

8th September 2022(Thursday)

Scribed Notes-Lecture 12

Student ID's

202212071

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Partial Order:

A partial order is a reflexive, anti-symmetric and transitive relation on a set.

Partial order is bounded by lower and upper value.

Transitive relations :

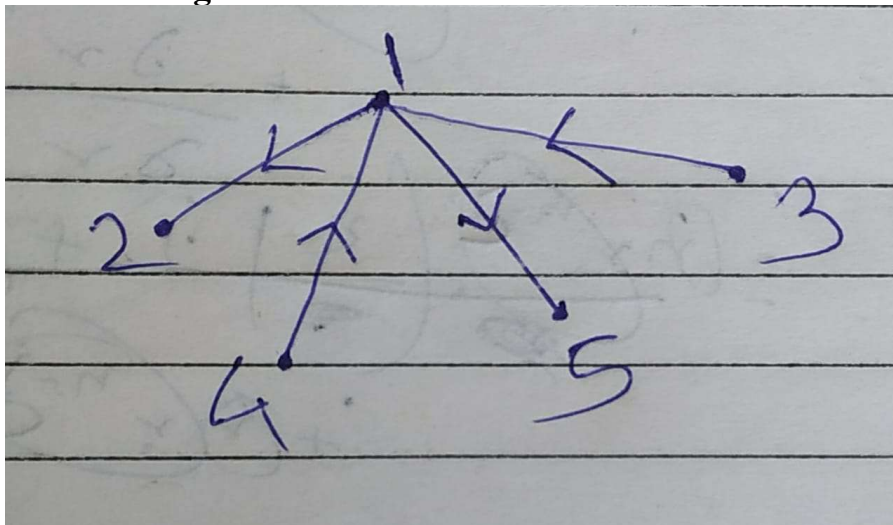
In transitive relation indirect path implies direct path.

$(a, b) \in R \ \& \ (b, c) \in R \Rightarrow (a, c) \in R$

Transitive Closure:

It can be achieved by applying transitivity rule again and again until applied iterative relation doesn't result in any change.

HASSE Diagram:



In Hasse diagram if there is a indirect path between two nodes then it removes the direct edge.

$S = \{1, 2, 3, 4, 5\}$

$R = \{(1, 1), (2, 2), (3, 3), (4, 4), (5, 5), (1, 2), (4, 1), (3, 1), (1, 5)\}$

Sink:

A node which has no outgoing arrow but has incoming arrow.

Ex. 2, 5 are sink.

Source:

A node which has no incoming arrow. but has outgoing arrow.

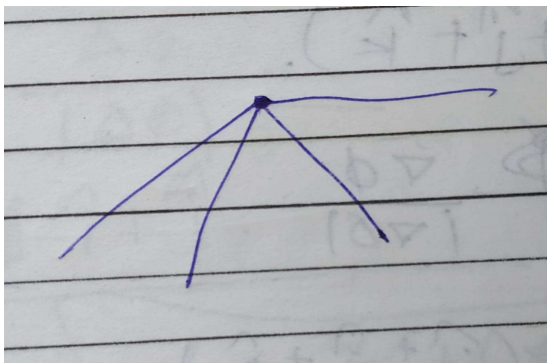
Ex. 3, 4

Others:

A node which has both incoming and outgoing arrow.

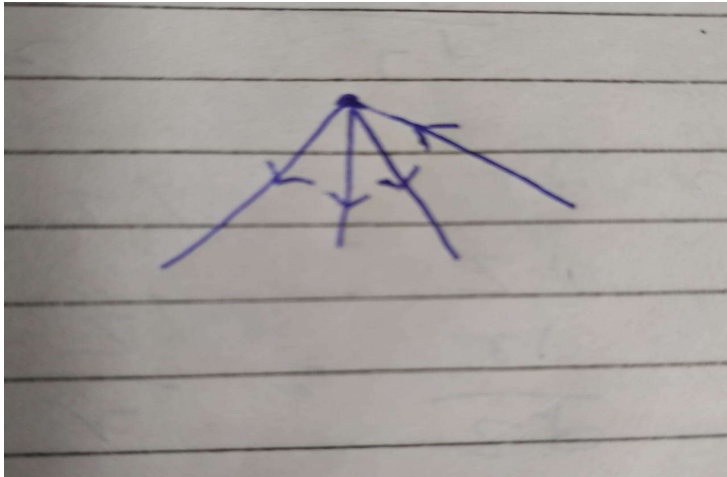
Ex. 1

Undirected Graph



Undirected Graph has degree 4.

Directed acyclic graph (DAG) is a directed graph with no directed cycles.



Directed Graph

Concept of indegree, outdegree

Degree=4

Indegree=1

Outdegree=3

Where Indegree=0 its called Source

Where Outdegree=0 its called Sink

Where Not Source NOT Sink it is Others

There are Three Categories of partial order:

Upper Lattice, Lower Lattice, Lattice

Upper Lattice(Unique source)

Lower Lattice(Unique sink)

Lattice(upper[^]lower)

Every Partial Order has ≥ 1 Source, sink