



Pune District Education Association's College Of Engineering

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Title of Assignment :-

~~Implement depth first search algorithm & Breadth first search algorithm. Use an Undirected graph & develop a recursive algorithm for searching all the vertices of a graph or tree data structure.~~

PREREQUISITE :-

~~Basic knowledge of Arrays, list, Stack, Queue, Graph, Tree etc.~~

Objectives :-

~~In this experiment, Education Association will be able to do the following :~~

- To Understand Uninformed Search Strategies.
- To make use of Graph & Tree Data Structure for implementations of Uninformed Search Strategies.
- Study the various Graph traversal algorithms & the difference b/w them.
- Understand the BFS Graph traversal Using queues.
- Demonstrate knowledge of time Complexity & Space Complexity of performing a BFS on a given Graph.

Outcome :-

~~Successfully able to find depth first search algorithm & Breadth First search algorithm~~

Software & Hardware Requirement :-

Open Source C++ Programming tool like
GCC, Python, Java & Ubuntu.

Theory :-

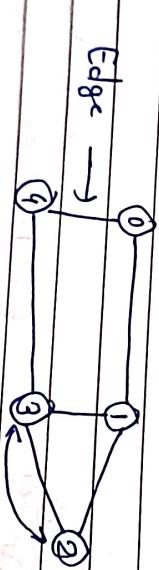
Uninformed (Blind Search) Search :

- Uninformed Search is a class of general purpose Search algorithms which operate in brute force-way.
- It examines each node of the tree or achieves the goal node.
- Uninformed Search algorithms do not additional about state or search space of how to traverse the tree & b to identify leaf & good nodes, so it also called blind search.
- Eg. DLS, BLS search algorithm -

Graphs definition :-

A graph is a pictorial representation of objects where some pairs of objects connected by links. The interconnected are represented by points termed as vertices. The links that connect the vertices called edges. Pictorial Representation of Graph.

Fig. Pictorial Representation of Graph



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Types of graph :-

- Undirected Graph :- Directions are not given to edges.
- Directed Graph :- Directions are given to edges with

Theory of Graph traversal techniques

- In Computer Science, graph traversal (also known as graph search) refers to the process of visiting (checking and/or updating) each vertex in a graph. Such traversals are classified by the order in which the vertices are visited. Depth First Traversal (DFT) is a special case of graph traversal.

Techniques of graph traversal

• DLS - A depth first search (DFS) is an algorithm for traversing a finite graph that visits the child vertices before visiting the sibling vertices; that is, it traverses the depth of any particular path before exploring its breadth. A stack (often the program's call stack via recursion) is generally used when implementing the algorithm.

• BFS - A breadth-first search (BFS) is another technique for traversing a finite graph. BFS visits the neighbor vertices before visiting the child vertices, & a queue is used in the search process. This algorithm is often used to

Find the Shortest Path from one vertex to another.



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An example which explain DFS Algorithm



- DFS - Depth First Search is a recursive algorithm
- Depth - First Search is a tree or graph data structure
- It is called depth - first search because it starts from the root node & follows it to its greatest depth node before moving to the next path.
- DFS uses a stack data structure for its implementation.

Initial Condition :-

Visited	0	0	0	0	0	0
	0	1	2	3	4	5

Depth First Search (DFS) Algorithm

Depth First Search (DFS) algorithm starts at the initial node of the graph G , & then goes deeper

until we find the goal node or the node which has no children. Then algorithm then backtracks from the deepest node to the most recent node that is yet to be completely explored. The structure which is being used in DFS is Stack.

- Step 1 : start by putting any one of the vertices on top of a stack. (Let us choose node 0 of DS).
- Step 2 : take the top item of the stack & its visited as 1.
- Step 3 : Create a list of the vertex's adjacent nodes. Add the ones whose visited is 0 to top of stack.
- Step 4 : keep repeating steps 2 & 3 until the stack is

Step 1:-
Start with node 0

Node 0 is pushed into stack & its visited value set to 1.

Visited	1	0	0	0	0	0
	0	1	2	3	4	5

Current Stack
DS Sequence--> [0]

Visited	1	0	0	0	0	0
	0	1	2	3	4	5

Step 2:-

Node 0 is popped from stack & its adjacent nodes and 3 are pushed into stack & visited value set to 1.

