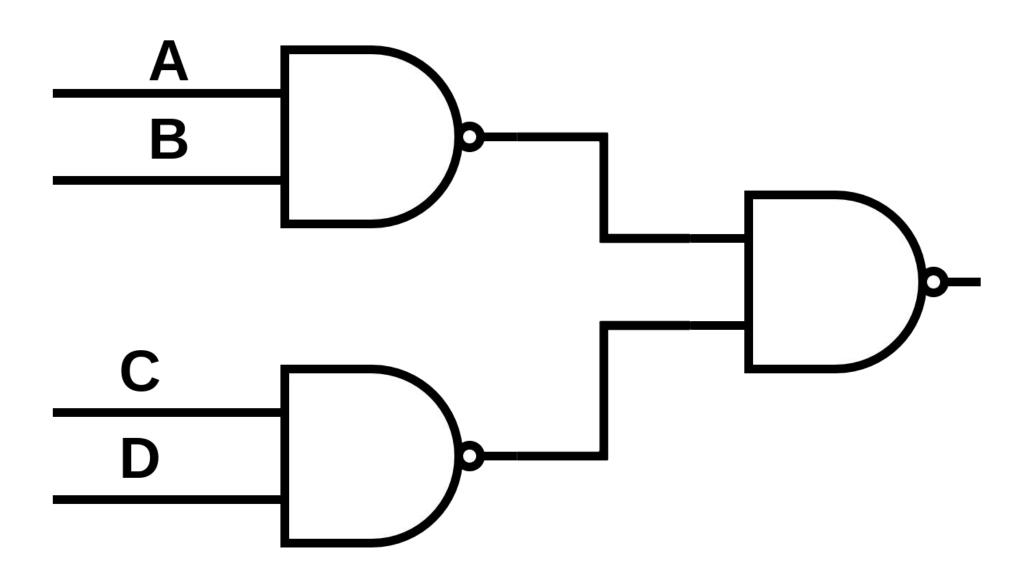
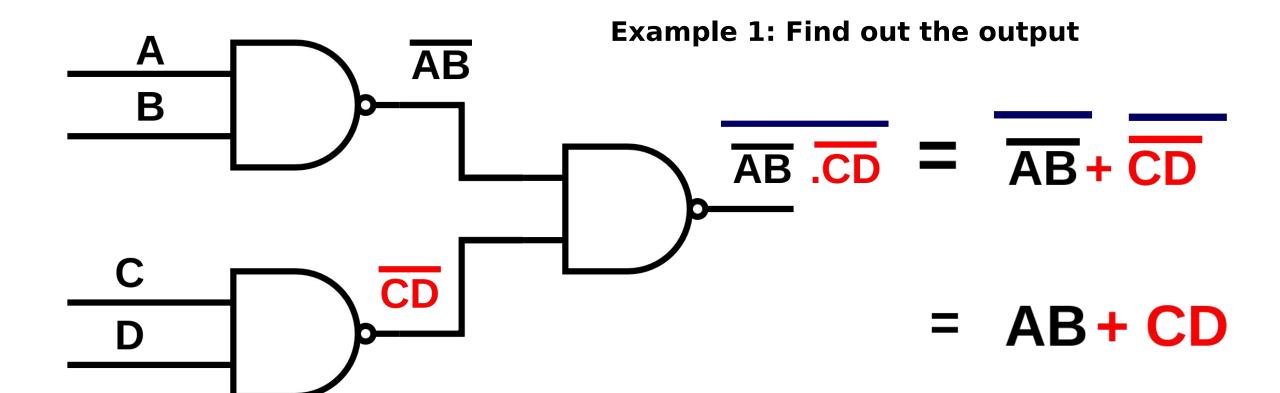
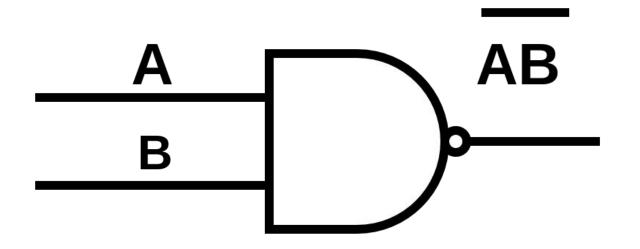
Universal Gates And Complement Arithmetic

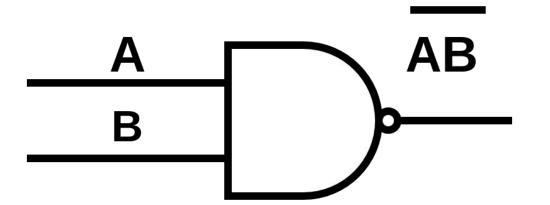
Example 1: Find out the output



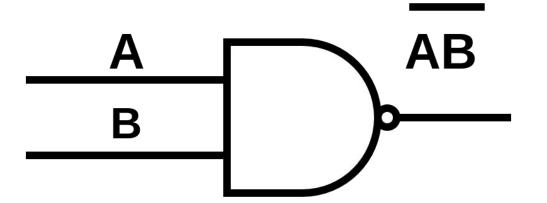




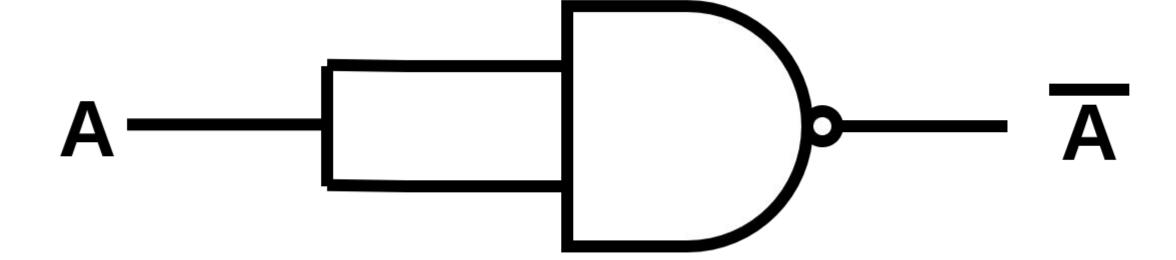
So, This is a Simple **NAND** Gate with inputs **A and B**

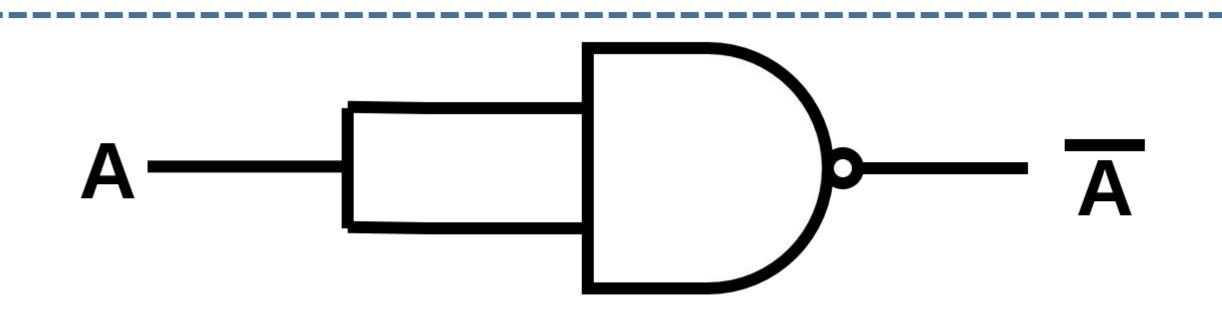


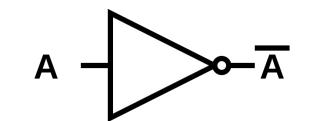
IF A=B, then

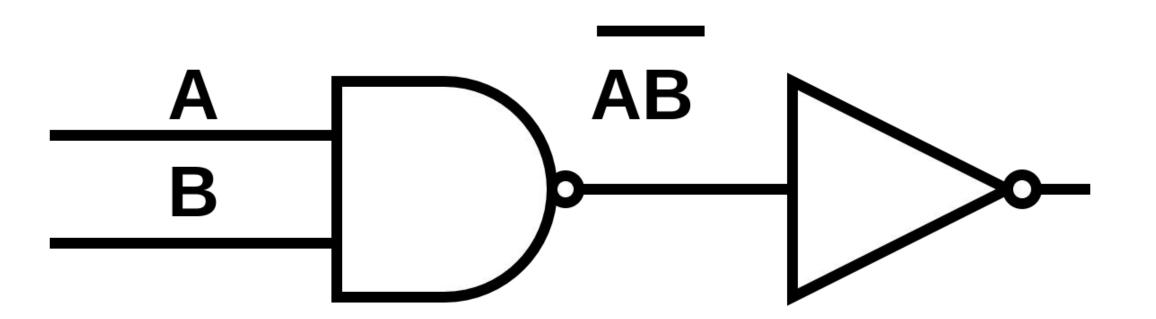


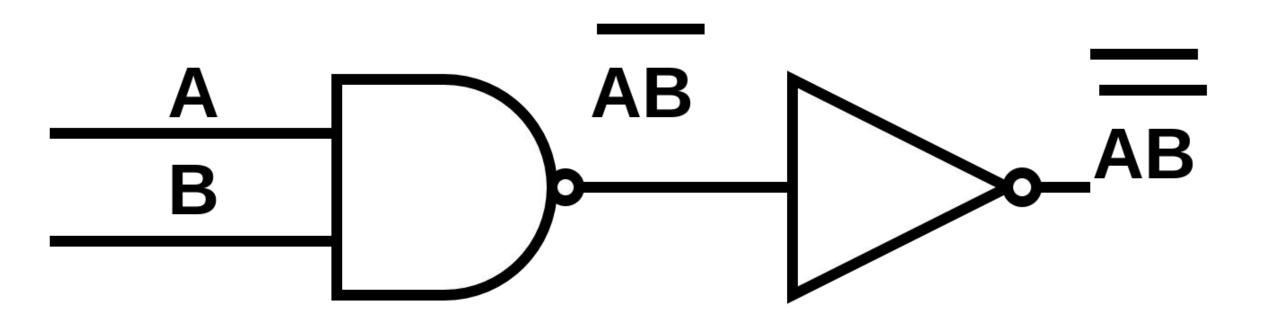
IF A=B, then

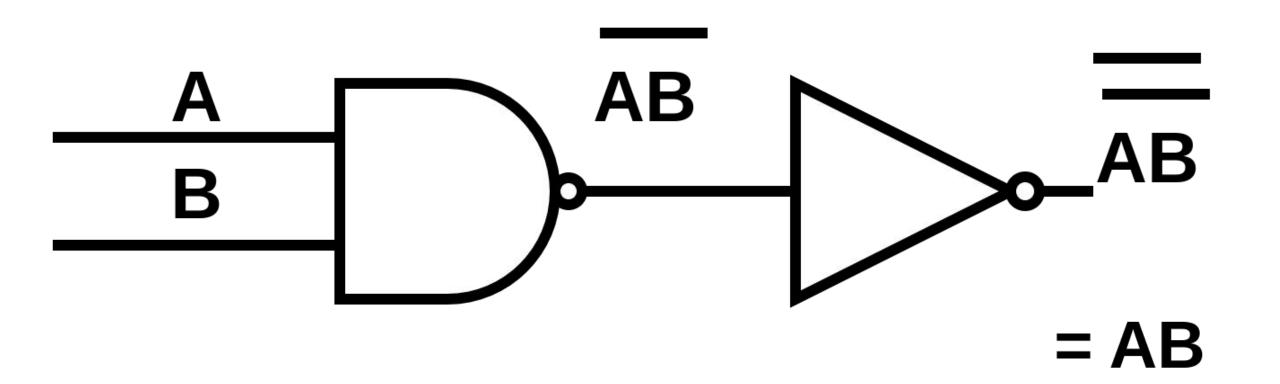


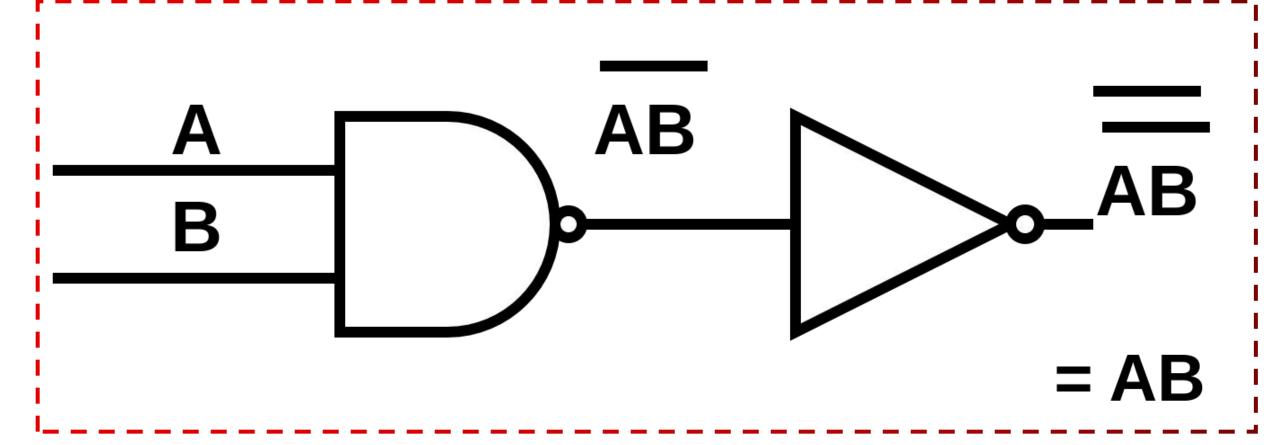


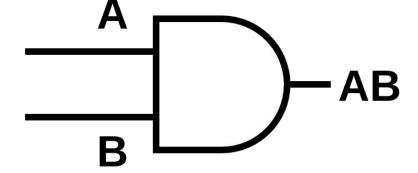


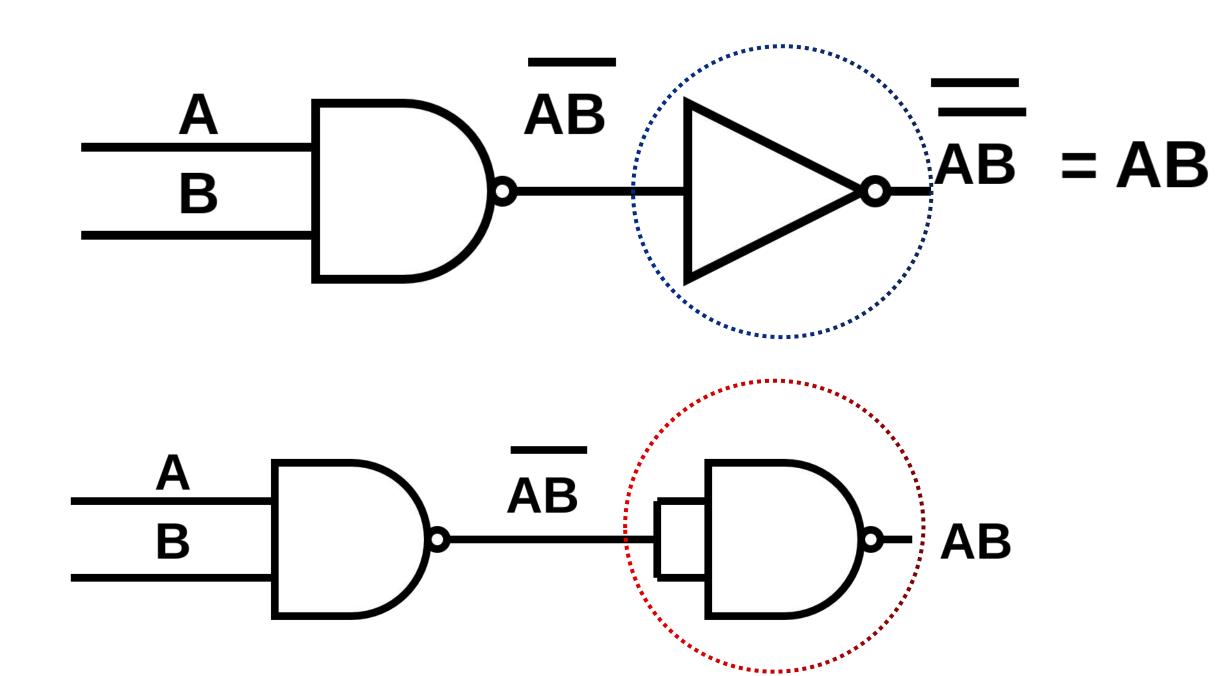


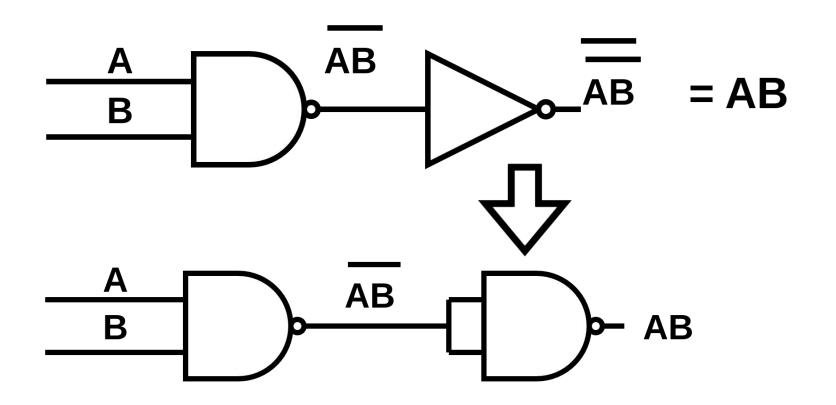




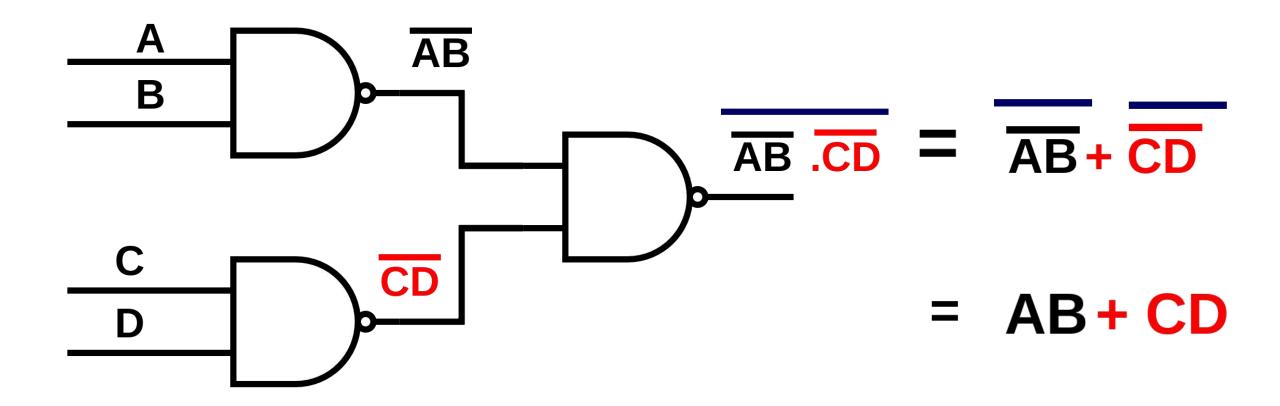








Two **NAND** are acting like **AND** Gate



REMEMBER THIS LOGIC CIRCUIT?

