

BFS

BFS(G, s)

for each vertex $v \in V$

$\text{color}(v) = \text{white}$

$\pi(v) = \text{Nil}$

$d(v) = \cancel{\infty}$

$\text{color}(s) = \text{gray}$

$\pi(s) = \text{Nil}$

$d(s) = 0$

Q as an empty queue

Enqueue(Q, s)

while ($Q \neq \emptyset$)

$u = \text{Dequeue}(Q)$

for each vertex $v \in \text{Adj}(u)$

if $\text{color}(v) = \text{white}$

$\text{color}(v) = \text{gray}$

$\pi(v) = u$

$d(v) = d(u) + 1$

Enqueue(Q, v)

$2|V|$
 $2|E|$ times

$\text{color}(u) = \text{black}$

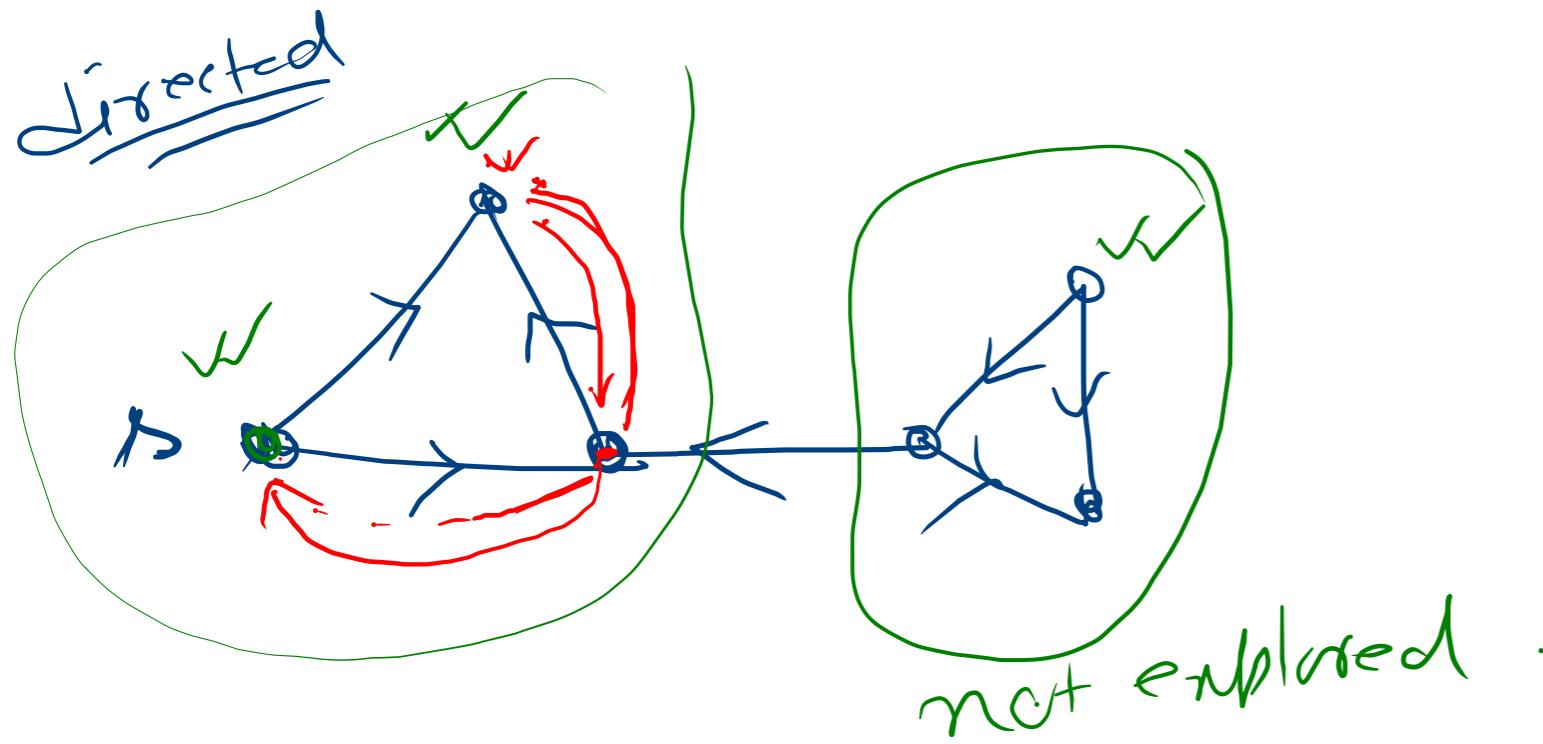
overall time:

$$O(|V|) + O(|E|)$$

$$= O(|V| + |E|)$$

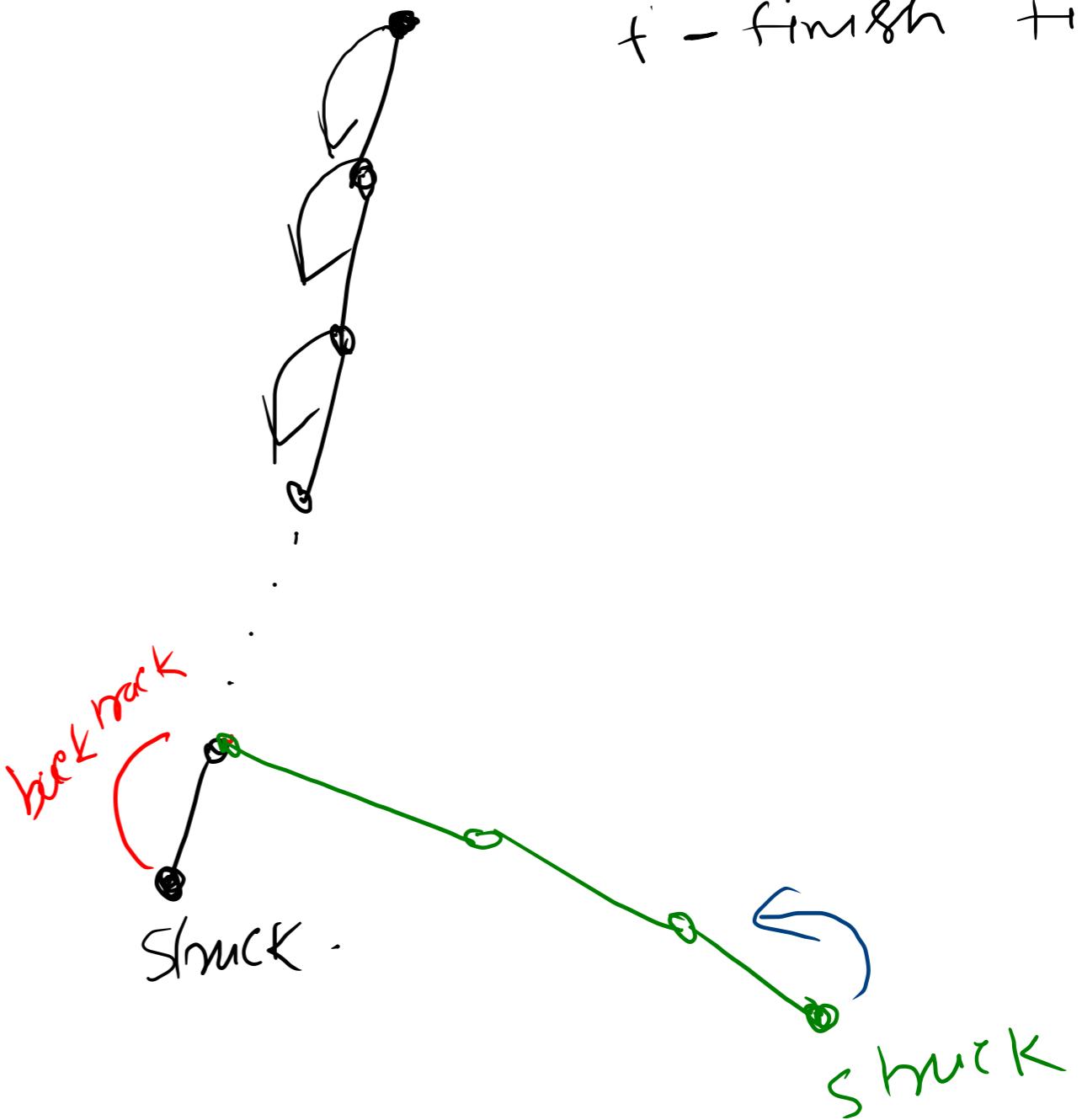
$(\pi(v), v)$

Depth - first Search (DFS)



it gives
forest : collection of
trees -

δ - discover time
 τ - finish time



$\text{DFS}(G)$

for each vertex $v \in V$
 $\text{color}(v) = \text{white}$
 $\pi(v) = \text{nil}$

