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Lecture 2 summary.

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## LOGIC GATES

AND Gate- it takes two inputs

TRUTH table

Input	Input	Output
0	0	0
1	0	0
0	1	0
1	1	1

OR GATE - takes two inputs

Truth Table

Input	Input	Output
0	0	0
0	1	1
1	0	1
1	1	1

NOT gate takes only a single input.

### Quantifiers

-it contains a formula which indicates the statement whose true value depends on the value of some variable.

-It is used to quantify the variables of predicates.

Two types of quantifiers:-

### Existential quantifiers-

- The existential quantifier are a type of element that contains some properties and denoted by  $\exists$ .
- ' $\exists$ ' this symbol is referred with a phrase 'there exists'.

### Universal quantifier-

If the properties are true for all the given variable values of a given domain than it is known as domain of discourse.

It is denoted with a symbol ' $\forall$ ' and is referred with a phrase 'for all'.

Operator related notions

#### 1. Commutative property

It is indicated with the arithmetic operation of addition and multiplication.

Changing the order or position of two numbers does not change the final result.

$$\forall x,y \mid X \circ Y = Y \circ X$$

For e.g.

$$3+5=5+3=8$$

Non commutative

Negation of a quantifier statement

$$\bullet \exists x,y \mid X \circ Y \neq Y \circ X$$

Division, Subtraction and concatenation are non-commutative.

For e.g.

$$4-8=-4$$

$$8-4=4$$

#### 2 . Associative property

The way in which numbers are bracketed, does not affect their final result.

Addition and multiplication are mainly denoted as associative.

Matrix multiplication is one of the example.

$$\text{For e.g. } (1+7)+3=1+(7+3)=11$$

Non associative

Division and subtraction are non associative. For e.g.

$$101-34-36=31 \text{ and } 101-(34-36)=103$$

#### 3 . Distributive property

It indicates the operation that includes dividing and distributing the elements

Addition cannot be distributed over multiplication whereas multiplication is distributed over addition.

For e.g.

$$4(8+3)=(4*8)+(4*3)$$

Non distributive e.g.

$$4(8+3) \neq 4+(8*3)$$

**Short Circuit evaluation :-**

AND Gate- as soon as AND gate encounters 0 as input it stops there for evaluation and output is given as 0.

OR Gate - when OR gate encounters 1 as input it stops evaluation there and output is given as 1.

AND is indicated for multiplication

OR is indicated for addition

**Proper bracketing** should be taken into consideration while using AND and OR together.

$(p \wedge q \vee r)$  —> Ambiguity

$(p \wedge q \wedge r)$  —> Correct operation

$(P \vee q \vee r)$  —> Correct operation