$$\begin{array}{c|c}
\hline
A \\
\hline
B
\end{array}$$

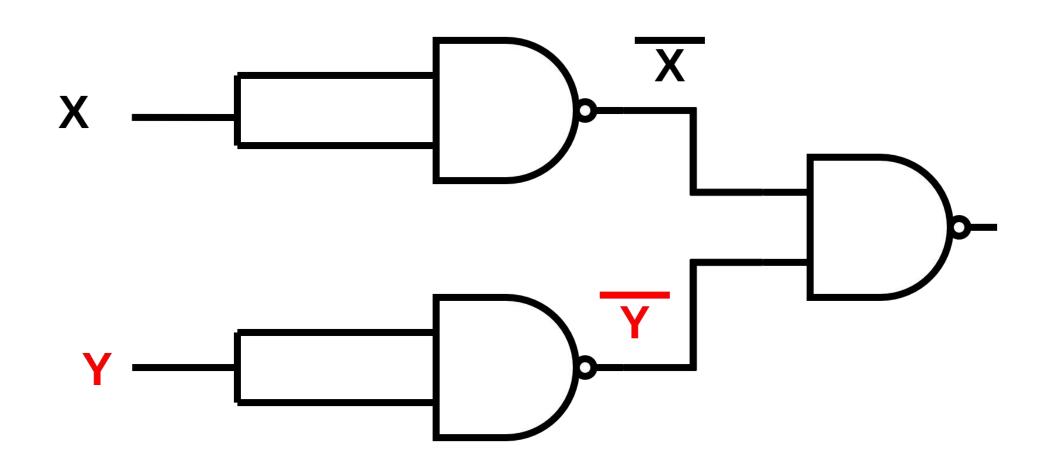
$$\begin{array}{c|c}
\hline
C \\
\hline
D
\end{array}$$

$$\begin{array}{c|c}
\hline
C \\
\hline
D
\end{array}$$

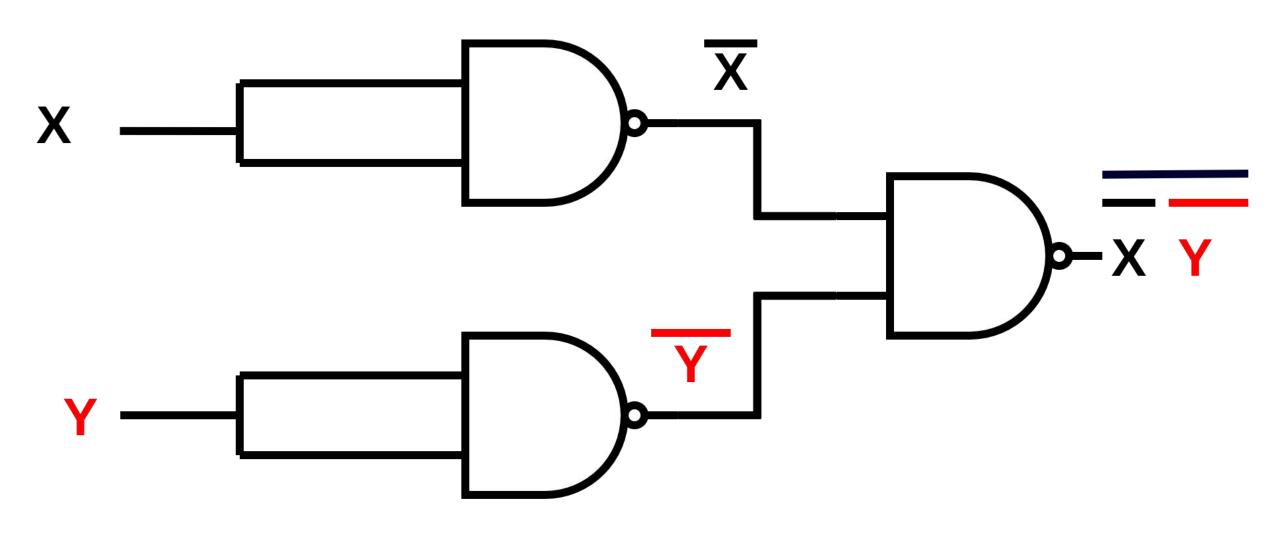
$$\begin{array}{c|c}
\hline
AB \cdot CD
\end{array}$$

