

3rd October 2022 (Monday)

Scribed Notes – Lecture 21

Student ID :-

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COUNTING

Permutation: -

- Arrangements of elements from a set
- It's a Bijective function having same Domain and Co-Domain
- Linear/ordered arrangements of r elements among n.
- The notation for No. of ways to achieving this is ${}^n P_r$.
- No. of Permutations > No. of Combinations (More than)
- You can use the same elements again
- Shorthand:
 - $[r] = \{1, \dots, r\}$ is an injective function.
 - $[r] \rightarrow [n]$ (Domain r to Co-Domain n).
- ${}^n P_r = (n!) / (n-r)!$

Combination: -

- Selection of r elements from a set among n.
- Due to the overcount in the permutation we have to remove the arrangements of r (i.e., $r!$) which is overcounted in the permutation
- Notation: $\binom{n}{r} = {}^n C_r = \frac{(n!)}{(r)! * (n-r)!}$
- $\binom{n}{r} = \binom{n}{n-r}$
- ${}^n C_r + {}^n C_{r-1} = {}^{n+1} C_r$

Combination: -

- The Binomial Theorem is the method of expanding an expression that has been raised to any finite power.
- Formula:

$$(x + y)^n = \sum_{k=0}^n \binom{n}{k} x^{n-k} y^k$$

“sigma notation” simply indicates we’ll be adding together a bunch of these guys

“n choose k” combinations formula we learned about earlier

$$(x + y)^0 = 1,$$

$$(x + y)^1 = x + y,$$

$$(x + y)^2 = x^2 + 2xy + y^2,$$

$$(x + y)^3 = x^3 + 3x^2y + 3xy^2 + y^3,$$

$$(x + y)^4 = x^4 + 4x^3y + 6x^2y^2 + 4xy^3 + y^4,$$

$$(x + y)^5 = x^5 + 5x^4y + 10x^3y^2 + 10x^2y^3 + 5xy^4 + y^5,$$

$$(x + y)^6 = x^6 + 6x^5y + 15x^4y^2 + 20x^3y^3 + 15x^2y^4 + 6xy^5 + y^6,$$

$$(x + y)^7 = x^7 + 7x^6y + 21x^5y^2 + 35x^4y^3 + 35x^3y^4 + 21x^2y^5 + 7xy^6 + y^7,$$

$$(x + y)^8 = x^8 + 8x^7y + 28x^6y^2 + 56x^5y^3 + 70x^4y^4 + 56x^3y^5 + 28x^2y^6 + 8xy^7 + y^8.$$