

Data Storage

- Bits and Their Storage
- Main Memory
- Mass Storage
- Representing Information as Bit Patterns
- The Binary System
- Storing Integers
- Storing Fractions

Bits and Their Storage

- **Bit:** Binary Digit (0 or 1)
- Bit Patterns are used to represent information
 - Numbers
 - Text characters
 - Images
 - Sound
 - And others

Boolean Operations

- **Boolean Operation:** An operation that manipulates one or more true/false values
- Specific operations
 - AND
 - OR
 - XOR (exclusive or)
 - NOT

The possible input and output values of Boolean operations AND, OR, and XOR (exclusive or)

The AND operation

$$\begin{array}{r} 0 \\ \text{AND } 0 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 0 \\ \text{AND } 1 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 1 \\ \text{AND } 0 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 1 \\ \text{AND } 1 \\ \hline 1 \end{array}$$

The OR operation

$$\begin{array}{r} 0 \\ \text{OR } 0 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 0 \\ \text{OR } 1 \\ \hline 1 \end{array}$$

$$\begin{array}{r} 1 \\ \text{OR } 0 \\ \hline 1 \end{array}$$

$$\begin{array}{r} 1 \\ \text{OR } 1 \\ \hline 1 \end{array}$$

The XOR operation

$$\begin{array}{r} 0 \\ \text{XOR } 0 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 0 \\ \text{XOR } 1 \\ \hline 1 \end{array}$$

$$\begin{array}{r} 1 \\ \text{XOR } 0 \\ \hline 1 \end{array}$$

$$\begin{array}{r} 1 \\ \text{XOR } 1 \\ \hline 0 \end{array}$$

Gates

- **Gate:** A device that computes a Boolean operation
 - Often implemented as small electronic circuits called transistors
 - Can be constructed from a variety of other technologies
 - Provide the building blocks from which computers are constructed

A pictorial representation of AND, OR, XOR, and NOT gates as well as their input and output values

AND



Inputs	Output
0 0	0
0 1	0
1 0	0
1 1	1

OR



Inputs	Output
0 0	0
0 1	1
1 0	1
1 1	1

XOR



Inputs	Output
0 0	0
0 1	1
1 0	1
1 1	0

NOT

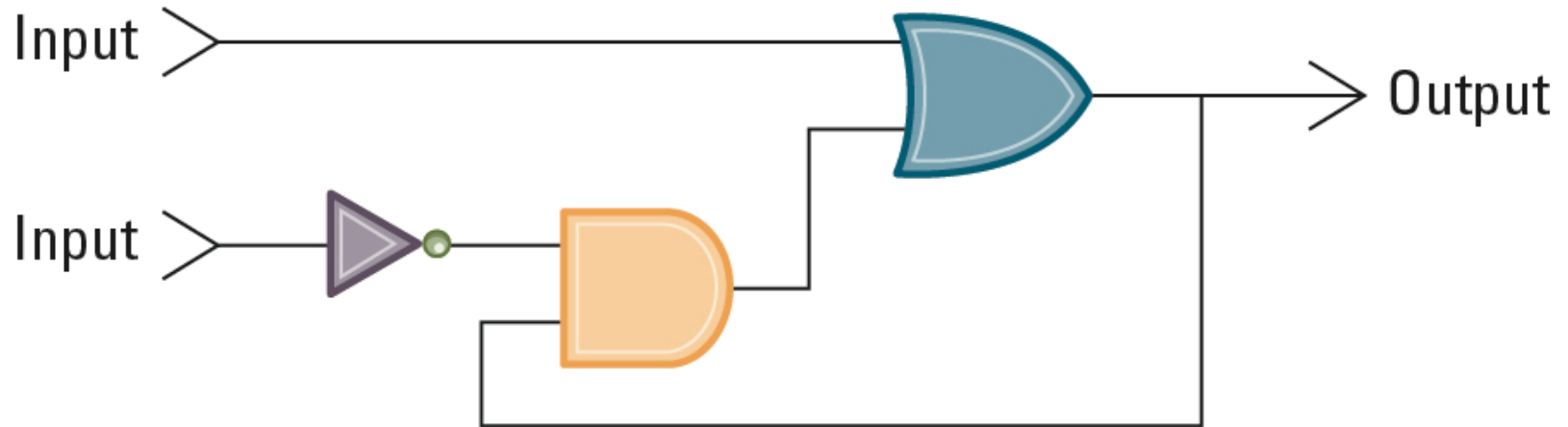


Inputs	Output
0	1
1	0

Flip-flops

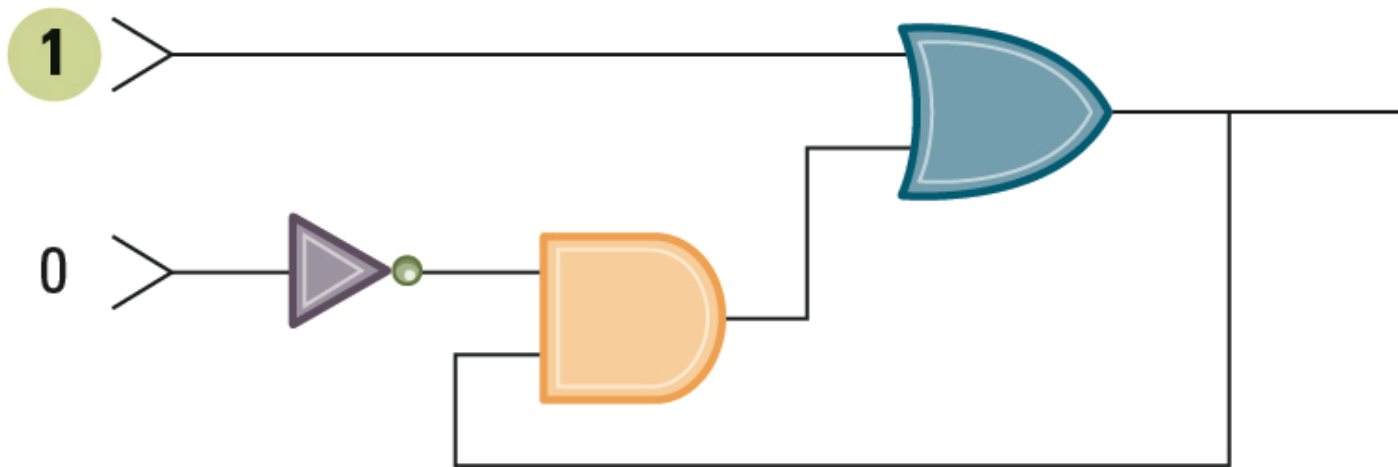
- Circuits built from gates that act as a fundamental unit of computer memory
 - One input line is used to set its stored value to 1
 - One input line is used to set its stored value to 0
 - While both input lines are 0, the most recently stored value is preserved