$$\begin{array}{c|c}
\hline
AB + CD
\end{array}$$

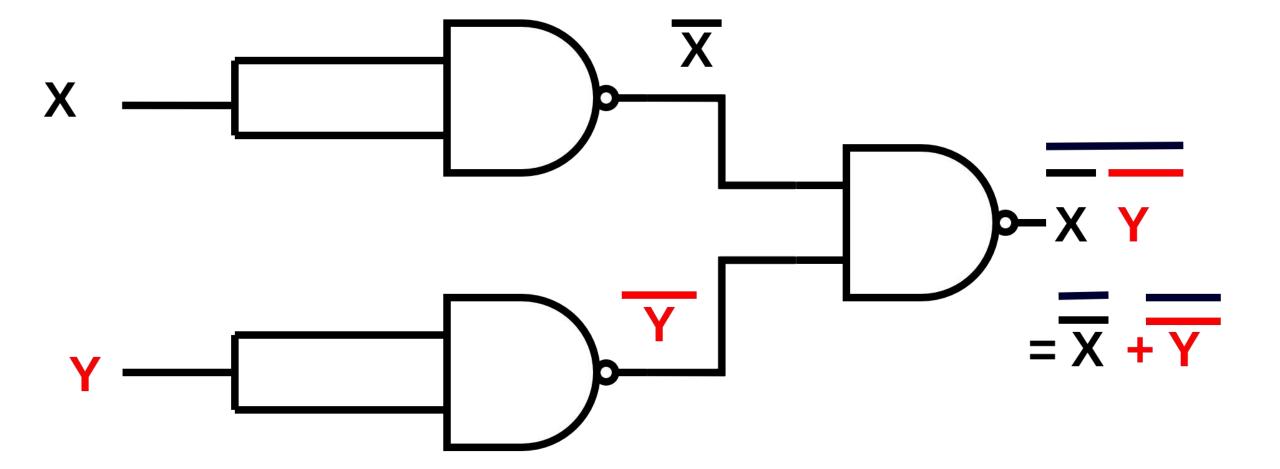
$$IF A=B=X \& C=D=Y, THEN$$

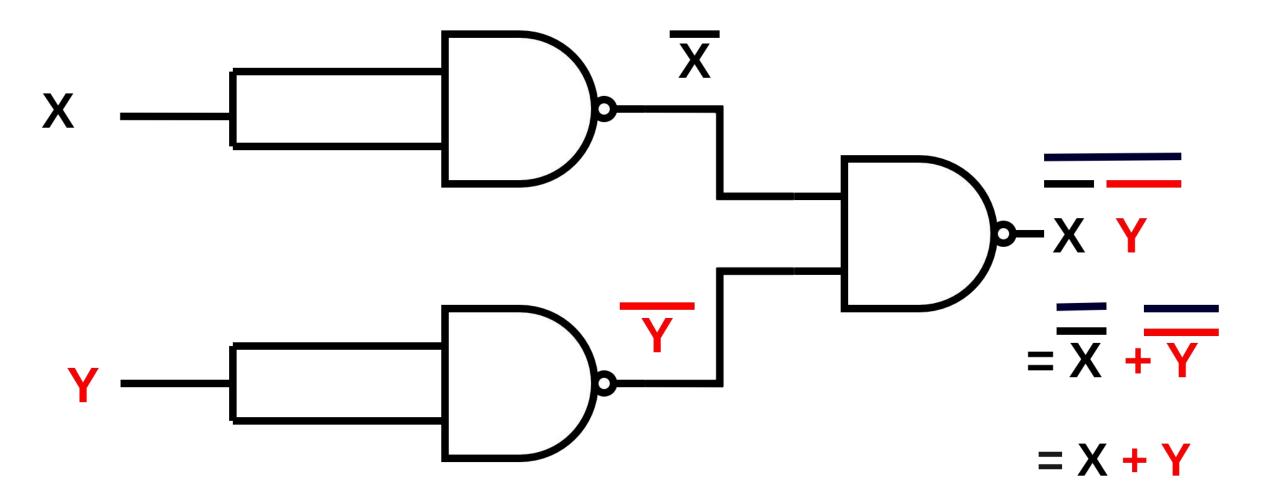


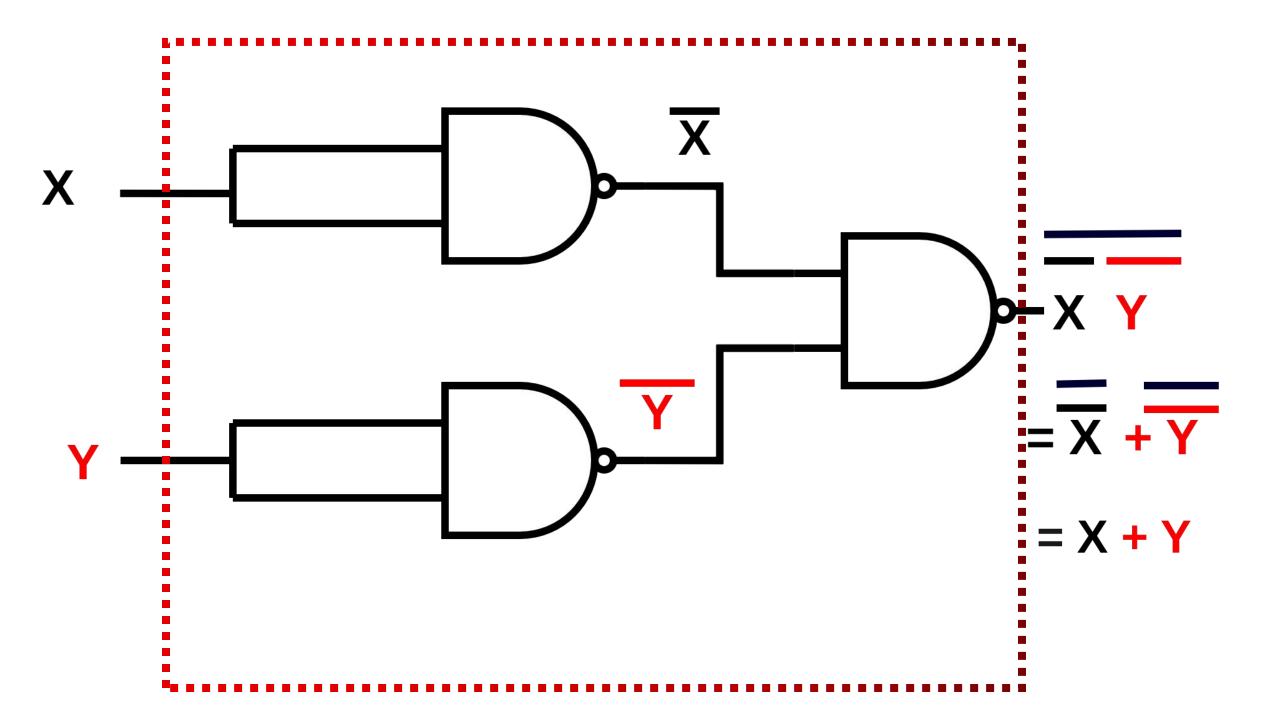
$$IF A=B=X \& C=D=Y, THEN$$

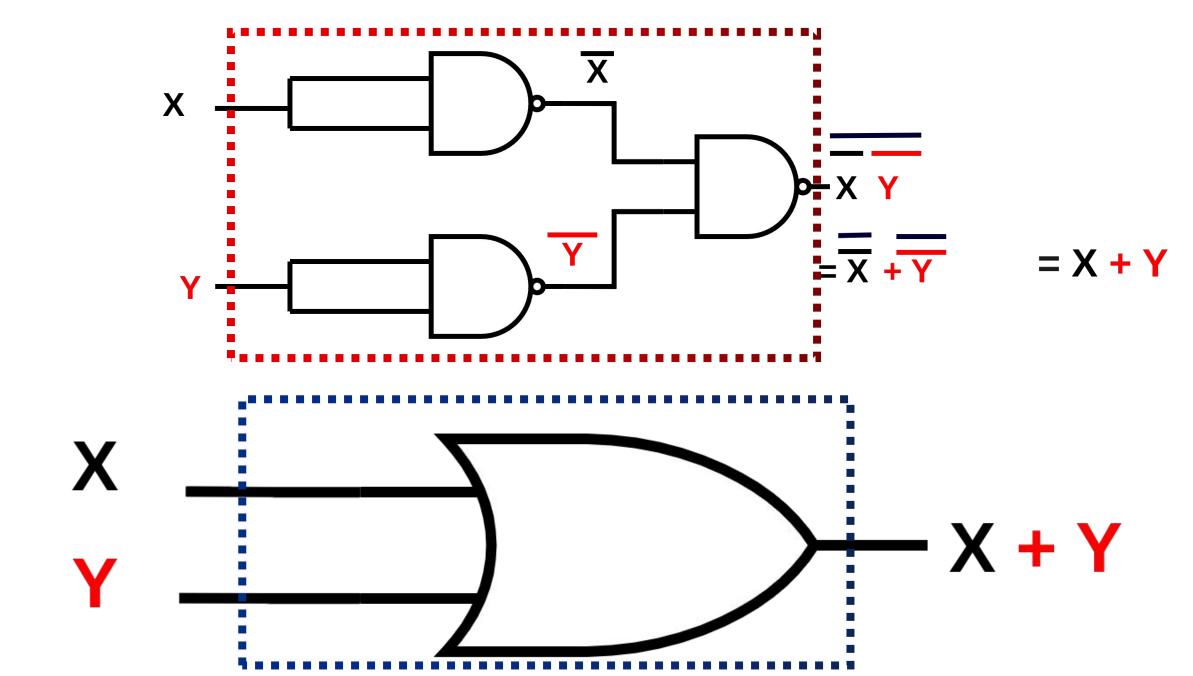


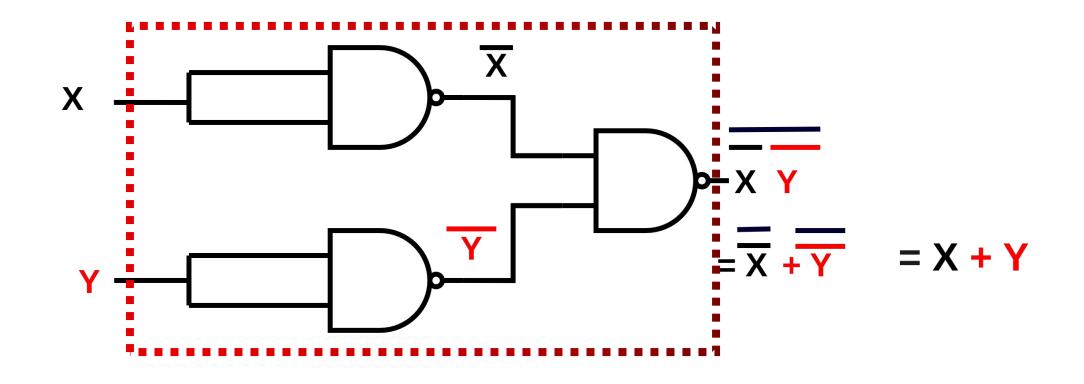
$$IF A=B=X \& C=D=Y, THEN$$



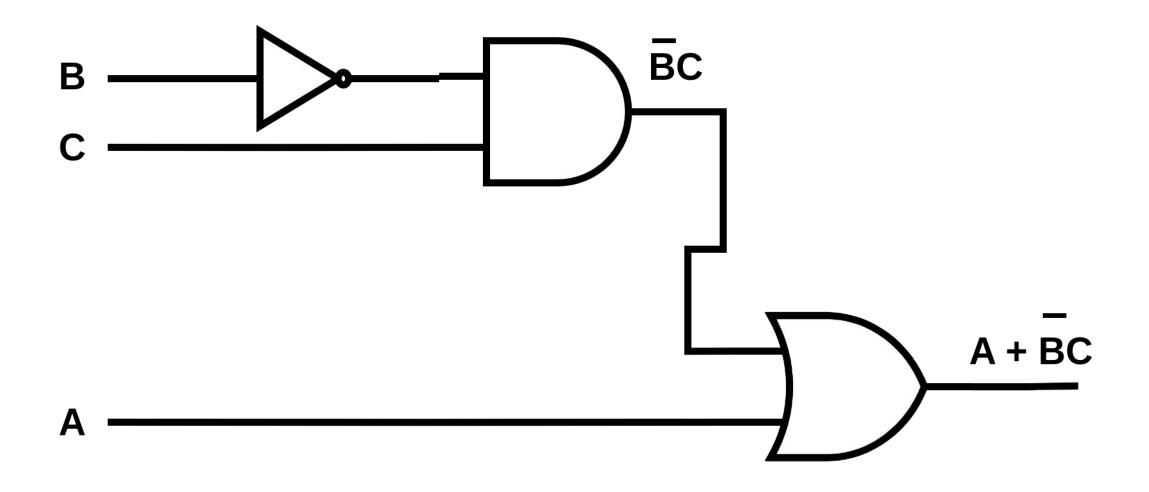


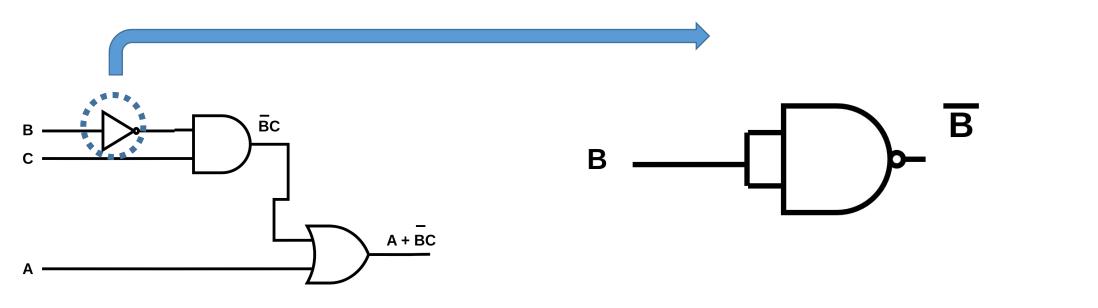


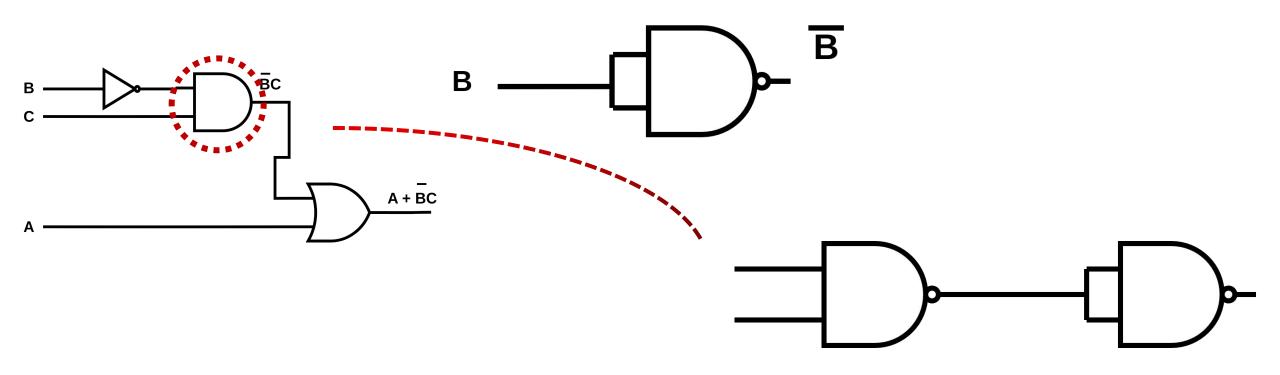


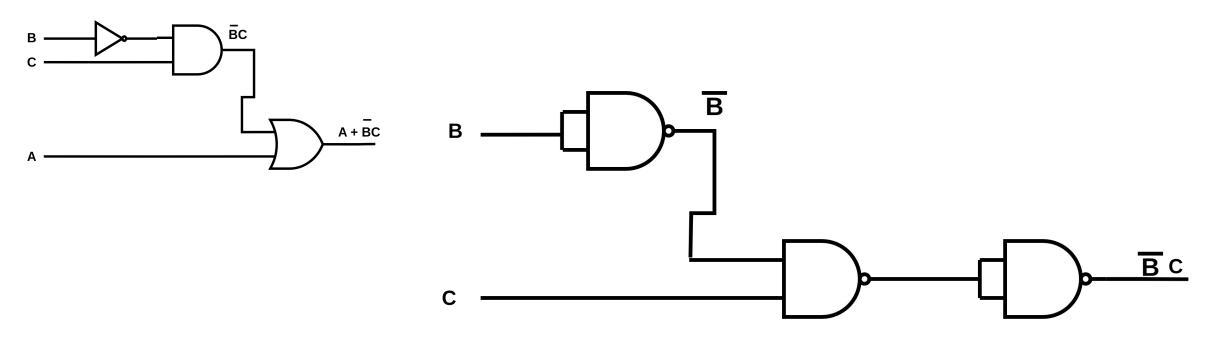


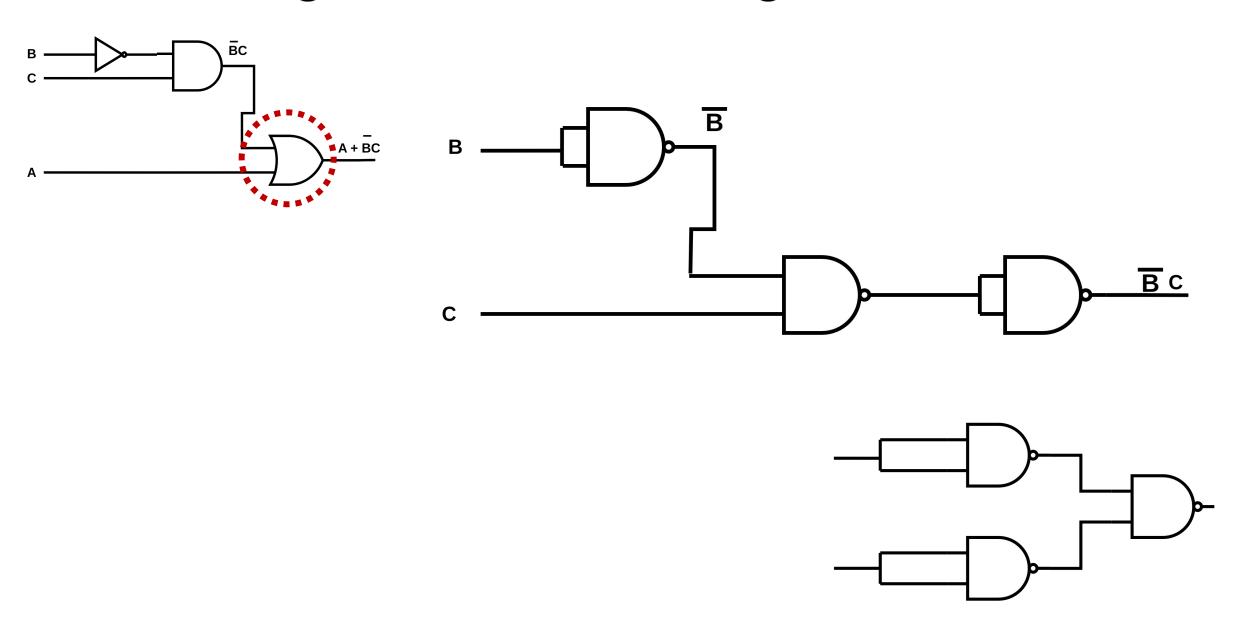
Three **NAND** are acting like **OR** Gate

