

Ath Magical No.

Q Given an integer A, B & C
find Ath magical no.

Magical no.: Divisible by B or C or Both.

Eg A=8, B=2, C=3

~~1~~, 2, 3, 4, ~~5~~, 6, ~~7~~, 8, 9, 10, ~~11~~, 12, ~~13~~
1 2 3 4 5 6 7 8
↓

Solⁿ > Brute Force

⇒ Iterate from 1 till you find the Ath magical no.

Code

```
int findAthMagicalNo(A, B, C) {
```

```
    count = 0;
```

```

int i = 1;
while (count < A) {
    if ((i % B == 0) || (i % C == 0)) {
        count++;
    }
    i++;
}
return i;

```

$$T.C. = O(\min(B, C) \times A)$$

$$\underline{A=8}, \quad B=2, \quad C=3$$

8th no. divisible by 2 $\Rightarrow 2, 4, 6, 8, \dots$ $\underline{8 \times 2}$

8th no. divisible by 3 $\Rightarrow 3, 6, 9, \dots$ 8×3

$$\textcircled{A=8} \quad B=2, \quad C=\cancel{2}^3$$

1st multiple of 2(6)
 ↑
 $\underline{16}$

2 $\Rightarrow 2, 4, 6, 8, 10, 12, 14, \underline{16}$

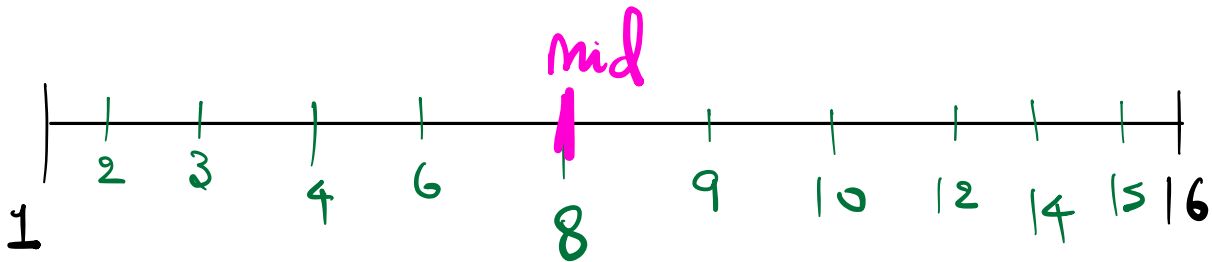
20 $\Rightarrow 20, 40, 60, \dots$ 160

$$\text{Ans} \Rightarrow \underline{1, \min(B, C) \times A}$$

↓ Optimise

Answer space ??

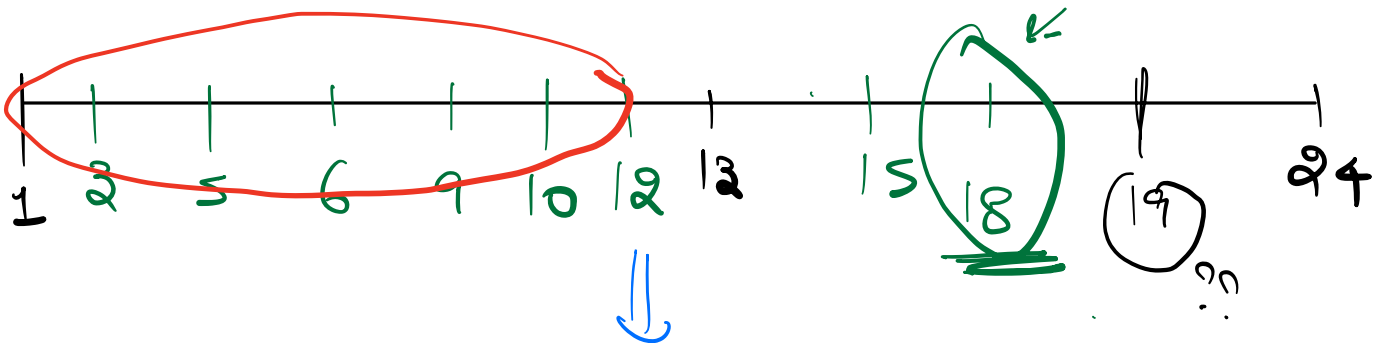
$$A=8, B=2, C=3$$



↓
Count of rigid nos ≤ 8

$$\underline{\underline{(5)}} = \textcircled{A}$$

$$\underline{A=8}, \underline{B=3}, C=5$$



↓
6 Rigid no ≤ 12

Q ^{Given B & C} Count of magical no's from [1 to X]

$$X = 50, \quad B = 2, \quad C = 5$$

Count of no's divisible by 2 or 5 or both from 1 to 50.

