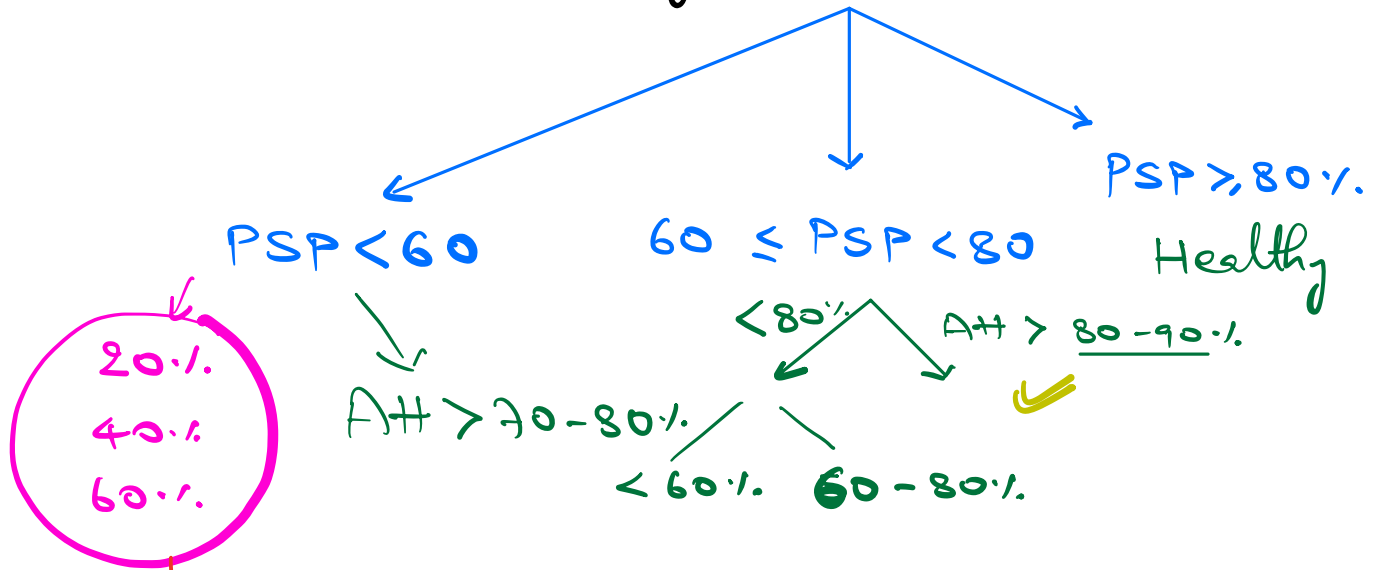


Average PSP \Rightarrow $> 75\%$.



Just attending the class is not enough.

Assignment \leftarrow

Additional

\Downarrow
Solution \checkmark
Pseudo Code \checkmark

\Downarrow
Easy \Rightarrow — mins
Medium \Rightarrow — mins
Hard \Rightarrow — mins } Improve this day by day.

Sorting

Arrangement of data in a specific order based on some parameter

\swarrow Ascending \searrow Descending.

$A = \langle 2, 3, 9, 12, 17, 19 \rangle$

↓
Sorted in Asc. based on value of elements

$A = \langle 19, 17, 12, 9, 3, 2 \rangle$

↓
Sorted in Desc. based on value of elements

$A = \langle 1, 13, 9, 6, 12 \rangle$

Count of factors = $\langle 1, 2, 3, 4, 6 \rangle$ ↗ Sorted on the basis of no. of factors.

Q Why is sorting important??

Q Given an integer array of size N .
Remove all elements one by one.

Cost of removing an element = Sum of values of all elements present in the array before removing the element.