A simple flip-flop circuit



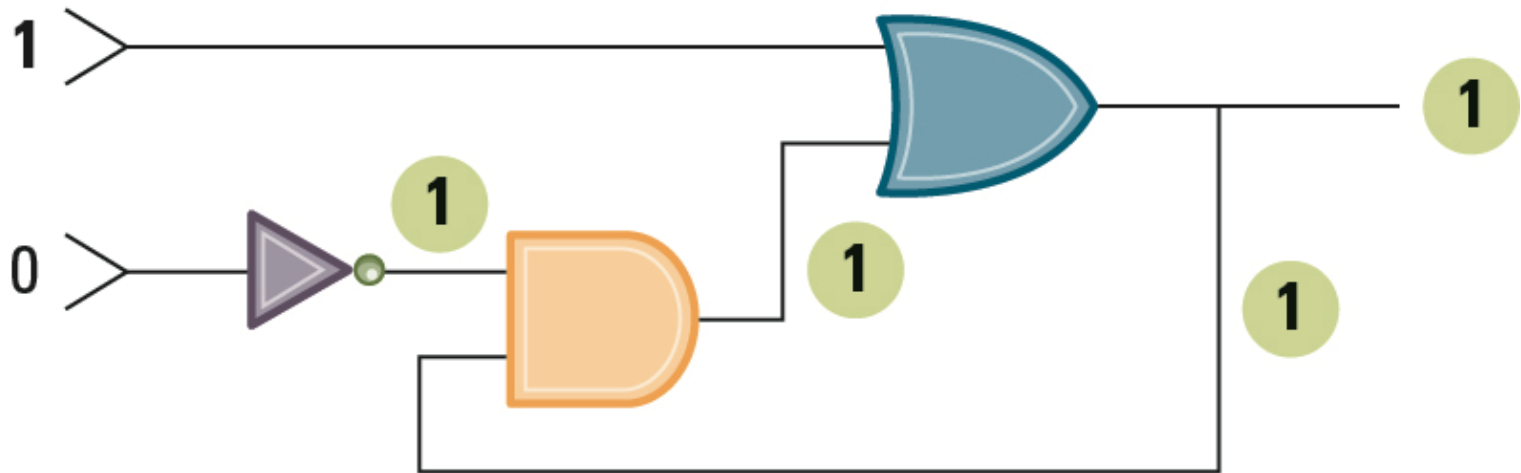
Setting the output of a flip-flop to 1

a. First, a 1 is placed on the upper input.



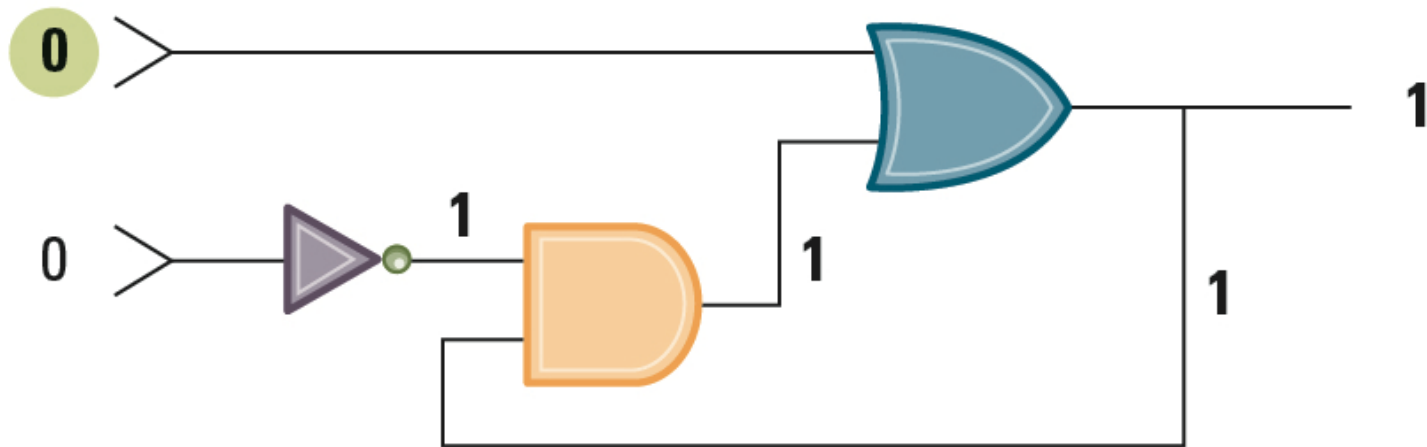
Setting the output of a flip-flop to 1 (continued)

b. This causes the output of the OR gate to be 1 and, in turn, the output of the AND gate to be 1.

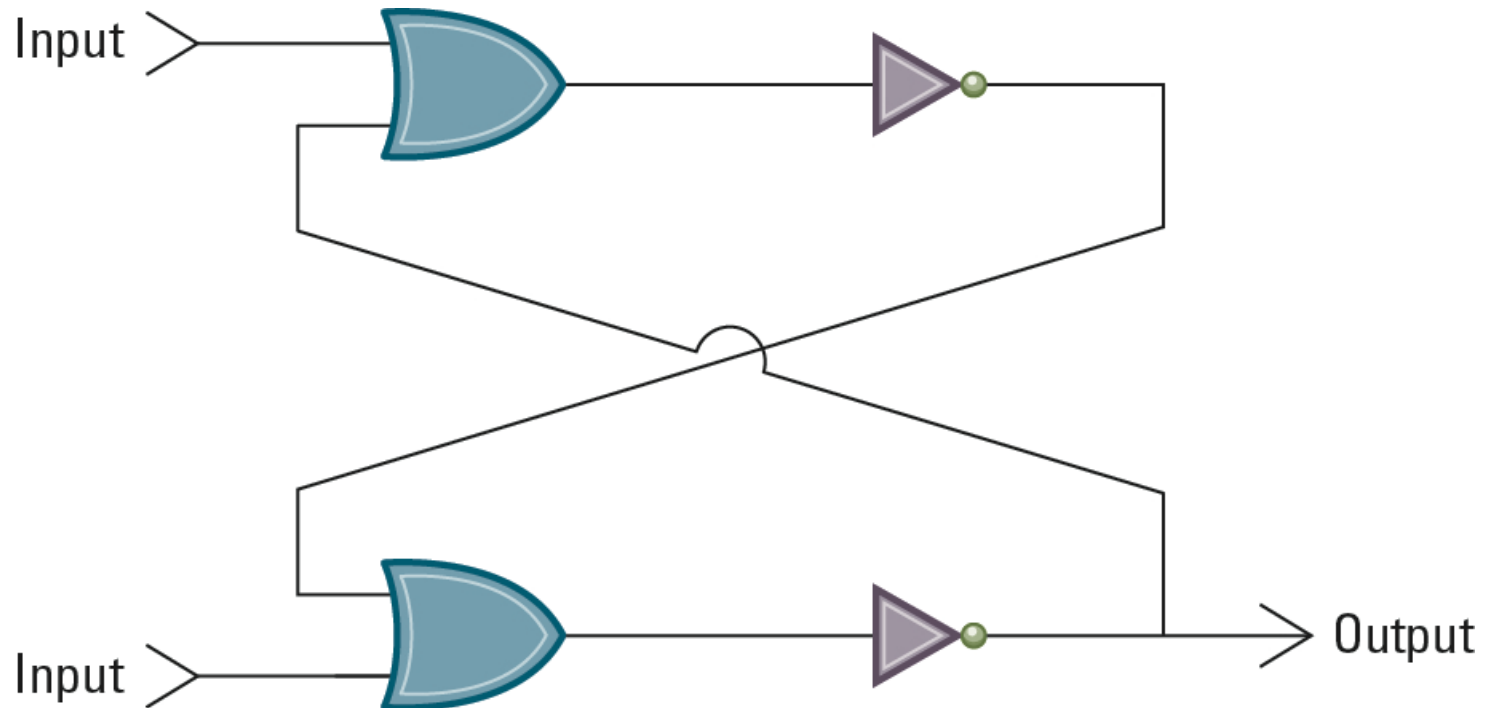


Setting the output of a flip-flop to 1 (continued)

c. Finally, the 1 from the AND gate keeps the OR gate from changing after the upper input returns to 0.



