	count fitte R	50	2	4.0	0.1	0.0000000	0.0000000	0
zinb	count fitte R	100	2	4.0	0.1	0.0000000	0.0000000	0
zinb	count fitte R	200	2	4.0	0.1	0.0000000	0.0000000	0
zinb	count fitte R	50	5	2.5	0.1	0.0470000	0.2117447	0
zinb	count fitte R	100	5	2.5	0.1	0.1720000	0.3775693	0
zinb	count fitte R	200	5	2.5	0.1	0.5190000	0.4998889	0
zinb	count fitte R	50	5	5.0	0.1	0.0180000	0.1330176	0
zinb	count fitte R	100	5	5.0	0.1	0.0740000	0.2619019	0
zinb	count fitte R	200	5	5.0	0.1	0.3160000	0.4651455	0
zinb	count fitte R	50	5	10.0	0.1	0.0160000	0.1255379	0
zinb	count fitte R	100	5	10.0	0.1	0.0460000	0.2095899	0
zinb	count fitte R	200	5	10.0	0.1	0.1230000	0.3286016	0
zinb	count fitte R	50	10	5.0	0.1	0.2640000	0.4410198	0
zinb	count fitte R	100	10	5.0	0.1	0.4980000	0.5002462	0
zinb	count fitte R	200	10	5.0	0.1	0.7720000	0.4197525	0
zinb	count fitte R	50	10	10.0	0.1	0.1070000	0.3092679	0
zinb	count fitte R	100	10	10.0	0.1	0.2360000	0.4248347	0
zinb	count fitte R	200	10	10.0	0.1	0.4250000	0.4945904	0
zinb	count fitte R	50	10	20.0	0.1	0.0420000	0.2006895	0
zinb	count fitte R	100	10	20.0	0.1	0.0950000	0.2933617	0
zinb	count fitte R	200	10	20.0	0.1	0.1420000	0.3492248	0
zinb	count fitte R	50	2	1.0	0.2	0.0010000	0.0316228	0
zinb	count fitte R	100	2	1.0	0.2	0.0080000	0.0891288	0
zinb	countfitteR	200	2	1.0	0.2	0.0680000	0.2518719	0
zinb	countfitteR	50	2	2.0	0.2	0.0000000	0.0000000	0
zinb	countfitteR	100	2	2.0	0.2	0.0030000	0.0547174	0
zinb	countfitteR	200	2	2.0	0.2	0.0250000	0.1562031	0
zinb	countfitteR	50	2	4.0	0.2	0.0000000	0.0000000	0
zinb	countfitteR	100	2	4.0	0.2	0.0000000	0.0000000	0
zinb	countfitteR	200	2	4.0	0.2	0.0060000	0.0772656	0
zinb	countfitteR	50	5	2.5	0.2	0.1690000	0.3749394	0
zinb	countfitteR	100	5	2.5	0.2	0.5580000	0.4968731	0
zinb	countfitteR	200	5	2.5	0.2	0.9250000	0.2635231	0
zinb	countfitteR	50	5	5.0	0.2	0.1110000	0.3142893	0
zinb	countfitteR	100	5	5.0	0.2	0.3580000	0.4796520	0
zinb	countfitteR	200	5	5.0	0.2	0.6670000	0.4715224	0
zinb	countfitteR	50	5	10.0	0.2	0.0500000	0.2180540	0
zinb	countfitteR	100	5	10.0	0.2	0.1350000	0.3418946	0
zinb	countfitteR	200	5	10.0	0.2	0.2500000	0.4332294	0
zinb	countfitteR	50	10	5.0	0.2	0.5650000	0.4960051	0
zinb	countfitteR	100	10	5.0	0.2	0.8300000	0.3758208	0
zinb	count fitte R	200	10	5.0	0.2	0.9660000	0.1813198	0

model	method	n	lambda	size	r	pow_mean	pow_sd	uncomputable
zinb	countfitteR	50	10	10.0	0.2	0.2930000	0.4553662	0
zinb	countfitteR	100	10	10.0	0.2	0.4550000	0.4982201	0
zinb	countfitteR	200	10	10.0	0.2	0.7070000	0.4553662	0
zinb	countfitteR	50	10	20.0	0.2	0.0940000	0.2919747	0
zinb	countfitteR	100	10	20.0	0.2	0.1750000	0.3801572	0
zinb	countfitteR	200	10	20.0	0.2	0.2700000	0.4441816	0
zinb	countfitteR	50	2	1.0	0.2	0.0060000	0.0772656	0
zinb	countfitteR	100	$\frac{2}{2}$	1.0	0.3	0.0250000	0.1562031	0
zinb	countfitteR	200	$\frac{2}{2}$	1.0	0.3	0.1430000	0.3502480	0
zinb	countfitteR	50	$\frac{2}{2}$	2.0	0.3	0.0030000	0.0547174	0
zinb	countfitteR	100	$\frac{2}{2}$	2.0	0.3	0.0130000	0.1133307	0
zinb	countfitteR	200	$\frac{2}{2}$	$\frac{2.0}{2.0}$	0.3	0.1400000	0.3471607	0
zinb	countfitteR	50	$\frac{2}{2}$	$\frac{2.0}{4.0}$	0.3	0.0000000	0.0000000	0
zinb	countfitteR	100	$\frac{2}{2}$	4.0	0.3	0.0030000	0.0547174	0
zinb	countfitteR	200	$\frac{2}{2}$	4.0	0.3	0.0430000	0.2029586	0
zinb	countfitteR	50	5	$\frac{1.0}{2.5}$	0.3	0.3930000	0.4886612	0
zinb	countfitteR	100	5	$\frac{2.5}{2.5}$	0.3	0.8010000	0.3994478	0
