

# Extracting Parallelism (2D cases)

## 1. Coin Collection

Q. Complexity  $O(n \cdot m)$

Dependency

$$F[n][m] - 11$$

①

$$\left. \begin{array}{l} F[0][1]w, \dots, F[0][m]w \\ F[0][2]w \end{array} \right\} Km$$

$$\textcircled{m} \rightarrow \textcircled{m-1} \rightarrow \dots$$

$$\textcircled{1} \rightarrow \textcircled{0}$$

$$F[1][0]w$$

$$F[1][2]w$$

$$F[1][3]w$$

⋮

$$F[1][m]w$$

$$F[2][0]w$$

$$F[2][2]w$$

$$F[2][3]w$$

⋮

$$F[2][m]w$$

⋮

⋮

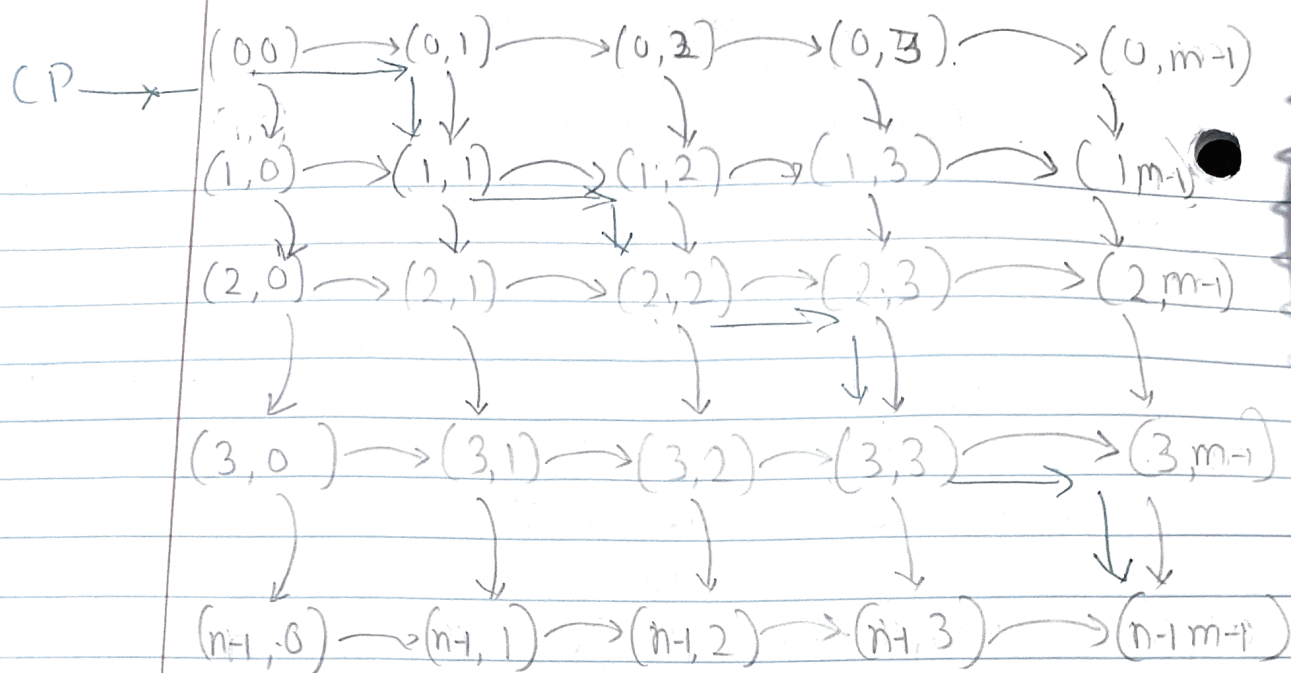
$$F[n][0]w$$

$$F[n][2]w$$

$$F[n][3]w$$

⋮

$$F[n][m]w$$



Work  $(n+1) \cdot (m+1) = \Theta(n \times m)$