1) Count of no's divisible by 2 from 1 to 50 $\Rightarrow 25 \Rightarrow 50/2$

2) Count of no's divisible by 5 from 1 to 50 $\Rightarrow 10 \Rightarrow 50/5$

2 \Rightarrow 2, 4, 6, 8, 10, 12, 14, 16, 18, 20, 22, 24, 26, 28, 30, 32, 34, 36, 38, 40, 42, 44, 46, 48, 50

5 \Rightarrow 5, 10, 15, 20, 25, 30, 35, 40, 45, 50

$$\text{Ans} = \frac{X}{B} + \frac{X}{C} - \text{Duplicate} \quad ??$$

$$X = 24 \quad B = 6, \quad C = 4$$

$$[1, 24]$$

$$12 \rightarrow \underline{\underline{LCM(6, 4)}}$$

$$4, 6, 8, 12, 16, 18, 20, 24 \Rightarrow 8$$

$$\rightarrow \text{Multiples of } 12 \Rightarrow \underline{\underline{B \times C}}$$

$$6 \Rightarrow 24 / 6 = 4 \quad 6 \times 4 = 24$$

$$4 \Rightarrow 24 / 4 = 6$$

- Duplicates (2)

Count of no's
divisible by B
or C or both for
[1, X]

$$\Rightarrow \frac{X}{B} + \frac{X}{C} - \frac{X}{\text{lcm}(B, C)}$$

Code

```
int AthMejicalNo (A, B, C) {
    int x = lcm(B, C);
    S = 1;
    e = min(B, C) * A;
```

while ($s \leq e$) {

mid = $s + (e - s) / 2$;

count = $(\text{mid} / B + \text{mid} / C - \text{mid} / \underline{\underline{X}})$;

if (count == A) {

if ($\text{mid} \% B == 0$ // $\text{mid} \% C == 0$) {

return mid;

} else { // Go to L

e = mid - 1;

}

} else if (count > A) { // Go to L

e = mid - 1;

} else { // Go to R

s = mid + 1;

}

}

}

$$T.C. = O(\log(\min(B, C) \times A))$$

$$LCM(A, B) = \frac{A \times B}{GCD(A, B)}$$



$$\log(\min(A, B))$$

Painter's partition

Given N Boards with their lengths.

$$A = [L_0, L_1, L_2, L_3, \dots, L_{N-1}]$$

Given K painters \nsubseteq Each painter takes
1 unit of time to paint 1 unit length
of board.

Board (Length = 4) \Rightarrow 4 units of times

Calculate the min amount of time in which
all the boards can be painted.

Constr: 1) Two painters cannot share a board
to paint.

2) A painter will only paint
contiguous boards.

P_1 P_2

$[B_1, B_2, B_3, \cancel{B_4}, B_5, B_6]$
 $\quad P_1 \quad P_2 \quad \quad \cancel{P_1}$



Eg $N=15$, $K=3$
 (# Boards) (# Painters)

$$A = \begin{bmatrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 & 13 & 14 \\ 3, 5, 1, 7, 8, 2, 5, 3, 10, 1, 4, 7, 5, 4, 6 \\ 31 & 25 & 15 \end{bmatrix}$$

$$A = \begin{bmatrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 & 13 & 14 \\ 3, 5, 1, 7, 8, 2, 5, 3, 10, 1, 4, 7, 5, 4, 6 \\ 26 & 23 & 22 \end{bmatrix}$$

$$A = \begin{bmatrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 & 13 & 14 \\ 3, 5, 1, 7, 8, 2, 5, 3, 10, 1, 4, 7, 5, 4, 6 \\ 24 & 25 & 22 \end{bmatrix}$$

Eg $A = [10, 20, 30, 40]$ $K=2$

P_1	P_2
10 (10)	20, 30, 40 (90) \Rightarrow 90
10, 20 (30)	30, 40 (70) \Rightarrow 70
10, 20, 30 (60)	40 (40) \Rightarrow 60

Solⁿ \Rightarrow Greedy

$$\frac{(\text{Sum of all lengths})}{(\# \text{ painters})}$$

$$A = [1, 2, 3, 4, 100] \quad K = 2$$

~~$$\text{Sum} = \frac{110}{2} = \underline{\underline{55}} \quad ??$$~~

Min amount of Time = Max length of a board.