zinb	countfitteR	200	5	$\frac{2.5}{2.5}$	0.3	0.9880000	0.3334478 $0.1089397$	0
zinb	countfitteR	50	5	5.0	0.3	0.2680000	0.1003337 $0.4431392$	0
zinb	countfitteR	100	5	5.0	0.3	0.5570000	0.4451332 $0.4969889$	0
zinb	countfitteR	200	5	5.0	0.3	0.8500000	0.4505005 $0.3572501$	0
zinb	countfitteR	50	5	10.0	0.3	0.3300000	0.3079917	0
zinb	countfitteR	100	5	10.0	0.3	0.1000000	0.3079917 $0.4285086$	0
zinb	countfitteR	200	5	10.0	0.3	0.2420000	0.4269030 $0.4848774$	0
zinb	countfitteR	50	10	5.0	0.3	0.7520000	0.4320679	0
zinb	countfitteR	100	10	5.0	0.3	0.9500000	0.4320013	0
zinb	countfitteR	200	10	5.0	0.3	0.9820000	0.2130340 $0.1330176$	0
zinb	countfitteR	50	10	10.0	0.3	0.3620000 $0.4050000$	0.4911377	0
zinb	countfitteR	100	10	10.0	0.3	0.4630000	0.4711311 $0.4729214$	0
zinb	countfitteR	200	10	10.0	0.3	0.7590000	0.4279043	0
zinb	countfitteR	50	10	20.0	0.3	0.1750000	0.3801572	0
zinb	countfitteR	100	10	20.0	0.3	0.2770000	0.4477404	0
zinb	countfitteR	200	10	20.0	0.3	0.4110000	0.4922614	0
zinb	countfitteR	50	2	1.0	0.4	0.0070000	0.0834144	0
zinb	countfitteR	100	2	1.0	0.4	0.0500000	0.2180540	0
zinb	countfitteR	200	2	1.0	0.4	0.2350000	0.4242110	0
zinb	countfitteR	50	2	2.0	0.4	0.0020000	0.0446990	0
zinb	countfitteR	100	2	2.0	0.4	0.0260000	0.1592148	0
zinb	countfitteR	200	2	2.0	0.4	0.2590000	0.4383048	0
zinb	countfitteR	50	2	4.0	0.4	0.0020000	0.0446990	0
zinb	countfitteR	100	2	4.0	0.4	0.0060000	0.0772656	0
zinb	countfitteR	200	2	4.0	0.4	0.1260000	0.3320154	0
zinb	countfitteR	50	5	2.5	0.4	0.5420000	0.4984822	0
zinb	countfitteR	100	5	$\frac{2.5}{2.5}$	0.4	0.9140000	0.2805043	0
zinb	countfitteR	200	5	2.5	0.4	0.9990000	0.0316228	0
zinb	countfitteR	50	5	5.0	0.4	0.3980000	0.4897304	0
zinb	countfitteR	100	5	5.0	0.4	0.6920000	0.4618976	0
zinb	countfitteR	200	5	5.0	$0.4 \\ 0.4$	0.9450000	0.4010910 $0.2280943$	0
zinb	countfitteR	50	5	10.0	0.4	0.1600000	0.3667895	0
zinb	countfitteR	100	5	10.0	0.4	0.3070000	0.4614802	0
zinb	countfitteR	200	5	10.0	0.4	0.5260000	0.4995734	0
zinb	countfitteR	50	10	5.0	0.4	0.8620000	0.4350734 $0.3450726$	0
21110	Committeett	50	10	5.0	0.4	0.0020000	0.0100120	U

model	method	n	lambda	size	r	pow_mean	pow_sd	uncomputable
zinb	countfitteR	100	10	5.0	0.4	0.9720000	0.1650553	0
zinb	countfitteR	200	10	5.0	0.4	0.9880000	0.1089397	0
zinb	countfitteR	50	10	10.0	0.4	0.5280000	0.4994652	0
zinb	countfitteR	100	10	10.0	0.4	0.7510000	0.4326502	0
zinb	countfitteR	200	10	10.0	0.4	0.8460000	0.3611294	0
zinb	countfitteR	50	10	20.0	0.4	0.2020000	0.4016931	0
zinb	countfitteR	100	10	20.0	0.4	0.3590000	0.4799472	0
zinb	countfitteR	200	10	20.0	0.4	0.5320000	0.4992246	0
zinb	countfitteR	50	2	1.0	0.5	0.0100000	0.0995485	0
zinb	countfitteR	100	2	1.0	0.5	0.0720000	0.2586173	0
zinb	countfitteR	200	2	1.0	0.5	0.2820000	0.4501985	0
zinb	countfitteR	50	2	2.0	0.5	0.0040000	0.0631505	0
zinb	countfitteR	100	$\frac{2}{2}$	2.0	0.5	0.0440000	0.2051977	0
zinb	countfitteR	200	$\frac{2}{2}$	2.0	0.5	0.3060000	0.4610603	0
zinb	countfitteR	50	$\frac{2}{2}$	4.0	0.5	0.0010000	0.0316228	0
zinb	countfitteR	100	2	4.0	0.5	0.0130000	0.1133307	0
zinb	countfitteR	200	2	4.0	0.5	0.1910000	0.3932857	0
zinb	countfitteR	50	5	2.5	0.5	0.6640000	0.4725752	0
zinb	countfitteR	100	5	$\frac{2.5}{2.5}$	0.5	0.9510000	0.2159760	0
zinb	countfitteR	200	5	$\frac{2.5}{2.5}$	0.5	1.0000000	0.0000000	0
zinb	countfitteR	50	5	$\frac{2.0}{5.0}$	0.5	0.5130000	0.5000811	0
