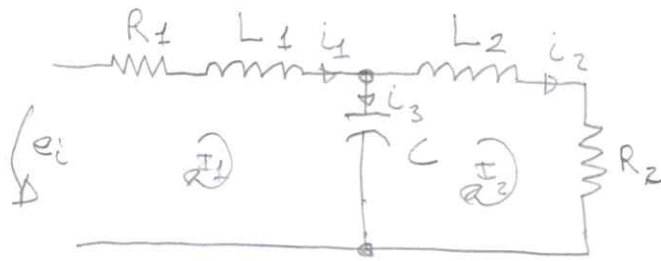


1b)



$$\frac{i_2(s)}{E_i(s)} = ?$$

$$\begin{cases} e_i = R_1 i_1(t) + L_1 \frac{d}{dt} i_1(t) + \frac{1}{C} \int i_1(t) dt - \frac{1}{C} \int i_2(t) dt \\ 0 = L_2 \frac{d}{dt} i_2(t) + R_2 i_2(t) + \frac{1}{C} \int i_2(t) dt - \frac{1}{C} \int i_1(t) dt \\ i_1(t) = i_3(t) + i_2(t) \end{cases}$$

$L$ ; valores iniciales nulos.

$$\begin{cases} E_i(s) = R_1 I_1(s) + L_1 s I_1(s) + \frac{1}{C} \frac{1}{s} I_1(s) - \frac{1}{sC} I_2(s) \\ 0 = L_2 s I_2(s) + R_2 I_2(s) + \frac{1}{sC} I_2(s) - \frac{1}{sC} I_1(s) \\ I_1(s) = I_3(s) + I_2(s) \end{cases}$$

$$\begin{cases} E_i(s) = (R_1 + sL_1 + \frac{1}{sC}) I_1(s) - \frac{1}{sC} I_2(s) \\ \frac{1}{sC} I_1(s) = (L_2 s + R_2 + \frac{1}{sC}) I_2(s) \Rightarrow I_1(s) = sC (L_2 s + R_2 + \frac{1}{sC}) I_2(s) \\ = (s^2 L_2 C + sR_2 C + 1) I_2(s) \end{cases}$$

$$E_i(s) = (R_1 + sL_1 + \frac{1}{sC}) \cdot (s^2 L_2 C + sR_2 C + 1) I_2(s) - \frac{1}{sC} I_2(s)$$

expand.

$$\begin{aligned} E_i(s) &= (s^2 R_1 L_2 C + s R_1 R_2 C + R_1 + s^3 L_1 L_2 C + s^2 L_1 R_2 C + s L_1 + \\ &\quad s L_2 + R_2 + \frac{1}{sC}) I_2(s) - \frac{1}{sC} I_2(s) \\ &= (s^2 R_1 L_2 C + s R_1 R_2 C + R_1 + s^3 L_1 L_2 C + s^2 L_1 R_2 C + s L_1 + s L_2 + R_2) \\ &\quad I_2(s) \end{aligned}$$

$$\frac{I_2(s)}{E_i(s)} = \frac{1}{s^3 L_1 L_2 C + s^2 (R_1 L_2 C + L_2 R_2 C) + s (R_1 R_2 C + L_1 + L_2) + R_1 + R_2}$$

1b)

$$\begin{pmatrix} E_i(s) \\ 0 \end{pmatrix} = \begin{bmatrix} sL_1 + R_1 + \frac{1}{sC} & -\frac{1}{sC} \\ -\frac{1}{sC} & sL_2 + R_2 + \frac{1}{sC} \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$

$$\begin{pmatrix} E_i(s) \\ 0 \end{pmatrix} = \begin{bmatrix} sL_1 + R_1 + \frac{1}{sC} & -\frac{1}{sC} \\ -1 & s^2 L_2 C + sR_2 C + 1 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$

$$I_2(s) = \frac{\begin{bmatrix} sL_1 + R_1 + \frac{1}{sC} & -\frac{1}{sC} \\ -1 & 0 \end{bmatrix} E_i(s)}{\begin{vmatrix} sL_1 + R_1 + \frac{1}{sC} & -\frac{1}{sC} \\ -1 & s^2 L_2 C + sR_2 C + 1 \end{vmatrix}}$$

$$= \frac{E_i(s)}{(sL_1 + R_1 + \frac{1}{sC})(s^2 L_2 C + sR_2 C + 1) - \frac{1}{sC}}$$

c.a)

$$s^3 L_1 L_2 C + s^2 L_1 R_2 C + sL_1 + s^2 L_2 R_1 C + sR_1 R_2 C + R_1 + sL_2 + R_2 + \frac{1}{sC} - \frac{1}{sC}$$