Another way of constructing a flip-flop



Hexadecimal Notation

- **Hexadecimal notation:** A shorthand notation for long bit patterns
 - Divides a pattern into groups of four bits each
 - Represents each group by a single symbol
- Example: 10110101 becomes 0xB5

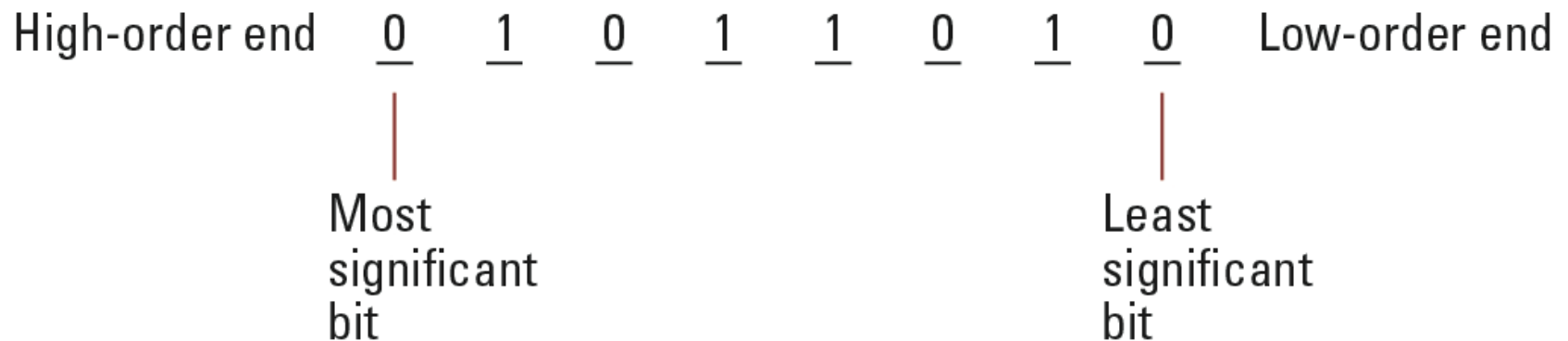
The hexadecimal coding system

Bit pattern	Hexadecimal representation
0000	0x0
0001	0x1
0010	0x2
0011	0x3
0100	0x4
0101	0x5
0110	0x6
0111	0x7
1000	0x8
1001	0x9
1010	0xA
1011	0xB
1100	0xC
1101	0xD
1110	0xE
1111	0xF

Main Memory

- **Cell:** A unit of main memory (typically 8 bits which is one **byte**)
 - **Most significant bit:** the bit at the left (high-order) end
 - **Least significant bit:** the bit at the right (low-order) end

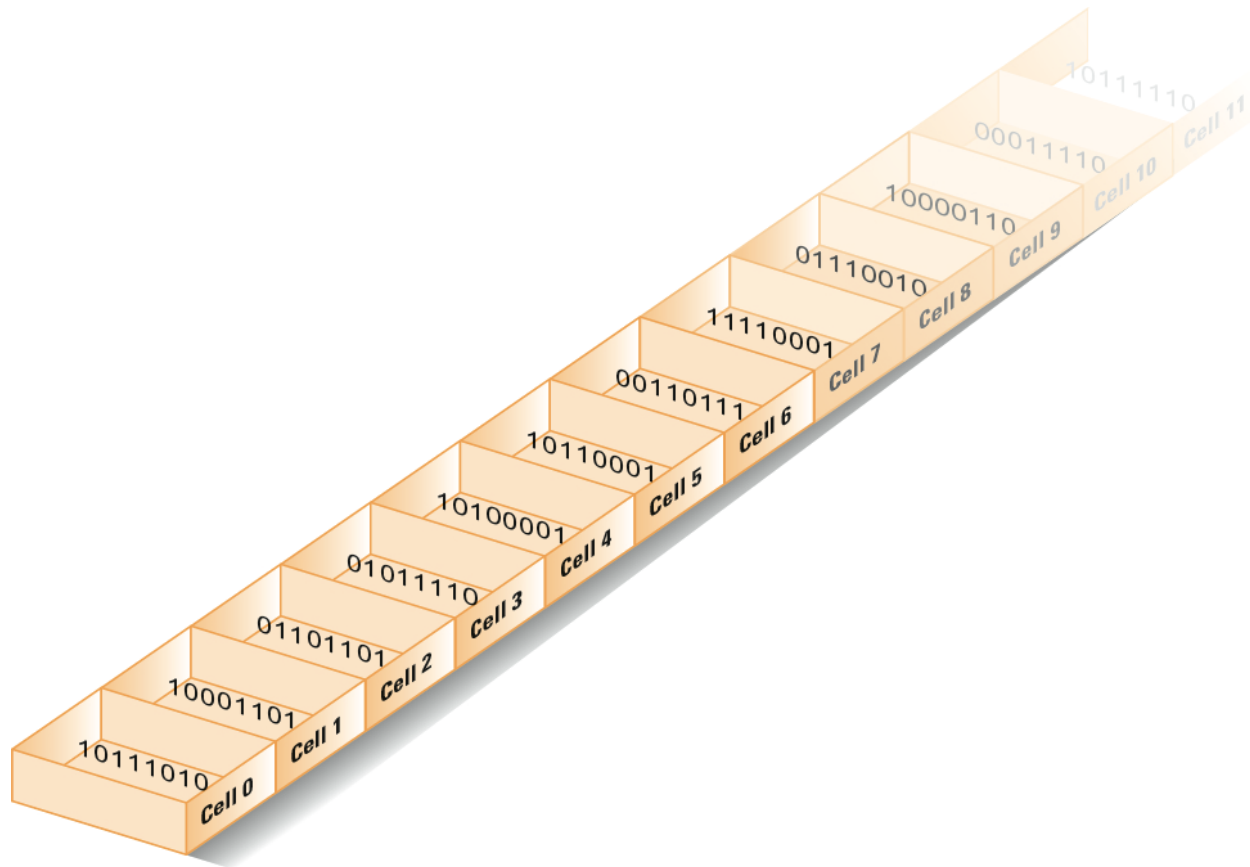
The organization of a byte-size memory cell



Main Memory Addresses

- **Address:** A “name” that uniquely identifies one cell in the computer’s main memory
 - The names are actually numbers.
 - These numbers are assigned consecutively starting at zero.
 - Numbering the cells in this manner associates an order with the memory cells.