zinb	countfitteR	100	5	5.0	0.5	0.7830000	0.4124089	0
zinb	countfitteR	200	5	5.0	0.5	0.9740000	0.1592148	0
zinb	countfitteR	50	5	10.0	0.5	0.2190000	0.4137756	0
zinb	countfitteR	100	5	10.0	0.5	0.3770000	0.4848774	0
zinb	countfitteR	200	5	10.0	0.5	0.6330000	0.4822277	0
zinb	countfitteR	50	10	5.0	0.5	0.9260000	0.2619019	0
zinb	countfitteR	100	10	5.0	0.5	0.9740000	0.1592148	0
zinb	countfitteR	200	10	5.0	0.5	0.9970000	0.0547174	0
zinb	countfitteR	50	10	10.0	0.5	0.6280000	0.4835802	0
zinb	countfitteR	100	10	10.0	0.5	0.7390000	0.4393997	0
zinb	countfitteR	200	10	10.0	0.5	0.8720000	0.3342570	0
zinb	countfitteR	50	10	20.0	0.5	0.2910000	0.4544508	0
zinb	countfitteR	100	10	20.0	0.5	0.3480000	0.4765744	0
zinb	countfitteR	200	10	20.0	0.5	0.6580000	0.4746170	0
zinb	count fitte R	50	2	1.0	0.6	0.0250000	0.1562031	0
zinb	countfitteR	100	2	1.0	0.6	0.0880000	0.2834367	0
zinb	countfitteR	200	2	1.0	0.6	0.2210000	0.4151281	0
zinb	countfitteR	50	$\overline{2}$	2.0	0.6	0.0040000	0.0631505	0
zinb	countfitteR	100	$\overline{2}$	2.0	0.6	0.0530000	0.2241456	0
zinb	countfitteR	200	$\overline{2}$	2.0	0.6	0.3260000	0.4689818	0
zinb	count fitteR	50	2	4.0	0.6	0.0000000	0.0000000	0
zinb	countfitteR	100	$\overline{2}$	4.0	0.6	0.0120000	0.1089397	0
zinb	count fitte R	200	2	4.0	0.6	0.1790000	0.3835441	0
zinb	count fitte R	50	5	2.5	0.6	0.7060000	0.4558199	0
zinb	count fitte R	100	5	2.5	0.6	0.9580000	0.2006895	0
zinb	countfitteR	200	5	2.5	0.6	1.0000000	0.0000000	0
zinb	countfitteR	50	5	5.0	0.6	0.5890000	0.4922614	0
zinb	countfitteR	100	5	5.0	0.6	0.8600000	0.3471607	0
zinb	countfitteR	200	5	5.0	0.6	0.9850000	0.1216133	0
zinb	countfitteR	50	5	10.0	0.6	0.2910000	0.4544508	0
zinb	count fitte R	100	5	10.0	0.6	0.4470000	0.4974318	0

model	method	n	lambda	size	r	pow_mean	pow_sd	uncomputable
zinb	countfitteR	200	5	10.0	0.6	0.6890000	0.4631344	0
zinb	countfitteR	50	10	5.0	0.6	0.9770000	0.1499783	0
zinb	countfitteR	100	10	5.0	0.6	0.9750000	0.1562031	0
zinb	countfitteR	200	10	5.0	0.6	0.9990000	0.0316228	0
zinb	countfitteR	50	10	10.0	0.6	0.6960000	0.4602128	0
zinb	countfitteR	100	10	10.0	0.6	0.7770000	0.4164666	0
zinb	countfitteR	200	10	10.0	0.6	0.8900000	0.3130463	0
zinb	countfitteR	50	10	20.0	0.6	0.3030000	0.4597852	0
zinb	countfitteR	100	10	20.0	0.6	0.4540000	0.4981286	0
zinb	countfitteR	200	10	20.0	0.6	0.7640000	0.4248347	0
zinb	countfitteR	50	2	1.0	0.7	0.0160000	0.1255379	0
zinb	countfitteR	100	2	1.0	0.7	0.0690000	0.2535810	0
zinb	countfitteR	200	$\frac{2}{2}$	1.0	0.7	0.1890000	0.3917045	0
zinb	countfitteR	50	2	2.0	0.7	0.0060000	0.0772656	0
zinb	countfitteR	100	2	2.0	0.7	0.0470000	0.2117447	0
zinb	countfitteR	200	2	2.0	0.7	0.2790000	0.4487319	0
zinb	countfitteR	50	2	4.0	0.7	0.0010000	0.0316228	0
zinb	countfitteR	100	2	4.0	0.7	0.0090000	0.0944877	0
zinb	countfitteR	200	2	4.0	0.7	0.1620000	0.3686352	0
zinb	countfitteR	50	5	2.5	0.7	0.6810000	0.4663223	0
zinb	countfitteR	100	5	2.5	0.7	0.9250000	0.2635231	0
zinb	countfitteR	200	5	2.5	0.7	0.9950000	0.0705690	0
zinb	countfitteR	50	5	5.0	0.7	0.6370000	0.4811055	0
zinb	countfitteR	100	5	5.0	0.7	0.9280000	0.2586173	0
zinb	countfitteR	200	5	5.0	0.7	0.9950000	0.0705690	0
zinb	countfitteR	50	5	10.0	0.7	0.3090000	0.4623124	0
zinb	countfitteR	100	5	10.0	0.7	0.5250000	0.4996245	0
zinb	countfitteR	200	5	10.0	0.7	0.7770000	0.4164666	0
zinb	countfitteR	50	10	5.0	0.7	0.9850000	0.1216133	0
zinb	countfitteR	100	10	5.0	0.7	0.9770000	0.1499783	0