Visited	1	1	0	1	0	0
	0	1	2	3	4	5



① P Sequence : 0
 Current Stack [3]
 [1]

Step 3:
 Node 3 is popped from stack & its
 adjacent nodes 0, 4, 5 are pushed into stack
 because their visited value is 0,
 Set visited value to 1

Visited [1 | 1 | 1 | 1 | 1 | 1]
 0 1 2 3 4 5

Current Stack [3]
 [2]
 [1]

② P Sequence : 0, 3

Step 4:
 Node 5 is popped from stack . No adjacent
 node to add in stack .

Visited [1 | 1 | 1 | 1 | 1 | 1]
 0 1 2 3 4 5

Current Stack [4]
 [2]
 [1]

③ P Sequence : 0, 3, 5

Step 5:
 Node 6 is popped from stack
 So on need to push it into stack

Visited [1 | 1 | 1 | 1 | 1 | 1]
 0 1 2 3 4 5

Current Stack [2]
 [1]

④ P Sequence : 0, 3, 5, 4

Step 6:
 Node 5 is popped from stack , adjacent
 nodes visited value is already 1, so no
 need to push it into stack .

Visited [1 | 1 | 1 | 1 | 1 | 1]
 0 1 2 3 4 5

Current Stack [1]

⑤ P Sequence : 0, 3, 5, 4, 2

Step 7:
 Node 1 is popped from stack as No adjacent node
 One remain unvisited
 no other nodes are pushed into stack

⑥ P Sequence : 0, 3, 5, 4, 2

Current Stack []
 []

⑦ P Sequence : 0, 3, 5, 4, 2



- DLS Advantages :- It requires less memory.
- It only needs to store a stack of nodes.
- Current node.
- It takes less time to reach goal.
- DLS disadvantages :- There is possibility many states keep occurring infinite loop.

many states keep occurring infinite loop.

- Application :- DLS Algorithm can be used implement the topological sorting.

- It can be used to find the two paths the vertices.

- DLS algorithm is also used for one puzzles.

BFS algorithm :-

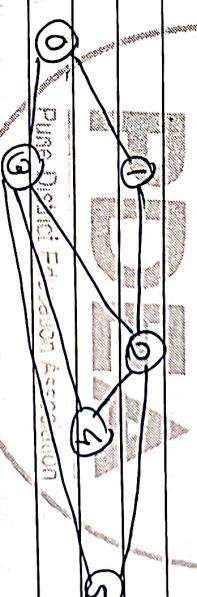
The algorithm starts with given source node & all its neighbour

Queues Definition :-

A queue is a linear structure which follows a particular order in which the operations are performed

The algorithm starts with the source node & of its neighbours. In the next step, the neighbours of the nearest node of the source node are explored. The algorithm then explores all neighbours of all the nodes & ensures that each node is visited exactly once & no node is visited twice.

An example which explains BFS Algorithm



Initial Condition
Visited : [0 0 0 0 0 0]

0 1 2 3 4 5

Curr. Queue [-]

BFS Sequence [-]

Step 1 :

Node '0' is selected as source node of the source node & all its neighbour

Visited [1 0 0 0 0 0]

0 1 2 3 4 5

A

queue is a linear structure which follows a particular order in which the operations are performed

A

queue is a linear structure which follows a particular order in which the operations are performed

A

queue is a linear structure which follows a particular order in which the operations are performed

A

queue is a linear structure which follows a particular order in which the operations are performed

A



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Step 2 :- Node '0' is deep dequeued from queue & its adjacent nodes are enqueued into queue i.e. 1, 3, by changing value to '1'.

Visited	[1 1 0 1 0 0]
	0 1 2 3 4 5

Curr. Queue	[1 3]
	0 1 2 3 4 5

BFS Sequence	[0 1 3 2 4 5]
	0 1 2 3 4 5

Step 3 :- Node '1' is dequeued from Queue & adjacent nodes are enqueued into queue i.e. 2, 3 but only node 2 is having visited value 0 but node 3 is already having visited value 1.

