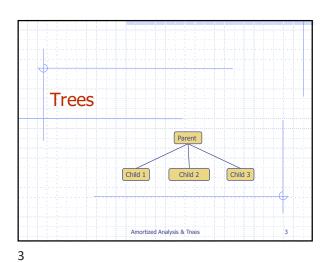


## Wholeness Statement

The Tree ADT is a generalization of the linked-list in which each tree node can have any number of children instead of just one; trees provide wide ranging capabilities and a highly flexible perspective on a set of element objects. Science of Consciousness. The whole infinite range of space and time is open to individuals with fully developed awareness. Regular transcending enlivens the qualities of the unified field in individual awareness and collective life.

Amortized Analysis & Trees

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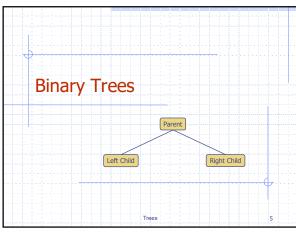


**Outline** 

- ◆ BinaryTree ADT
- Data structures for trees
- Preorder and postorder traversals
- ◆ Inorder traversal
- Euler Tour traversal
- ◆ Template method pattern

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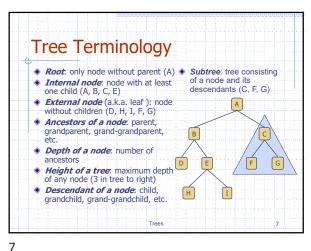
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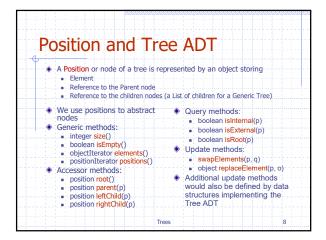


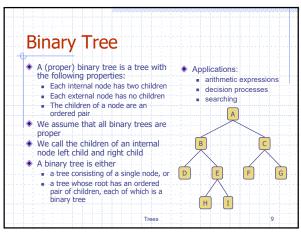
**Outline** 

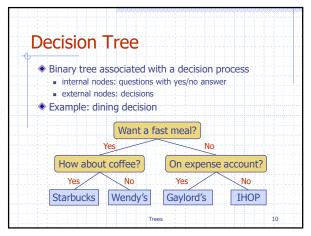
- BinaryTree ADT
- Data structures for trees
- Preorder and postorder traversals
- Inorder traversal

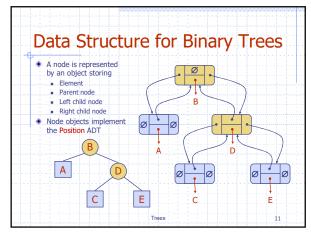
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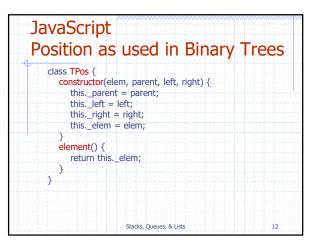


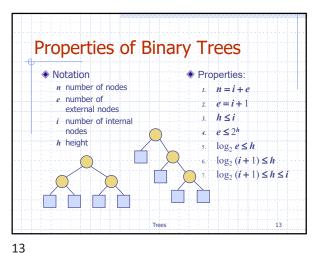






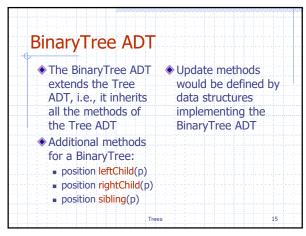






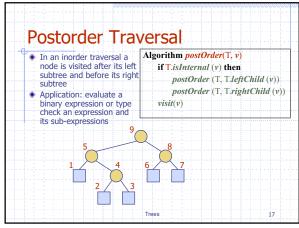
Main Point 1. Each internal node of a Binary Tree has two children and each external node has no children. Thus the height, h, of a binary tree ranges as follows:  $i>h>log_2e$ , that is,  $O(n)>h>O(log_2n)$ . Science of Consciousness: Pure consciousness spans the full range of life, from smaller than the smallest to larger than the largest.

