

1 d)

$$P(s) = s^4 + s^3 + 3s^2 + 3s + 2$$

two
sign
changes

+4	1	3	2		
+3	1	3			
+2	ϵ	2			
-1	$\frac{3\epsilon-2}{\epsilon}$				
+0	2				

$$b_{n-1} = - \frac{(1 \cdot 3 - 1 \cdot 3)}{1}$$

$$= \phi$$

$$b_{n-3} = - \frac{(1 \cdot 0 - 1 \cdot 2)}{1}$$

$$= 2$$

Special case 1:

- If a first-column term in any row is zero, but the remaining terms are not zero or there is no remaining term
- the zero term is replaced by a very small positive number ϵ .

$$c_{n-1} = - \frac{(1 \cdot 2 - \epsilon \cdot 3)}{\epsilon} = \frac{3\epsilon - 2}{\epsilon}$$

$$d_{n-1} = - \frac{(\epsilon \cdot \phi - \frac{3\epsilon - 2}{\epsilon} \cdot 2)}{\frac{3\epsilon - 2}{\epsilon}} = 2$$

considering $\epsilon > 0$ (but very small):

$$\frac{3\epsilon - 2}{\epsilon} = 3 - \frac{2}{\epsilon} \rightarrow c_{n-1} \text{ will have negative sign}$$

∴ $P(s)$ has two roots with real part.