Width  $n+1, m+1 = \Theta(n+m)$

Critical Path:  $1 + (n-1) + (m-1) = \Theta(n+m)$

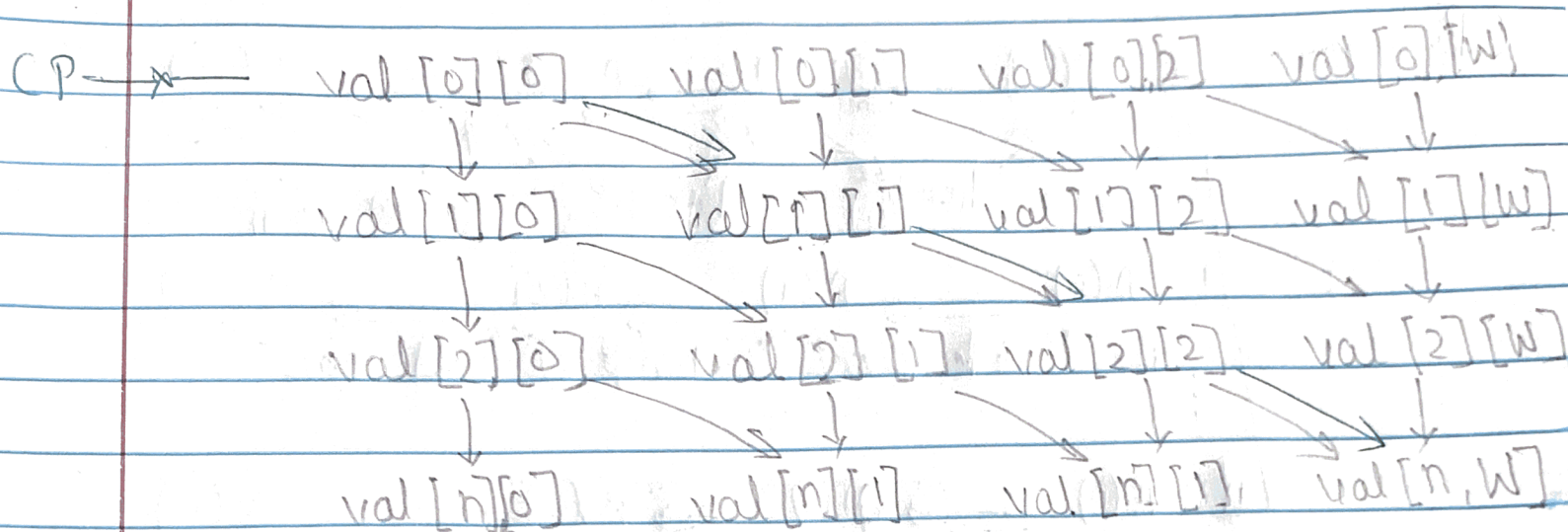
# Knapsack

Q. Complexity

Soln  $\Rightarrow$

$$\theta(n \cdot w)$$

Q. Dependencies



width  $\Rightarrow$   $w$   $\theta(w)$

work  $(w+1)(n+1) \theta(w \cdot n)$

Critical Path:

$n > w: n \theta(n)$

$w > n: w \theta(w)$

} length



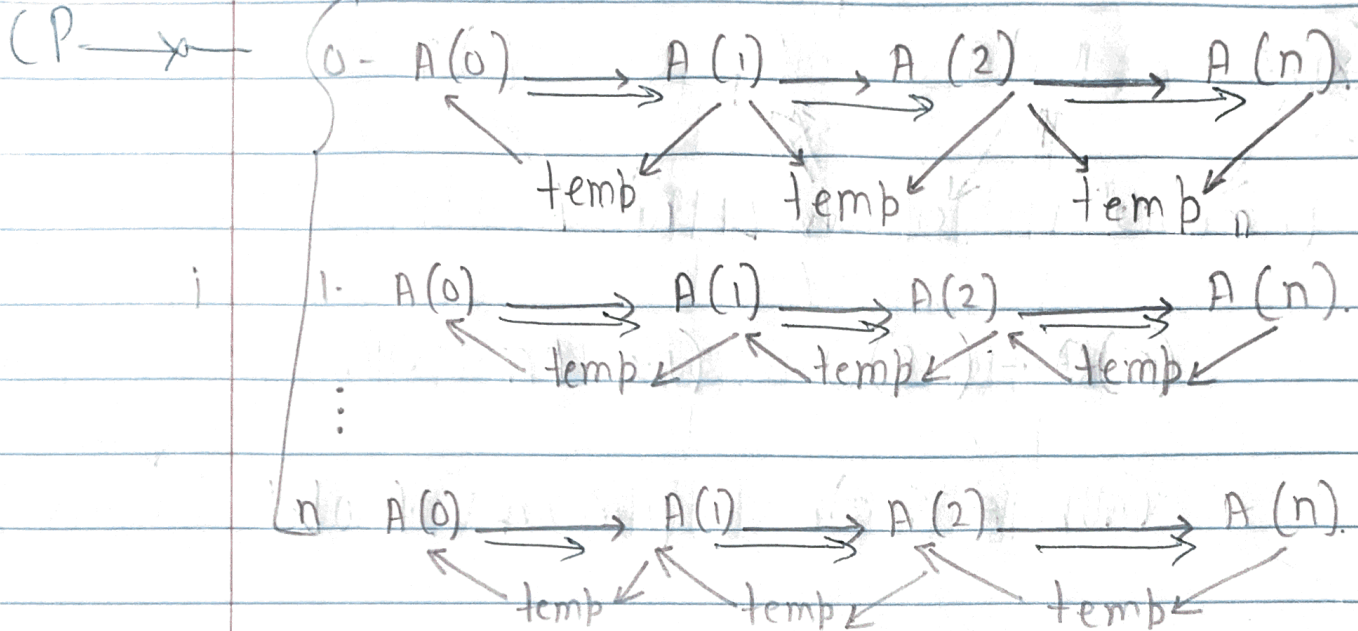
# Bubble Sort

Q. Complexity

Soln -

$$O(n^2)$$

Q Dependencies.



Width

$$n/2$$

$\Theta(n/2)$  (Swapping alternately)

Work

$$n$$

Critical Path

$$n^2$$

$$\Theta(n^2)$$