Visited	[1 1 1 1 0 0]
	0 1 2 3 4 5

Curr. Queue	[]
	0 1 2 3 4 5

BFS Sequence	[0 1]
	0 1 2 3 4 5

Step 4 & 5 :-

Node 3 is dequeued from queue & adjacent nodes 4,5 enqueued into queue & visited & also 2 is dequeued from queue if adjacent nodes already having visited

Value 1 So No enqueue node 4,5,6

Visited	[1 1 1 1 1]
	0 1 2 3 4 5

BFS Sequence	[0 1 3 2 4 5]
	0 1 2 3 4 5

As queue is empty, BFS is done on node '0' Nodes Visited in sequence : 0, 1, 3, 2, 4, 5

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- BFS Application :
- Path 4 minimum spanning tree for Unweighted graph.

• In peer to peer network search is used to torrent, breadth first search is used to find all neighbour nodes.

• GPS Navigation system, breadth first search is used to find all neighbouring location.

• Time Complexity : $T(B) = 1 + b^2 + b^3 + \dots b^d = O(b^d)$

Space Complexity : Space Complexity of BFS is given by the memory size of frontier which is $O(b^d)$



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Assignment No.: 2



- D.P.F. b/w BFS & DFS :
- BFS is a vertex-based algorithm.
- DFS is an edge-based algorithm.

- Queue data structure is used in BFS.
- The other hand, DFS uses stack.

- Memory space is efficiently utilized while space utilization in BFS is effective.

- DFS constructs narrow & long trees.

- where as BFS constructs wide & short tree.

Conclusion :-

In this way we have studied informed search strategy, how to implement depth first search algorithm for breadth first search algorithms. We can Undirected graph & develop a search algorithm for searching all the vertices of a graph or tree data structure.

Outcome :-

Succesfully able to find depth first search & Breadth First search algorithm.

Software & Hardware Requirements :-

Programming tool like C++/C/C++, Python, Java & Ubuntu.

Title of Assignment :-

Implement A Star algo - width for a puzzle game search problems.

Prerequisite :-

Basic knowledge of graph tree, informed search, Uniformed search, best first search etc.

Objectives :-

To this experiment, we will be able to the following:
To understand informed we will be able to the search strategies.

To make use of Graph & tree data structures for implementation of informed search strategies.

To study how A Star Algorithm is useful for implementation of a puzzle game search pro.



Theory:-

Informed Search:-

- Informed Search algorithm contains an array of knowledge about the goal state, how to reach the goal node, the knowledge search algorithm is more cost, for large search space.
- Informed search algorithm be the informed search algorithm called Heuristic function.

Heuristic function:-

• Heuristic is a function used in Informed Search, & it

- The most promising path.
- It takes the current state of the agent as input & produces the estimation of close the agent to from the goal.
- The heuristic method, however, might not always give the best solution, but it guaranteed to find a good solution in reasonable time.

- Heuristic function estimates how close is to goal. It represented by h if calculates the cost of an open path both the pair of states.
- The value of the heuristic function is always positive.

- A * Search Algorithm.
- * Search is the most commonly known for best-first search.

- It uses the heuristic function $h(n)$ to reach the node n from the start state $g(n)$.
- It has combined features of a greedy best-first search by which it solves the problem efficiently.
- A * search algorithm finds the shortest path through the search space using the heuristics function.
- This search algorithm expands less nodes.

To A * algorithm, we use formula $f(n) = g(n) + h(n)$

$$f(n) = g(n) + h(n)$$

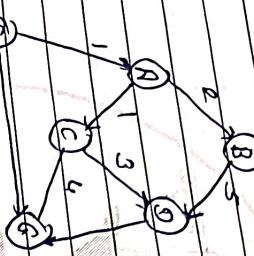
Estimated cost of each node n from start node to goal node.

In this example, we will increase the given graph using the A * algorithm. The heuristic value of all states is given in the below table so we will calculate the $f(n)$ of each state using the formula, $f(n) = g(n) + h(n)$.



where $g(n)$ is the cost to reach any node from start state. + closed list.

Here we will use Open + closed list.



