

Assignment 1

R-1.1 Graph the functions $12n$, $6n \log n$, n^2 , n^3 , and 2^n using logarithmic scale for the x- and y-axes; that is, if the function value $f(n)$ is y , plot this as a point with x -coordinate at $\log n$ and y -coordinate at $\log y$.

R-1.2 Algorithm A uses $10n \log n$ operations, while algorithm B uses n^2 operations. Determine the value n_0 such that A is better than B for $n \geq n_0$.

R-1.6 Order the following list of functions by the big-O notation.

$n \log n$	$\log \log n$	$1/n$	$4n^{3/2}$
$5n$	$2n \log^2 n$	2^n	4^n
n^3	$n^2 \log n$	$4^{\log n}$	$\sqrt[n]{n}$

R-1.10 Give a big-O characterization, in terms of n , of the running time of the Loop1 method below:

```
Algorithm Loop1( $n$ )  
   $s \leftarrow 0$   
  for  $i \leftarrow 1$  to  $n$  do  
     $s \leftarrow s + i$ 
```

R-1.14 Perform a similar analysis for method Loop5 below:

```
Algorithm Loop5( $n$ )  
   $s \leftarrow 0$   
  for  $i \leftarrow 1$  to  $n^2$  do  
    for  $j \leftarrow 1$  to  $i$  do  
       $s \leftarrow s + i$ 
```

Prove:

$$\log_b x^a = a \log_b x$$