Memory cells arranged by address



Memory Terminology

- **Random Access Memory (RAM):** Memory in which individual cells can be easily accessed in any order
- **Dynamic Memory (DRAM):** RAM composed of volatile memory

Measuring Memory Capacity

- **Kilobyte:** 2^{10} bytes = 1024 bytes
 - Example: 3 KB = 3 times 1024 bytes
- **Megabyte:** 2^{20} bytes = 1,048,576 bytes
 - Example: 3 MB = 3 times 1,048,576 bytes
- **Gigabyte:** 2^{30} bytes = 1,073,741,824 bytes
 - Example: 3 GB = 3 times 1,073,741,824 bytes

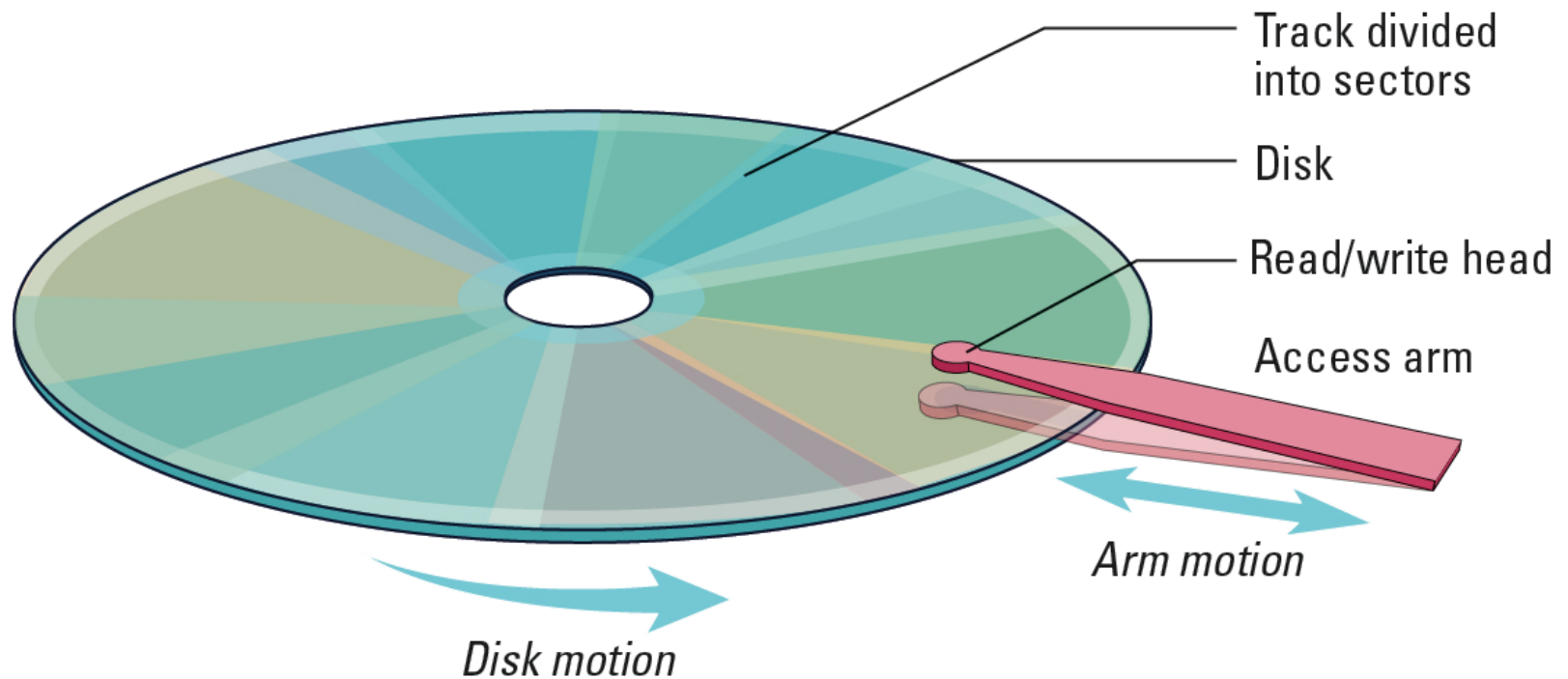
Mass Storage

- Additional devices:
 - Magnetic disks
 - CDs
 - DVDs
 - Magnetic tapes
 - Flash drives
 - Solid-state drives
- Advantages over main memory
 - Less volatility
 - Larger storage capacities
 - Low cost
 - In many cases can be removed

