```
if ((partitionPoints.getLeft() - leftPointer) < (rightPointer - partitionPoints.getRight())) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             private static void QuickSort1(int[] a, int leftPointer, int rightPointer, int cutoff, Random r)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              QuickSort1(a, partitionPoints.getRight(), rightPointer, cutoff, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               pair partitionPoints = outsideIn(a, leftPointer, rightPointer, pivot);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      QuickSort1(a, leftPointer, partitionPoints.getLeft(), cutoff, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int pivot = r.nextInt(rightPointer - leftPointer) + leftPointer;
                                                                                                                     @description this file includes ArraySorts which have all the code for
                                                                                                                                                                                it incluedes the Pair class which was ued in some of the sorts
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               public static void AlmostQS1(int[] a, int n, int cutoff) {
                                                                                                                                                                                                                                                                                                                                    public static void QuickSort1(int[] a, int n, int cutoff)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             while (rightPointer - leftPointer >= (cutoff - 1)) {
                                                                                                                                                                                                                                                                                                                                                                                          //handle the situation if cutoff of 0 is passed in
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           //handle the situation if cutoff of 0 is passed in
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          //and change the pointer to simulate the other
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    leftPointer = partitionPoints.getRight();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           rightPointer = partitionPoints.getLeft();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             //recursively sort the smaller partition
                                                                                                                                                                                                                                                                                                     '*********QuickSort1****************
                                                                                                                                                   the diffrent sorting algorithms in addition
                                                                                                                                                                                                                                                                                                                                                                                                                         cutoff = (cutoff < 2) ? 2 : cutoff;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      cutoff = (cutoff < 2) ? 2 : cutoff;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     QuickSort1(a, 0, n - 1, cutoff, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                       QuickSort1(a, 0, n - 1, cutoff, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        //choose random pivot in range
                            @class COMP 282 meeting at 2:00 PM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Random r = new Random();
                                                                                                                                                                                                                                                                                                                                                                  Random r = new Random();
(dauthor Bishoy A Abdelmalik
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   //insertionSort(a,n);
                                                                                         @DateTurnedIn Nov 20, 2019
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      insertionSort(a, n);
                                                            (AAssigment Program #3
                                                                                                                                                                                                                                        10 import java.util.Random;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   //partition
                                                                                                                                                                                                                                                                          11 class ArraySorts {
                                                                                                                                                                                                                                                                                                                                                                                                                            16
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private static void QuickSort2(int[] a, int leftPointer, int rightPointer, int cutoff, Random r)
while (rightPointer - leftPointer >= (cutoff - 1)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (((partitionPoints - 1) - leftPointer) < (rightPointer - (partitionPoints + 1)))</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int partitionPoints = leftToRight1Pivot(a, leftPointer, rightPointer, pivot);
                                                                                                                                                                                                                                                                                                                                                                                                                                                       int pivot = r.nextInt(rightPointer - leftPointer;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     QuickSort2(a, partitionPoints + 1, rightPointer, cutoff, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           QuickSort2(a, leftPointer, partitionPoints - 1, cutoff, r);
                                                                         public static void QuickSort2(int[] a, int n, int cutoff) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         public static void QuickSort3(int[] a, int n, int cutoff) {
                                                                                                                                                                                                                          public static void AlmostQS2(int[] a, int n, int cutoff)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          //and change the pointer to simulate the other
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 /**********End QuickSort2*************
                      **********End QuickSort1**************
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   //recursively sort the smaller partition
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rightPointer = partitionPoints - 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    leftPointer = partitionPoints + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                /***********Ouicksort3***************/
                                                '*********Qu1ckSort2**************
                                                                                                                                                                                                                                                                            cutoff = (cutoff < 2) ? 2 : cutoff;
                                                                                                                       cutoff = (cutoff < 2) ? 2 : cutoff;</pre>
                                                                                                                                                  QuickSort2(a, 0, n - 1, cutoff, r);
                                                                                                                                                                                                                                                                                                      QuickSort2(a, 0, n - 1, cutoff, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                 //choose random pivot in range
                                                                                                                                                                                                                                                   Random r = new Random();
                                                                                                 Random r = new Random()
                                                                                                                                                                                                                                                                                                                               //insertionSort(a,n);
                                                                                                                                                                          insertionSort(a, n);
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int sizeOfMiddlePartition = (partitionPoints.getRight() - 1) - (partitionPoints.getLeft() + 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         QuickSort3(a, partitionPoints.getLeft() + 1, partitionPoints.getRight() - 1, cutoff, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               QuickSort3(a, partitionPoints.getLeft() + 1, partitionPoints.getRight() - 1, cutoff, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    else if (sizeOfLessThan > sizeOfGreaterThan && sizeOfLessThan > sizeOfMiddlePartition)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        private static void QuickSort3(int[] a, int leftPointer, int rightPointer, int cutoff, Random r)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (sizeOfGreaterThan > sizeOfLessThan && sizeOfGreaterThan > sizeOfMiddlePartition) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // sort the smallest 2 partitions recursively and simulate the third call with a loop
