

Subject 1 - Student 1.

$$b_7 = 16$$

$$x = 1257A9_{(16)}$$

$$y = 350F6_{(16)}$$

The addition of the two numbers is performed starting with the units digit (with index 0), from right to left, the process being repetitive with a number of $\max(m, n) + 1$ iteration (m, n - number of digits - 1)

At each iterations, the digits (after they have been converted to decimal) from the homologous positions and the carry digit (0 or 1) from the previous iteration are added.

The sum provides 2 digits:

- the transport figure used in the next iteration is the quotient of dividing the sum by base.
- the positionally corresponding figure in number C is the remainder of dividing the sum by base

$$1257A9_{(16)} + 350F6_{(16)} = ?_{(16)}$$

$$m=6$$

$$n=5$$

$$\begin{array}{r} 000^{\wedge}00 \\ 1257A9_{(16)} + \\ 0350F6_{(16)} \\ \hline 15A89F_{(16)} \end{array}$$

$$i=0 \quad x_0=0$$

$$9_{(16)} + 6_{(16)} + 0_{(16)} = 9 + 6 + 0 = 15_{(16)}$$

$$x_1 = \lfloor 15/16 \rfloor = 0$$

$$c'_0 = 15 - 0 \cdot 16 = 15 \Rightarrow c_0 = F_{(16)}$$

$$i=1 : x_1 = 0$$

~~$$A(16) + F(16) = 10 + 15 + 0 = 25$$~~

$$A(16) + F(16) + Q(16) = 10 + 15 + 0 = 25$$

$$x_2 = \lfloor 25/16 \rfloor = 1, \quad C'_1 = 25 - 1 \cdot 16 = 9$$

$$C_1 = 9(16)$$

$$i=2 : x_2 = 1$$

$$T(16) + Q(16) + 1(16) = 7 + 0 + 1 = 8$$

$$x_3 = \lfloor 8/16 \rfloor = 0, \quad C'_2 = 8 - 0 \cdot 16 = 8$$

$$C_2 = 8(16)$$

$$i=3 : x_3 = 0$$

$$S(16) + S(16) + Q(16) = 5 + 5 + 0 = 10$$

$$x_4 = \lfloor 10/16 \rfloor = 0, \quad C'_3 = 10 - 0 \cdot 16 = 10$$

$$C_3 = 10(16)$$

$$i=4 : x_4 = 0$$

$$2(16) + 3(16) + Q(16) = 2 + 3 + 0 = 5$$

$$x_5 = \lfloor 5/16 \rfloor = 0, \quad C'_4 = 5 - 0 \cdot 16 = 5$$

$$C_4 = 5(16)$$

$$i=5 : x_5 = 0$$

$$1(16) + Q(16) + Q(16) = 1 + 0 + 0 = 1$$

$$x_6 = \lfloor 1/16 \rfloor = 0, \quad C'_5 = 1 - 0 \cdot 16 = 1$$

$$C_5 = 1(16)$$

$$\Rightarrow \boxed{D = 15A897(16)}$$

$$b_2 = 8$$

$$a = 135246_8$$

$$L = 5_8$$

The multiplication is performed starting with the units digit (with index 0), from right to left, the process being repetitive with a number of $m+1$ iterations.

At each iteration, the current digit a_i is multiplied by b , after they have been converted to decimal, and the carry digit from the previous iteration is added.

The calculated value provides 2 digits:

- the transport figure used in the next iteration is the quotient of dividing the calculated value by b base;
- the positionally corresponding figure in number C is the remainder of the division of the calculated value by b base.

$$135246_8 * 5_8 = ?_8$$

$$m=6.$$

$$i=0 : x_0=0.$$

$$\begin{array}{r} 135246_8 \cdot 5_8 \\ \hline 722476_8 \end{array}$$

$$6_8 \cdot 5_8 + 0_8 = 6 \cdot 5 + 0 = 30.$$

$$x_1 = \lfloor 30/8 \rfloor = 3, C_0 = 30 - 3 \cdot 8 = 30 - 24 = 6$$

$$C_0 = 6_8$$

$$i=1 : x_1=3$$

$$4_8 \cdot 5_8 + 3_8 = 4 \cdot 5 + 3 = 23$$

$$x_2 = \lfloor 23/8 \rfloor = 2, C_1 = 23 - 2 \cdot 8 = 23 - 16 = 7$$

$$C_1 = 7_8$$

$$i=2 : x_2=2$$

$$2_8 \cdot 5_8 + 7_8 = 2 \cdot 5 + 7 = 12 \Rightarrow x_3 = \lfloor 12/8 \rfloor = 1$$

$$C_2 = 12 - 8 \cdot 1 = 12 - 8 = 4$$

$$C_2 = 4_8$$

$$i=3 : t_3 = 1.$$

$$5(0) \cdot 5(0) + 1(0) = 5 \cdot 5 + 1 = 26.$$

$$t_4 = \lfloor 26/8 \rfloor = 3 \quad c'_3 = 26 - 8 \cdot 3 = 26 - 24 = 2$$

$$c_3 = 2(0)$$

$$i=4 : t_4 = 3$$

$$3(0) \cdot 5(0) + 3(0) = 3 \cdot 5 + 3 = 18.$$

$$t_5 = \lfloor 18/8 \rfloor = 2 \quad c'_4 = 18 - 8 \cdot 2 = 18 - 16 = 2.$$

$$c_4 = 2(0)$$

$$i=5 : t_5 = 2$$

$$1(0) \cdot 5(0) + 2(0) = 1 \cdot 5 + 2 = 7$$

$$t_6 = \lfloor 7/8 \rfloor = 0 \quad c'_5 = 7 - 8 \cdot 0 = 7.$$

$$c_5 = 7(0)$$

$$\Rightarrow \boxed{n = 722 \ 476(0)}$$