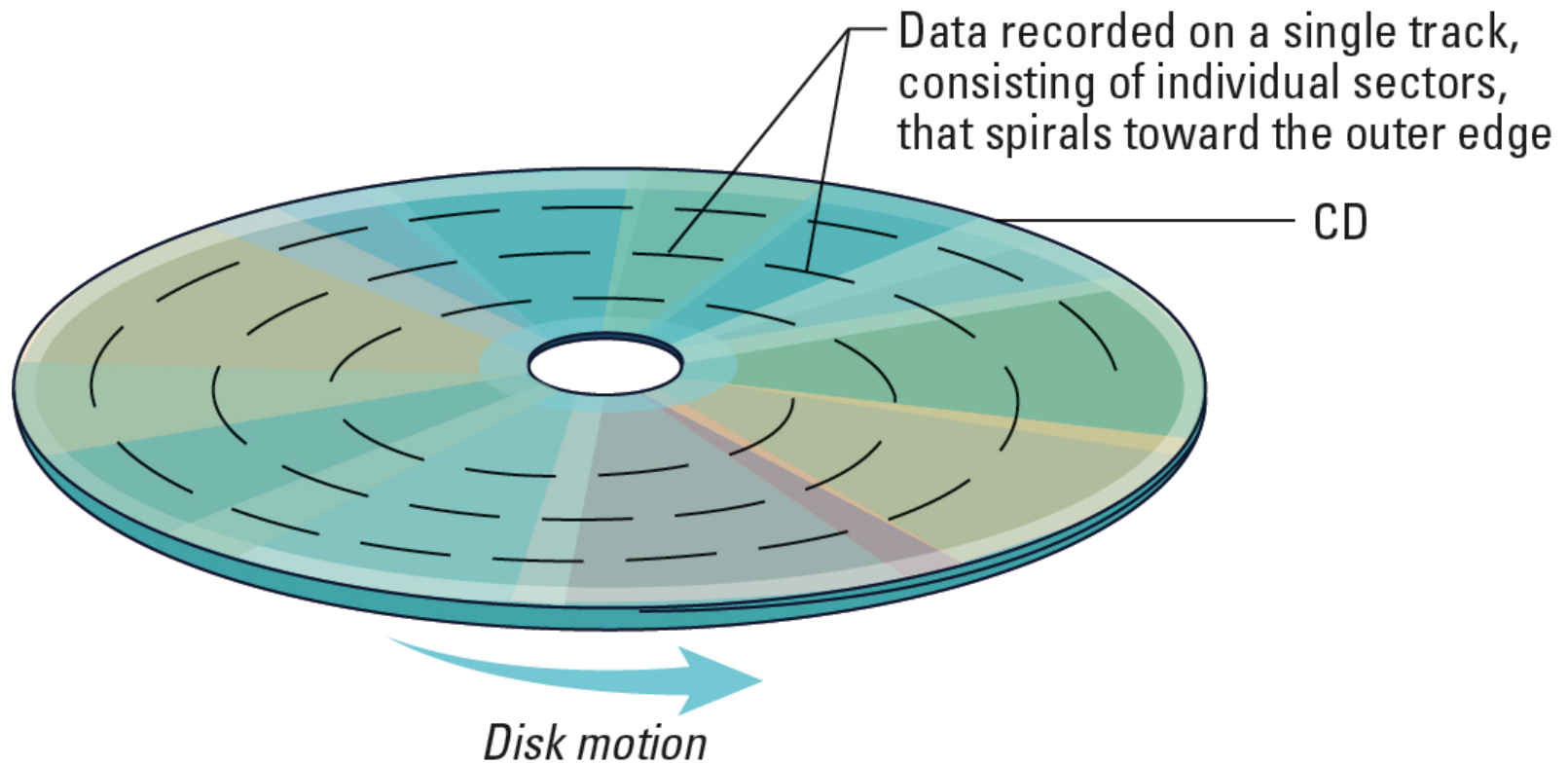
Mass Storage Performance

- **Bandwidth:** The total amount of bits that can be transferred in a unit of time
- **Latency:** The total time between the request for data transfer and its arrival

A magnetic disk storage system



CD storage



Flash Drives

- **Flash Memory** – circuits that traps electrons in tiny silicon dioxide chambers
- Repeated erasing slowly damages the media
- Mass storage of choice for:
 - Digital cameras
 - Smartphones
- **SD Cards** provide GBs of storage

Representing Information as Bit Patterns

- Many different kinds of information can be encoded as bit patterns
- Systems for encoding information have been established for
 - Text
 - Numeric Data
 - Images
 - Sound
 - Other data

Representing Text

- **Each character (letter, punctuation, etc.) is assigned a unique bit pattern.**
 - **ASCII:** Uses patterns of 7-bits to represent most symbols used in written English text
 - **ISO** developed a number of 8 bit extensions to ASCII, each designed to accommodate a major language group
 - **Unicode:** Uses patterns up to 21-bits to represent the symbols used in languages world wide, 16-bits for world's commonly used languages

The message “Hello.” in ASCII or UTF-8 encoding

01001000	01100101	01101100	01101100	01101111	00101110
H	e	l	l	o	.

Representing Numeric Values

- **Binary notation:** Uses bits to represent a number in base two
 - All numeric values in a computer are stored in sequences of 0s and 1s
 - Counting from 0 to 8:
 - 0000, 0001, 0010, 0011, 0100, 0101, 0110, 0111, 1000

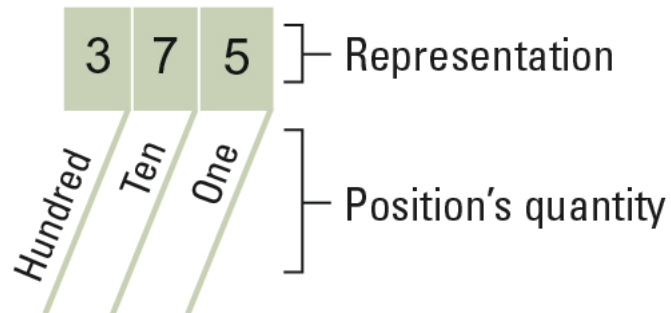
The Binary System

The traditional decimal system is based on powers of ten.

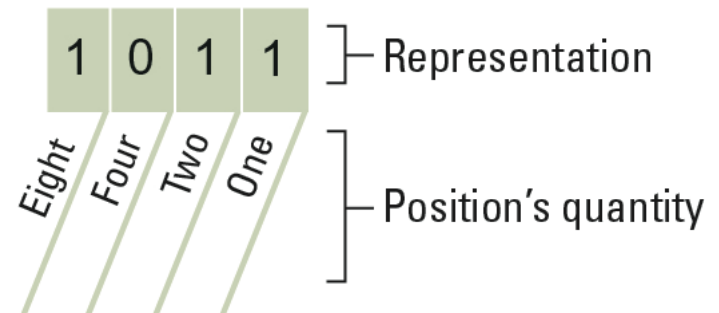
The Binary system is based on powers of two.