Find min cost of removing all elements.

$$A = \langle 2^0, 1^1, 4^2 \rangle$$

Approach 1

$$\begin{array}{lcl} 2 & \Rightarrow & 7 \Rightarrow \langle 1, 4 \rangle \\ 1 & \Rightarrow & 5 \Rightarrow \langle 4 \rangle \\ 4 & \Rightarrow & 4 \Rightarrow \langle \rangle \\ \hline & & 16 \end{array}$$

Approach 2

$$\begin{array}{lcl} 4 & \Rightarrow & 7 \Rightarrow \langle 2, 1 \rangle \\ 2 & \Rightarrow & 3 \Rightarrow \langle 1 \rangle \\ 1 & \Rightarrow & 1 \Rightarrow \langle \rangle \\ \hline & & 11 \end{array}$$

② Min cost to remove all ele. from
 $\langle 4, 6, 1 \rangle$

$$\begin{array}{lcl} 6 & \Rightarrow & 11 \Rightarrow \langle 4, 1 \rangle \\ 4 & \Rightarrow & 5 \Rightarrow \langle 1 \rangle \\ 1 & \Rightarrow & 1 \Rightarrow \langle \rangle \\ \hline & & 17 \end{array}$$

② Min cost to remove all ele. from

$$\langle 3, 5, 1, -3 \rangle$$

$$\begin{array}{lcl} 5 & \Rightarrow & 6 \Rightarrow \langle 3, 1, -3 \rangle \\ 3 & \Rightarrow & 1 \Rightarrow \langle 1, -3 \rangle \\ 1 & \Rightarrow & -2 \Rightarrow \langle -3 \rangle \\ -3 & \Rightarrow & -3 \Rightarrow \langle \rangle \end{array}$$

2

Approach

$A = [a, b, c, d]$

$\xrightarrow{\hspace{2cm}}$

	Cost	Array
Remove a	$a + b + c + d$	$[b, c, d]$
Remove b	$b + c + d$	$[c, d]$
Remove c	$c + d$	$[d]$
Remove d	d	$[\]$

Total cost : $a + 2 \times b + 3 \times c + 4 \times d.$

$\begin{matrix} \uparrow & \uparrow & \uparrow & \dots \end{matrix}$
 $\begin{matrix} \text{Max} & \text{2nd} & \text{3rd} & \end{matrix}$
 $\begin{matrix} & \text{Mex} & \text{Mex} & \end{matrix}$

\Downarrow
Remove the elements in descending order.

1) Sort the element in descending order. ??

ans = 0;

for ($i=0$; $i < N$; $i++$) & // $O(N)$
 $\text{ans} = \text{ans} + (i+1) \times A[i];$

}

return ans;

$$\begin{aligned} \text{T.C.} &= O(N \log N + N); \\ &= O(N \log N) \end{aligned}$$

$$\text{S.C.} = \underline{\hspace{2cm}}$$

Q Given an integer array of size N .
Find the count of Noble integers
in the array. (All elements are distinct)

Noble integer \rightarrow $\text{arr}[i]$ is a noble integer
if the count of elements
less than $\text{arr}[i]$ is equal
to $\text{arr}[i]$ itself.