zinb	countfitteR	200	10	5.0	0.7	0.9990000	0.0316228	0
zinb	countfitteR	50	10	10.0	0.7	0.7640000	0.4248347	0
zinb	count fitte R	100	10	10.0	0.7	0.8290000	0.3766974	0
zinb	count fitte R	200	10	10.0	0.7	0.9000000	0.3001501	0
zinb	count fitte R	50	10	20.0	0.7	0.3230000	0.4678567	0
zinb	count fitte R	100	10	20.0	0.7	0.5460000	0.4981286	0
zinb	count fitte R	200	10	20.0	0.7	0.8410000	0.3658591	0
zinb	count fitte R	50	2	1.0	0.8	0.0160000	0.1255379	0
zinb	count fitteR	100	2	1.0	0.8	0.0580000	0.2338604	0
zinb	count fitte R	200	2	1.0	0.8	0.1060000	0.3079917	0
zinb	count fitte R	50	2	2.0	0.8	0.0000000	0.0000000	0
zinb	count fitte R	100	2	2.0	0.8	0.0310000	0.1734044	0
zinb	count fitte R	200	2	2.0	0.8	0.1920000	0.3940702	0
zinb	count fitte R	50	2	4.0	0.8	0.0000000	0.0000000	0
zinb	count fitte R	100	2	4.0	0.8	0.0030000	0.0547174	0
zinb	count fitte R	200	2	4.0	0.8	0.0660000	0.2484063	0
zinb	count fitte R	50	5	2.5	0.8	0.5370000	0.4988786	0
zinb	count fitte R	100	5	2.5	0.8	0.7950000	0.4039036	0
zinb	count fitte R	200	5	2.5	0.8	0.9730000	0.1621644	0
zinb	count fitte R	50	5	5.0	0.8	0.5920000	0.4917090	0
zinb	count fitte R	100	5	5.0	0.8	0.9210000	0.2698737	0
zinb	count fitte R	200	5	5.0	0.8	0.9990000	0.0316228	0

model	method	n	lambda	size	r	pow_mean	pow_sd	uncomputable
zinb	countfitteR	50	5	10.0	0.8	0.3150000	0.4647483	0
zinb	countfitteR	100	5	10.0	0.8	0.5650000	0.4960051	0
zinb	countfitteR	200	5	10.0	0.8	0.8350000	0.3713663	0
zinb	count fitte R	50	10	5.0	0.8	0.9850000	0.1216133	0
zinb	count fitte R	100	10	5.0	0.8	0.9950000	0.0705690	0
zinb	count fitte R	200	10	5.0	0.8	1.0000000	0.0000000	0
zinb	count fitte R	50	10	10.0	0.8	0.7860000	0.4103320	0
zinb	count fitte R	100	10	10.0	0.8	0.8330000	0.3731625	0
zinb	count fitte R	200	10	10.0	0.8	0.8970000	0.3041110	0
zinb	count fitte R	50	10	20.0	0.8	0.4080000	0.4917090	0
zinb	count fitte R	100	10	20.0	0.8	0.6010000	0.4899378	0
zinb	count fitte R	200	10	20.0	0.8	0.8680000	0.3386601	0
zinb	count fitte R	50	2	1.0	0.9	0.0150000	0.1216133	0
zinb	count fitte R	100	2	1.0	0.9	0.0270000	0.1621644	0
zinb	count fitte R	200	2	1.0	0.9	0.0500000	0.2180540	0
zinb	count fitte R	50	2	2.0	0.9	0.0010000	0.0316228	0
zinb	count fitte R	100	2	2.0	0.9	0.0130000	0.1133307	0
zinb	count fitte R	200	2	2.0	0.9	0.0510000	0.2201078	0
zinb	count fitte R	50	2	4.0	0.9	0.0000000	0.0000000	0
zinb	count fitte R	100	2	4.0	0.9	0.0000000	0.0000000	0
zinb	count fitte R	200	2	4.0	0.9	0.0100000	0.0995485	0
zinb	count fitte R	50	5	2.5	0.9	0.2610000	0.4393997	0
zinb	count fitte R	100	5	2.5	0.9	0.4230000	0.4942826	0
zinb	count fitte R	200	5	2.5	0.9	0.6520000	0.4765744	0
zinb	count fitte R	50	5	5.0	0.9	0.3190000	0.4663223	0
zinb	count fitte R	100	5	5.0	0.9	0.7020000	0.4576084	0
zinb	count fitte R	200	5	5.0	0.9	0.9480000	0.2221381	0
zinb	count fitte R	50	5	10.0	0.9	0.1980000	0.3986916	0
zinb	count fitte R	100	5	10.0	0.9	0.5600000	0.4966353	0
zinb	count fitte R	200	5	10.0	0.9	0.8710000	0.3353677	0
zinb	count fitte R	50	10	5.0	0.9	0.8930000	0.3092679	0
zinb	count fitte R	100	10	5.0	0.9	0.9880000	0.1089397	0
zinb	count fitte R	200	10	5.0	0.9	1.0000000	0.0000000	0
zinb	count fitte R	50	10	10.0	0.9	0.7830000	0.4124089	0
zinb	count fitte R	100	10	10.0	0.9	0.8420000	0.3649235	0
zinb	count fitte R	200	10	10.0	0.9	0.9260000	0.2619019	0
zinb	count fitte R	50	10	20.0	0.9	0.4090000	0.4918953	0
zinb	count fitte R	100	10	20.0	0.9	0.6540000	0.4759312	0
