

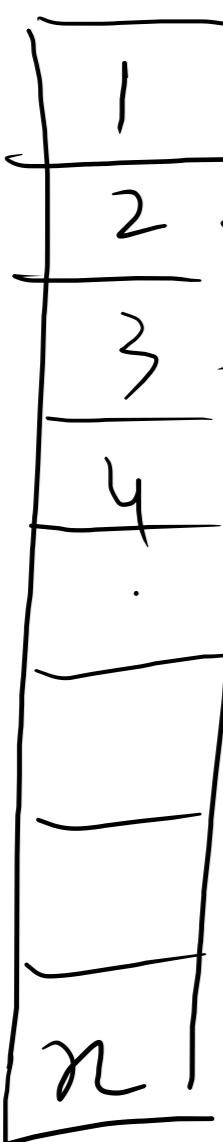
## Graph representations

### Adjacency matrix

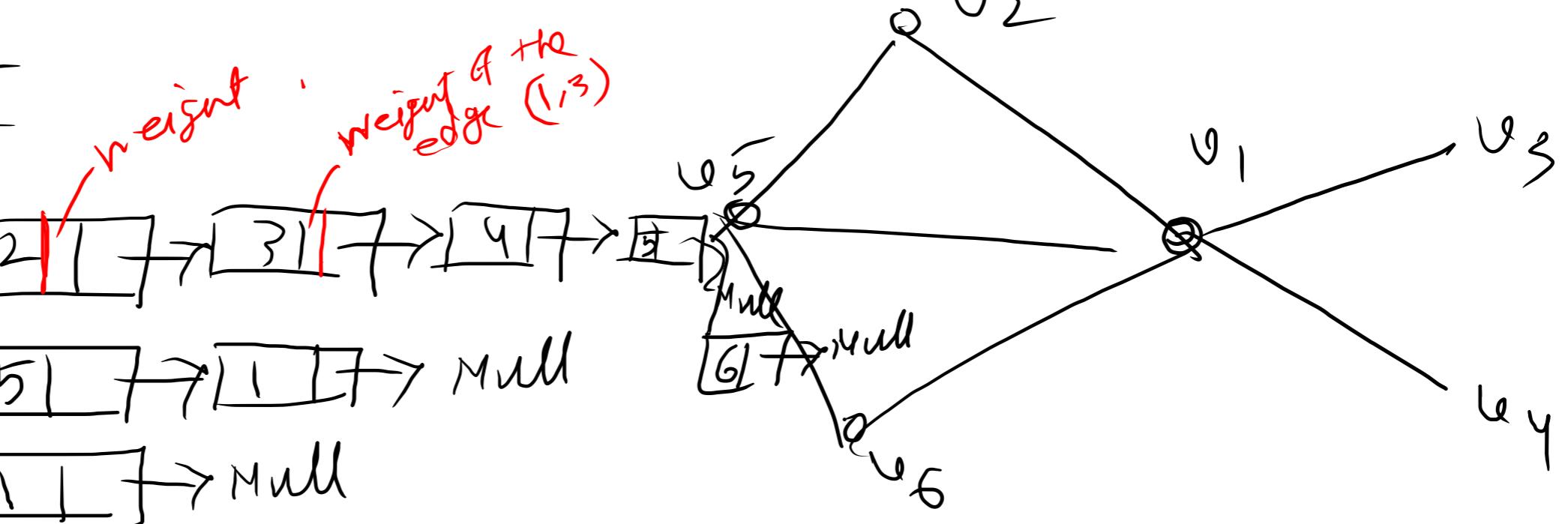
$$M = \begin{bmatrix} & & \\ & & \\ & & \\ & & \\ & & \\ & & \end{bmatrix}$$

$n \times n$

## Adjacency list



Adj:



undirected      unweighted

Space requirement:

- Adjacency Matrix :  $O(|V|^2)$  Sparse  $\ll |V|^2$
- Adjacency List :  $O(|V| + |E|)$

Q:

check whether  $(v_i, v_j)$  have an edge or not ?