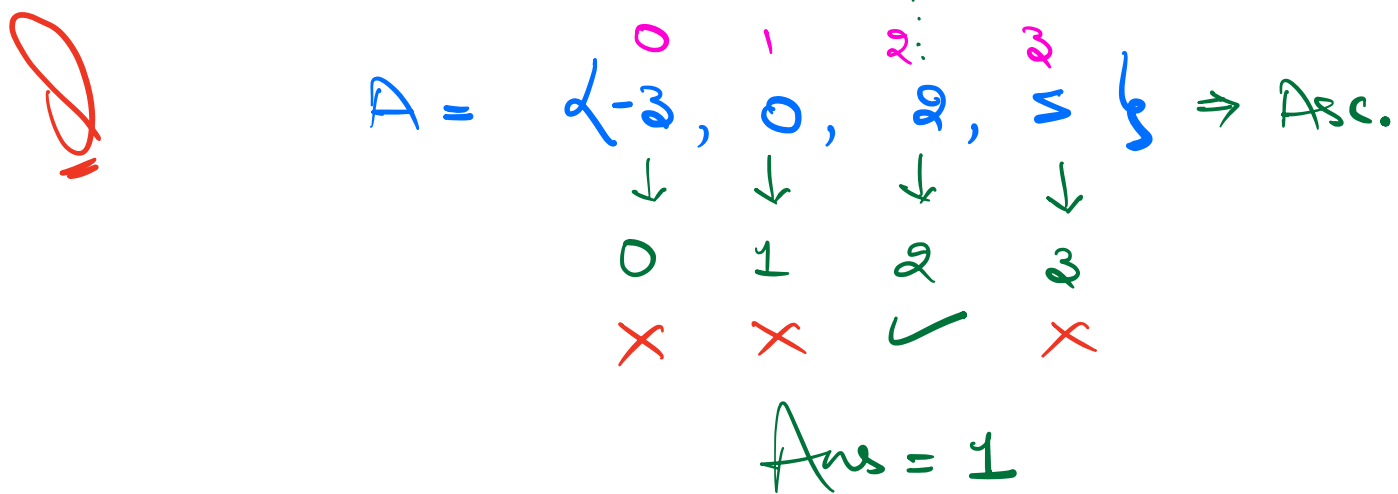
	0	1	2	3	4	5
$A =$	1	-5	3	5	-10	4
	↓	↓	↓	↓	↓	↓
	2	1	3	5	0	4
	X	X	✓	✓	X	✓

Count of
no. smaller
than $\text{arr}[i]$.

$$\text{Ans} = \underline{\underline{3}}$$

NOTE: -ve elements can never be noble integers

as count can never be negative.



Solⁿ \Rightarrow Brute force

\Rightarrow \forall element \Rightarrow Iterate & find the count of smaller elements.

Code

```
ans = 0;
for (i = 0; i < N; i++) {
    count = 0;
    for (j = 0; j < N; j++) {
        if (A[j] < A[i]) {
            count++;
        }
        if (count == A[i]) { ans++; }
    }
}
```

Find the count of elements smaller than $A[i]$.

return ans;

$$T.C. = O(N^2)$$

$$S.C. = O(1)$$

2) Optimise

Goal: Count of elements on left of any element on index i .

$A = \langle \overset{0}{1}, \overset{1}{-5}, \overset{2}{3}, \overset{3}{5}, \overset{4}{-10}, \overset{5}{4} \rangle$

$SA = \langle \overset{0}{-10}, \overset{1}{-5}, \overset{2}{1}, \overset{3}{3}, \overset{4}{4}, \overset{5}{5} \rangle$

↓ ↓ ↓ ↓ ↓ ↓

0 1 2 3 4 5

for any element on index i

⇒ Count of element from $[0, i-1]$

$$= \underline{i}$$

⇓
 $\forall i$ if $(A[i] == i) \Rightarrow$ Noble Integer

$$T.C. = O(N \log N)$$

Q Given an integer array of size N .
Find the count of Noble Integers.

$$A = \{ \overset{0}{0}, \overset{1}{1}, \overset{2}{1}, \overset{3}{2}, \overset{4}{4}, \overset{5}{4} \}$$

Quiz

$$A = \{ \overset{0}{-10}, \overset{1}{1}, \overset{2}{1}, \overset{3}{3}, \overset{4}{100} \}$$

$\uparrow \quad \uparrow \quad \uparrow \quad \uparrow \quad \uparrow$
 0 1 1 3 4

Quiz

$$A = \{ \overset{0}{-10}, \overset{1}{1}, \overset{2}{1}, \overset{3}{2}, \overset{4}{4}, \overset{5}{4}, \overset{6}{4}, \overset{7}{8}, \overset{8}{10} \}$$