zinb	count fitte R	200	10	20.0	0.9	0.9190000	0.2729716	0
zinb	two-step	50	2	1.0	0.1	0.0679916	0.2518633	44
zinb	two-step	100	2	1.0	0.1	0.0720000	0.2586173	0
zinb	two-step	200	2	1.0	0.1	0.0520000	0.2221381	0
zinb	two-step	50	2	2.0	0.1	0.1007121	0.3011003	17
zinb	two-step	100	2	2.0	0.1	0.1121121	0.3156624	1
zinb	two-step	200	2	2.0	0.1	0.1220000	0.3274496	0
zinb	two-step	50	2	4.0	0.1	0.1499493	0.3572028	13
zinb	two-step	100	2	4.0	0.1	0.1490000	0.3562667	0
zinb	two-step	200	2	4.0	0.1	0.2200000	0.4144536	0
zinb	two-step	50	5	2.5	0.1	0.1011122	0.3016298	11
zinb	two-step	100	5	2.5	0.1	0.1880000	0.3909077	0
zinb	two-step	200	5	2.5	0.1	0.4330000	0.4957386	0
zinb	two-step	50	5	5.0	0.1	0.1285141	0.3348294	4

$\operatorname{model}$	method	n	lambda	$\operatorname{size}$	$\mathbf{r}$	pow mean	$pow\_sd$	uncomputable
zinb	two-step	100	5	5.0	0.1	0.2270000	0.4191022	0
zinb	two-step	200	5	5.0	$0.1 \\ 0.1$	0.5500000	0.4191022 $0.4977427$	0
zinb	two-step	50	5	10.0	0.1	0.3300000 $0.1440081$	0.4577427 $0.3512748$	7
zinb	two-step	100	5	10.0	0.1	0.2350000	0.4242110	0
zinb	two-step	200	5	10.0	0.1	0.4780000	0.4242110 $0.4997657$	0
zinb	two-step	50	10	5.0	0.1	0.4750000 $0.0170512$	0.4337037 $0.1295270$	3
zinb	two-step	100	10	5.0	0.1	0.0230000	0.1499783	0
zinb	two-step	200	10	5.0	0.1	0.0170000	0.1293357	0
zinb	two-step	50	10	10.0	0.1	0.0030181	0.0548820	6
zinb	two-step	100	10	10.0	0.1	0.0070000	0.0834144	0
zinb	two-step	200	10	10.0	0.1	0.0000000	0.0000000	0
zinb	two-step	50	10	20.0	0.1	0.0000000	0.0000000	3
zinb	two-step	100	10	20.0	0.1	0.0010000	0.0316228	0
zinb	two-step	200	10	20.0	0.1	0.0000000	0.0000000	0
zinb	two-step	50	2	1.0	0.2	0.0760761	0.2652526	1
zinb	two-step	100	$\overline{2}$	1.0	0.2	0.0770000	0.2667248	0
zinb	two-step	200	2	1.0	0.2	0.0780000	0.2683058	0
zinb	two-step	50	2	2.0	0.2	0.1130000	0.3167512	0
zinb	two-step	100	$\overline{2}$	2.0	0.2	0.1000000	0.3001501	0
zinb	two-step	200	$\overline{2}$	2.0	0.2	0.1900000	0.3924972	0
zinb	two-step	50	$\overline{2}$	4.0	0.2	0.1661662	0.3724162	1
zinb	two-step	100	$\overline{2}$	4.0	0.2	0.2030000	0.4024338	0
zinb	two-step	200	$\overline{2}$	4.0	0.2	0.3480000	0.4765744	0
zinb	two-step	50	5	2.5	0.2	0.1750000	0.3801572	0
zinb	two-step	100	5	2.5	0.2	0.4450000	0.4972145	0
zinb	two-step	200	5	2.5	0.2	0.8530000	0.3542831	0
zinb	two-step	50	5	5.0	0.2	0.2170000	0.4124089	0
zinb	two-step	100	5	5.0	0.2	0.5180000	0.4999259	0
zinb	two-step	200	5	5.0	0.2	0.7700000	0.4210431	0
zinb	two-step	50	5	10.0	0.2	0.2280000	0.4197525	0
zinb	two-step	100	5	10.0	0.2	0.5230000	0.4997206	0
zinb	two-step	200	5	10.0	0.2	0.5080000	0.5001862	0
zinb	two-step	50	10	5.0	0.2	0.0310310	0.1734884	1
zinb	two-step	100	10	5.0	0.2	0.0190000	0.1365930	0
zinb	two-step	200	10	5.0	0.2	0.0050000	0.0705690	0
zinb	two-step	50	10	10.0	0.2	0.0090000	0.0944877	0
zinb	two-step	100	10	10.0	0.2	0.0010000	0.0316228	0
zinb	two-step	200	10	10.0	0.2	0.0000000	0.0000000	0
zinb	two-step	50	10	20.0	0.2	0.0000000	0.0000000	0
zinb	two-step	100	10	20.0	0.2	0.0000000	0.0000000	0
zinb	two-step	200	10	20.0	0.2	0.0000000	0.0000000	0
zinb	two-step	50	2	1.0	0.3	0.0680000	0.2518719	0
zinb	two-step	100	2	1.0	0.3	0.0660000	0.2484063	0
zinb	two-step	200	2	1.0	0.3	0.1080000	0.3105357	0
zinb	two-step	50	2	2.0	0.3	0.1030000	0.3041110	0
zinb	two-step	100	2	2.0	0.3	0.1420000	0.3492248	0
zinb	two-step	200	2	2.0	0.3	0.2400000	0.4272968	0
