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## Scribed Lecture 3 Notes

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## Structural Induction:-

Building bigger formulae from smaller formulae using logical connectives

## Logical Connectives

1: NOT	: $\neg$
2: OR / DISJUNCTION	: $\vee$
3: AND / CONJUNCTION	: $\wedge$
4: EXCLUSIVE OR (XOR)	: $\oplus$ , $\asymp$
5: IMPLICATION	: $\rightarrow$
6: EQUIVALENCE / BI-IMPLICATIONS	: $\Leftrightarrow$
7: NAND $\rightarrow$ NOT + AND	
8: NOR $\rightarrow$ NOT + OR	

Note : all operations are generally binary except negation

Note : Implications are not commutative

## Atomic Propositions

An atomic proposition is a statement or assertion that must be true or false.

Example :  $P = \{(P_0), (P_1), (P_2) \dots\}$

## Complicated Formulae

- (i) If  $\Psi$  is a formula then so is:  $\neg (\Psi)$   
(ii) If  $\Psi_1$  is a formula and  $\Psi_2$  is a formula then so are :
- $\Psi_1 \vee \Psi_2$
  - $\Psi_1 \wedge \Psi_2$
  - $\Psi_1 \Rightarrow \Psi_2$
  - $\Psi_1 \Leftarrow \Psi_2$
  - $\Psi_1 \text{ XOR } \Psi_2$

\* formula trees

$$(p_0 \Rightarrow ((\neg p_1) \wedge (p_2 \vee p_3)))$$