State	$h(n)$
S	5
A	3
B	4
C	2
D	1
E	0

- * A* Search Algorithm - Advantages :-
- A* Search algorithm is the best algorithm than other search algorithms.
- This algorithm is optimal & complete.
- The main drawback of A* is memory requirement as it keeps all generated nodes in the memory, so it is not practical for various problems.

Iteration : 5 (5.5) ?

Iteration 1 : S (S -> A, 6) (S -> C, 10)

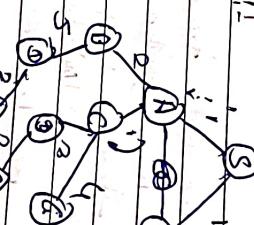
Iteration 2 : S (S -> A -> C, 4) (S -> A -> B, 7)

Iteration 3 : S (S -> A -> C -> G, 6), (S -> A -> C -> B, 7), (S -> C -> G, 11)

Iteration 4: we will give the final result

$S \rightarrow A \rightarrow C \rightarrow G$ provides the optimal path with cost 6.

5th



Time Complexity :- The time complexity is $O(b^n)$, where 'b' is the branching factor.

Space Complexity :- The space complexity of A* search algorithm is $O(b^n)$.

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a puzzle invented + popularization by Noyce had been Chapman in the 1970's. It is played on a 3-day 3 grid with 8 square blocks. You labelled 1 through 8 + a blank square. You goal is to rearrange the blocks so that they are in order. You can permuted to slide

blocks horizontally or vertically into the blank square.

1	2	3
4	5	6
7	8	:

1	2	3
4	5	6
7	8	:

Initial state good state.
Solution At algorithm:

$h(n) = \text{no. of misplaced tiles}$.

1	2	3
4	5	6
7	8	:

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1	2	3
7	4	6
5	8	:

↓

1	2	3
7	4	6
5	8	:

↓

1	2	3
7	4	6
5	8	:

↓

1	2	3
4	5	6
7	8	:

↓

1	2	3
4	5	6
7	8	:

↓

1	2	3
4	5	6
7	8	:

↓

1	2	3
4	5	6
7	8	:

↓

1	2	3
4	5	6
7	8	:

↓

1	2	3
4	5	6
7	8	:

↓

1	2	3
4	5	6
7	8	:



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Conclusion:-

In this way we have studied informed search strategy how to calculate heuristic function & implementation of 8 puzzle problem using A Star algorithm.

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Practical No:- 3



- Title of Assignment :-

algorithm for Selection Sort. Implement Greedy search

- Prerequisite :-

+ Basic knowledge of Greedy algorithm
+ Sorting Concept.

- Objective :-

In the experiment, we will be able to do the following :

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- Study how Selection Sort works greedy Search algorithm.

- Outcome :-

Successfully able to sort, Unsorted list of numbers

- Software & hardware Requirement :-

Open source C++ programming tool like G++ / GCC, Python, Java & Ubuntu.

Theory :-

Selection Sort is a Comparison-based sorting algorithm. It sort an array by repeatedly selecting the smallest (or largest)



The Unsorted portions. The element from the first Unsorted element. Then it with the first until the entire contiguous process sorted.

Initiation behind the Algorithm :-

Initial	Unsorted	Array
15	21	15
21	15	5
15	5	23
5	23	15

- 1) First we find the smallest among remaining elements. This way we get the first element at its correct position.

- 2) Then we find the smallest among all elements (or second smallest) & swap the second element.

- 3) We keep doing this until we get element moved to correct position.

- In Selection Sort, we take the simplest initiative approach to sort an array. Choose the smallest number, place it in first position. Then choose the next smallest number out of remaining elements & place it in the second position & so on till the end.

The Selection Sort algorithm sorts mainly two parts:

- ① The first part that is already sorted.
 ② The second part is yet to be sorted.

The algorithm works by repeatedly finding the minimum element from the unsorted

part & putting it at the end of the sorted part.