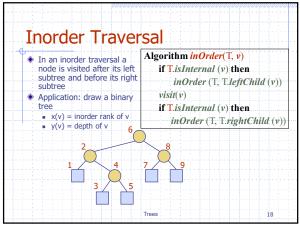
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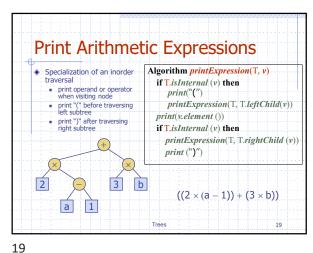


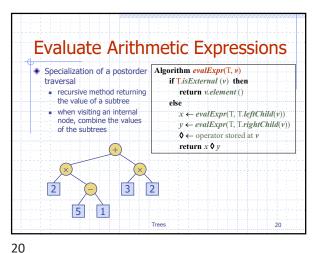
Preorder Traversal A traversal visits the nodes of a tree in a systematic Algorithm preOrder(T, v) visit(v) manner if T.isInternal (v) then In a preorder traversal, a preOrder (T, T.leftChild (v)) node is visited before its descendants preOrder (T, T.rightChild (v)) Application: print a structured document 16

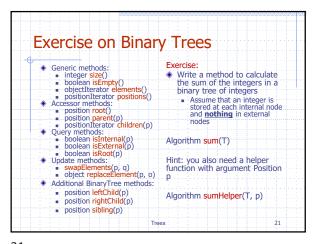
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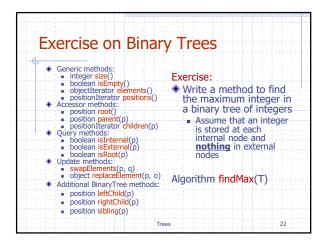












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```
Euler Tour Template
(pseudo-code)
  Algorithm Euler Tour(T, v)
      if T.isExternal (v) then
         visitExternal(T, v, result)
         visitPreOrder(T, v, result)
         \operatorname{result}[0] \leftarrow EulerTour(\mathbb{T},\,\mathbb{T}.leftChild(v))
         visitInOrder(v, result)
         result[2] \leftarrow EulerTour(T, T.rightChild(v))
         visitPostOrder(T, v, result)
       return result[1]
                                 Merge Sort
                                                                         23
```

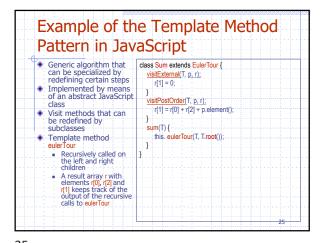
```
Example of the Template Method
Pattern in JavaScript
     Generic algorithm that
                                                     class EulerTour {
    can be specialized by
redefining certain steps
Implemented by means
of an abstract JavaScript
class
                                                         visitExternal(T, p, r) {}
visitPreOrder(T, p, r) {}
                                                         visitInOrder(T, p, r) {}
visitPostOrder(T, p, r) {}
                                                          eulerTour(T, p) {
    Visit methods that can
be redefined by
subclasses
                                                             let r = new Array(3):
                                                             if (T.isExternal(p)) { this.visitExternal(T, p, r); }
    Template method eulerTour
                                                                     this.visitPreOrder(T, p, r);

    Recursively called on
the left and right
children

                                                                     r[0] = this.eulerTour(T.leftChild(p));
this.visitInOrder(T, p, r);
r[2] = eulerTour(T.rightChild(p));
       children

• A result array r with elements r[0], r[1] and r[2] keeps track of the output of the recursive calls to eulerTour
                                                                     this.visitPostOrder(T, p, r);
                                                            }
                                                             return r[1];
```

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Main Point The positions (nodes and elements) of a Binary Tree are visited by traversing the tree in one of three ways: pre-order, in-order, post-order. The Euler Tour allows us to traverse any given binary tree in all three ways. The Euler Tour algorithm is non-changing, but we can insert actions (change) during the traversals by overriding the default (hook) methods of the template.

Science of Consciousness: Pure consciousness is non-changing and supports the everchanging relative creation. When we practice the TM technique, scientific research shows that mind and body are changed for the betterment of the individual and society.

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## Connecting the Parts of Knowledge with the Wholeness of Knowledge 1. The tree ADT is a generalization of the linkedlist in which each tree node can have any number of children instead of just one. A proper binary tree is a special case of the

2. Any ADT will have a variety of implementations of its operations with varying

generic tree ADT in which each node has either 0 or 2 children (a left and right child).

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efficiencies, e.g., the binary tree can be implemented as either a set of recursively defined nodes or as an array of elements. 27

3. Transcendental Consciousness is pure intelligence, the abstract substance out of which the universe is made. Impulses within Transcendental Consciousness: Within this field, the laws of nature continuously organize and govern all activities and processes in creation. Wholeness moving within itself: In Unity Consciousness, awareness is awake to its own value, the full value of the intelligence of nature. One's consciousness supports the knowledge that outer is the expression of inner, creation is the play and display of the Self. Amortized Analysis & Trees 28