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 while (rightPointer - leftPointer >= (cutoff - 1) && leftPointer <= rightPointer)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                QuickSort3(a, partitionPoints.getRight() + 1, rightPointer, cutoff, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    QuickSort3(a, partitionPoints.getRight() + 1, rightPointer, cutoff, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         pair partitionPoints = leftToRight2Pivot(a, leftPointer, rightPointer, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        QuickSort3(a, leftPointer, partitionPoints.getLeft() - 1, cutoff, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            QuickSort3(a, leftPointer, partitionPoints.getLeft() - 1, cutoff, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int sizeOfGreaterThan = rightPointer - (partitionPoints.getRight() + 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int sizeOfLessThan = (partitionPoints.getLeft() - 1) - leftPointer;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  leftPointer = partitionPoints.getRight() + 1;//greater than
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rightPointer = partitionPoints.getLeft() - 1;//Less than
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rightPointer = partitionPoints.getRight() - 1; //middle
                                                                                                                                                                                                                                                                                                                                   public static void AlmostQS3(int[] a, int n, int cutoff) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                leftPointer = partitionPoints.getLeft() + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // calculate the sizes of the partitions
                                             cutoff = (cutoff < 2) ? 2 : cutoff;</pre>
                                                                                                             QuickSort3(a, 0, n - 1, cutoff, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                             cutoff = (cutoff < 2) ? 2 : cutoff;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      QuickSort3(a, 0, n - 1, cutoff, r);
Random r = new Random();
                                                                                                                                                                                                                                                                                                                                                                                                Random r = new Random();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  //qreater than
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  //greater than
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                //insertionSort(a,n);
                                                                                                                                                          insertionSort(a, n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  //less than
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if ((partitionPoints.getLeft() - leftPointer) < (rightPointer - partitionPoints.right)) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (((partitionPoints - 1) - leftPointer) < (rightPointer - (partitionPoints + 1))) \{
                                                                                                                                                                                                                                                                                        private static void QuickSort4(int[] a, int leftPointer, int rightPointer, int cutoff) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              private static void QuickSort5(int[] a, int leftPointer, int rightPointer, int cutoff) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int partitionPoints = leftToRight1Pivot(a, leftPointer, rightPointer, pivot);
                                                                                                                                                                                                                                                                                                                                                                pair partitionPoints = outsideIn(a, leftPointer, rightPointer, pivot);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   QuickSort4(a, partitionPoints.getRight(), rightPointer, cutoff);
                                                                                                                                                                                                                                                                                                                                                                                                                      QuickSort4(a, leftPointer, partitionPoints.getLeft(), cutoff);
                                                                                                                               public static void QuickSort4(int[] a, int n, int cutoff) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      public static void QuickSort5(int[] a, int n, int cutoff)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        while (rightPointer - leftPointer >= (cutoff - 1)) {
                                                                                                                                                                                                                                                                                                                 while (rightPointer - leftPointer >= (cutoff - 1)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                 leftPointer = partitionPoints.getRight();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rightPointer = partitionPoints.getLeft();
                                                                            /**********End QuickSort3****************
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   /**********End QuickSort4******************
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             /**********Qu1ckSort5****************
                                                                                                    /**********Quicksortd**************/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            cutoff = (cutoff < 2) ? 2 : cutoff;</pre>
                                                                                                                                                        cutoff = (cutoff < 2) ? 2 : cutoff;
                                                                                                                                                                                QuickSort4(a, 0, n - 1, cutoff);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          QuickSort5(a, 0, n - 1, cutoff);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int pivot = 0 + leftPointer;
                                                                                                                                                                                                                                                                                                                                          int pivot = 0 + leftPointer;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   insertionSort(a, n);
                                                                                                                                                                                                          insertionSort(a, n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             159
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private static int leftToRight1Pivot(int[] a, int lastSmall, int lastIndex, int pivot)
                                                            QuickSort5(a, partitionPoints + 1, rightPointer, cutoff);
QuickSort5(a, leftPointer, partitionPoints - 1, cutoff);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      boolean pivotAndFUEqual = a[firstUnknown] == pivotValue;
                                                                                                                                                                                                                                                                                                                                                                                                                                            // if the array has a lot of values that are equal to the pivot
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // it is smaller than the pivotValue in that case swap it
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (pivotAndFUEqual && pivotDuplicate) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                pivotDuplicate = (!pivotDuplicate);
                                                                                                                                                                                                                                                                                                                  int pivotValue = a[pivot];// save pivot value
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // keep advancing the first unknown until
                                                                                                                                                                                                                                /**********End QuickSort5*************
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        //sometimes swap and sometimes don't
                                                                                 rightPointer = partitionPoints - 1;
                    leftPointer = partitionPoints + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (a[firstUnknown] > pivotValue) {
                                                                                                                                                                                                                                                                                                                                     // swap the pivot and the first element
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // it runs of the end of the array
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    while (firstUnknown <= lastIndex) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                   int firstUnknown = lastSmall + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                               boolean pivotDuplicate = false;