Max amount of Time = Sum of lengths of all boards.
(# painters = 1)

[max Length, Sum of all length]

$$K = 4$$

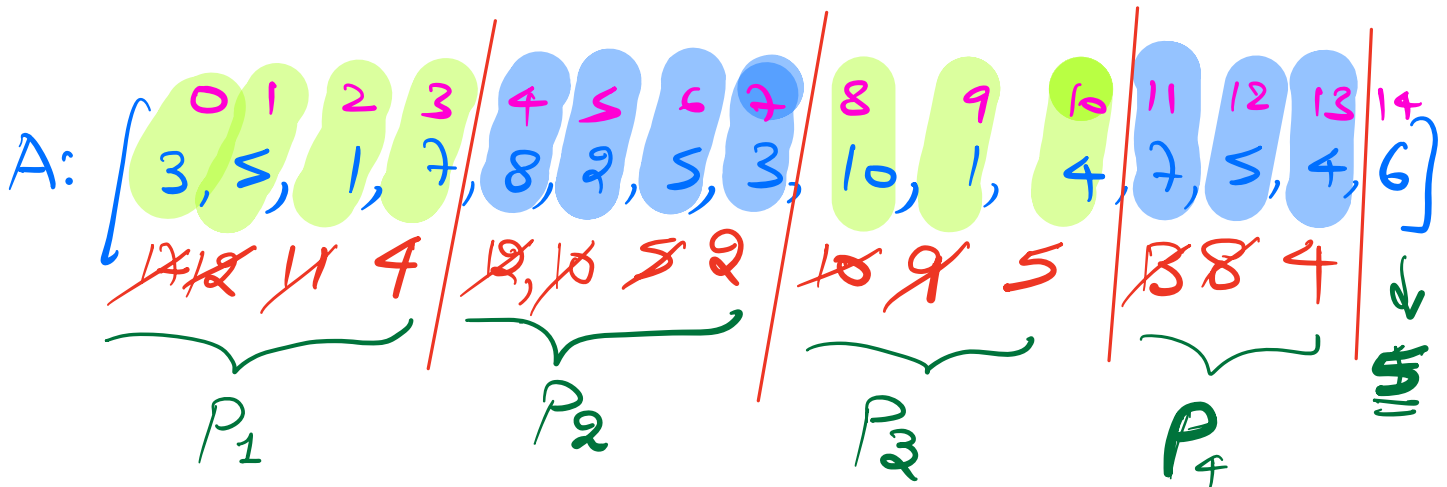
$$A: \overset{0}{3}, \overset{1}{5}, \overset{2}{1}, \overset{3}{7}, \overset{4}{8}, \overset{5}{2}, \overset{6}{5}, \overset{7}{3}, \overset{8}{10}, \overset{9}{1}, \overset{10}{4}, \overset{11}{7}, \overset{12}{5}, \overset{13}{4}, \overset{14}{6}]$$

$$\text{Min} = 10$$

$$Max = 71$$

$$Time = 20 \text{ units}$$

Is it possible to paint all the boards in 20 units of time with 4 painters??



Code

bool check (A, T, K) {

curr_time = T;

count = 1;

for (i = 0; i < N; i++) {

if (A[i] > curr_time) {

curr_time += A[i];

} else {

count++;
curr-time = T;

if (count > K) &
return false;

return true;

K = 4

A: $\int \begin{array}{c} 0 \ 1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7 \ 8 \ 9 \ 10 \ 11 \ 12 \ 13 \ 14 \\ 3, 5, 1, 7, 8, 2, 5, 3, 10, 1, 4, 7, 5, 4, 6 \end{array}$

$\underbrace{\hspace{1.5cm}}_{P_1} \quad \underbrace{\hspace{1.5cm}}_{P_2} \quad \underbrace{\hspace{1.5cm}}_{P_3} \quad \underbrace{\hspace{1.5cm}}_{P_4} \quad \underbrace{\hspace{1.5cm}}_{\cancel{P_5}}$

Min = 10
Max = 71

s	e	mid	
10	71	40	$\Rightarrow \text{check}(A, 40, 4) \Rightarrow \text{True}$ $\text{check}(A, 39, 4) \Rightarrow \text{True}$
10	39	24	$\Rightarrow \text{check}(A, 24, 4) \Rightarrow \text{True}$ $\text{check}(A, 23, 4) \Rightarrow \text{True}$
10	23	16	$\Rightarrow \text{check}(A, 16, 4) \Rightarrow \text{false}$
17	23	20	$\Rightarrow \text{check}(A, 20, 4) \Rightarrow \text{false}$
21	23	22	$\Rightarrow \text{check}(A, 22, 4) \Rightarrow \text{True}$ $\text{check}(A, 21, 4) \Rightarrow \text{false}$