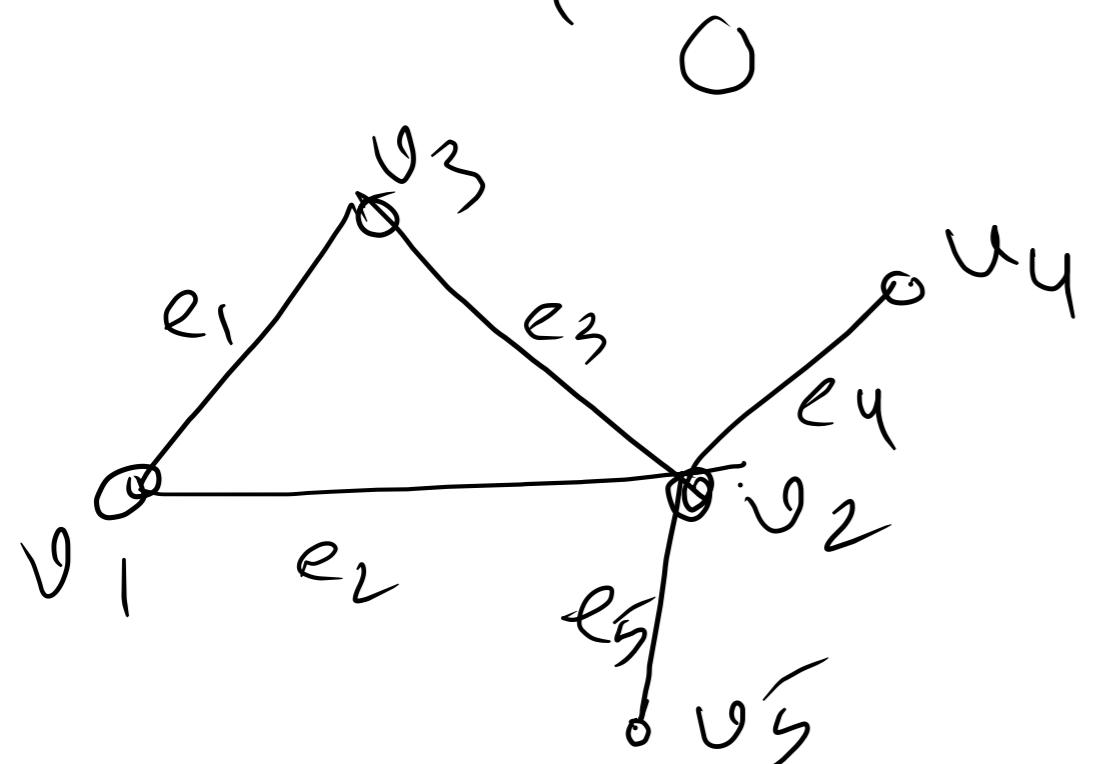
adjacency matrix -  $O(1)$

,, List  $O(n)$

## Incident matrix

$$I = (a_{ij})_{n \times m}$$

$$a_{ij} = \begin{cases} 1 & \text{if } e_j \text{ is incident on } v_i \\ 0 & \text{otherwise} \end{cases}$$



	$e_1$	$e_2$	$e_3$	$e_4$	$e_5$
$v_1$	1	1	0	0	0
$v_2$	0	1	1	1	1
$v_3$	1	0	1	0	0
$v_4$	0	0	0	1	0
$v_5$	0	0	0	0	1

$n \times m$

## Graph Search / explore

- need to visit all vertices of a graph.