zinb	${\rm two\text{-}step}$	50	2	4.0	0.3	0.1580000	0.3649235	0
zinb	two-step	100	2	4.0	0.3	0.2260000	0.4184484	0
zinb	${\rm two\text{-}step}$	200	2	4.0	0.3	0.4730000	0.4995203	0
zinb	${\rm two\text{-}step}$	50	5	2.5	0.3	0.2740000	0.4462321	0
zinb	two-step	100	5	2.5	0.3	0.6640000	0.4725752	0

model	method	n	lambda	size	r	pow mean	pow_sd	uncomputable
zinb	two-step	200	5	2.5	0.3	0.9220000	0.2683058	0
zinb	two-step	50	5	5.0	0.3	0.3220000 $0.4330000$	0.4957386	0
zinb	two-step	100	5	5.0	0.3	0.4550000 $0.7540000$	0.4308940	0
zinb	two-step	200	5	5.0	0.3	0.7940000	0.4303940 $0.4911377$	0
zinb	_	50	5	10.0	0.3	0.3930000 $0.4100000$	0.4911377 $0.4920794$	0
zinb	two-step	100	5 5	10.0 $10.0$	0.3	0.4100000 $0.6330000$	0.4920794 $0.4822277$	0
zinb	two-step two-step	200	5	10.0	0.3	0.0330000	0.4822277 $0.4216833$	0
zinb	-	50	10	5.0	0.3	0.2310000 $0.0350000$	0.4210833 $0.1838717$	0
	two-step							
zinb	two-step	100	10	5.0	0.3	0.0140000 $0.0040000$	0.1175492	0
zinb	two-step	200	10	5.0	0.3		0.0631505	0
zinb	two-step	50	10	10.0	0.3	0.0060000	0.0772656	0
zinb	two-step	100	10	10.0	0.3	0.0000000	0.0000000	0
zinb	two-step	200	10	10.0	0.3	0.0000000	0.0000000	0
zinb	two-step	50	10	20.0	0.3	0.0000000	0.0000000	0
zinb	two-step	100	10	20.0	0.3	0.0000000	0.0000000	0
zinb	two-step	200	10	20.0	0.3	0.0000000	0.0000000	0
zinb	two-step	50	2	1.0	0.4	0.0580000	0.2338604	0
zinb	two-step	100	2	1.0	0.4	0.0640000	0.2448754	0
zinb	two-step	200	2	1.0	0.4	0.0980000	0.2974634	0
zinb	two-step	50	2	2.0	0.4	0.1210000	0.3262905	0
zinb	two-step	100	2	2.0	0.4	0.1240000	0.3297465	0
zinb	two-step	200	2	2.0	0.4	0.2690000	0.4436618	0
zinb	two-step	50	2	4.0	0.4	0.1630000	0.3695505	0
zinb	two-step	100	2	4.0	0.4	0.2310000	0.4216833	0
zinb	two-step	200	2	4.0	0.4	0.4740000	0.4995734	0
zinb	two-step	50	5	2.5	0.4	0.3970000	0.4895208	0
zinb	two-step	100	5	2.5	0.4	0.7840000	0.4117202	0
zinb	two-step	200	5	2.5	0.4	0.8520000	0.3552777	0
zinb	two-step	50	5	5.0	0.4	0.5950000	0.4911377	0
zinb	two-step	100	5	5.0	0.4	0.8120000	0.3909077	0
zinb	two-step	200	5	5.0	0.4	0.3490000	0.4768925	0
zinb	two-step	50	5	10.0	0.4	0.6030000	0.4895208	0
zinb	two-step	100	5	10.0	0.4	0.5820000	0.4934770	0
zinb	two-step	200	5	10.0	0.4	0.0730000	0.2602667	0
zinb	two-step	50	10	5.0	0.4	0.0690000	0.2535810	0
zinb	two-step	100	10	5.0	0.4	0.0200000	0.1400701	0
zinb	two-step	200	10	5.0	0.4	0.0000000	0.0000000	0
zinb	two-step	50	10	10.0	0.4	0.0070000	0.0834144	0
zinb	two-step	100	10	10.0	0.4	0.0000000	0.0000000	0
zinb	two-step	200	10	10.0	0.4	0.0000000	0.0000000	0
zinb	two-step	50	10	20.0	0.4	0.0000000	0.0000000	0
zinb	two-step	100	10	20.0	0.4	0.0000000	0.0000000	0
zinb	two-step	200	10	20.0	0.4	0.0000000	0.0000000	0
zinb	two-step	50	2	1.0	0.5	0.0450000	0.2074079	0
zinb	two-step	100	2	1.0	0.5	0.0330000	0.1787259	0
zinb	two-step	200	2	1.0	0.5	0.1060000	0.3079917	0
zinb	two-step	50	2	2.0	0.5	0.1000000	0.3001501	0
zinb	two-step	100	2	2.0	0.5	0.1160000	0.3203852	0
zinb	two-step	200	2	2.0	0.5	0.2840000	0.4511624	0
zinb	two-step	50	2	4.0	0.5	0.1630000	0.3695505	0
zinb	two-step	100	2	4.0	0.5	0.2360000	0.4248347	0
zinb	two-step	200	2	4.0	0.5	0.5040000	0.5002342	0

model	method	n	lambda	size	r	pow mean	pow_sd	uncomputable
zinb	two-step	50	5	2.5	0.5	0.4840000	0.4999940	0
zinb	two-step	100	5	$\frac{2.5}{2.5}$	0.5	0.8100000	0.3924972	0
zinb	two-step	200	5	$\frac{2.5}{2.5}$	0.5	0.8370000	0.3695505	0
zinb	two-step	50	5	5.0	0.5	0.6790000	0.4670944	0
