数学笔记

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Part I 知识整理

Chapter 1

向量丛与示性类

1.1 Constructions of vector bundles

• Tensor bundle: Let ξ^m and η^n be two vector bundles over paracompact base space B. There are bundle maps

$$f: \xi \to \gamma^m,$$
$$g: \eta \to \gamma^n.$$

Let

$$\otimes : \operatorname{Gr}_m \times \operatorname{Gr}_n \to G_{mn}$$

 $(V_1, V_2) \mapsto V_1 \otimes V_2,$

where $V_1, V_2 \subset \mathbb{R}^{\infty}$, dim $V_1 = m$, dim $V_2 = n$. Then $\xi \otimes \eta$ can be view as the pull-back bundle of γ^{mn} via the map

$$B \xrightarrow{\bar{f} \times \bar{g}} \operatorname{Gr}_m \times \operatorname{Gr}_n \xrightarrow{\otimes} \operatorname{Gr}_{mn}.$$

Bibliography

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