Smallest ele. out of these	[21]	[19]	[23]	[15]	[15]	[15]
Smallest ele. out of these	[21]	[23]	[15]	[15]	[15]	[15]

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Smallest ele. out of these	[23]	[15]	[19]	[21]	[23]
Smallest ele. out of these	[23]	[15]	[19]	[21]	[23]

Smallest ele. out of these	[23]	[15]	[19]	[21]	[23]
Smallest ele. out of these	[23]	↓	Swap		

Selection Sort algorithm :

Initial Unsorted Array

Arranging

34 [20] 3 14

i=1

↓

184 [20] 3 14 → 34 [20] 3 14 → 3 [20] 34



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Manjari (Bk.) H-1

3	14	34	20
3	14	34	20
3	14	34	20
3	14	34	20

$$\begin{array}{|c|c|c|c|} \hline 3 & 14 & 20 & 34 \\ \hline \end{array} \Rightarrow \begin{array}{|c|c|c|c|} \hline 3 & 14 & 20 & 34 \\ \hline \end{array} \Rightarrow \begin{array}{|c|c|c|c|} \hline 3 & 14 & 20 & 34 \\ \hline \end{array}$$

Running Time of Selection Sort

We are sorting N. elements of a given array. Using Selection sort.

o

To complete one iteration we traverse a portion of the array (from index 0 to end). Once the longest length we ever found so far is found, we can break.

Given iteration is N , time complexity of selection sort, we can N iterations, which takes $O(N)$ time. Hence overall time complexity become $O(N \times N)$.

Space Complexity of Selection Sort

elements, we need some extra space to store temporary value. Other than that, the thinking can be done-in-place. Hence, complexity is O(1) or constant space.

To be Stable if no objects with equal keys appear in the same order in sorted output as they are in the input. Unsorted some algorithm:-

Unsorted Array

56	10	23	9	34	23*
----	----	----	---	----	-----

9 10 23 23* 34 56

Is Selectionine Disorder Educable?

is a stable sorting algorithm. When looking for the smallest element we choose the element with lower index in case there are two or more equal elements that are the smallest elements in the array. This makes sure that we preserve the relative ordering between equal elements.

Conclusion:- Studied how

the temporary value. Other than that space can be done-in-place. Hence

Space is solid or constant space.

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Practical no : 4

Title of Assignment :-

Implement Greedy Search
algorithm for Prim's minimal Spanning tree
(algorithm)

Prerequisite :- बहुजन हिताय बहुजन सुखाय।

- Basic knowledge of Graph theory & Spanning trees
- Understanding of Greedy Algorithms & Priority Queues.

Objective :-

- In this experiment we will be able to :
- Understand the Concept of minimum Spanning Tree (mst)
- Compare time between Prim's algorithm with Kruskal's Algorithm.

Outcome :-

- Successfully able to implement & find the Minimum Spanning Tree (mst) Using Prim's Algorithm.
- Understand the greedy strategy used in MST algorithms.
- Compare time complexities of different MST algorithm.

Software & Hardware requirement:-

- Open-Source programming tools such as C, Java.

• Operating System: Window / Linux / Ubuntu.

Theory :-

Prim's Algorithm

- Prim's Algorithm is a greedy algorithm that grows the MST from a single starting edge that adds the smallest possible edge that connects a new vertex to the MST.

Working of Prim's Algorithm

- Start from an arbitrary vertex (usually vertex A).
- Add the smallest edge that connects a new vertex to the MST.
- Repeat Until all vertices are included in the MST.

Steps of Prim's Algorithm:

① Initialize :-

- Select an arbitrary vertex as the starting node.
- Create a visited array to keep track of nodes in MST.
- Use priority queue (min-heap) to pick the smallest edge.

② Iterate Until MST is formed:

- Pick the edge with the smallest weight that connects a new vertex.
- mark the newly added vertex as visited.
- Add its adjacent edges to the priority queue.

③ Repeat Until All vertices are Added :

Let's consider a graph with 5 vertices (A,B,C,D,E) & the following weighted edges :

Edge	Weight
A-B	2
B-C	1
B-D	4
C-D	3
C-E	2
D-E	1
E-C	1
G-E	1

Step-by-Step Execution of Prim's Algorithm

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- 1) Start with any vertex (Let's start with A)

- 2) Choose the smallest edge from A $\Rightarrow (A,B) = 2$

- 3) Add B to MST $\Rightarrow (B,C) = 1$

- 4) Choose the smallest edge from E, B, C $\Rightarrow (A,C) = 3$

- 5) Add C to MST $\Rightarrow (C,D) = 2$

- 6) Choose the smallest edge from G, D, E $\Rightarrow (C,E) = 1$

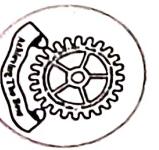
- 7) Add G to MST $\Rightarrow (G-E) = 1$