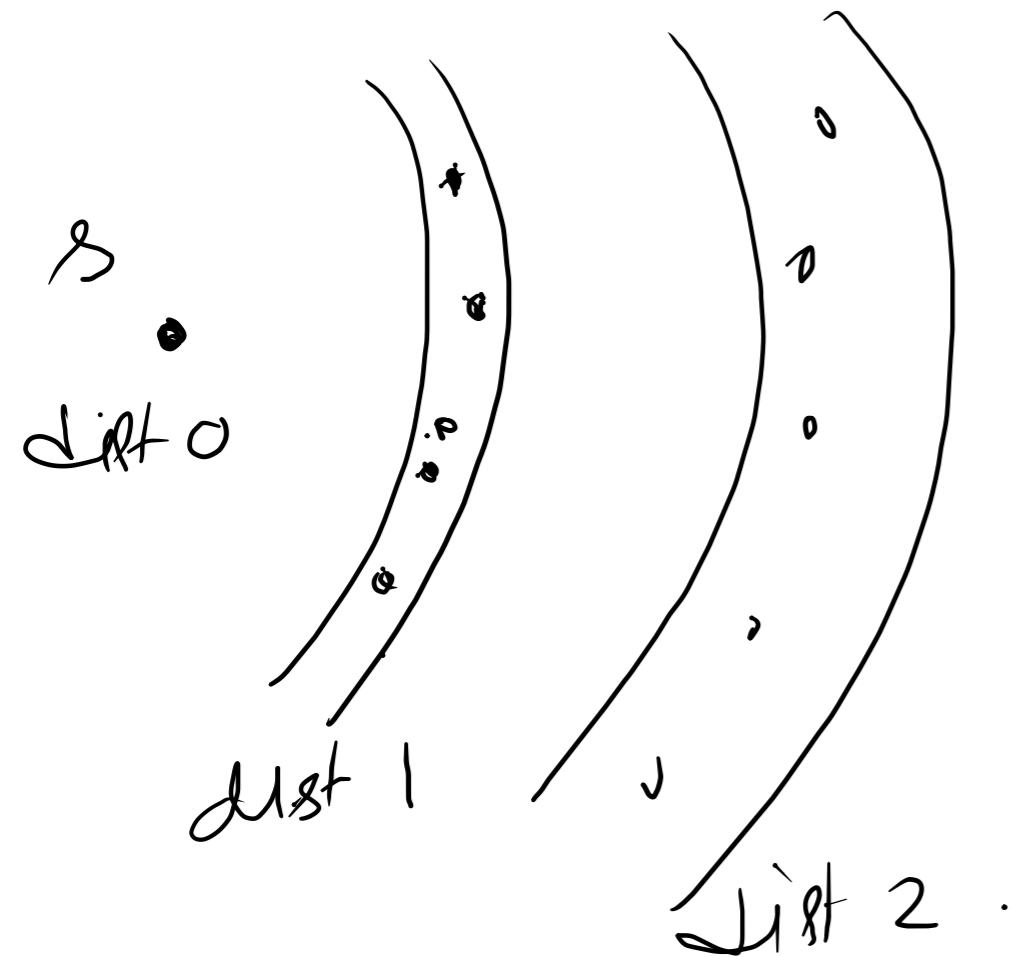
Two major ~~searching~~ algorithms

1> BFS - Breadth first search

2> DFS - Depth first search.

## BFS

- It starts from a distinguish vertex called source.



Queue  
FIFO

3 - categories of vertices .

white  $\leftarrow$  vertices are not yet captured .

{ gray  $\leftarrow$  vertices are encountered but not  
finish its processing .

black  $\leftarrow$  vertices already explored .

inside the  
queue .

BFS ( $G_G, s$ )

for each vertex  $v \in V$

color( $v$ ) = white  
||  $\pi[v] = \text{null}$   
||  $d(v) = \infty$

color( $s$ ) = gray .

||  $\pi[s] = \text{null}$   
||  $d[s] = 0$

Enqueue ( $Q, s$ )

while ( $Q \neq \emptyset$ )