Ans

Code

```
int minTime (A, K) {
```

```
    s = max(A[i]);
```

```
    e = Σ(A[i]);
```

```
    while (s <= e) {
```

```
        mid = s + (e - s) / 2;
```

```
        if (check(A, mid, K)) {
```

```
            if (check(A, mid - 1, K)) {
```

```
                e = mid - 1;
```

```
            } else {
```

```
                return mid;
```

```
            }
```

```
        } else {
```

```
            s = mid + 1;
```

```
        }
```

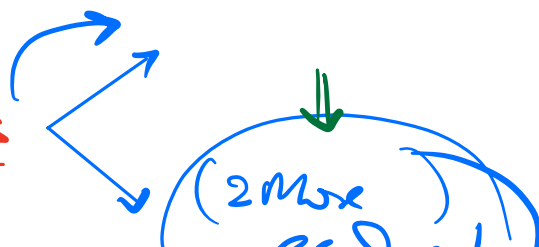
```
    }
```

```
}
```

T.C. = $O(\log(\text{Range of answer}) \times N)$

T.C. = $\log(\Sigma(A[i]) - \text{Max}(A[i])) \times N$;

1 Ques \Rightarrow Aggressive Cows





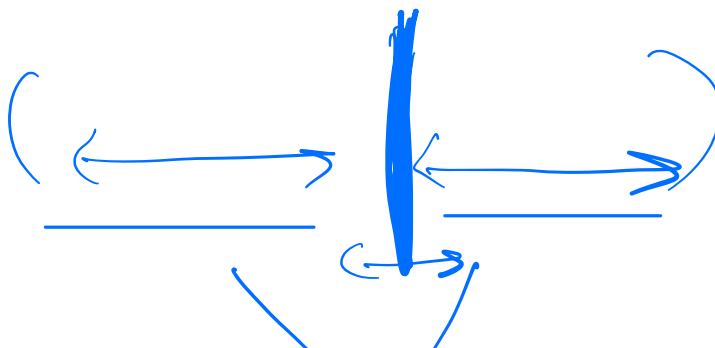
Q2nd
 \Downarrow
2nd Night
10 days X

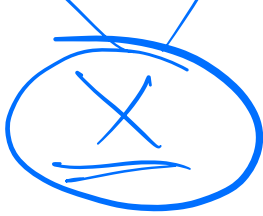
Holiday \Rightarrow 5 Ass. Quesⁿ
Non Holiday \Rightarrow Attend 2 Ass. Ques.

Yes \Rightarrow
 \Downarrow

Sat & Sunday (23 & 24) \Rightarrow R2 C2

3 loop





$1 \leq A[i] \leq 10^8$ > Triplet

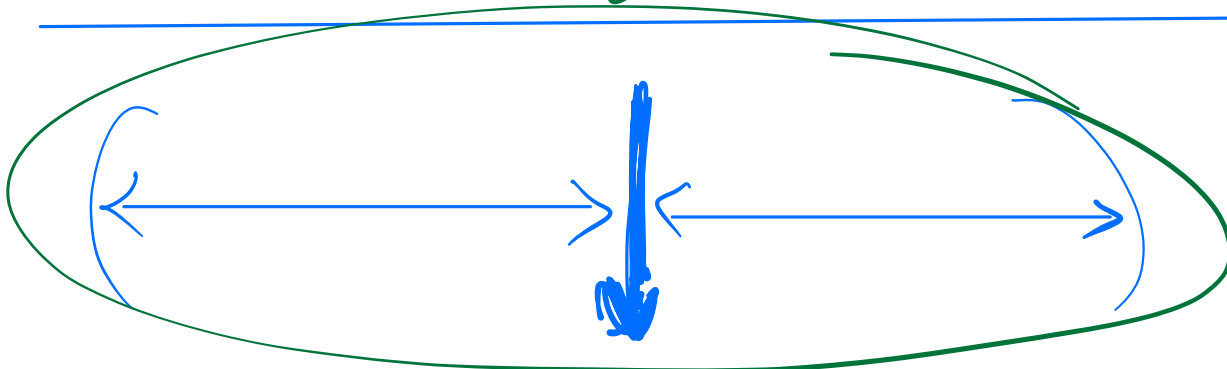
3×10^8

$[1, 3 \times 10^8] \Rightarrow$ mid

\Downarrow
BT
 \Downarrow $O(N^3)$

\Downarrow
Count of Triplets where
 $sum \leq$ mid

\swarrow $< B$
Go to Right
 \searrow B
 \nearrow $> B$
Left



2 pointer \rightarrow $O(N^2)$