- 8) Choose the smallest edge from E, A, B, C, D $\Rightarrow (E-C) = 1$

- 9) Add E to MST

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Find MST (Minimum Spanning tree)

Edges included in the MST:

- A-B (2)
- B-C (1)
- C-D (4)
- C-E (1)
- Total Cost of MST = $2+1+4+6=13$

Kruskals Algorithm Advantages :-

- Works well with dense graphs (When the no. of edges is large).
- Always finds the optimal solution (i.e., MST is the smallest weight).
- Efficient with Priority Queues ($O(E \log V)$) using a ^{HAVING DISTINCT COLORATION ASSOCIATION} min-heap.

Kruskals Algorithm Disadvantages :-

- Not suitable for disconnected graphs (does not work if all nodes are not reachable).
- More complex than Kruskal's Algorithm for sparse graphs.

Conclusion :-

In this way we have studied how Kruskals algorithm is a greedy method for finding the minimum spanning tree (MST). It uses a priority queue (min-heap) for efficient edge selection. It is particularly efficient for dense graphs.



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Practical no: 5

Title of Assignment:-

Implementation of Kruskal's Minimal Spanning Tree (MST) algorithm.

Prerequisite:-

- Basic knowledge of Graph theory & Spanning tree
- Understand of Greedy Algorithm & Disjoint Set (Union-Find) Data Structure

Objective:-

In this experiment, we will be able to:

- Understand the concept of minimum spanning tree
- Implement Kruskal's Algorithm for Constructing the MST of a given graph
- Compare Kruskal's algorithm with Prim's Algorithm

Outcome:-

- Successfully able to implement & find the Minimum Spanning Tree (MST) Using Kruskal's algorithm
- Understand the greedy strategy used in MST algorithm.
- Compare time complexities of different MST algorithms.

Software & Hardware Requirement :

Open-Source programming tools Such as C++

Java : Operating System : Windows | Linux | Ubuntu

Java : Operating System : Windows | Linux | Ubuntu

Operating System : Windows | Linux | Ubuntu

Theory :-

Minimum Spanning Tree (MST)

- A Minimum Spanning tree (MST) is a subset of edges of a weighted graph that :
- 1) forms a connected spanning tree.
- 2) includes all vertices of the graph.
- 3) Has the minimum possible total edge weight.

There are two major algorithms to find MST

1) Prim's Algorithm (Greedy algorithm using Priority Queue).

2) Kruskal's Algorithm (Greedy algorithm using Priority Queue).

Doubting If Union-Find

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Kruskal's Algorithm :

- Kruskal's Algorithm is a greedy algorithm that builds the MST by selecting edges in increasing order of weight while ensuring no cycles are formed.
- It uses the Union-Find (Disjoint Set) data structure to check for cycles efficiently.

Working of Kruskal's Algorithm:-

- Sort all edges in ascending order of weight.
- Pick the smallest edge & check if adding it forms a cycle using the Union-Find data structure.
- If adding the edge does not form a cycle add it to the MST.
- Repeat until $(V-1)$ edges are included in the MST (V is the number of vertices).

Graphs Representation with weight :-

Edge	Weight
A-B	2
A-C	3
B-C	4
B-D	5
C-D	6
C-E	7
D-E	8

Step-by-Step Execution of Kruskal's Algorithm:-

- Sort all edges by weight : $(A, B, 2) \rightarrow (B, D, 4) \rightarrow (C, D, 5) \rightarrow (C, E, 6) \rightarrow (D, E, 7) \rightarrow (A, C, 3) \rightarrow (B, C, 4)$
- It uses the Union-Find (Disjoint Set) data structure to check for cycles efficiently.