zinb	two-step	100	5	5.0	0.5	0.8090000	0.3932857	0
zinb	two-step	200	5	5.0	$0.5 \\ 0.5$	0.3030000	0.3932637 $0.4279043$	0
zinb	two-step	50	5	10.0	0.5	0.7000000	0.4584869	0
zinb	two-step	100	5	10.0	0.5	0.4960000	0.5002342	0
zinb	two-step	200	5	10.0	0.5	0.4300000	0.3002342 $0.1089397$	0
zinb	two-step	50	10	5.0	$0.5 \\ 0.5$	0.0120000 $0.1320000$	0.1089397	0
zinb	two-step	100	10	5.0	$0.5 \\ 0.5$	0.1320000	0.3360001 $0.1706726$	0
zinb	_	200	10	5.0	$0.5 \\ 0.5$	0.0000000	0.1700720	0
zinb	two-step	50		10.0	$0.5 \\ 0.5$	0.0060000		0
zinb	two-step	100	10	10.0	$0.5 \\ 0.5$	0.0000000	0.0772656 $0.0000000$	0
zinb	two-step	$\frac{100}{200}$	10	10.0 $10.0$	$0.5 \\ 0.5$	0.0000000	0.0000000	0
zinb	two-step	50	10	20.0		0.0010000	0.0000000 $0.0316228$	0
	two-step		10		0.5			
zinb	two-step	100	10	20.0	0.5	0.0000000	0.0000000	0
zinb	two-step	200	10	20.0	0.5	0.0000000	0.0000000	0
zinb	two-step	50	2	1.0	0.6	0.0380000	0.1912919	0
zinb	two-step	100	2	1.0	0.6	0.0390000	0.1936918	0
zinb	two-step	200	2	1.0	0.6	0.0720000	0.2586173	0
zinb	two-step	50	$\frac{2}{2}$	2.0	0.6	0.0700000	0.2552747	0
zinb	two-step	100		2.0	0.6	0.1060000	0.3079917	0
zinb	two-step	200	2	2.0	0.6	0.2100000	0.4075120	0
zinb	two-step	50	2	4.0	0.6	0.1370000	0.3440194	0
zinb	two-step	100	2	4.0	0.6	0.1960000	0.3971671	0
zinb	two-step	200	2	4.0	0.6	0.4550000	0.4982201	0
zinb	two-step	50	5	2.5	0.6	0.4780000	0.4997657	0
zinb	two-step	100	5	2.5	0.6	0.7910000	0.4067978	0
zinb	two-step	200	5	2.5	0.6	0.8690000	0.3375692	0
zinb	two-step	50	5	5.0	0.6	0.7110000	0.4535247	0
zinb	two-step	100	5	5.0	0.6	0.8270000	0.3784365	0
zinb	two-step	200	5	5.0	0.6	0.2020000	0.4016931	0
zinb	two-step	50	5	10.0	0.6	0.7600000	0.4272968	0
zinb	two-step	100	5	10.0	0.6	0.5090000	0.5001691	0
zinb	two-step	200	5	10.0	0.6	0.0150000	0.1216133	0
zinb	two-step	50	10	5.0	0.6	0.2650000	0.4415540	0
zinb	two-step	100	10	5.0	0.6	0.0370000	0.1888562	0
zinb	two-step	200	10	5.0	0.6	0.0180000	0.1330176	0
zinb	two-step	50	10	10.0	0.6	0.0270000	0.1621644	0
zinb	two-step	100	10	10.0	0.6	0.0010000	0.0316228	0
zinb	two-step	200	10	10.0	0.6	0.0020000	0.0446990	0
zinb	two-step	50	10	20.0	0.6	0.0060000	0.0772656	0
zinb	two-step	100	10	20.0	0.6	0.0020000	0.0446990	0
zinb	two-step	200	10	20.0	0.6	0.0000000	0.0000000	0
zinb	two-step	50	2	1.0	0.7	0.0270000	0.1621644	0
zinb	two-step	100	2	1.0	0.7	0.0290000	0.1678904	0
zinb	two-step	200	2	1.0	0.7	0.0490000	0.2159760	0
zinb	two-step	50	2	2.0	0.7	0.0670000	0.2501471	0
zinb	two-step	100	2	2.0	0.7	0.0660000	0.2484063	0
zinb	two-step	200	2	2.0	0.7	0.1310000	0.3375692	0
zinb	two-step	50	2	4.0	0.7	0.1010000	0.3014795	0

model	method	n	lambda	size	r	pow_mean	pow_sd	uncomputable
zinb	two-step	100	2	4.0	0.7	0.1440000	0.3512654	0
zinb	two-step	200	2	4.0	0.7	0.3030000	0.4597852	0
zinb	two-step	50	5	2.5	0.7	0.3410000	0.4742826	0
zinb	two-step	100	5	2.5	0.7	0.7090000	0.4544508	0
zinb	two-step	200	5	$\frac{2.5}{2.5}$	0.7	0.9100000	0.2863250	0
zinb	two-step	50	5	$\frac{2.0}{5.0}$	0.7	0.6960000	0.4602128	0
zinb	two-step	100	5	5.0	0.7	0.8790000	0.3262905	0
zinb	two-step	200	5	5.0	0.7	0.3790000	0.4853809	0
zinb	two-step	50	5	10.0	0.7	0.7840000	0.4117202	0
zinb	two-step	100	5	10.0	0.7	0.6070000	0.4886612	0
zinb	two-step	200	5	10.0	0.7	0.0400000	0.1960572	0
zinb	two-step	50	10	5.0	0.7	0.4390000	0.4965134	0
zinb	two-step	100	10	5.0	0.7	0.0840000	0.2775266	0
zinb	two-step	200	10	5.0	0.7	0.1000000	0.3001501	0
