

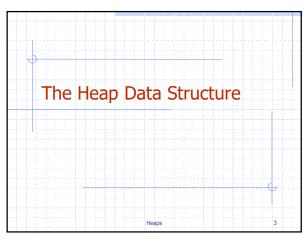
## Wholeness Statement

A heap is a binary tree that stores sortable elements at each internal node and maintains heap-order and is complete (balanced). Heap-order means that for every node v (except the root),  $key(v) \ge key(parent(v))$ . Science of Consciousness. Pure consciousness is the field of wholeness, perfectly orderly, balanced, and complete. Through regular TM practice we release stress and automatically develop the qualities of the unified field in our lives.

Amortized Analysis & Trees

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Min-Heap ADT

A Heap stores a collection of sortable elements

Main methods of the Heap ADT

InsertElem(e)

Inserts and returns the new Position (node) inserted into the Heap that contains the element e

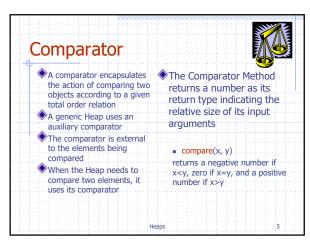
removeMin()

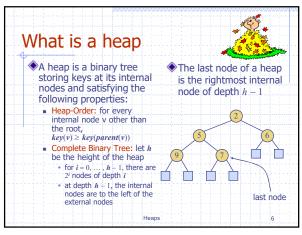
removes and returns the smallest element in the Heap

Heap

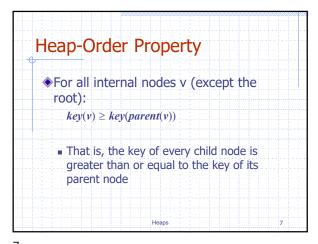
Heaps

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Other Properties of a Heap

A heap is a binary tree whose values are in ascending order on every path from root to leaf

Values are stored in internal nodes only

A heap is a binary tree whose root contains the minimum value and whose subtrees are heaps

Heap

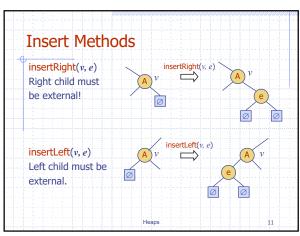
All leaves of the tree are on two adjacent levels
The binary tree is complete on every level except the deepest level.

depth
0
1
h-2
h-1
h
Heaps
9

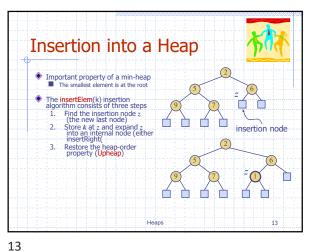
Adding Nodes to a Heap

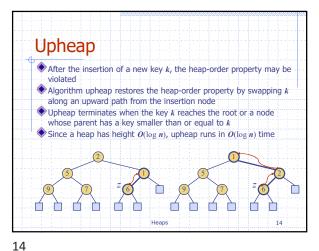
New nodes must be added left to right at the lowest level, i.e., the level containing internal and external nodes or containing all external nodes

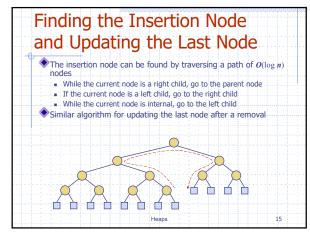
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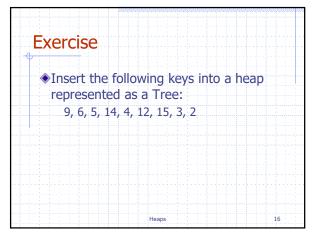


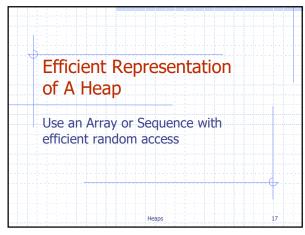
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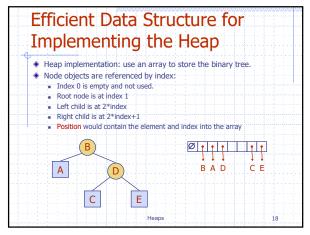