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Comparison : Prim's vs Kruskal's Algorithm

Approach	Prim's Algorithm	Kruskal's Algorithm
feature	Greedy Nearest-based	Greedy edge-based.
Data Structure	Priority Queue (Minheap)	Disjoint Set (Union-Set)
Complexity	$O(E \log V)$ (with Min-heap)	$O(E \log V)$ (with sorting)

Best for Dense Graphs Sparse Graphs

Conclusion:-

In this way we have studied how kruskal's algorithm is a greedy method for finding the Minimum Spanning Tree (MST).

Algorithm is a greedy method for finding the MST. It uses edge sorting & the disjoint set (union-find) data structure to efficiently construct the MST. This is most efficient for sparse graphs, while Prim's algorithm is better for dense graphs.

- Easy to implement using Sorting + Union-Find.

Disadvantages of Kruskal's Algorithm:

- Slower for dense graphs compared to Prim's algorithm
- Requires sorting of edges, which adds $O(\log E)$ complexity.

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Practical Assignment no:-6

Title of Assignment :-

Implementation of Dijkstra's Minimal Spanning Tree Algorithm

Prerequisite :-

- Basic knowledge of Graph Theory & weighted Graphs
- Understanding of Greedy Algorithms & Priority Queue (min-heaps).

Objective in this experiment we will be able to :

- Understand Dijkstra's Algorithm & its real-world applications
- Implement Dijkstra's Algorithm to find the shortest path in a weighted graph.
- Compare Dijkstra's Algorithm with other shortest path algorithms like Bellman - Ford.

Outcome :-

- Successfully able to implement & find the shortest path from a source vertex to all other vertices using Dijkstra's Algorithm.
- Understand the greedy approach used in path-finding algorithms.
- Learn to use priority queues (min-heaps) to optimize

Dijkstra's Algorithm



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- Software & Hardware requirement tools such as C, Java.
- Open-Source System : Windows / Linux / Ubuntu.
- Operating System : Window / Linus / Ubuntu.

- Operating System : Window / Linus / Ubuntu.
- Theory :

Dijkstra's Shortest Path algorithm:

- Dijkstra's Algorithm is a greedy algorithm used to find the shortest path from a single source vertex to all other vertices in a weighted graph.
- It is application to graphs with non-negative weights.
- It uses using Priority Queue (min-heap) to always expand the closest vertex first.

Graph Representation with weight:



Working Dijkstra's Algorithm:

1) Initialize:

- Set the distance to the source vertex to 0 for all other vertices as ∞ .
- Create a priority queue (min-heap) to store (distance, vertex) pairs.

2) Process Vertices:

- Pick the vertex with the smallest distance from the priority queue.

Step-by-step Execution of Dijkstra's Algorithm

(Starting from A):

- 1) Initialize distances: $A=0, B=\infty, C=\infty, D=\infty, E=\infty$
- 2) Pick the smallest distance node ($A=0$).

- 3) Update: $B=4, C=1$

- 4) Pick the smallest distance node ($B=3$)

- 5) Update: $D=8$



- 5) Pick the Smallest distance node ($E = 5$)
 • Update : $E = 10$
 o) Pick the Smallest distance node ($E = 10$)
 • Update)

Find Shortest Distance from A :

- $A \rightarrow A = 0$
- $A \rightarrow B = 3$
- $A \rightarrow C = 1$
- $A \rightarrow D = 8$
- $A \rightarrow E = 10$

Advantages of Dijkstra's Algorithm :

- Guaranteed to find the Shortest path in graphs with non-negative weights.

- Efficient for graphs with small edge weights.

- Can be Optimised using Fibonacci Heap ($O(V \lg V + E \lg E)$)

Disadvantages of Dijkstra's Algorithm :

- Does not work with negative weights (use Bellman-Ford Algorithm instead).

- More Complex than BFS for Unweighted Graphs.

- Inefficient for dense graphs without a priority queue (O(V²) complexity).

Comparison : Dijkstra's vs other shortest path algorithms .

Feature	Dijkstra's Algo.	Bellman-Ford Algo.	Floyd-Warshall Algo.
Approach	Greedy	Dynamic programming	Matrix-based
Works for	Non-negative weights	Negative weights allowed	All pair shortest
Time Complexity	$O(V \log V + E)$	$O(VE)$	$O(V^3)$
Best for	Single-Source shortest path	Single-Source, negative edges	All pairs shortest paths

Conclusion :-

- Dijkstra's Algorithm is a greedy algorithm used to find the shortest path from a single source to all vertices in a weighted graph.