The base ten and binary systems

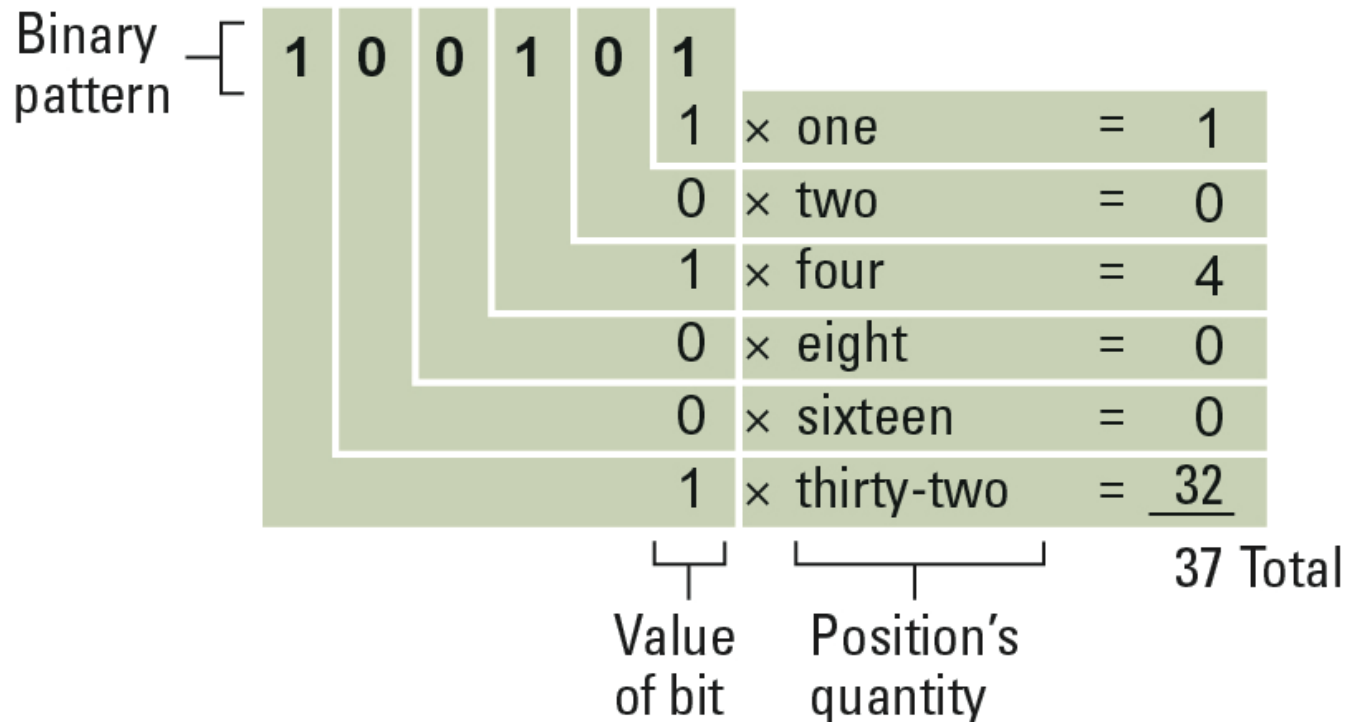
a. Base 10 system



b. Base two system



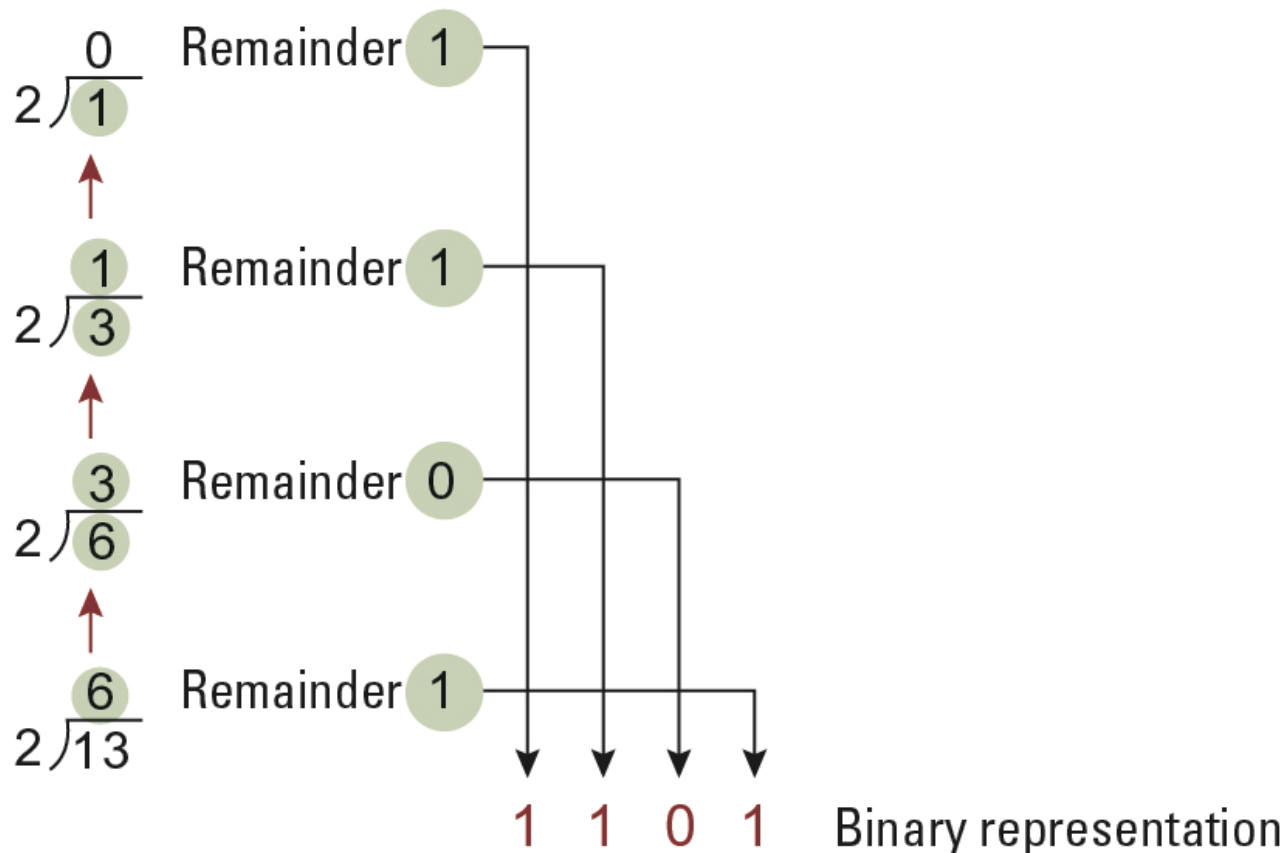
Decoding the binary representation 100101



An algorithm for finding the binary representation of a positive integer

- Step 1. Divide the value by two and record the remainder.
- Step 2. As long as the quotient obtained is not zero, continue to divide the newest quotient by two and record the remainder.
- Step 3. Now that a quotient of zero has been obtained, the binary representation of the original value consists of the remainders listed from right to left in the order they were recorded.

Applying the algorithm to obtain the binary representation of thirteen



The binary addition facts

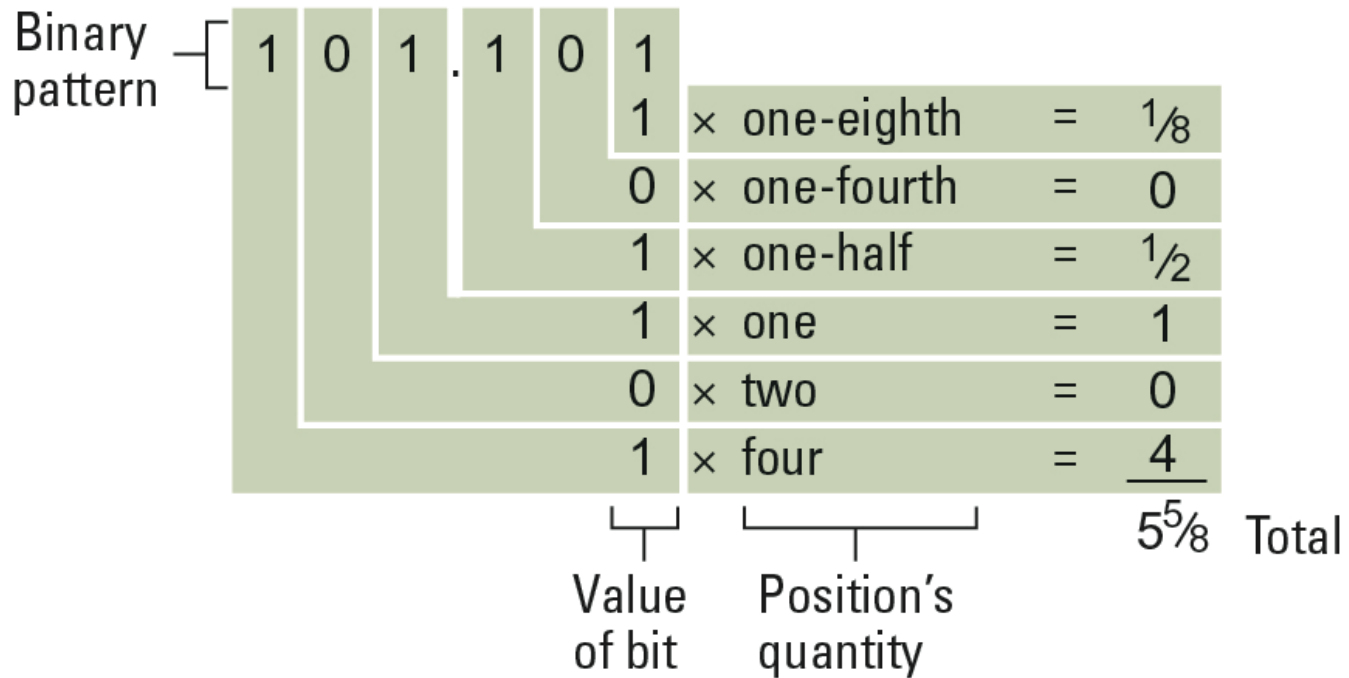
$$\begin{array}{r} 0 \\ + 0 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 1 \\ + 0 \\ \hline 1 \end{array}$$