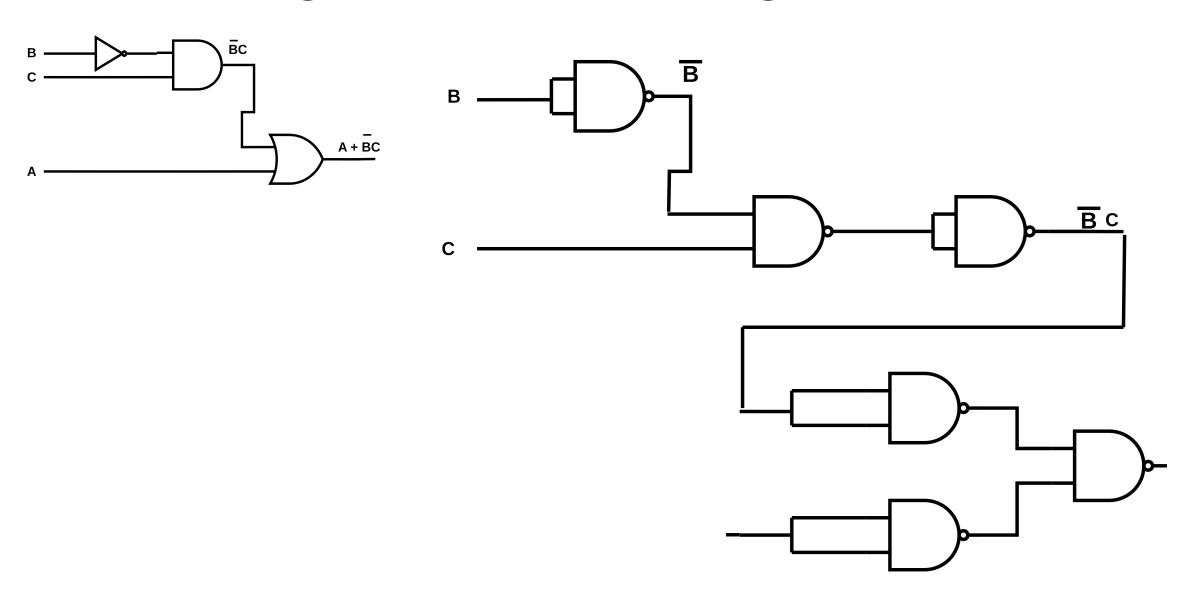


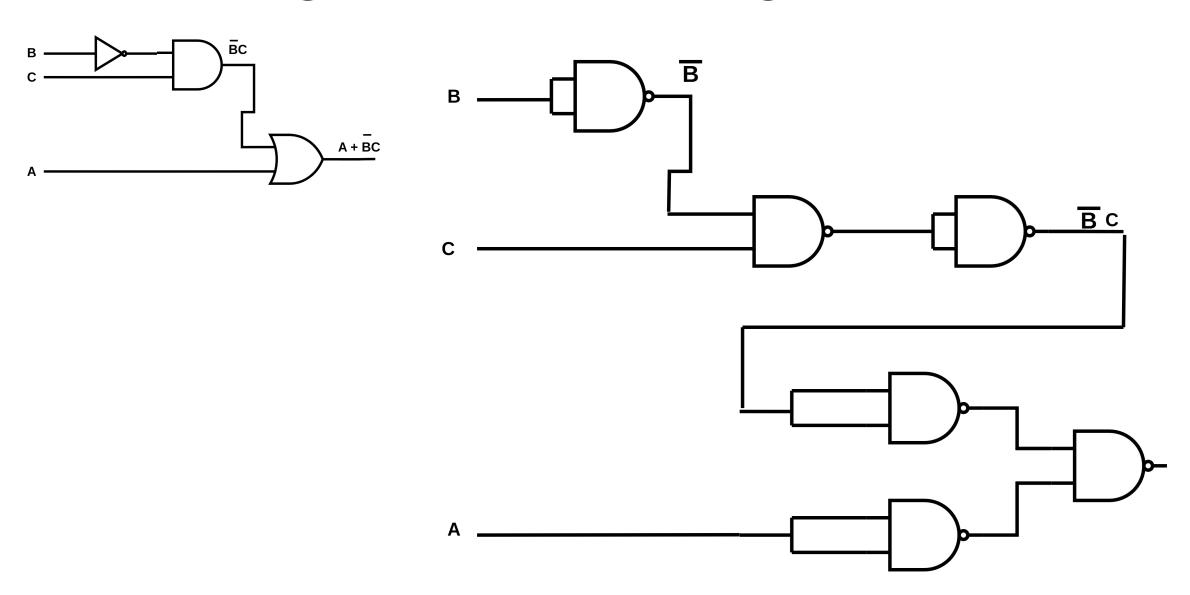


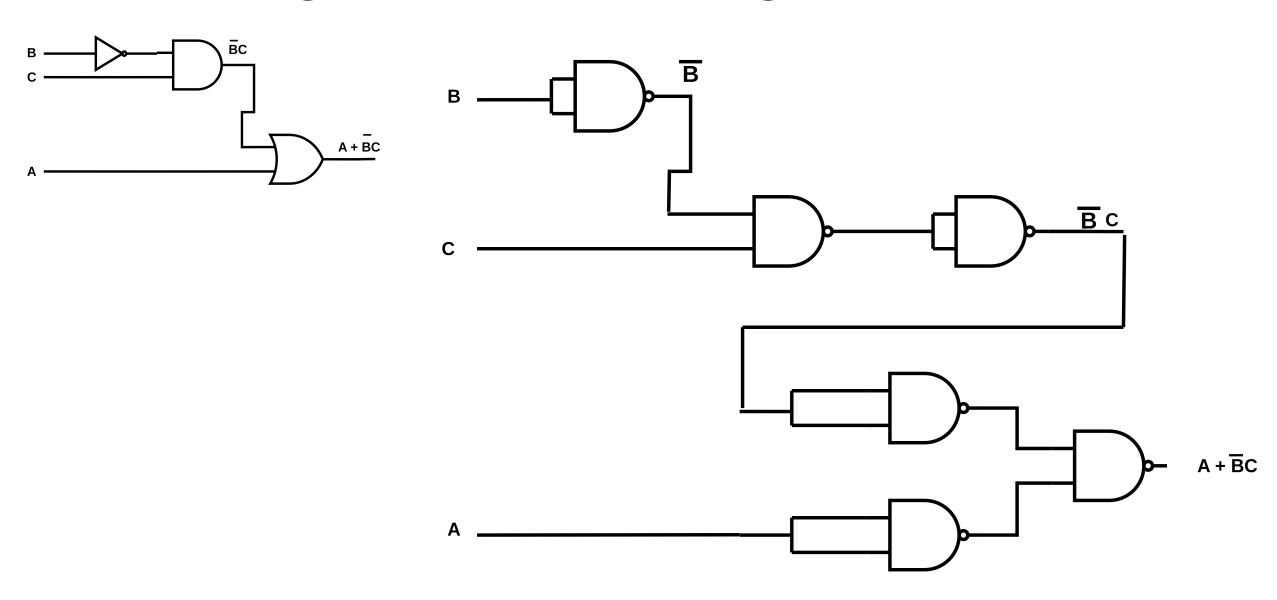


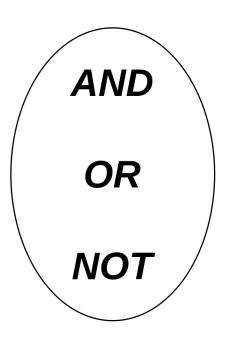




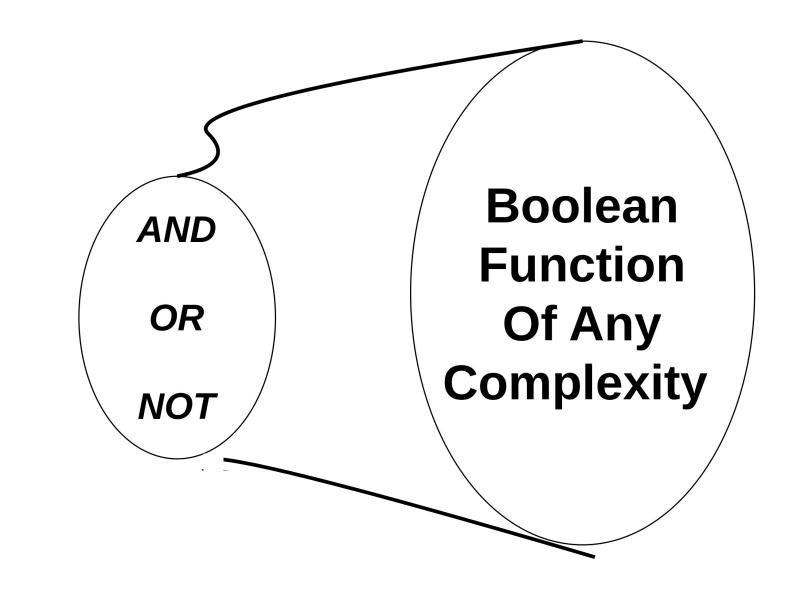


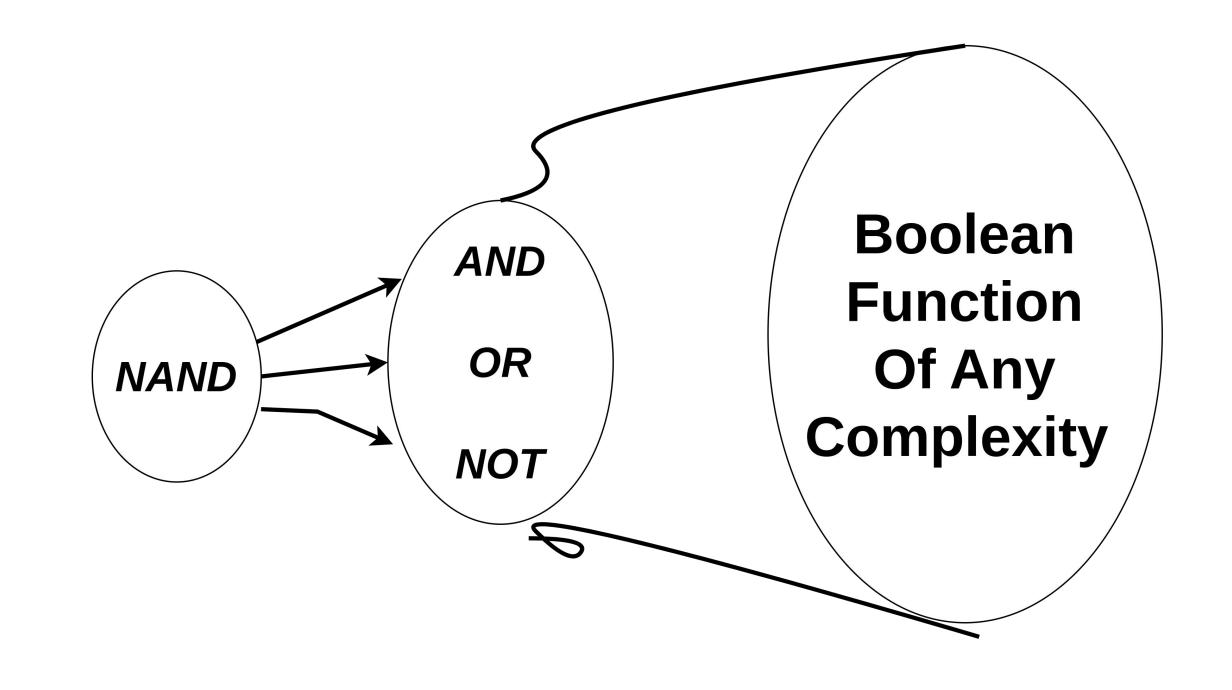


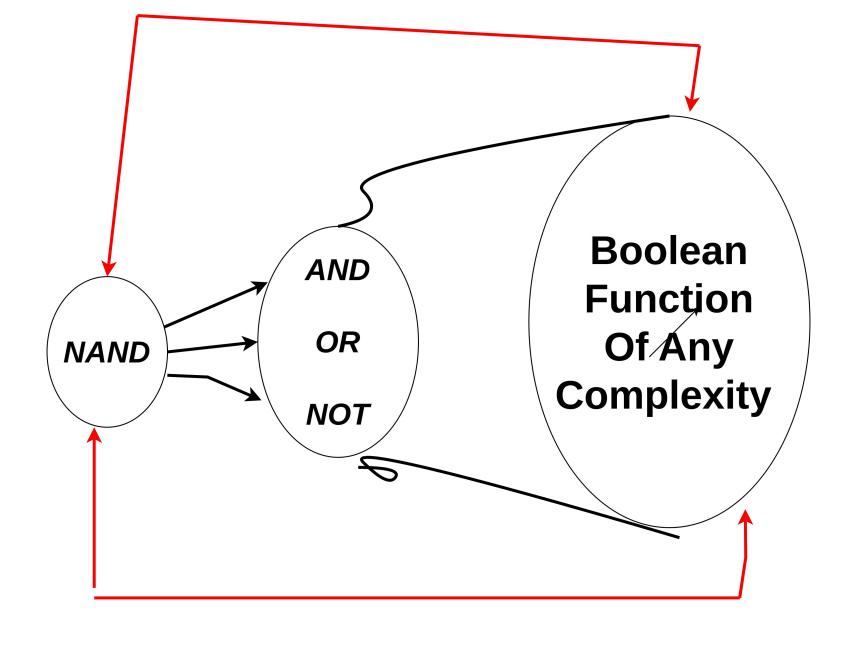




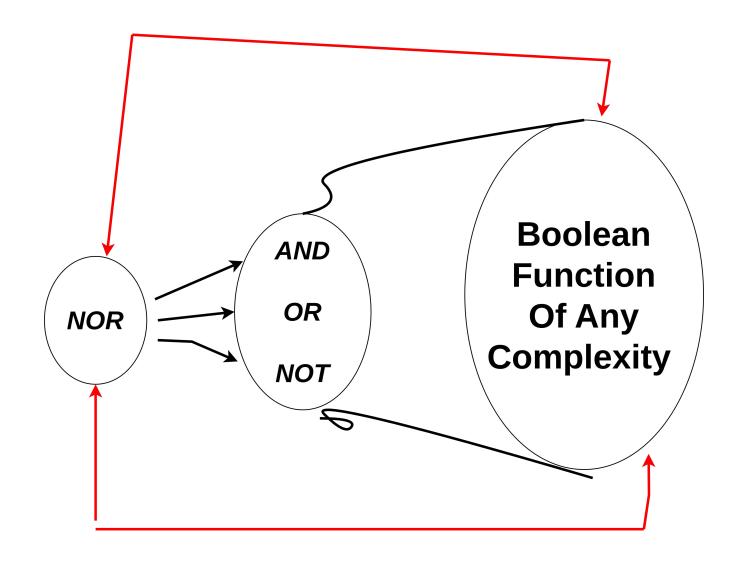
Boolean
Function
Of Any
Complexity



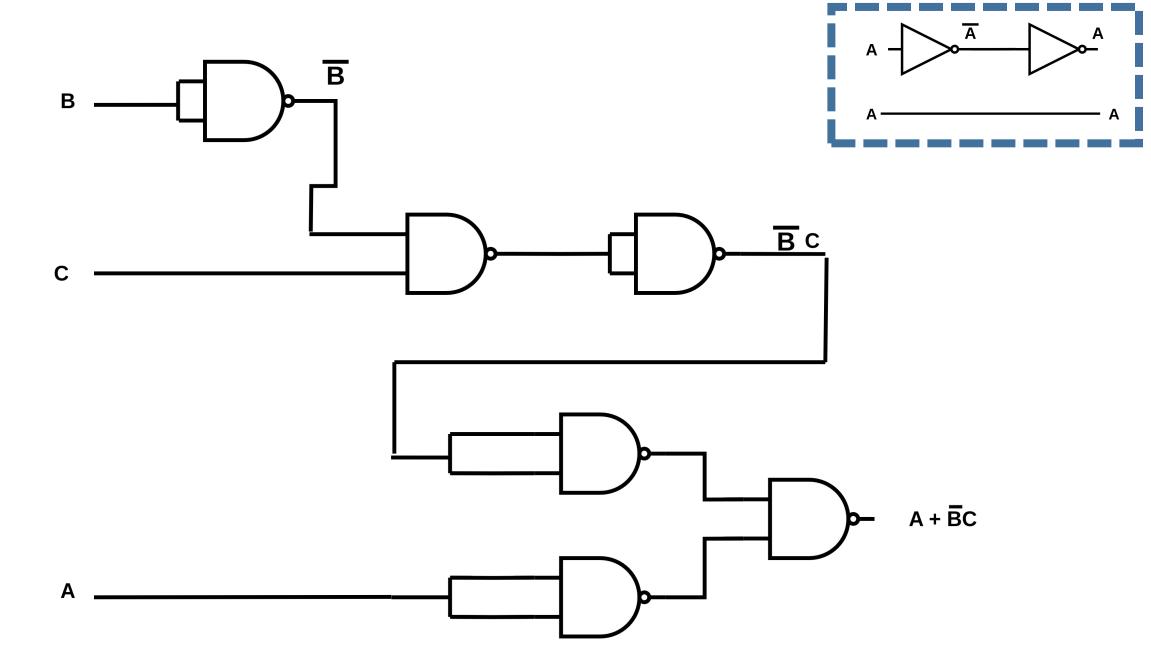


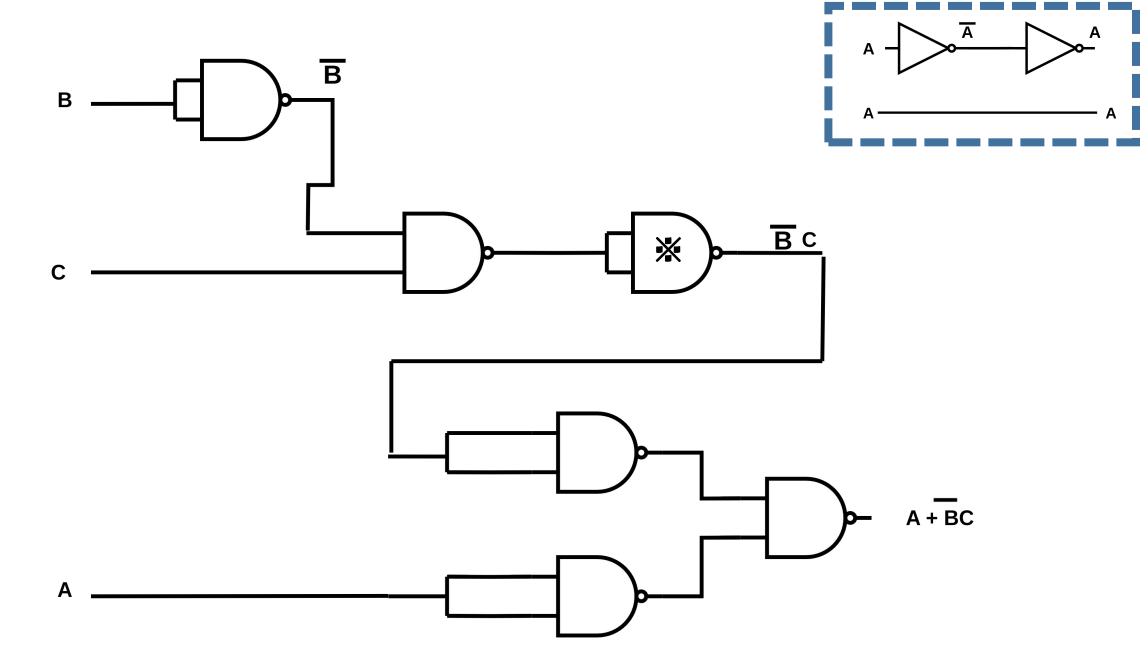


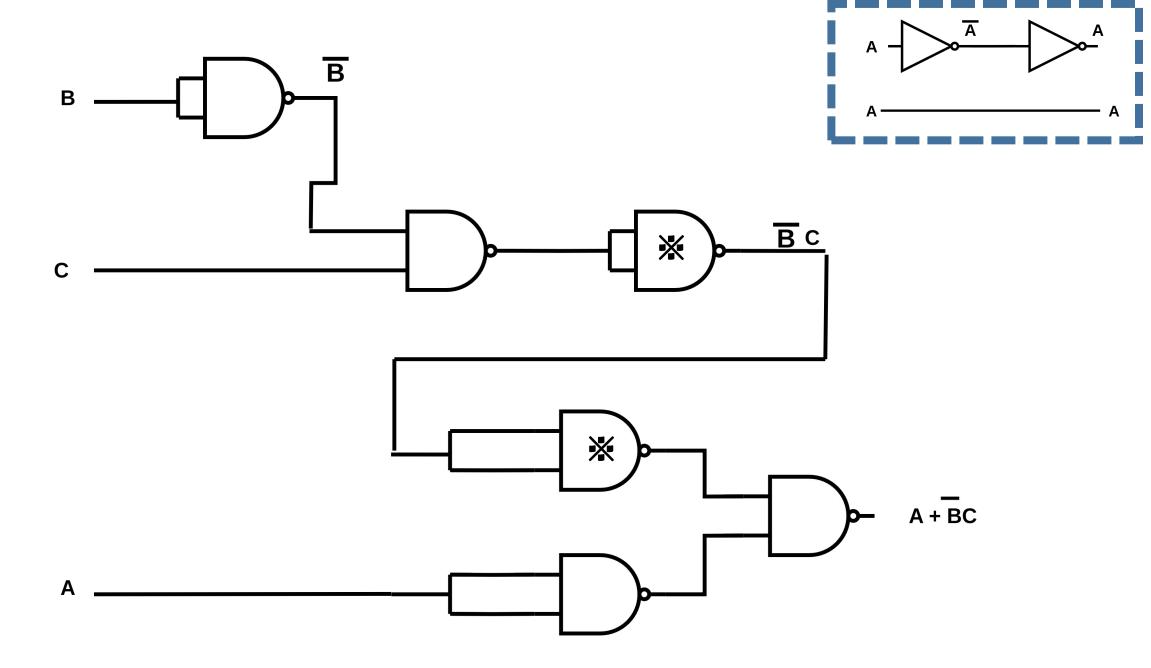
UNIVERSAL GATE

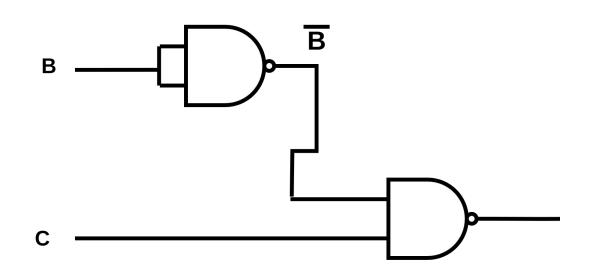


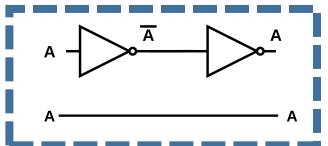
UNIVERSAL GATE

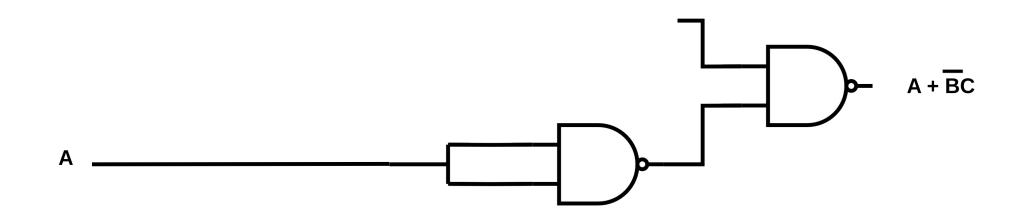


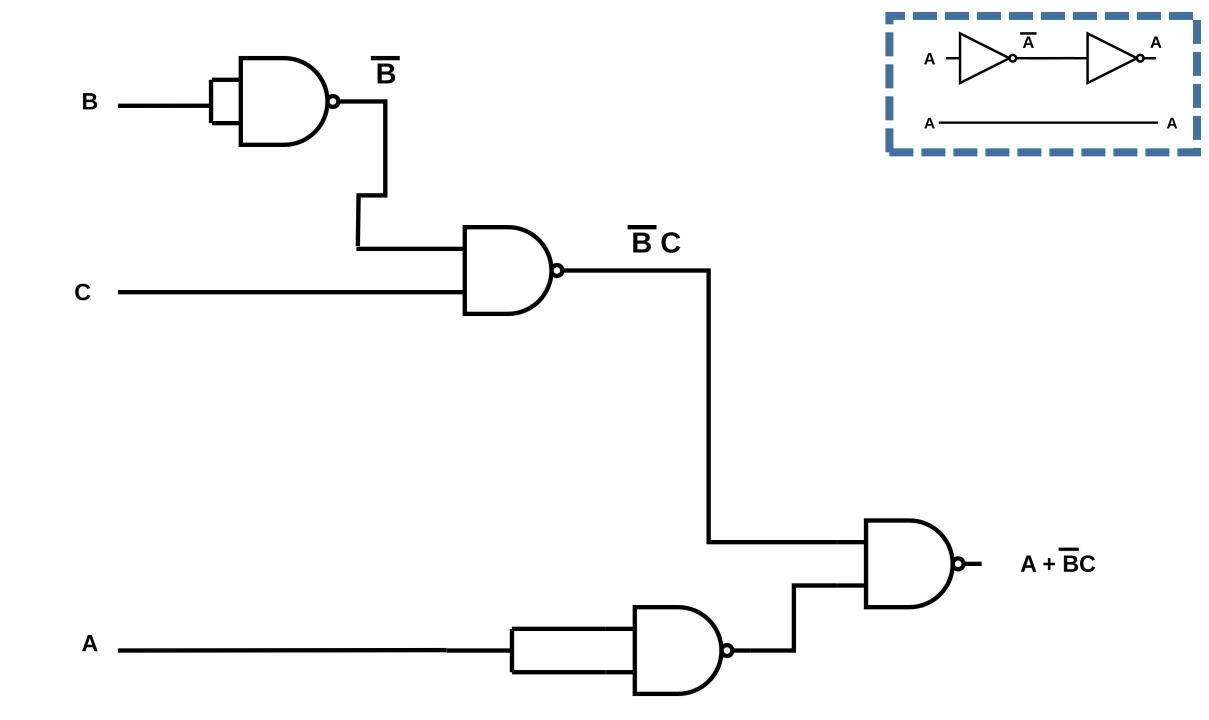




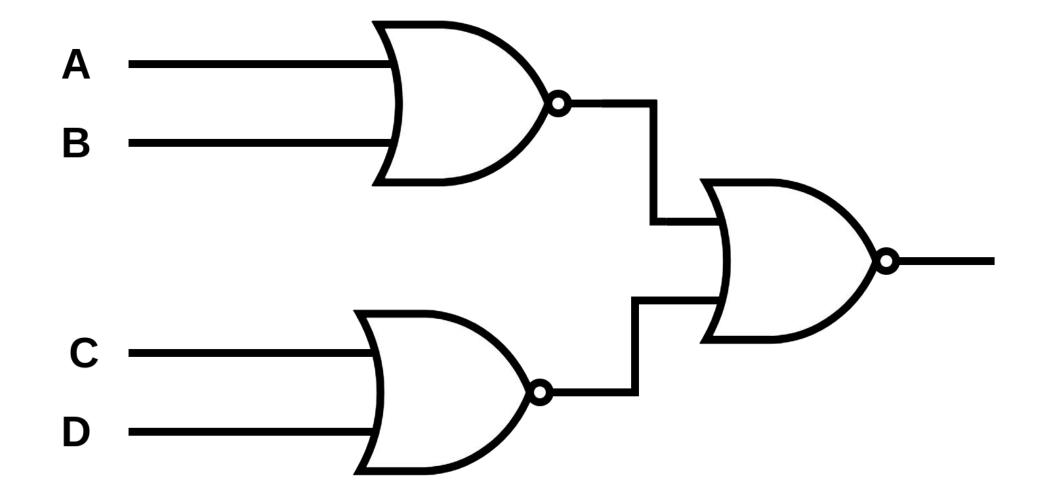


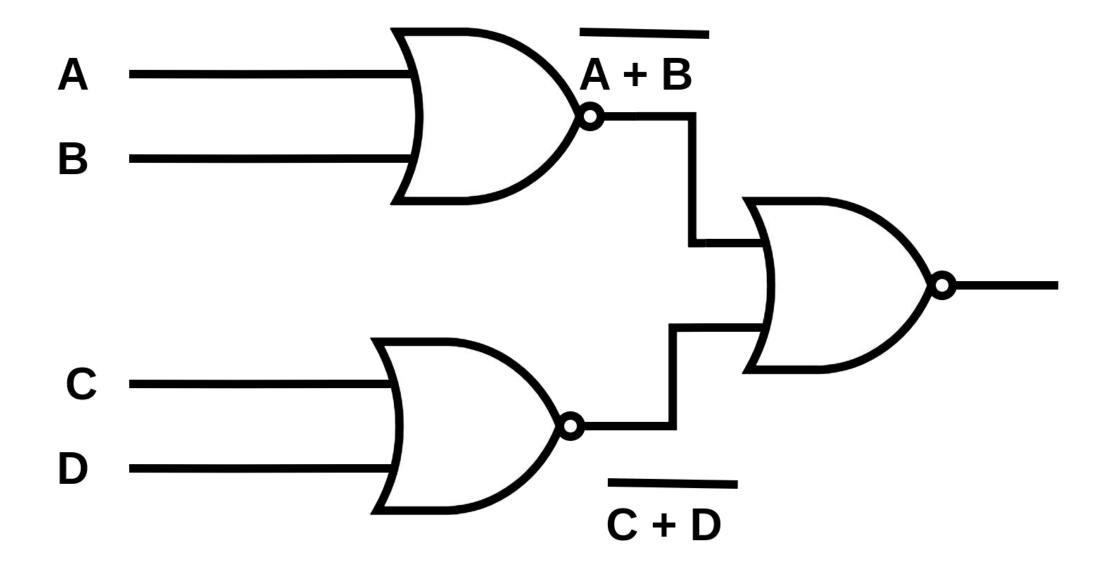


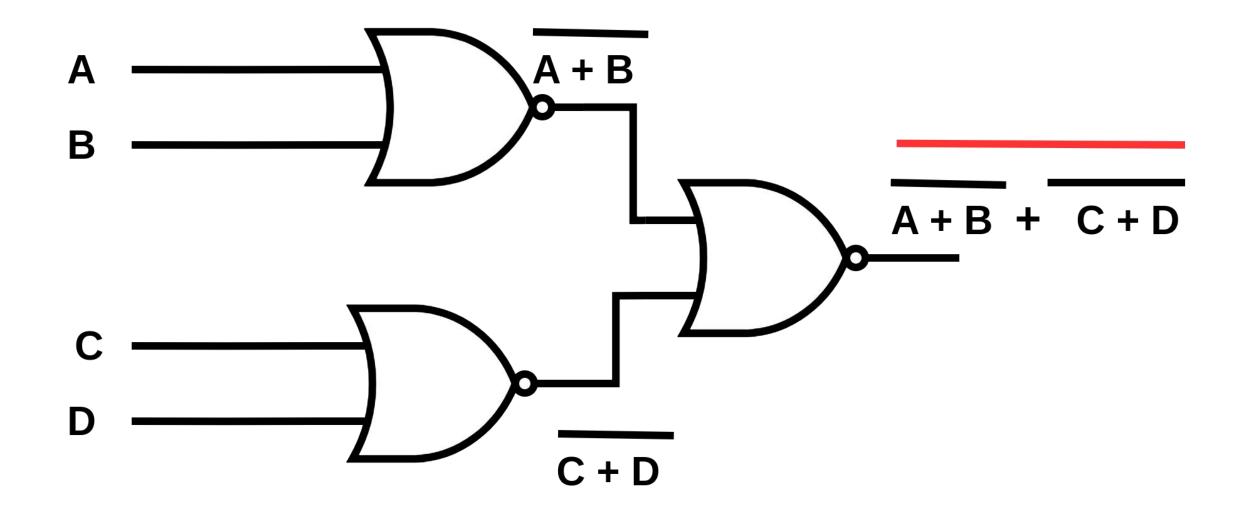


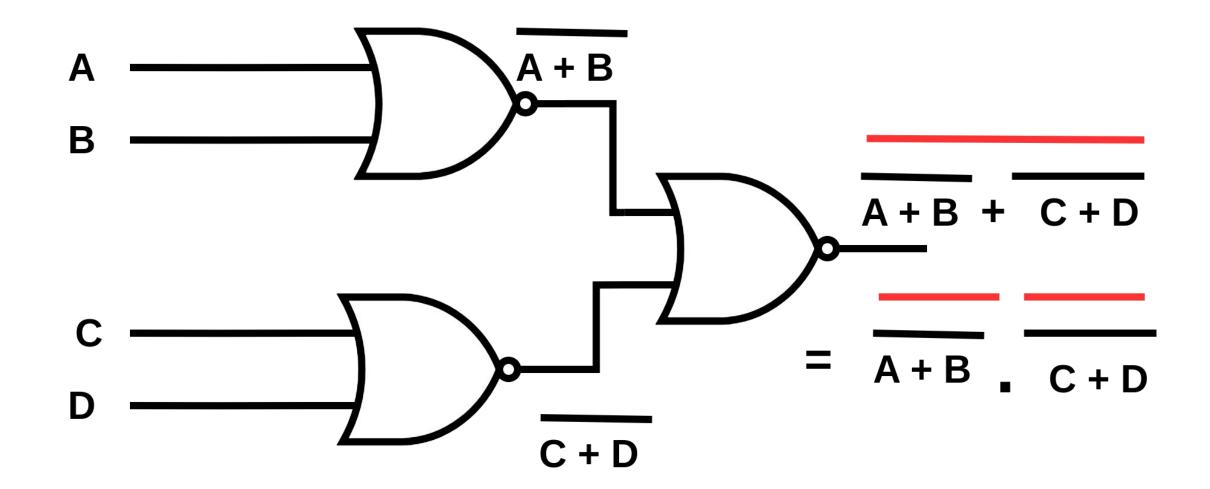


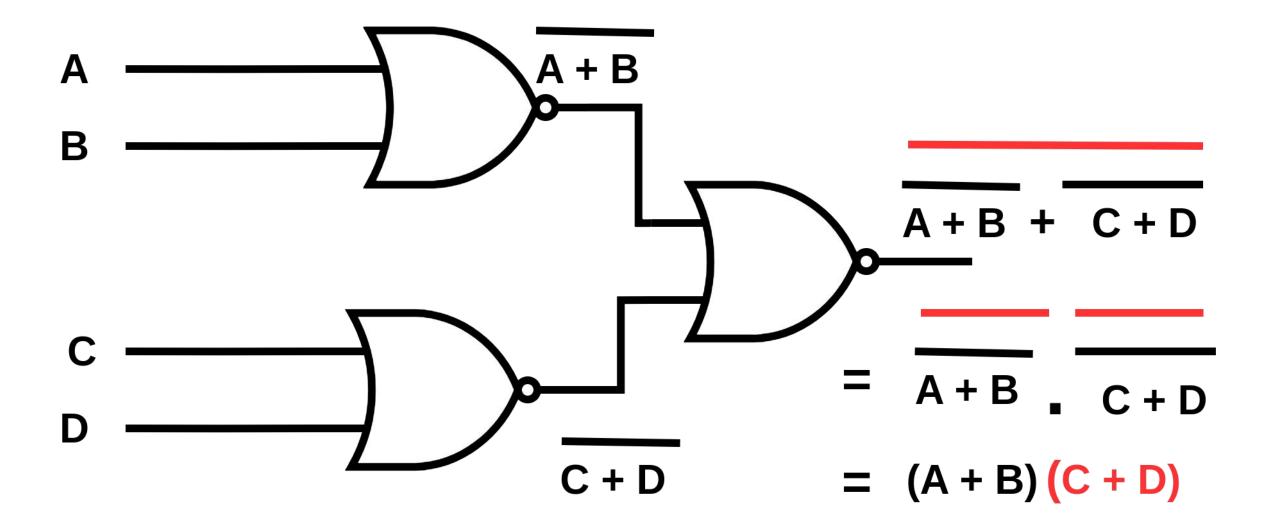
UNIVERSAL NOR GATE

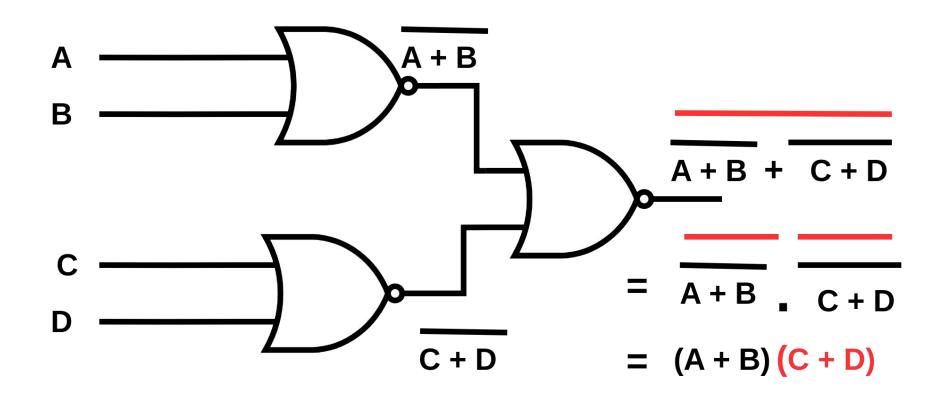




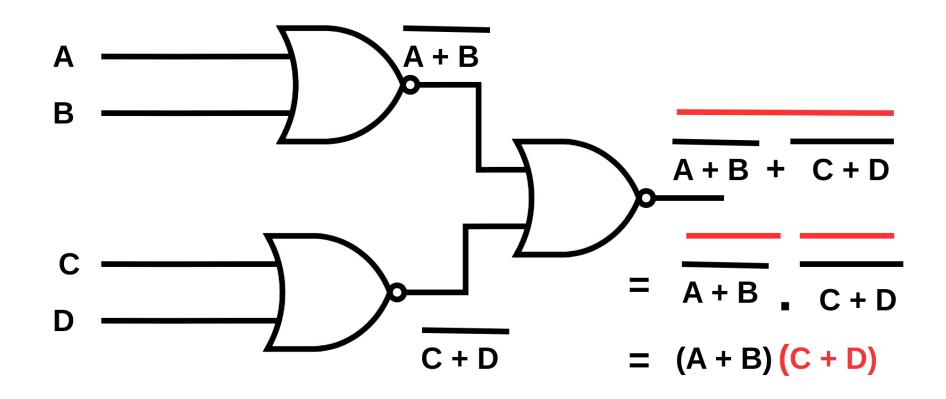




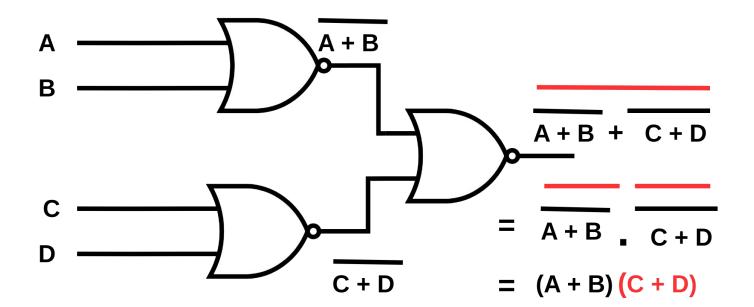


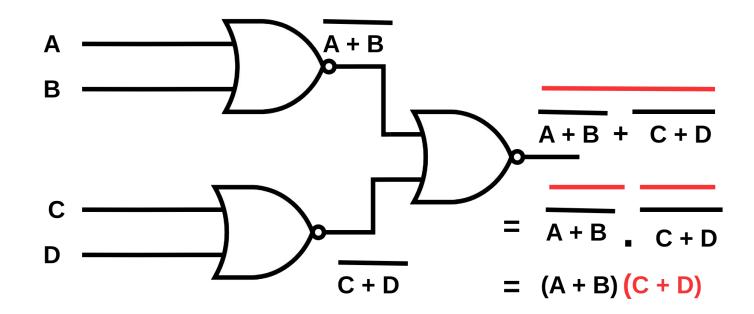


IF A=B=X and C=D=Y

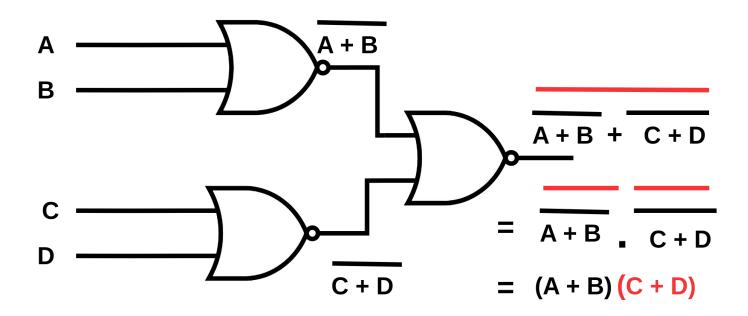