- It is optimal for non-negative weights & is widely used in routing algorithms like Google Maps, GPS navigation.



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Assignment no:- 5

- Title of Assignment :- Implement a Solution for a Constraint Satisfaction Problem Using Branch & Bound / Backtracking for n-queens problem.
- Pre-requisite :- Basic knowledge of CSP, Backtracking
- Objectives :-
 - In this assignment, we will be able to do the following :-
 - Study how to place N! queens on board with non attacking mode using backtracking.
 - What is CSP problem.
- Outcome :- Successfully able to place N queens on board with non attacking mode using backtracking.
- Software & Hardware Requirements :-
 - Open Source C++ Programming tool like G++/GCC ; python ; java ; Ubuntu .

- Relevant Theory / literature Survey:
 - Constraint means theory satisfaction problem.
 - CSP means solving a problem under certain constraints or rules
 - CSP depends on three Components x : It is a set of variables
 - ① : It is set of domains ~~for each variable reside~~
There is a specific domain for each variable
 - c : It is set of constraints which are followed by ~~प्रकृति वर्तन विधि, बंदुक युवा विधि~~ a set of variables.

Backtracking Algorithm

Backtracking is an algorithm - technique for solving problems recursively by trying to build a solution incrementally, one piece at a time, removing those solutions that fail to satisfy the constraints of the problem at any point of time (by time, here, is referred to the time elapsed till reaching any level of the search tree).

N-Queens problem

The N-Queens problem is a puzzle of placing exactly N queens on an $N \times N$ chessboard, such that no two queens can attack each other in that configuration. Thus, no two queens can lie in the same



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row, Column or diagonal

0	1	2	3	4	5	6	7	0	1	2	3
0	Q							0			Q
1							Q				
2				Q							
3							Q				
4		Q									
5				Q							
6						Q					
7			Q								

Solution 1: 0, 4, 7, 5, 2, 6, 1, 3

Solution 2: 1, 3, 0, 2, 7, 6, 4, 5

N- Queens problem Algorithm

- 1) Start in the leftmost column.
- 2) If all queens are placed return true.
- 3) try for all rows in the current column.
Do the following for every tried row.

a) If the queen can be placed safely in this row then mark this [row, column] as part of the solution & recursively check if placing the queen here leads to a solution.

b) If placing the queen in [row, column] leads to a solution then return false.

doesn't lead to a
sleeping [in] [var]. [Columbus]

c) If filing there unmarked by line
Solicitor → 4 or 5 step (a) to my office

(Backtrack)
have been tried & nothing

4) If all rows have false, trigger backtracking

Branch & Bound is an algorithm design paradigm. Branch & bound is generally used for solving combinatorial optimization problems. The problem are typically exponential in terms of time and complexity and may require exploring all possible permutations in the worst case. The Branch & Bound Algorithm

technique have been used quickly.

• Applying ~~the~~ branch and bound approach:

The branch and bound approach suggests that we create a partial solution that we use it to ascertain whether we need to continue in a particular direction or not.



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Parameter	Backtracking	Branch & Bound
Approach	Backtracking is used to find all possible solutions available to a problem.	Branch & Bound is used to solve optimization problems.
Solution	Realize that it has realized that it has a better option.	Solution that the problem leads to pre solution leads to it abandoning the problem.
Choice	Choice by backtracking.	Pre-selection. It pre-selects space tree completely.
Search	Searches the state space tree to get a solution for the problem.	Searches the state space tree to get an optimal solution.
Traversal	Backtracking traverses branch-and-bound branch. And-Bound traversal the tree in a depth first search manner.	Traverses the tree in a depth first search manner.
Function	Backtracking is used for solving decision problems. A feasibility function is involved.	Branch-and-Bound function.

Efficiency	Backtracking is more efficient	Branch-and-Bound is less efficient
Application	Useful in solving n-Queen problem, Sum of Subset	Useful in solving knapsack problem, Traveling Salesman Problem.

~~Conclusion :- In this way we have studied how to solve the CSP problem → how to place N queens on board with non attacking mode using backtracking.~~



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