Count \rightarrow

0 1 1 3 4 4 4 7 8
 ✓ ✓ ✓ ✓ ✓

Code

```

int findNobelIntegers ( A[], N ) {
    int ans = 0;
    sort (A);
    int count = 0;
    if (A[0] == 0) { ans++; }

    for (i = 1; i < N; i++) {
        if (A[i] != A[i-1]) {
            count = i;
        }
    }
}

```


if (count == A[i]) {
 ans++;

}

}

return ans;

}

T.C. = $O(N \log N)$

S.C. =

Sorting

⇒ Inbuilt sorting functions.

Java ⇒ `collections.sort(ArrayList);`
`Arrays.sort(Array);`

C++ ⇒ `sort(a.begin(), a.end());`

Python ⇒ `A.sort()`
`A = sorted(A)`

JS \Rightarrow A.sort()

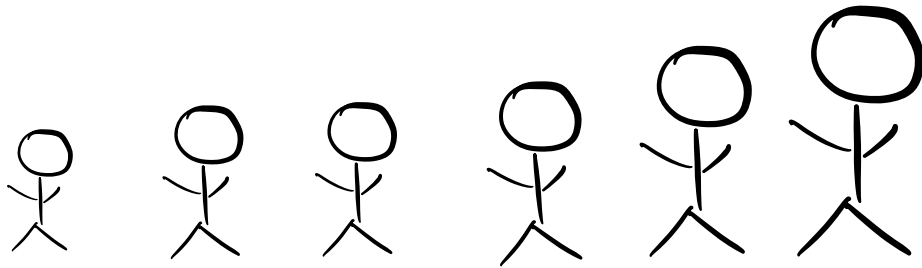
$$\begin{aligned} \text{T.C.} &= O(N \log N) \\ \text{S.C.} &= O(\log N) \end{aligned}$$

H.W. \Rightarrow figure out function call to sort the array in decreasing order.

Selection

Sort

Scenario



Code

```
void selectionSort ( A[], N) {
```

```
    end = N-1;
```

```
    for (j = 0; j < N-1; j++) { // (N-1) times
```

```
        maxEle = INT_MIN
```