IF A=B=X and C=D=Y



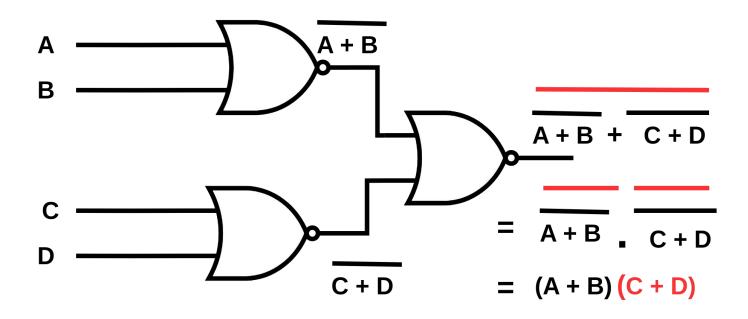


$$= (A + B) (C + D)$$



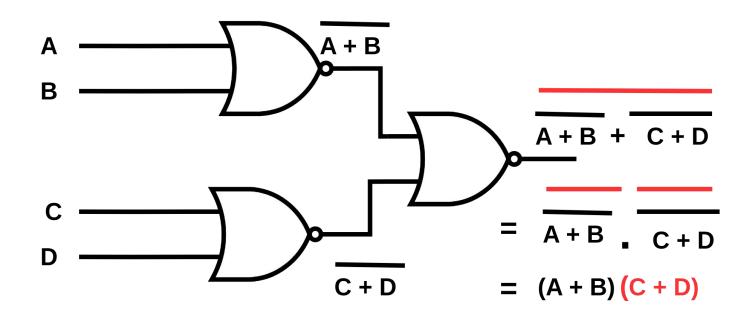
$$= (A + B) (C + D)$$

$$= (X+X) (Y+Y)$$



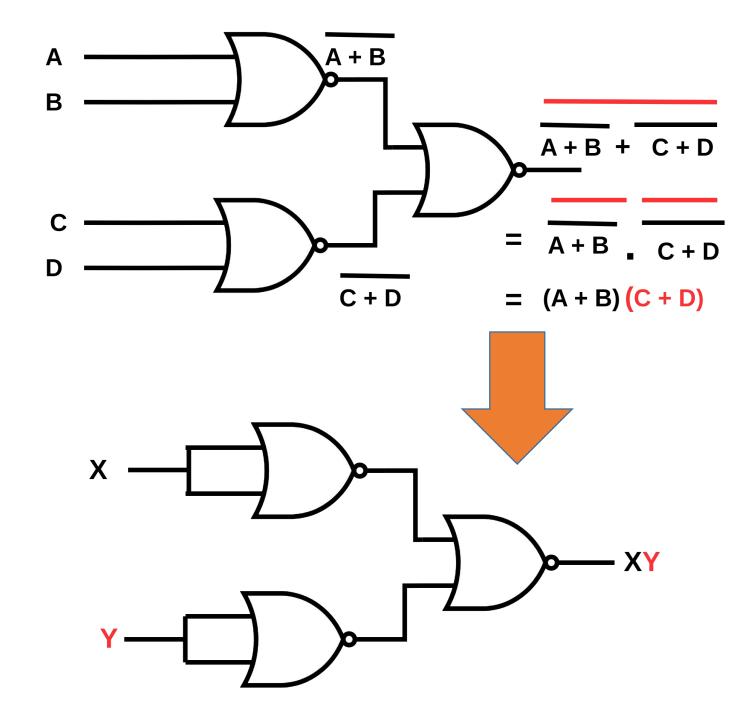
$$= (A + B) (C + D)$$

$$= (X+X) (Y+Y)$$



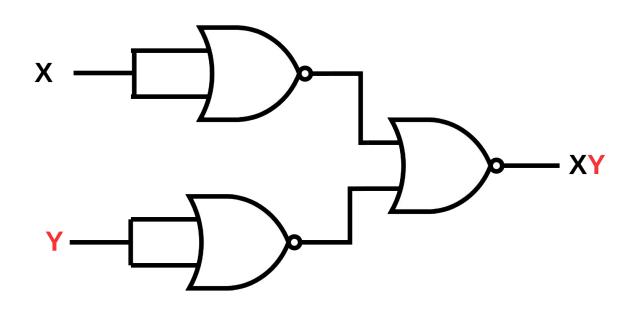
$$= (A + B) (C + D)$$

$$= (X+X) (Y+Y)$$

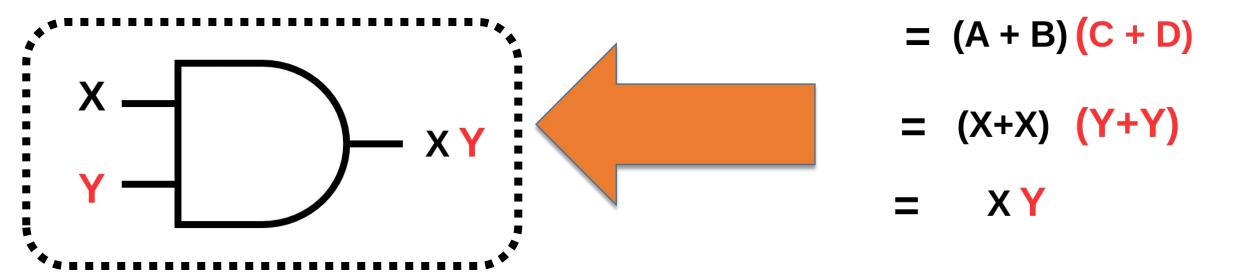


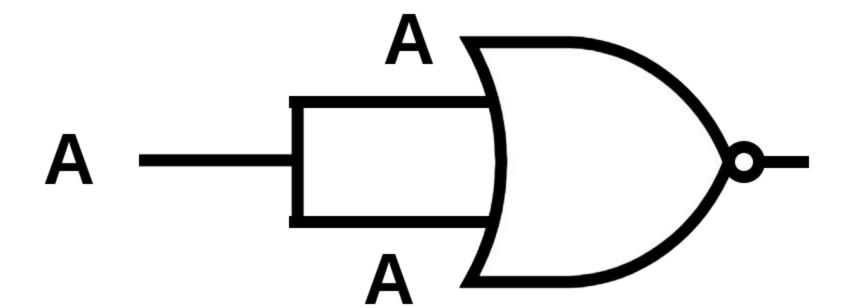
$$= (A + B) (C + D)$$

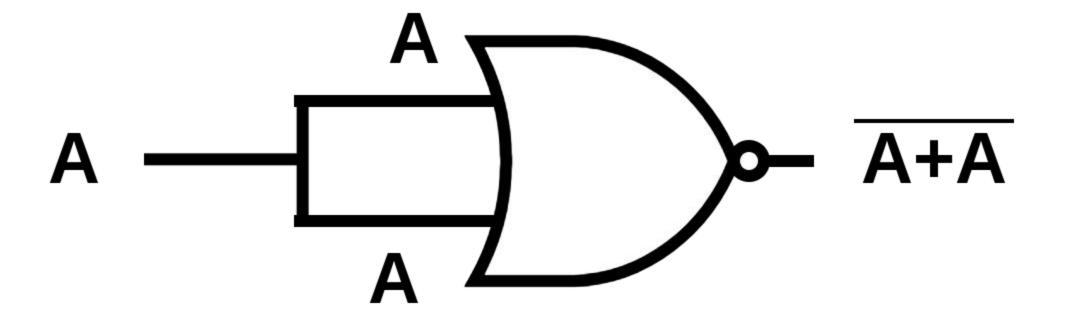
$$= (X+X) (Y+Y)$$

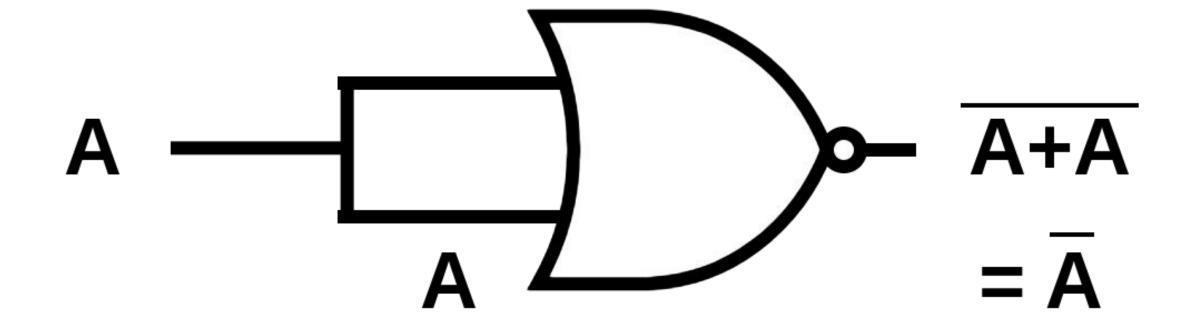


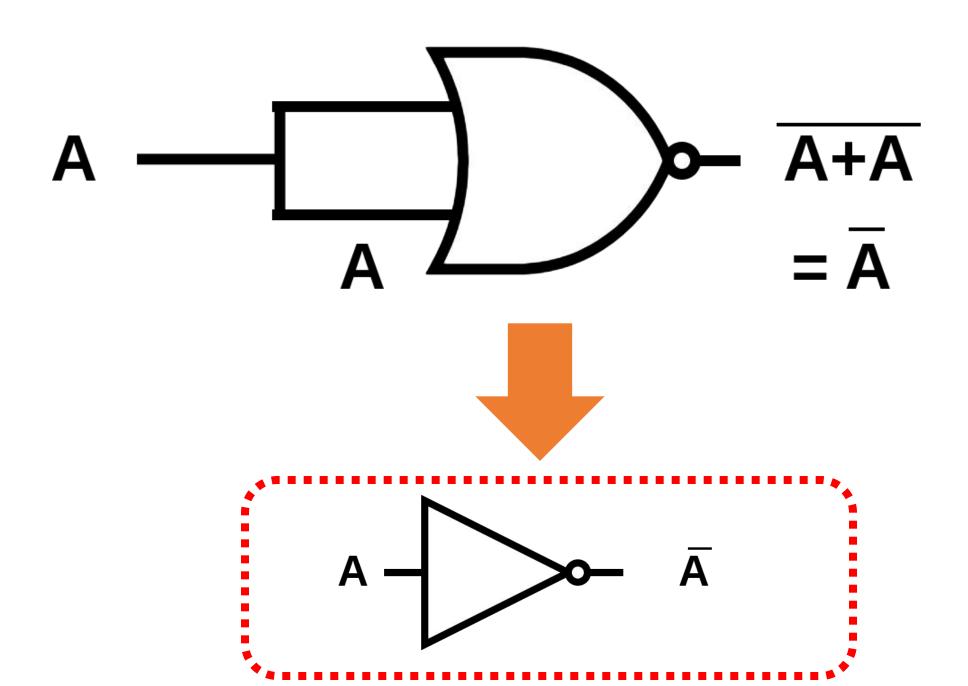
IF A=B=X and C=D=Y

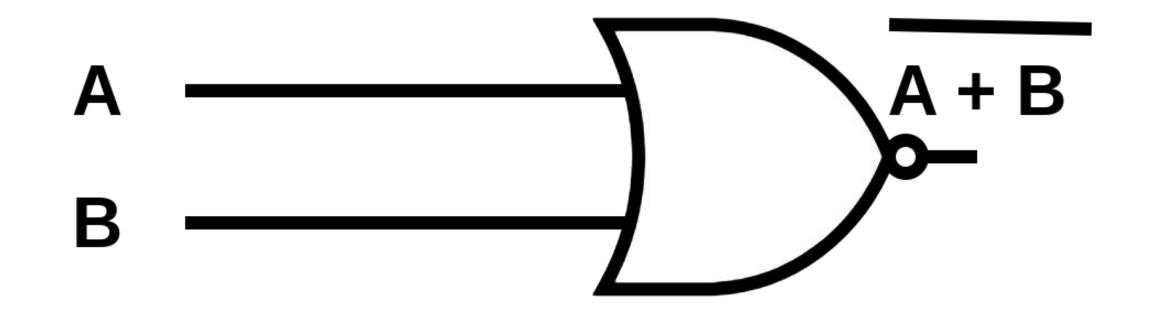


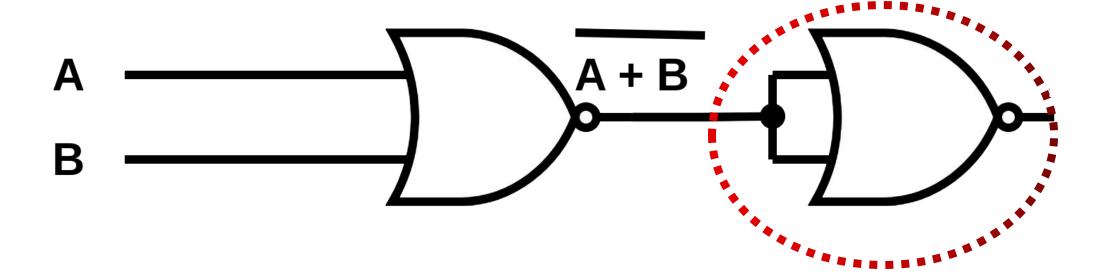


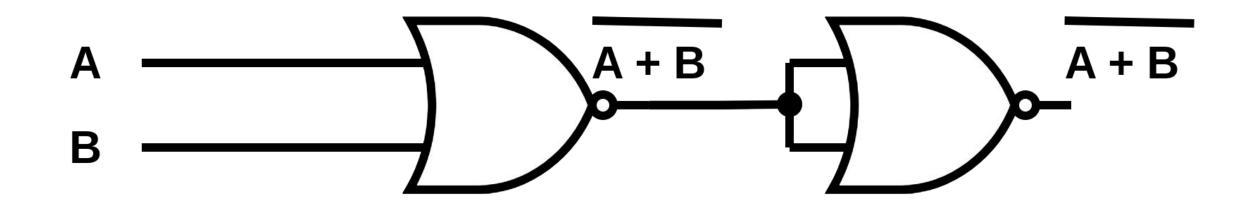


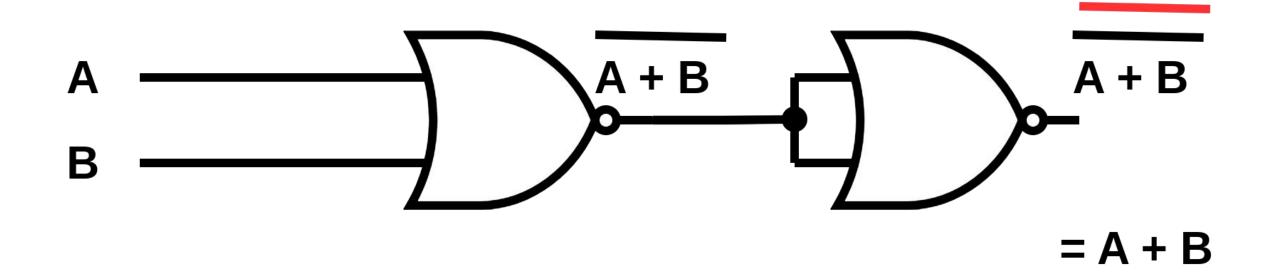


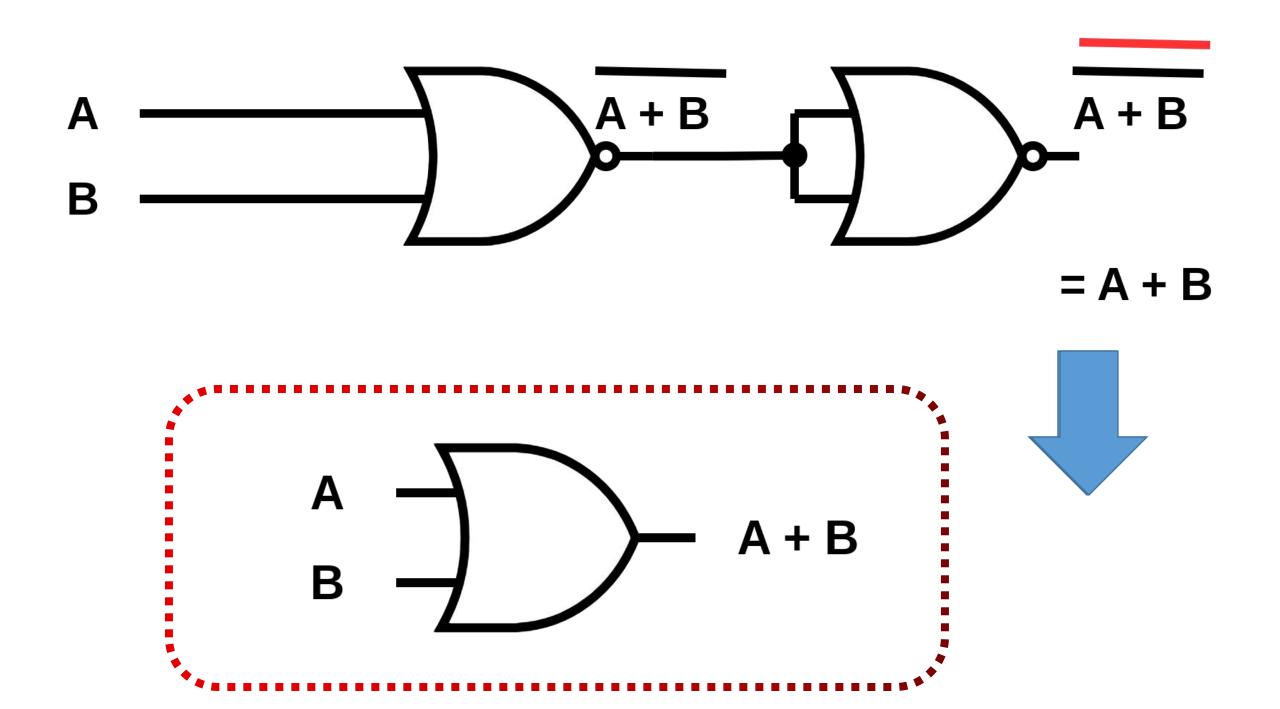












Solve 19-26 using 1's Complement

Solve 19-26 using 1's Complement

Let **19-26** = Result

19 + (-26) = Result

Apply 1's Complement on Both Sides

1's Complement of 19 + 1's Complement of (-26)= 1's Complement Of Result

Solve 19-26 using 1's Complement

Let **19-26** = Result

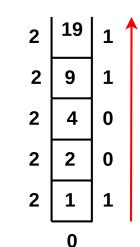