$\text{time} = 0$

for each vertex $v \in V$
if $\text{color}(v) = \text{white}$
 $\text{DFS-visit}(G, v)$



$\text{DFS-visit}(G, v)$

$\text{time} = \text{time} + 1$

$s(v) = \text{time}$

$\text{color}(v) = \text{gray}$

for each vertex $w \in \text{Adj}(v)$

if $\text{color}(w) = \text{white}$ ✓

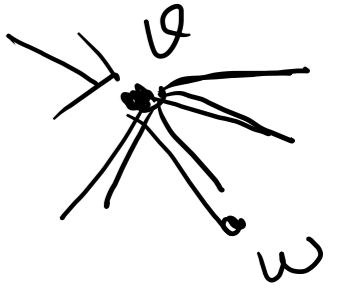
$\pi(w) = v$

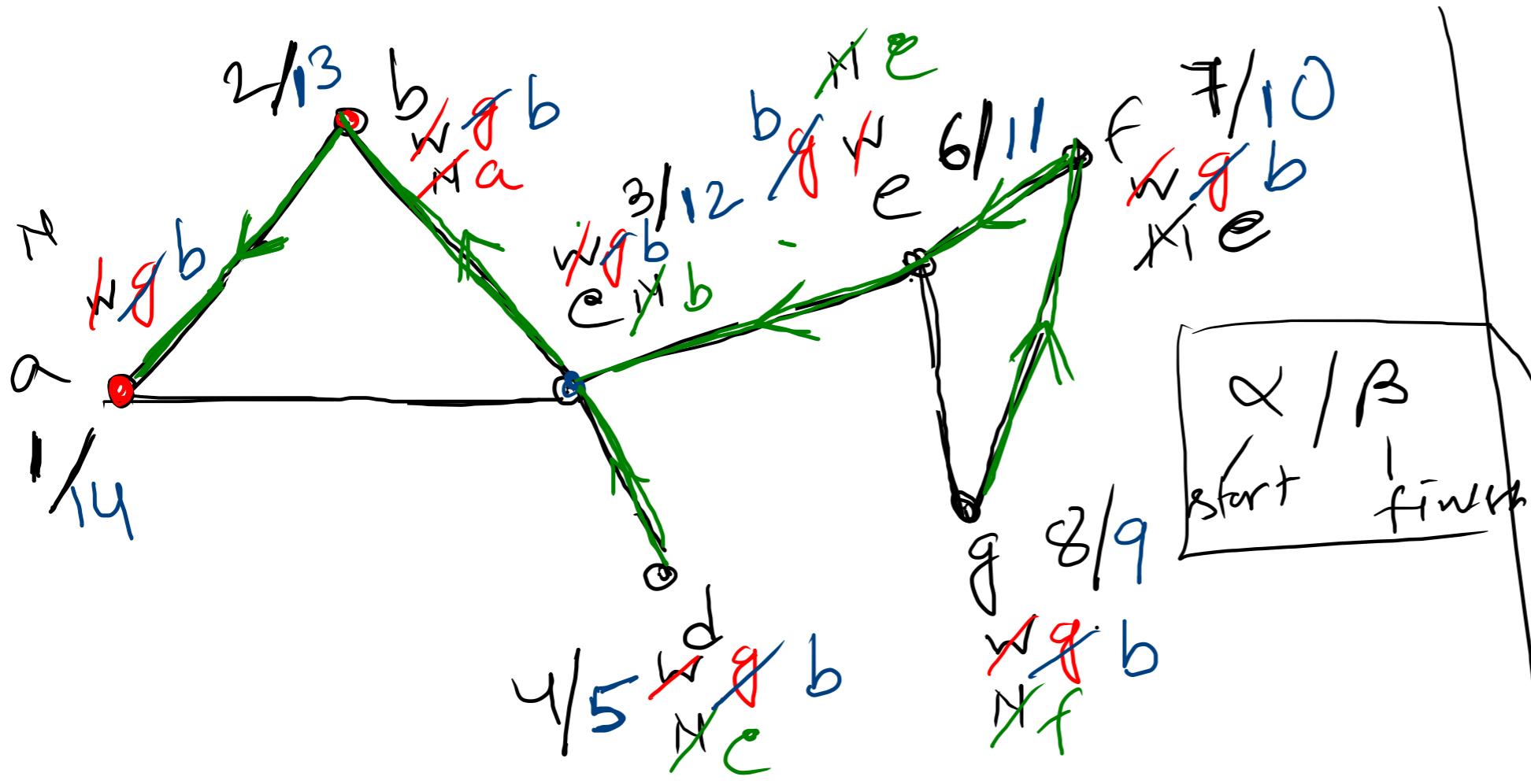
DFS-visit(G, w) ✓

$\text{time} = \text{time} + 1$

$f(v) = \text{time}$

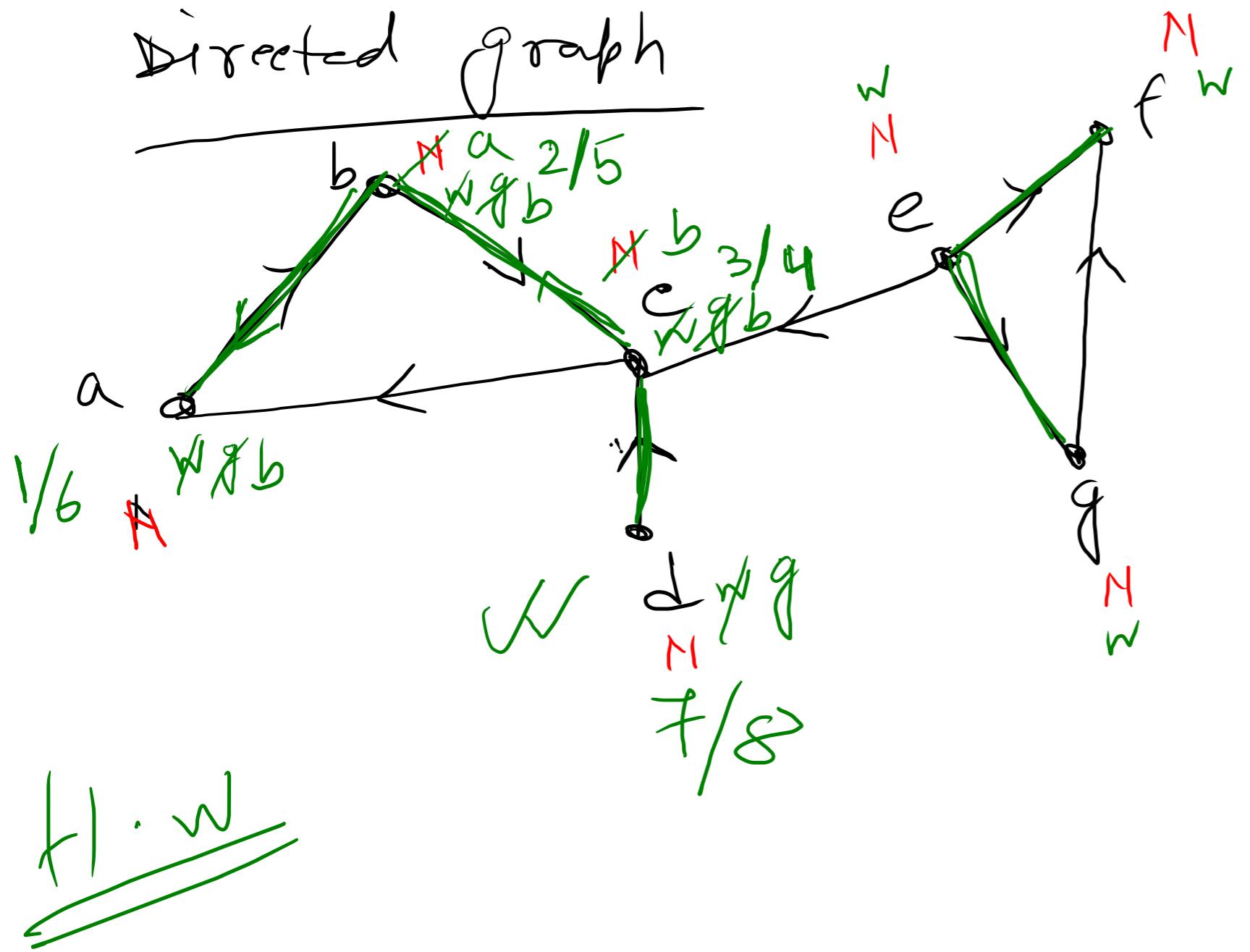
$\text{color}(v) = \text{black}$.





Adjacency List representation

Directed graph



Adjacency list

a - b
b - c
c - a
d - c
e - c, f, g
f -
g - f