$$\begin{array}{r} 0 \\ + 1 \\ \hline 1 \end{array}$$

$$\begin{array}{r} 1 \\ + 1 \\ \hline 10 \end{array}$$

Decoding the binary representation 101.101



Storing Integers

- **Two's complement notation:** The most popular means of representing integer values
- **Excess notation:** Another means of representing integer values

Two's complement notation systems

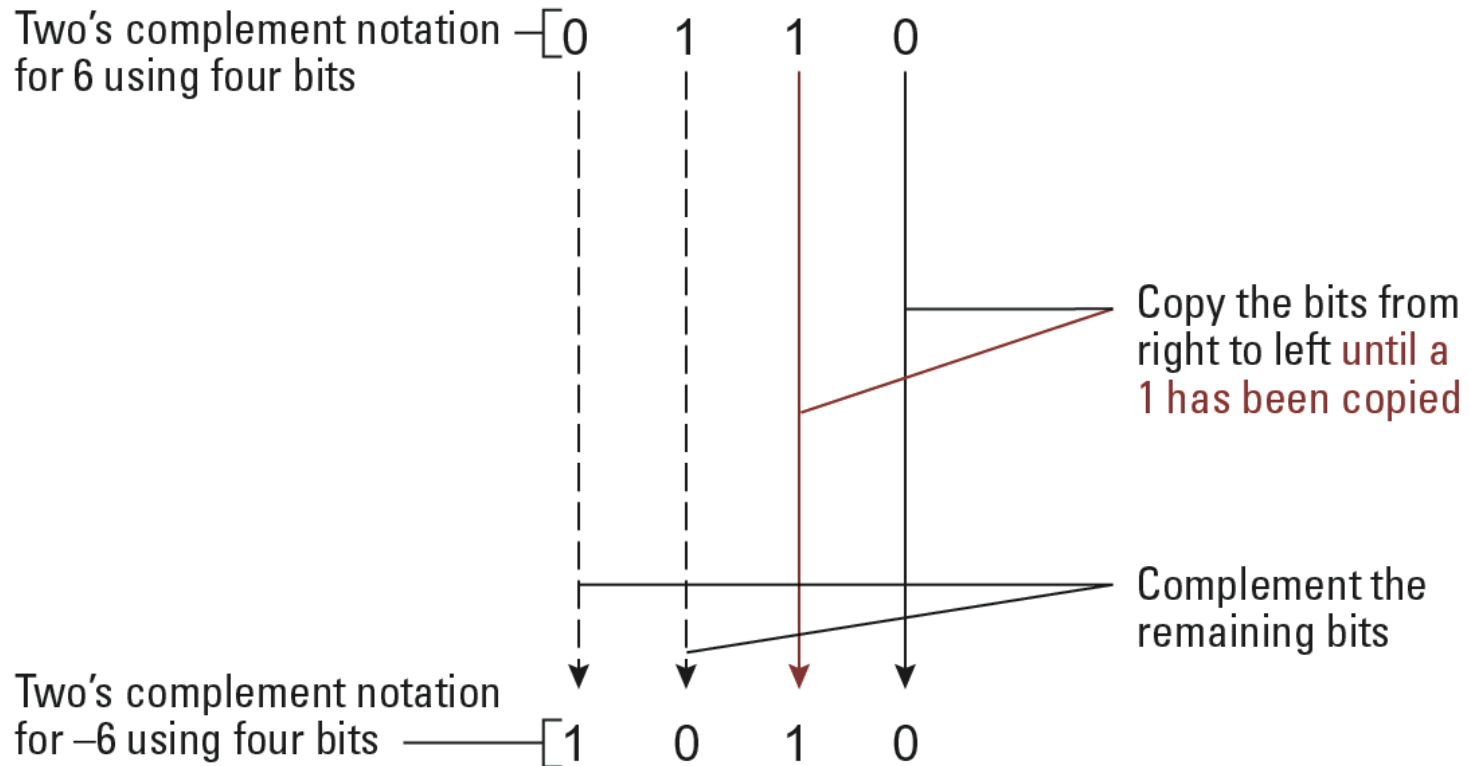
a. Using patterns of length three

Bit pattern	Value represented
011	3
010	2
001	1
000	0
111	-1
110	-2
101	-3
100	-4

b. Using patterns of length four

Bit pattern	Value represented
0111	7
0110	6
0101	5
0100	4
0011	3
0010	2
0001	1
0000	0
1111	-1
1110	-2
1101	-3
1100	-4
1011	-5
1010	-6
1001	-7
1000	-8

Coding the value -6 in two's complement notation using four bits



Addition problems converted to two's complement notation

Problem in base 10		Problem in two's complement		Answer in base 10
$\begin{array}{r} 3 \\ + 2 \\ \hline \end{array}$	→	$\begin{array}{r} 0011 \\ + 0010 \\ \hline 0101 \end{array}$	→	5
$\begin{array}{r} -3 \\ + -2 \\ \hline \end{array}$	→	$\begin{array}{r} 1101 \\ + 1110 \\ \hline 1011 \end{array}$	→	-5
$\begin{array}{r} 7 \\ + -5 \\ \hline \end{array}$	→	$\begin{array}{r} 0111 \\ + 1011 \\ \hline 0010 \end{array}$	→	2

The Problem of Overflow

- There is a limit to the size of the values that can be represented in any system
- Overflow
 - occurs when a computation produces a value that falls outside the range of values that can be represented in the machine
 - If the resulting sign bit is incorrect, an overflow has occurred
 - 16 bit systems have been upgraded to 32 bit systems

An excess eight conversion table

Bit pattern	Value represented
1111	7
1110	6
1101	5
1100	4
1011	3
1010	2
1001	1
1000	0
0111	-1
0110	-2
0101	-3
0100	-4
0011	-5
0010	-6
0001	-7
0000	-8