Apply 1's Complement on Both Sides

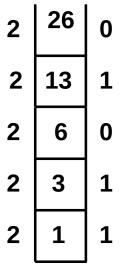
1's Complement of 19 + 1's Complement of (-26) = 1's Complement Of Result

Since Its a positive number, Its 1's Complement is same

$$1's Of +19 = 010011$$

Since Its a -ve number , Its 1's Complement will be





Solve 19-26 using 1's Complement

Let **19-26** = Result

Apply 1's Complement on Both Sides

1's Complement of 19 + 1's Complement of (-26) = 1's Complement Of Result

Binary Of 19 = 10011

SMR Binary Of **+19** = **010011**

Since Its a positive number, Its 1's Complement is same

1's Of +19 = 010011

Now, Binary Of **26**= **11010**

SMR Binary Of **-26** = **111010**

Since Its a -ve number , Its 1's Complement will be

1's Of -26 = 100101

010011

Solve 19-26 using 1's Complement

Let **19-26** = Result

Apply 1's Complement on Both Sides

1's Complement of 19 + 1's Complement of (-26) = 1's Complement Of Result

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010011
+ 100101

Solve 19-26 using 1's Complement

Let **19-26** = Result

Apply 1's Complement on Both Sides

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Since Its a **-ve** number , Its **1's** Complement will be