                                                                                                                                                                                                                                                                                                                                                                                                                        "Ia flag helps with big arrays
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (pivotAndFUEqual)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  firstUnknown++;
                                                                                                                                                                                                                                                                                                                                                         swap(a, pivot, lastSmall);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         lastSmall++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               firstUnknown++;
                                                                                                                                                                                                                                                                                                                                                                              pivot = lastSmall;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       . else .
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    199
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```
int lastSmall, firstBig, firstUnknown, smallPivot, smallPivotValue, bigPivotValue;
                                                                                                                                                                                                                                                                                                                       private static pair leftToRight2Pivot(int[] a, int firstIndex, int lastIndex, Random r)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int pivot2 = r.nextInt(lastIndex - (firstIndex + 1)) + (firstIndex + 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int pivot1 = r.nextInt(lastIndex - firstIndex) + (firstIndex);
                                                                                                                                                                                                                                                                                                                                                                                                                          //if array only has 2 elements decide which is bigger
swap(a, lastSmall, firstUnknown);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          //handle the case where the big pivot
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         //decide which pivot value is bigger
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 swap(a, firstIndex, lastIndex);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (a[firstIndex] >= a[lastIndex])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // and put it in its right place
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       smallPivotValue = a[pivot2];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   smallPivotValue = a[pivot1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          swap(a, firstIndex, smallPivot);
                                                                                                                                                                                                                                                                                                                                                                                         if ((lastIndex - firstIndex) < 2) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 bigPivotValue = a[pivot2];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     bigPivotValue = a[pivot1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (a[pivot1] > a[pivot2]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     swap(a, firstIndex, pivot1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  smallPivot = pivot1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     smallPivot = pivot2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     lastSmall = firstIndex;
                                     firstUnknown++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            bigPivot = pivot2;
                                                                                                                                                                          swap(a, pivot, lastSmall);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 bigPivot = pivot1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          firstBig = lastIndex;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                //and swap if needed
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       pivot1 = firstIndex;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              //choose the pivots
                                                                                                                                                                                                                   return lastSmall;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               else {
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if (smallPivotValue < a[firstUnknown] && a[firstUnknown] <= bigPivotValue) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (a[firstUnknown] == smallPivotValue && pivotDuplicate)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 we sometimes consider values = to pivot in middle
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       } else if (a[firstUnknown] > bigPivotValue)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                / but to handle duplicate pivot values
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        swap(a, firstUnknown, lastSmall);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (a[firstUnknown] == smallPivotValue)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 pivotDuplicate = (!pivotDuplicate);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              /the FU belong in the small part
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         swap(a, firstUnknown, firstBig);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          /the FU belong in the big part
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       in the middle
                                                                                                                                                                                                                                                                                                                                           /handle duplicate values with pivot
                                                                                                                                                                                                                                                                                                                                                                                                                                              while (firstUnknown < firstBig)</pre>
                                                                                                                                                                                                                                                                                                                                                                            / so we have unnecessary swaps
                                                                                                                                                                                                                                                                                                                                                                                                             boolean pivotDuplicate = false;
                                                                                                                                 swap(a, lastIndex, bigPivot);
                                                                                                                                                                                                                                                                                                         FirstUnknown = lastSmall + 1
// comes to the first index
                               (bigPivot == firstIndex)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   firstUnknown++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         firstUnknown++;
                                                              bigPivot = smallPivot;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      lastSmall++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      //the FU belong
                                                                                                                                                                      smallPivot = firstIndex;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          firstUnknown++;
                                                                                                                                                                                                                                                                       lastSmall = smallPivot
                                                                                                                                                                                                    bigPivot = lastIndex;
                                                                                                                                                                                                                                      firstBig = bigPivot;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            firstBig--;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               } else {
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private static pair outsideIn(int[] a, int leftPointer, int rightPointer, int pivot)
                                                                                                                                                                                                   while (leftPointer <= rightPointer) {//while the pointers didn't overlap