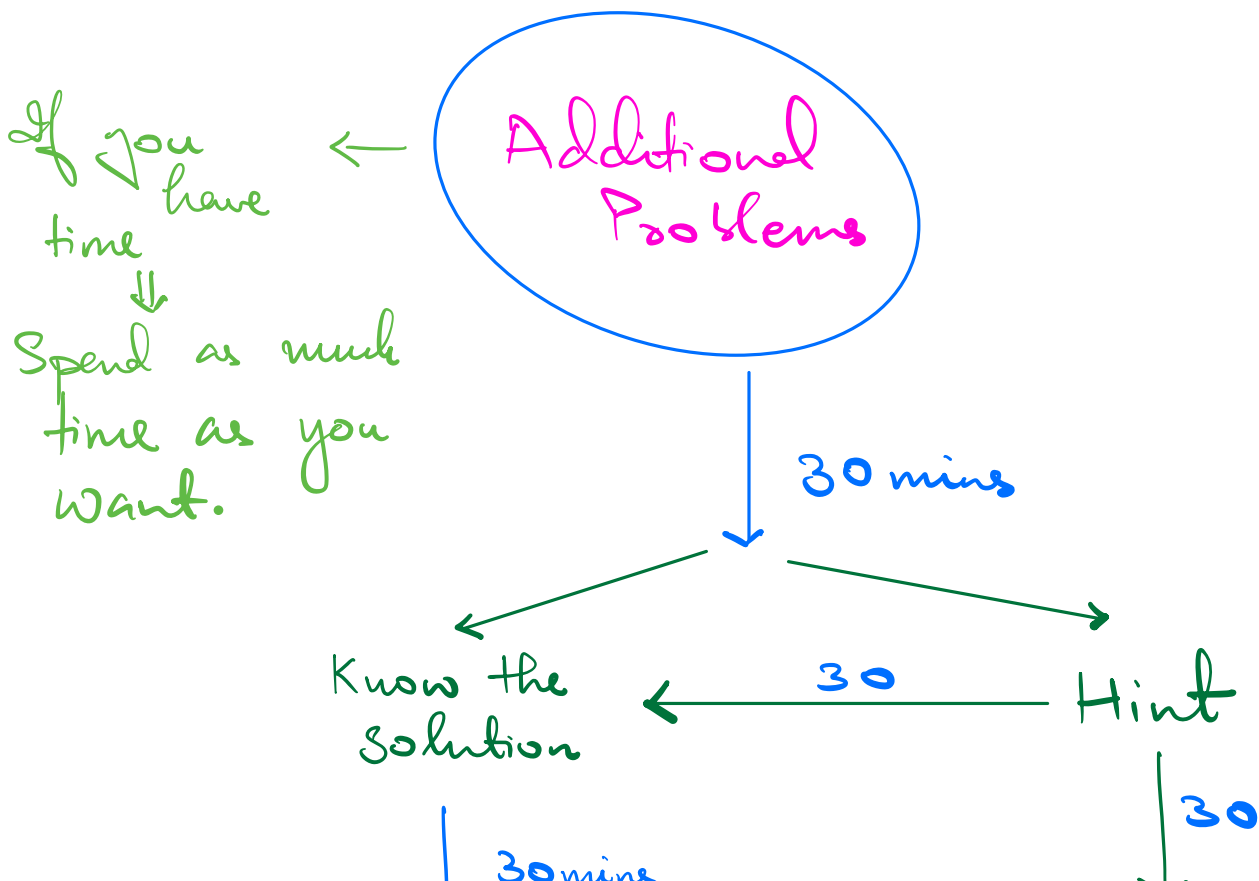
```
        max_index = -1;
```

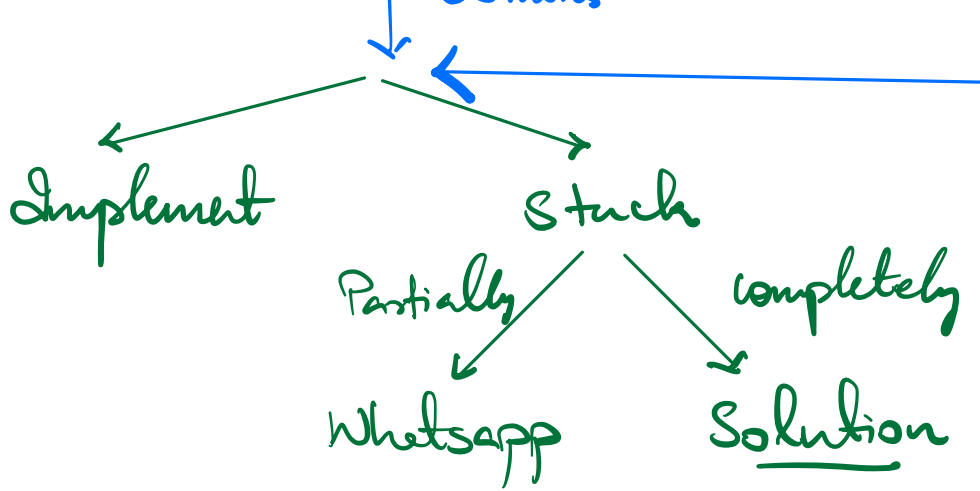
```
for (i = 0; i ≤ end; i++) {
```

```
    if (A[i] > maxEle) {  
        maxEle = A[i];  
        max_index = i;  
    }
```

```
    swap(A, max_index, end);  
    end--;
```

T.C. = $O(N^2)$
S.C. = $O(1)$





Complete Solution/
Video Explanation