1's Of -26 = 100101

010011 + 100101 111000

Solve 19-26 using 1's Complement

Let **19-26** = Result

Apply 1's Complement on Both Sides

1's Complement of 19 + 1's Complement of (-26) = 1's Complement Of Result

Binary Of 19 = 10011

SMR Binary Of +19 = 010011

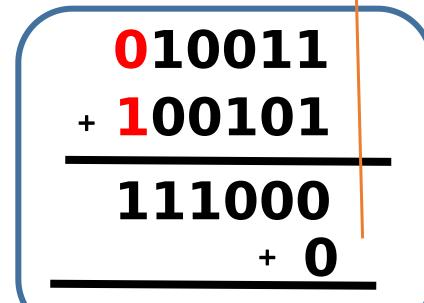
End Around Carry

Since Its a positive number, Its 1's Complement is same

$$1's Of +19 = 010011$$

Now, Binary Of **26**= **11010**

SMR Binary Of **-26** = **111010**



Solve 19-26 using 1's Complement

Let **19-26** = Result

Apply 1's Complement on Both Sides

1's Complement of 19 + 1's Complement of (-26) = 1's Complement Of Result

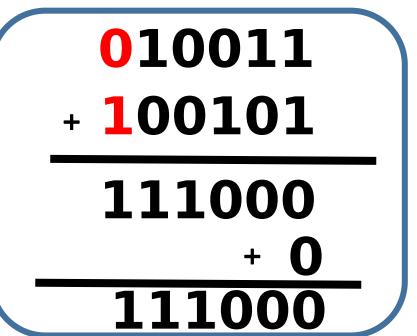
Binary Of
$$19 = 10011$$

Since Its a positive number, Its 1's Complement is same

$$1's Of +19 = 010011$$

Now, Binary Of **26**= **11010**

SMR Binary Of **-26** = **111010**



Solve 19-26 using 1's Complement

$$19+(-26) = Result$$

Apply 1's Complement on Both Sides

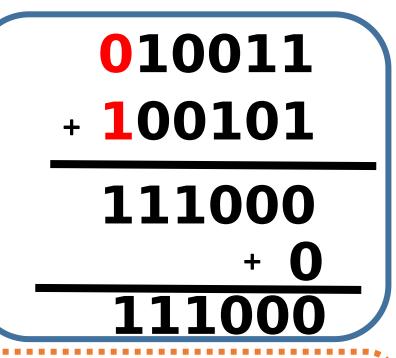
1's Complement of 19 + 1's Complement of (-26) = 1's Complement Of Result

Binary Of
$$19 = 10011$$

Since Its a positive number, Its 1's Complement is same

$$1's Of +19 = 010011$$

Since Its a **-ve** number , Its **1's** Complement will be



1's Com of Result: **111000**

Solve 19-26 using 1's Complement

Let **19-26** = Result

Apply 1's Complement on Both Sides

1's Complement of 19 + 1's Complement of (-26) = 1's Complement Of Result

SMR Binary Of **+19** = **010011**

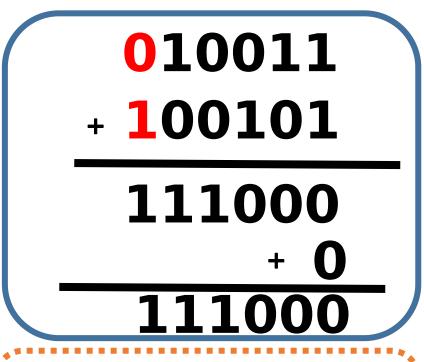
Since Its a positive number, Its 1's Complement is same

$$1's Of +19 = 010011$$

Now, Binary Of **26**= **11010**

SMR Binary Of **-26** = **111010**

Since Its a **-ve** number , Its **1's** Complement will be



1's Com of Result: 111000

Solve 19-26 using 1's Complement

Let **19-26** = Result

Apply 1's Complement on Both Sides

1's Complement of 19 + 1's Complement of (-26) = 1's Complement Of Result

SMR Binary Of +19 = 010011

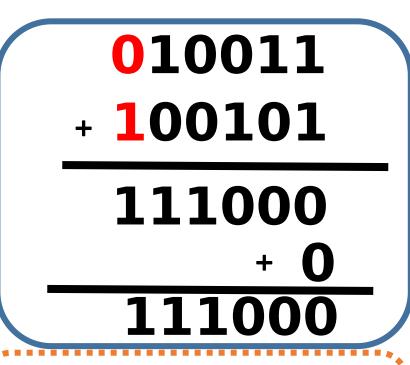
Since Its a positive number, Its 1's Complement is same

$$1's Of +19 = 010011$$

Now, Binary Of **26**= **11010**

SMR Binary Of **-26** = **111010**

Since Its a **-ve** number , Its **1's** Complement will be



1's Com of Result: 111000

Solve 19-26 using 1's Complement

Let **19-26** = Result

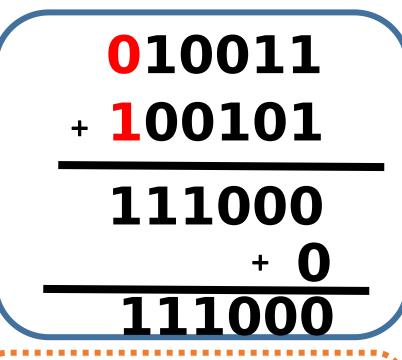
Apply 1's Complement on Both Sides

1's Complement of 19 + 1's Complement of (-26) = 1's Complement Of Result

Since Its a positive number, Its 1's Complement is same

$$1's Of +19 = 010011$$

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1's Com of Result: 111000

Solve 19-26 using 1's Complement

Let **19-26** = Result

Apply 1's Complement on Both Sides

1's Complement of 19 + 1's Complement of (-26) = 1's Complement Of Result

Binary Of **19** = **10011**

SMR Binary Of **+19** = **010011**

Since Its a positive number, Its 1's Complement is same

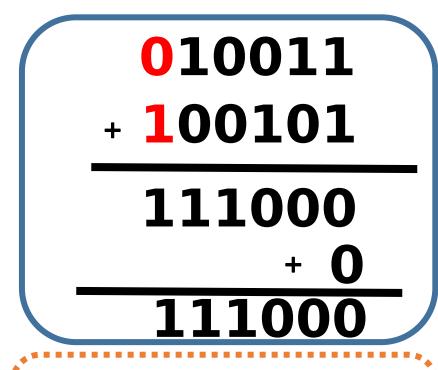
$$1's Of +19 = 010011$$

Now, Binary Of **26**= **11010**

SMR Binary Of **-26** = **111010**

Since Its a **-ve** number , Its **1's** Complement will be

1's Of -26 = 100101



1's Com of Result: **111000**

esult: 100111 -7

Solve 26-19 using 1's Complement

Solve 26-19 using 1's Complement

Let **26-19** = Result

Apply 1's Complement on Both Sides

1's Complement of 26 + 1's Complement of (-19) = 1's Complement Of Result

Since Its a positive number, Its 1's Complement is same

Now,

Binary Of **19**= **10011**

SMR Binary Of -19 = 110011

Since Its a -ve number , Its 1's Complement will be

011010

Solve 26-19 using 1's Complement

Let **26-19** = Result

Apply 1's Complement on Both Sides

1's Complement of 26 + 1's Complement of (-19) = 1's Complement Of Result

Since Its a positive number, Its 1's Complement is same

Now,

SMR Binary Of
$$-19 = 110011$$

Since Its a **-ve** number , Its **1's** Complement will be

011010 + 101100 1000110

Solve 26-19 using 1's Complement

Let **26-19** = Result

Apply 1's Complement on Both Sides

1's Complement of 26 + 1's Complement of (-19) = 1's Complement Of Result

Binary Of **26** = **11010**

SMR Binary Of **+26** = **011010**

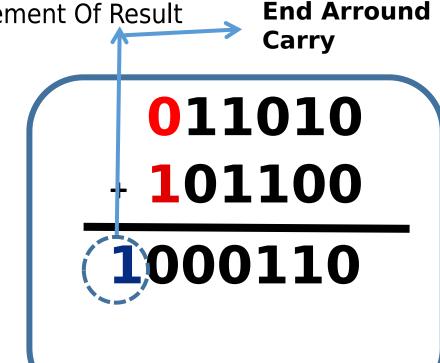
Since Its a positive number, Its 1's Complement is same

$$1's Of +26 = 011010$$

Now,

Binary Of **19**= **10011**

SMR Binary Of -19 = 10011



Solve 26-19 using 1's Complement

Let **26-19** = Result

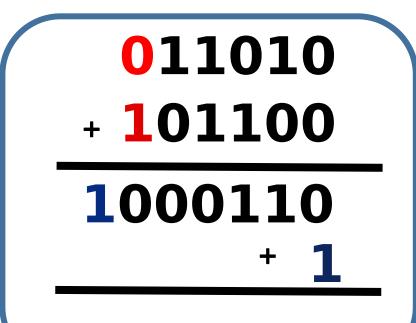
Apply 1's Complement on Both Sides

1's Complement of 26 + 1's Complement of (-19) = 1's Complement Of Result

Since Its a positive number, Its 1's Complement is same

Now,

SMR Binary Of
$$-19 = 110011$$



Solve 26-19 using 1's Complement

Let **26-19** = Result

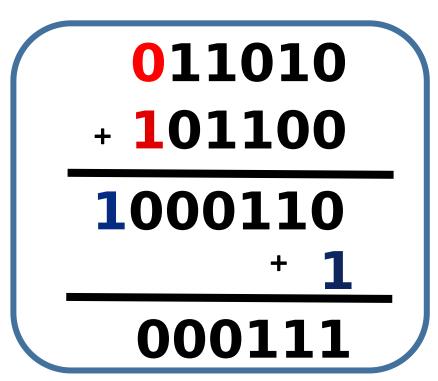
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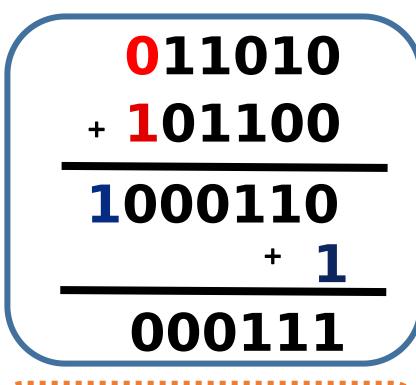
1's Complement of 26 + 1's Complement of (-19) = 1's Complement Of Result

Since Its a positive number, Its 1's Complement is same

Now,

SMR Binary Of
$$-19 = 10011$$

Since Its a **-ve** number , Its **1's** Complement will be



1's Com of Result: **000111**

Solve 26-19 using 1's Complement

Let **26-19** = Result

Apply 1's Complement on Both Sides

1's Complement of 26 + 1's Complement of (-19) = 1's Complement Of Result

Since Its a positive number, Its 1's Complement is same

$$1's Of +26 = 011010$$

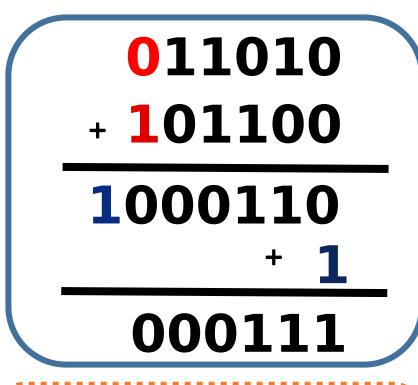
Now,

SMR Binary Of
$$-19 = 10011$$

Since Its a -ve number , Its 1's Complement will be

$$1's Of -19 = 101100$$

Sign Bit के छ?



1's Com of Result: 00111

Solve 26-19 using 1's Complement

Let **26-19** = Result

Apply 1's Complement on Both Sides

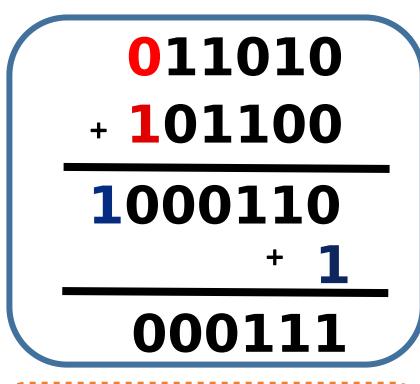
1's Complement of 26 + 1's Complement of (-19) = 1's Complement Of Result

Since Its a positive number, Its 1's Complement is same

Now,

SMR Binary Of
$$-19 = 110011$$

Since Its a **-ve** number , Its **1's** Complement will be



1's Com of Result: 000111

Using 2's Complement

$$26+(-7) = Result$$

26+(-7) = Result Apply 2's Complement on Both Sides

2's Complement of 26 + 2's Complement of (-7) = 2's Complement Of Result

Since Its a positive number, Its 2's Complement is same

Now

Binary Of
$$7 = 111$$

Note*: While doing Complement Arithmetic, Number of bits of second number should be equal to that of first Number

26+(-7) = Result Apply 2's Complement on Both Sides

2's Complement of 26 + 2's Complement of (-7) = 2's Complement Of Result

Since Its a positive number, Its 2's Complement is same

Now

Binary Of
$$7 = 111$$

Note*: While doing Complement Arithmetic, Number of bits of second number should be equal to that of first Number

$$26+(-7) = Result$$

26+(-7) = Result Apply 2's Complement on Both Sides

2's Complement of 26 + 2's Complement of (-7) = 2's Complement Of Result

Since Its a positive number, Its 2's Complement is same

Now

Binary Of
$$7 = 00111 \rightarrow 5$$
 Bits

Note*: While doing Complement Arithmetic, Number of bits of second number should be equal to that of first Number

Apply 2's Complement on Both Sides

2's Complement of 26 + 2's Complement of (-7) = 2's Complement Of Result

Since Its a positive number, Its 2's Complement is same

Now

Binary Of
$$7 = 00111$$

Since Its a **-ve** number , Its **2's** Complement will be

Right Hande Side Bata हेर्दी जाने जब सम्मन 1 भेटीन्न, And When You Find First 1, You copy as it is upto there and STOP

Apply 2's Complement on Both Sides

2's Complement of 26 + 2's Complement of (-7) = 2's Complement Of Result

Since Its a positive number, Its 2's Complement is same

Now

Binary Of
$$7 = 00111$$

Since Its a -ve number , Its 2's Complement will be

Right Hande Side Bata हर्दो जाने जब सम्मन 1 भेटीन्न, And When You Find First 1, You copy as it is upto there and STOP

Complement the Remaining MAgnitude Bits

Apply 2's Complement on Both Sides

2's Complement of 26 + 2's Complement of (-7) = 2's Complement Of Result

Since Its a positive number, Its 2's Complement is same

Now

Binary Of
$$7 = 00111$$

Since Its a -ve number , Its 2's Complement will be

Right Hande Side Bata हर्दो जाने जब सम्मन 1 भेटीन्न, And When You Find First 1, You copy as it is upto there and STOP

Complement the Remaining Magnitude Bits

Apply 2's Complement on Both Sides

2's Complement of 26 + 2's Complement of (-7) = 2's Complement Of Result

Since Its a positive number, Its 2's Complement is same

Now

Binary Of
$$7 = 00111$$

Since Its a -ve number , Its 2's Complement will be

011010

Apply 2's Complement on Both Sides

2's Complement of 26 + 2's Complement of (-7) = 2's Complement Of Result

Since Its a positive number, Its 2's Complement is same

Now

Binary Of
$$7 = 00111$$

Since Its a -ve number , Its 2's Complement will be

011010
111001

Apply 2's Complement on Both Sides

2's Complement of **26** + 2's Complement of (-7) = 2's Complement Of Result

Since Its a positive number, Its 2's Complement is same

Now

Binary Of
$$7 = 00111$$

Since Its a -ve number , Its 2's Complement will be

011010 + 111001 1010011

Apply 2's Complement on Both Sides

2's Complement of 26 + 2's Complement of (-7) = 2's Complement Of Result

Since Its a positive number, Its 2's Complement is same

DISCARD END CARRY

Now

Binary Of
$$7 = 00111$$

Since Its a -ve number , Its 2's Complement will be

11010 + 111001 1010011

Apply 2's Complement on Both Sides

2's Complement of **26** + 2's Complement of (**-7**) = 2's Complement Of Result

Since Its a positive number, Its 2's Complement is same

DISCARD END CARRY

Now

Binary Of
$$7 = 00111$$

Since Its a **-ve** number , Its **2's** Complement will be

011010 + 111001 1010011

2's Com of Result: **010011**

Apply 2's Complement on Both Sides

2's Complement of **26** + 2's Complement of (-7) = 2's Complement Of Result

Since Its a positive number, Its 2's Complement is same

DISCARD END CARRY

Now

Binary Of
$$7 = 00111$$

Since Its a **-ve** number , Its **2's** Complement will be

11010 + 111001 1010011

2's Com of Result: **010011**

Apply 2's Complement on Both Sides

2's Complement of **26** + 2's Complement of (-7) = 2's Complement Of Result

Since Its a positive number, Its 2's Complement is same

DISCARD END CARRY <

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Binary Of
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Since Its a -ve number , Its 2's Complement will be

Sign Bit के छ?