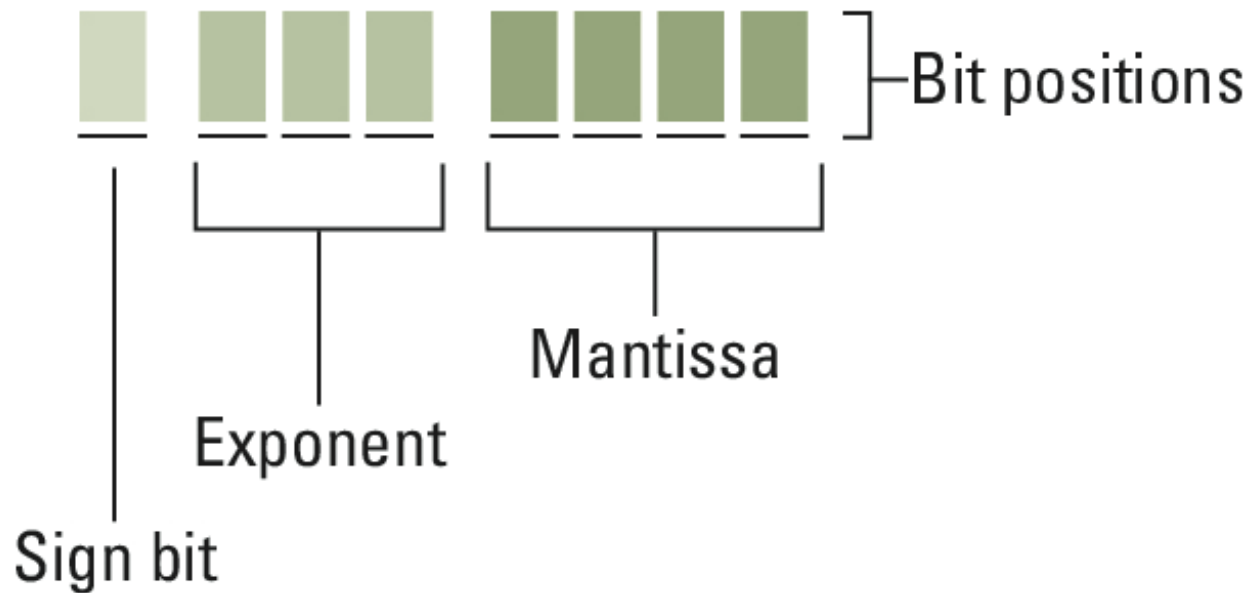
An excess notation system using bit patterns of length three

Bit pattern	Value represented
111	3
110	2
101	1
100	0
011	-1
010	-2
001	-3
000	-4

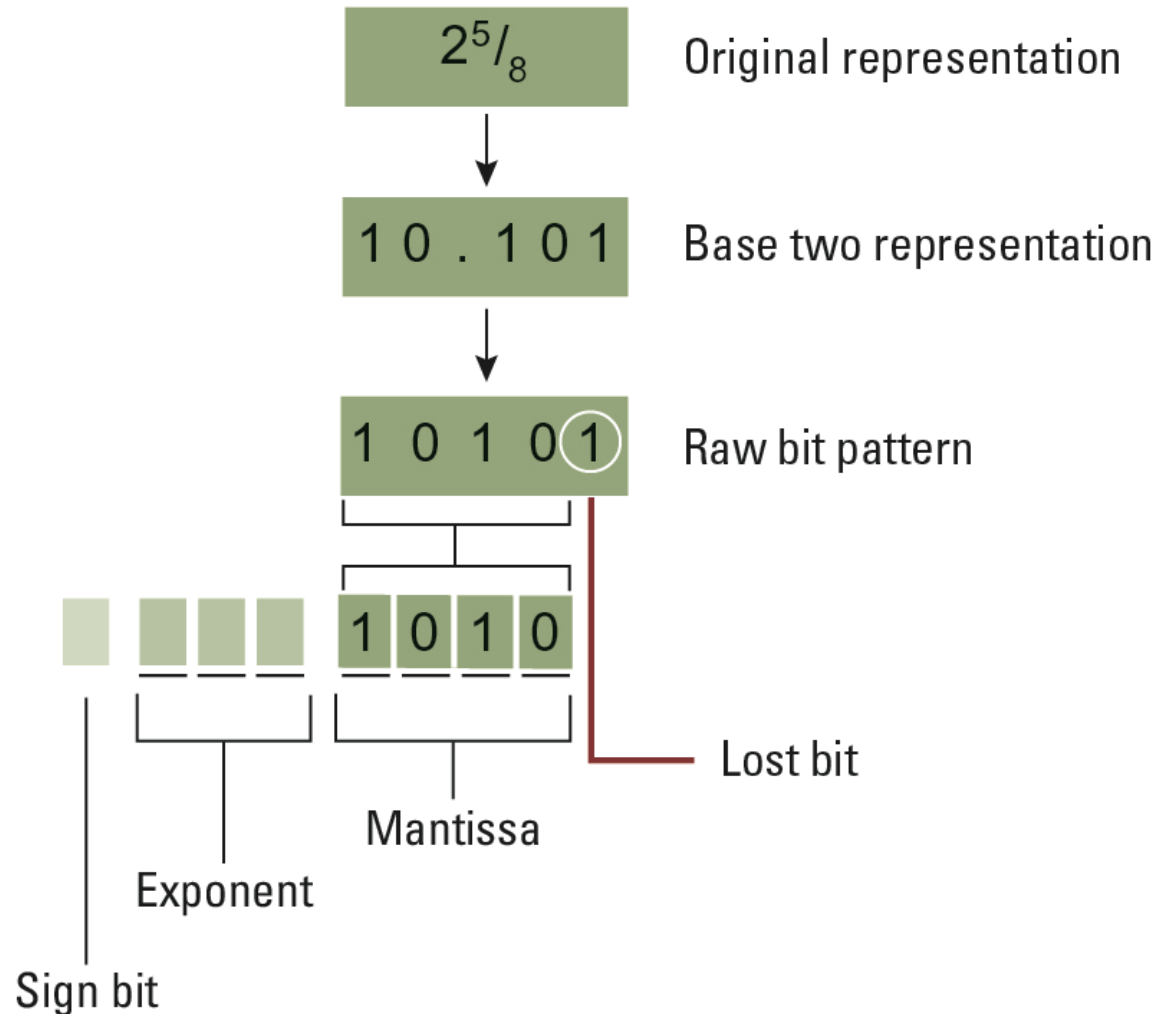
Storing Fractions

- **Floating-point Notation:** Consists of a sign bit, a mantissa field, and an exponent field.
 - Normalized form: fill the mantissa starting with the left-most 1

Floating-point notation components



Encoding the value $2 \frac{5}{8}$



Truncation (Round-off) Errors

- Occur when part of the value being stored is lost because the mantissa is not large enough
- Non-terminating expansions of fractions
 - This happens more often with binary notation
 - The value of one-tenth cannot be stored exactly in binary notation
 - Often these values are converted to integers

Numerical Analysis

- The study of dealing with problems when computing large values that require significant accuracy
- The order in which values are added can lead to two different results
- Adding very small values to very large values can result in errors