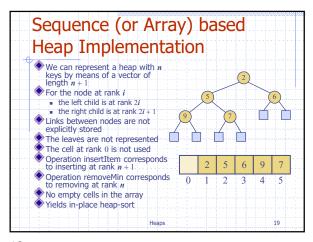


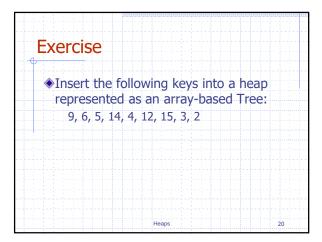






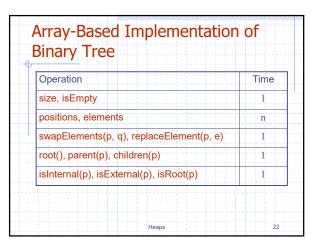




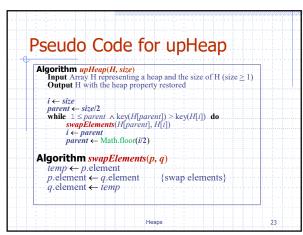


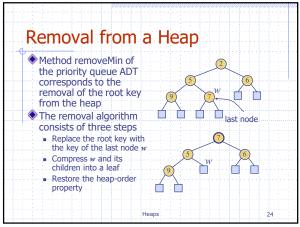
Array-Based Implementation of
Binary Tree

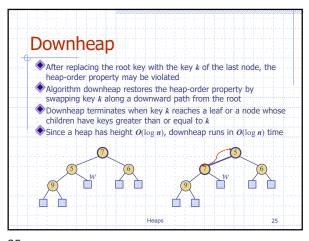
Operation
size, isEmpty
positions, elements
swapElements(p, q), replaceElement(p, e)
root(), parent(p), children(p)
isInternal(p), isExternal(p), isRoot(p)

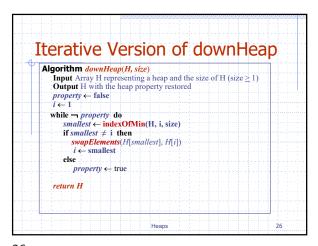


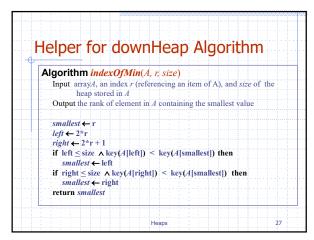
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Analysis of Heap Operations

Upheap()
Downheap()
insertElem(element)
removeMin()
removes element with minimum key if a min-heap (need a comparator for items)
removeMax() removes element with maximum key if a Max-Heap (parent is greater or equal to its children)

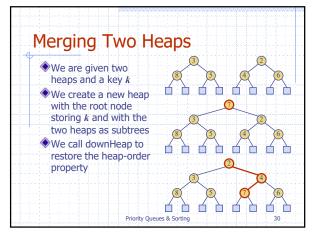
The Heap data structure is the basis of the HeapSort and is the basis of the proper implementation of a PriorityQueue (covered tomorrow)

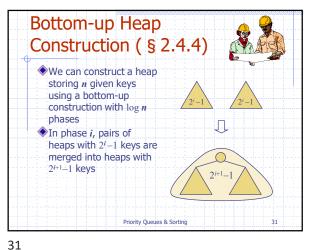
27 28

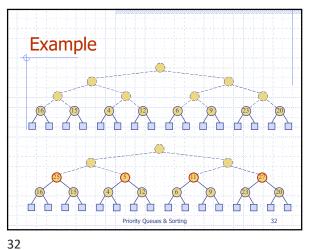
Main Point

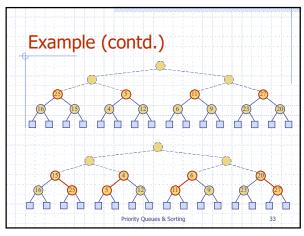
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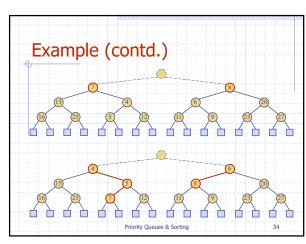
Heaps 29

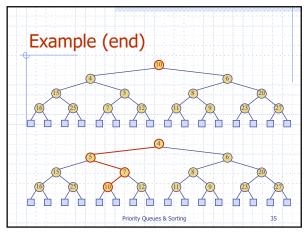


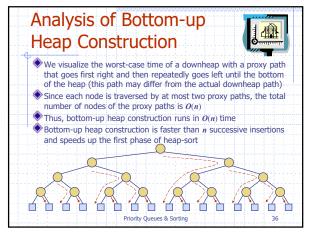












## Connecting the Parts of Knowledge with the Wholeness of Knowledge

- The Tree ADT models a hierarchical structure between objects simplified to a parent-child relation. A Heap is a binary tree with two properties, each path from root to leaf is in sorted order and the tree is always balanced.
- 2. The Heap can be implemented in two ways and thus its operations will have varying efficiencies, e.g., the binary tree can be implemented as either a set of recursively defined nodes or as an array of elements.

3. Transcendental Consciousness is pure intelligence, the abstract substance out of which the universe is made.

Impulses within Transcendental Consciousness: Within this field, the laws of nature continuously organize and govern all activities and processes in creation.

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5. Wholeness moving within itself: In Unity Consciousness, awareness is awake to its own value, the full value of the intelligence of nature. One's consciousness supports the knowledge that outer is the expression of inner, creation is the play and display of the Self.