011010 + 111001 1010011

2's Com of Result: **010011**

Apply 2's Complement on Both Sides

2's Complement of **26** + 2's Complement of (-7) = 2's Complement Of Result

Since Its a positive number, Its 2's Complement is same

DISCARD END CARRY

Now

Binary Of
$$7 = 00111$$

Since Its a -ve number , Its 2's Complement will be

+ve, So No Change

011010 + 111001 1010011

2's Com of Result: **010011**

Apply 2's Complement on Both Sides

2's Complement of **26** + 2's Complement of (-7) = 2's Complement Of Result

Since Its a positive number, Its 2's Complement is same

DISCARD END CARRY

Now

Binary Of
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Since Its a -ve number , Its 2's Complement will be

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011010 + 111001 1010011

2's Com of Result: **010011**

Apply 2's Complement on Both Sides

2's Complement of **26** + 2's Complement of (-7) = 2's Complement Of Result

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DISCARD END CARRY

Now

Binary Of
$$7 = 00111$$

Since Its a **-ve** number , Its **2's** Complement will be

011010 + 111001 1010011

2's Com of Result: **010011**

Assignment Work

Solve 7-26 using 2's Complement

Class Work

Solve 7-26 using 2's Complement

Apply 2's Complement on Both Sides

2's Complement of 7 + 2's Complement of (-26) = 2's Complement Of Result

Since Its a positive number, Its 2's Complement is same

$$2's Of +7 = 000111$$

Now

Since Its a -ve number, Its 2's Complement will be

000111 + 100110 0101101

2's Com of Result: **101101**



The OverFlow

Solve Using 2's Complement

Solve Using 2's Complement

SMR Of
$$-2 = 110$$

2's Complement Of -3: 101

Solve Using 2's Complement

SMR Of
$$2 = 010$$

2's Complement Of +2: 010

SMR Of
$$-2 = 110$$

2's Complement Of -2 : **110**

2's Complement Of +3: **011**

SMR Of
$$-3 = 111$$

2's Complement Of -3 : **101**

- a) -3+2 b) -2+3
- c) 3+2 d) -3-2

2's Complement Of +2 : **010**

2's Complement Of -2 : **110**

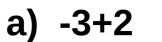
2's Complement Of +3: **011**

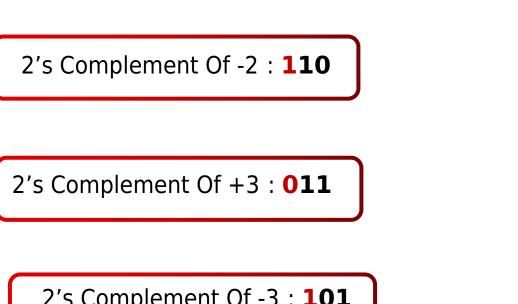
2's Complement Of -3: **101**

- a) -3+2 b) -2+3
- d) -3-2 c) 3+2

2's Complement Of +2 : **010**

2's Complement Of -3: 101





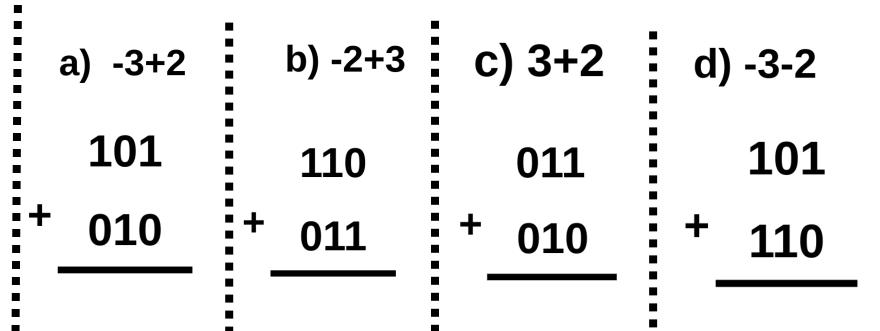
- a) -3+2 b) -2+3
- c) 3+2 d) -3-2

2's Complement Of +2 : **010**

2's Complement Of -2 : **110**

2's Complement Of +3: 011

2's Complement Of -3 : **101**



- a) -3+2 b) -2+3
- c) 3+2 d) -3-2

2's Complement Of +2 : **010**

2's Complement Of -2 : **110**

2's Complement Of +3: 011

2's Complement Of -3: 101

Solve Using 2's Complement



a) -3+2

b) -2+3

011

c) 3+2

d) -3-2

- 101
- 110
- 011

010

110

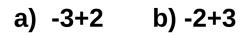
101

- 010
 - 0111
- 2's Com Of Result

Result
$$= -1$$

$$= 111$$





2's Complement Of -2: **110**

2's Complement Of +3: 011

2's Complement Of -3: 101

101



110

011

101

010

2's Com

= 111

101

Of Result

$$= 001$$

a) -3+2

b) -2+3

c) 3+2

d) -3-2

2's Complement Of +2 : **010**

2's Complement Of -2 : **110**

2's Complement Of +3: **011**

2's Complement Of -3: 101



a) -3+2

101



b) -2+3

110

011

c) 3+2

d) -3-2

011

+ 110

101

+ 010

2's Com

= 111

= 101

Of Result

0111

1001

0101

010

2's Com 2's Com
Of Result
= 001 = 101

= 001

Result = -1 Result = 1

= 111

Result = -3:

- a) -3+2 b) -2+3
- c) 3+2 d) -3-2

2's Complement Of +2 : **010**

2's Complement Of -2: **110**

2's Complement Of +3: 011

2's Complement Of -3: 101



a) -3+2

101



b) -2+3

110

c) 3+2

d) -3-2

Solve Using 2's Complement

010

011

1001

: Of Result:

2's Com

010

011

0101

= 111

110

101

1011

2's Com Of Result

0111

= 111

= 101

= 001

= 001

2's Com 2's Com Of Result Of Result = 101

= 011

Result = -3: Result = 3

Result = -1:Result = 1

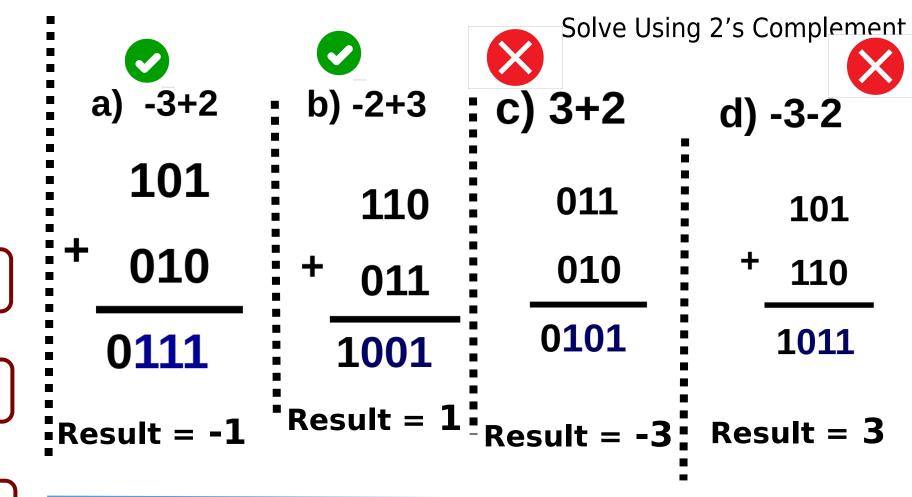
- a) -3+2 b) -2+3
- c) 3+2 d) -3-2

2's Complement Of +2 : **010**

2's Complement Of -2 : **110**

2's Complement Of +3: 011

2's Complement Of -3: 101



The Range Of The Decimal Number Which Can Be Represented using 3 bit 2's Complement form is -4 to 3.

-2ⁿ⁻¹ to 2ⁿ⁻¹-1

• • •





The Range Of The Decimal Number Which Can Be Represented using 3 bit 2's Complement form is -4 to 3.

 -2^{n-1} to $2^{n-1}-1$

Opposite Signs Will Cancel Out Each Others Magnitude, So it will never be out of Range.

Same Signs Will Increase Magnitude, So there is chances Out Of Range. For Example, 2+1 and -1-2 won't overflow, though they have same Sign

OverFlow May Occur On Addition Of Two Numbers with same sign.

The Range Of The Decimal Number Which Can Be Represented using 3 bit 2's Complement form is -4 to 3.



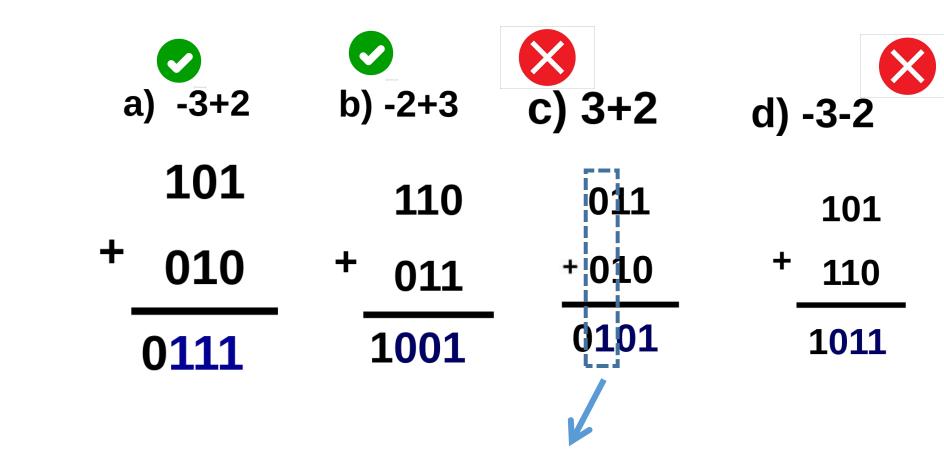
d) -3-2

 -2^{n-1} to $2^{n-1}-1$

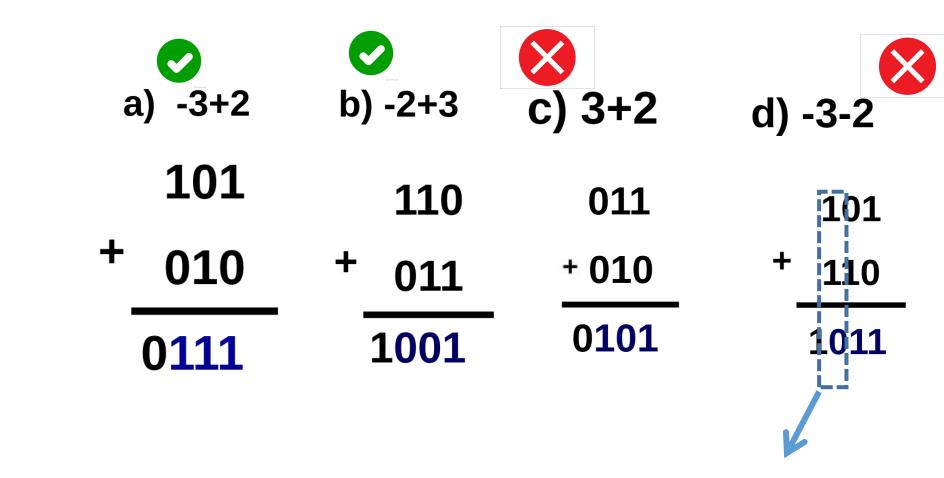
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Same Signs Will Increase Magnitude, So there is chances Out Of Range. For Example, 2+1 and -1-2 won't overflow, though they have same Sign

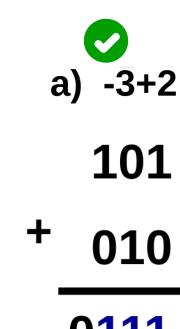
OverFlow May Occur On Addition Of Two Numbers with same sign.



2 +ve Numbers Sum is Coming in -ve ढुक्क Overflow



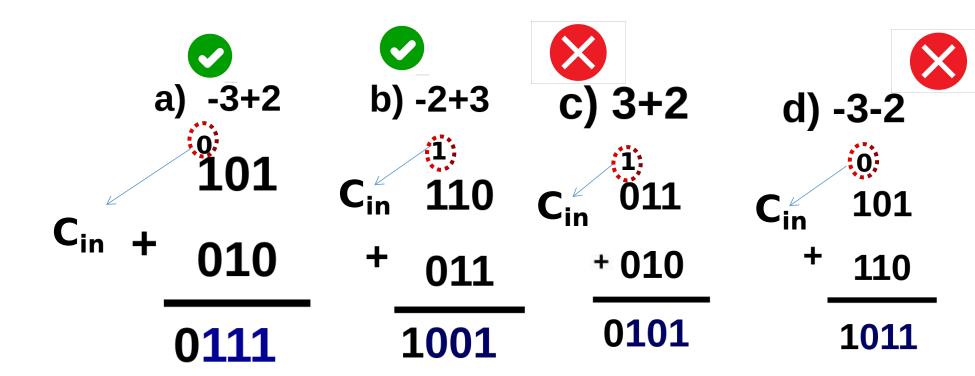
2 -ve Numbers Sum is Coming in +ve ढुक्क Overflow

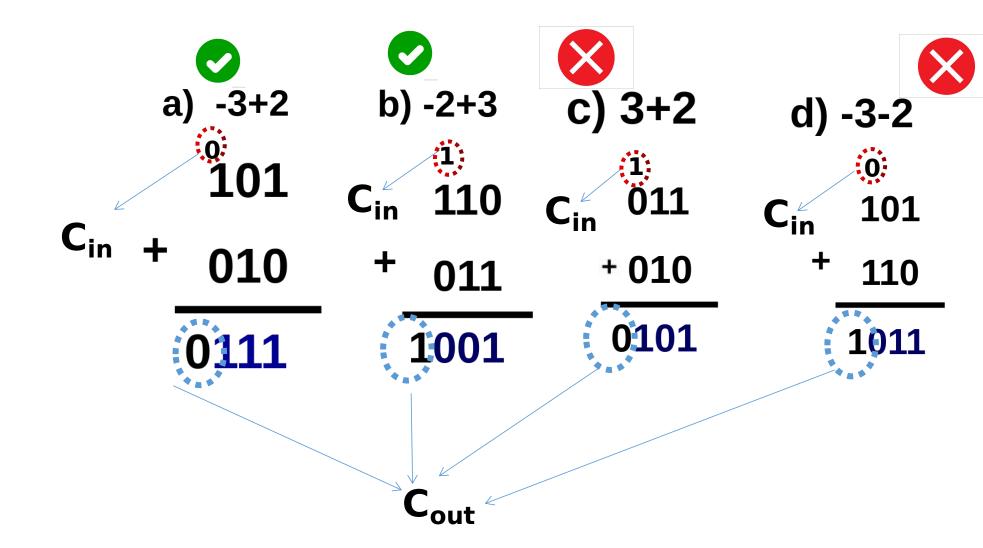


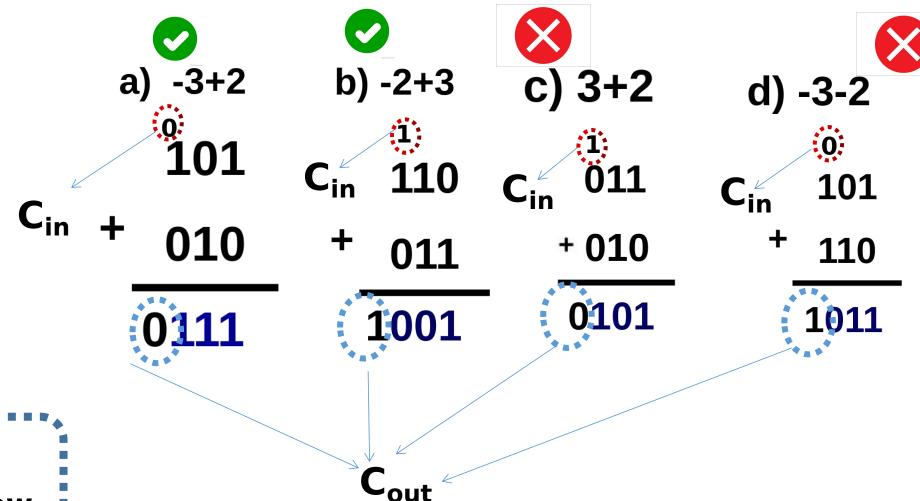


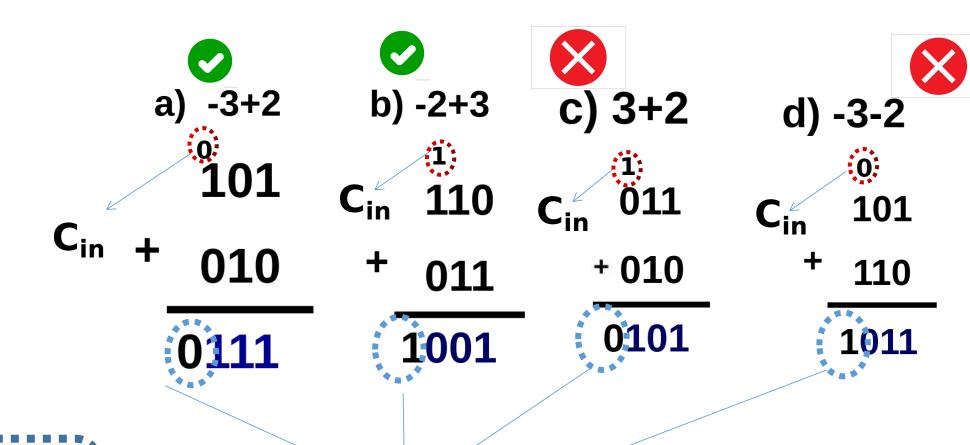












IF
$$C_{in} \oplus C_{out} = 1$$

= 100% OverFlow