                                                                                                                                                                                                                                                                                                                        while (leftPointer < rightPointer && a[rightPointer] > pivotValue) {
                                                                                                                                                                                                                                         while (leftPointer < rightPointer && a[leftPointer] < pivotValue)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                         if they are equal advance one of them so they cross
                                                                                                                                                                              int pivotValue = a[pivot];// save the value of the pivot
                                                                                                                                                                                                                                                                                                                                                                                     if the pointers are not equal swap them
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      else {//a[rightPointer] > pivotValue
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return new pair(rightPointer, leftPointer);
                                                                                                                                                                                                                                                                                                                                                                                                                                                swap(a, leftPointer, rightPointer);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (a[leftPointer] <= pivotValue) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        /*********Heap Sort BU**************
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          public static void HeapSortBU(int[] a, int n)
                                                                                                                                                                                                                        /find a value that needs swapping
                                                                                                                                                                                                                                                                                                      /find a value that needs swapping
                                                                             return new pair(lastSmall, firstBig);
                                                                                                                                                                                                                                                                                                                                                                                                                           (rightPointer != leftPointer)
                  swap(a, smallPivot, lastSmall);
                                     swap(a, bigPivot, firstBig);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rightPointer--;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   leftPointer++;
                                                                                                                                                                                                                                                                                                                                              rightPointer--;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rightPointer--;
                                                                                                                                                                                                                                                                 leftPointer++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     leftPointer++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               //Build heap
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             } else
                                                                                                                                                                                                                                                                                 295
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```
} else {
// trickle up if the element is greater than its parent
                                // swap the first and last elements
// then trickle down the first element into its right place
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // then trickle down the first element into its right place
                                                                                                                                                                                                                                                                                                                                                            /**********End Heap Sort BU***************
                                                                                                                                                                                                                                   ' do nothing if its less than or equal
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       trickleDown(a, i, n);
//check if any of the current node parents
                                                                                                                                                                           private static void buildHeapBU(int[] a, int n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  private static void buildHeapTD(int[] a, int n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         for (int j = i; j > 0; j = (j - 1) / 2) {
                                                                                                                                                                                                                                                                                                                                                                                                  public static void HeapSortTD(int[] a, int n) {
                                                                                                                                                                                                                                                                                                                                                                               swap the first and last elements
                                                                                                                                                                                               for (int i = n - 1; i >= 1; i--) {
   if (a[i] <= a[(i - 1) / 2]) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          for (int i = n - 1; i >= 1; i--) {
                                                                    for (int i = n - 1; i >= 1; i--) {
                                                                                                                                           } // heapsort with linear buildheap
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              } // heapsort with linear buildheap
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         / need to be trickled down
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (int i = 0; i < n; i++) {</pre>
                 // start from the end and
                                                                                                                                                                                                                                                                                                                                                                                                                                                     // start from the end and
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              trickleDown(a, 0, i);
                                                                                                     trickleDown(a, 0, i);
                                                                                       swap(a, 0, i);
                                                                                                                                                                                                                                                                                                                                                                                                                                    buildHeapTD(a, n);
buildHeapBU(a, n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           swap(a, 0, i);
                                                                                                                                                                                                                                                                                                                                                                                                                    //Build heap
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private static void trickleDown(int[] a, int i, int n) {
                                                                                                                                                                                                private static void trickleUp(int[] a, int i, int n)
                                                                                                                                                                          /**********End Heap Sort TD****************
if (a[(j - 1) / 2] < a[j]) {
   trickleDown(a, (j - 1) / 2, n);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     boolean secondChildExist = (2 * i + 2) < n;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      boolean firstChildExist = (2 * i + 1) < n;</pre>
                                                                                                                                                                                                                                                                                                                                                                                          if (i - 1 < 0) {//end of array
exit = true;</pre>