$u = \text{Dequeue} (Q)$

for all vertices  $v \in \text{Adj}(u)$

if color( $v$ ) = white

color( $v$ ) = gray

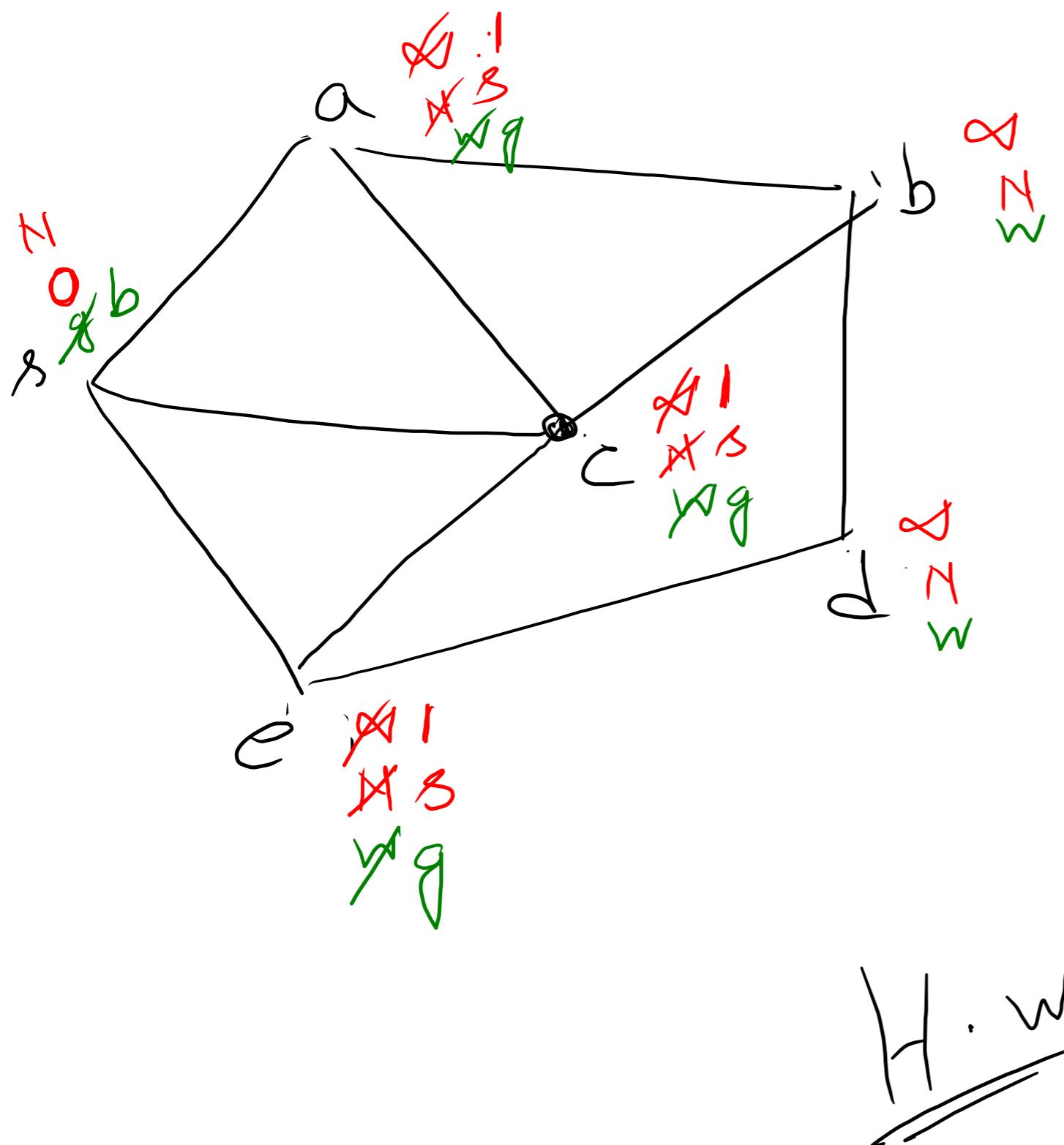
Enqueue ( $Q, v$ )



$\pi(v) \leftarrow$  parent of the node  $v$   
 $d(v) \leftarrow$  distance to  $v$  from  $s$ .

$\pi[v] = u$   
 $d[v] = d[u] + 1$

color( $u$ ) = black .



$$u = \varphi$$

$$u = \textcircled{c}$$

Finish this example

Directed: only directed edges are present in the list.

Weighted: use an extra field in the node.