zinb	two-step	50	10	10.0	0.7	0.1230000	0.3286016	0
zinb	two-step	100	10	10.0	0.7	0.0620000	0.2412762	0
zinb	two-step	200	10	10.0	0.7	0.2280000	0.4197525	0
zinb	two-step	50	10	20.0	0.7	0.0210000	0.1434558	0
zinb	two-step	100	10	20.0	0.7	0.0410000	0.1983894	0
zinb	two-step	200	10	20.0	0.7	0.0820000	0.2745020	0
zinb	two-step	50	2	1.0	0.8	0.0190000	0.1365930	0
zinb	two-step	100	$\frac{2}{2}$	1.0	0.8	0.0100000	0.0995485	0
zinb	two-step	200	$\frac{2}{2}$	1.0	0.8	0.0240000	0.0530406 $0.1531256$	0
zinb	two-step	50	$\frac{2}{2}$	2.0	0.8	0.0460000	0.2095899	0
zinb	two-step	100	$\frac{2}{2}$	$\frac{2.0}{2.0}$	0.8	0.0340000	0.1813198	0
zinb	two-step	200	$\frac{2}{2}$	2.0	0.8	0.0750000	0.2635231	0
zinb	two-step	50	$\frac{2}{2}$	$\frac{2.0}{4.0}$	0.8	0.0490000	0.2059261 $0.2159760$	0
zinb	two-step	100	$\frac{2}{2}$	4.0	0.8	0.0720000	0.2586173	0
zinb	two-step	200	$\frac{2}{2}$	4.0	0.8	0.1730000	0.3784365	0
zinb	two-step	50	5	2.5	0.8	0.1900000	0.3924972	0
zinb	two-step	100	5	2.5	0.8	0.4570000	0.4983968	0
zinb	two-step	200	5	2.5	0.8	0.8480000	0.3592005	0
zinb	two-step	50	5	5.0	0.8	0.4900000	0.5001501	0
zinb	two-step	100	5	5.0	0.8	0.8390000	0.3677149	0
zinb	two-step	200	5	5.0	0.8	0.7720000	0.4197525	0
zinb	two-step	50	5	10.0	0.8	0.6680000	0.4711666	0
zinb	two-step	100	5	10.0	0.8	0.8620000	0.3450726	0
zinb	two-step	200	5	10.0	0.8	0.3000000	0.4584869	0
zinb	two-step	50	10	5.0	0.8	0.7490000	0.4338055	0
zinb	two-step	100	10	5.0	0.8	0.3640000	0.4813894	0
zinb	two-step	200	10	5.0	0.8	0.0090000	0.0944877	0
zinb	two-step	50	10	10.0	0.8	0.4510000	0.4978422	0
zinb	two-step	100	10	10.0	0.8	0.1620000	0.3686352	0
zinb	two-step	200	10	10.0	0.8	0.3880000	0.4875384	0
zinb	two-step	50	10	20.0	0.8	0.2420000	0.4285086	0
zinb	two-step	100	10	20.0	0.8	0.0990000	0.2988115	0
zinb	two-step	200	10	20.0	0.8	0.7400000	0.4388537	0
zinb	two-step	50	2	1.0	0.9	0.0100000	0.0995485	0
zinb	two-step	100	$\overline{2}$	1.0	0.9	0.0040000	0.0631505	0
zinb	two-step	200	$\overline{2}$	1.0	0.9	0.0080000	0.0891288	0
zinb	two-step	50	$\overline{2}$	2.0	0.9	0.0120000	0.1089397	0
zinb	two-step	100	2	2.0	0.9	0.0170000	0.1293357	0
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model	method	n	lambda	size	r	pow_mean	$pow\_sd$	uncomputable
zinb	two-step	200	2	2.0	0.9	0.0150000	0.1216133	0
zinb	two-step	50	2	4.0	0.9	0.0170000	0.1293357	0
zinb	two-step	100	2	4.0	0.9	0.0300000	0.1706726	0
zinb	two-step	200	2	4.0	0.9	0.0260000	0.1592148	0
zinb	two-step	50	5	2.5	0.9	0.0570571	0.2320678	1
zinb	two-step	100	5	2.5	0.9	0.1180000	0.3227695	0
zinb	two-step	200	5	2.5	0.9	0.3230000	0.4678567	0
zinb	two-step	50	5	5.0	0.9	0.1301301	0.3366151	1
zinb	two-step	100	5	5.0	0.9	0.3400000	0.4739458	0
zinb	two-step	200	5	5.0	0.9	0.7610000	0.4266861	0
zinb	two-step	50	5	10.0	0.9	0.2352352	0.4243582	1
zinb	two-step	100	5	10.0	0.9	0.5900000	0.4920794	0
zinb	two-step	200	5	10.0	0.9	0.9250000	0.2635231	0
zinb	two-step	50	10	5.0	0.9	0.5533199	0.4973991	6
zinb	two-step	100	10	5.0	0.9	0.8690000	0.3375692	0
zinb	two-step	200	10	5.0	0.9	0.5660000	0.4958729	0
zinb	two-step	50	10	10.0	0.9	0.6723618	0.4695881	5
zinb	two-step	100	10	10.0	0.9	0.6410000	0.4799472	0
zinb	two-step	200	10	10.0	0.9	0.1480000	0.3552777	0
zinb	two-step	50	10	20.0	0.9	0.6844221	0.4649793	5
zinb	two-step	100	10	20.0	0.9	0.5200000	0.4998498	0
zinb	two-step	200	10	20.0	0.9	0.0690000	0.2535810	0

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