                                                                                                                                                                                                                                                              while (((i - 1) / 2) >= 0 && !exit) {
   if (save > a[(i - 1) / 2]) {
      a[i] = a[(i - 1) / 2];
   if (i > 0) {
      trickleDown(a, i, n);
}
                                                                                                                                                                                                                                                                                                                                                                                                                                                i = (i - 1) / 2;
                                                                                                                                                                                                                                             boolean exit = false;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 boolean exit = false;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   exit = true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int save = a[i];
                                                                                                                                                                                                                        int save = a[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 a[i] = save;
```



```
//start from the second element in the array and insert every element
                                                                                                                                                                                                                                                                                                                   swap method perform basic swap that is needed any of the sorts and doesn't swap if the 2 indices are the same
                                                                                                 \} else if (firstChildExist && save < a[2 * i + 1])
                                                                                                                                                                                                                                                                                                                                                            private static void swap(int[] a, int swap, int with) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         public static void insertionSort(int[] a, int n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           else if (save < a[2 * i + 1])
                                                                                                                                                                                                                 secondChildExist = (2 * i + 2)
                            a[i] = a[2 * i + 1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for (int i = 1; i <= n; i++) {
i = 2 * i + 2;
                                         i = 2 * i + 1;
                                                                       exit = true;
                                                                                                                                                                                                                                                                                                                                                                                                       int save = a[swap];
                                                                                                                                                                                                   firstChildExist =
                                                                                                                                                                                                                                                                                                                                                                                                                     = a[with];
                                                                                                                                                          exit = true;
                                                                                                                                                                                                                                                                                                                                                                          if (swap == with) {
                                                                                                                                                                                                                                                                                                                                                                                                                                 a[with] = save;
                                                         } else {
                                                                                                                                            } else {
                                                                                                                                                                                                                                                            a[i] = save;
                                                                                                                                                                                                                                                                                                                                                                                                                      a[swap]
                                                                                                                                                                                                                                                                                                                                                                                         } else {
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461 // use this class to return two values in the outside-in and the 2-pivot // partition methods
                                                                                                                                                                        /**********End insertionSort****************
                                                                                   for (i = n - 2; i >= 0 && save < a[i]; i--) {
    a[i + 1] = a[i];</pre>
                          private static void insert(int[] a, int n) {
  int i;
                                                                     //shift all the elements one spot
                                                                                                                                                                                                                                                                                                                                                  public pair(int left, int right) {
                                                                                                                                                                                                     return "Bishoy Abdelamlik";
                                                                                                                                                                                       public static String myName() {
                                                     int save = a[n - 1];
                                                                                                                                                                                                                                                                                                      462 class pair {
463 public int left, right;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 public int getRight() {
                                                                                                                                                                                                                                                                                                                                                                               this.right = right;
                                                                                                                                                                                                                                                                                                                                                                                                                                        public int getLeft() {
                                                                                                                                                                                                                                                                                                                                                                                                                          // some getters below
                                                                                                                                                                                                                                                                                                                                                                this.left = left;
                                                                                                                             a[i + 1] = save;
}// Insertion Sort
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return right;
                                                                                                                                                                                                                                                                                                                                                                                                                                                      return left;
                                                                                                                                                                                                                                                             459 }
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