

# Multiply complex numbers

$$1 \cdot (1+5i) \cdot (-3-i)$$

$$-3-i = 15i = 5i^2$$

$$\boxed{i^2 = -1}$$

$$-3-16i - (-5)$$

$$-3+5-16i = \underline{2-16i}$$

$$2 \cdot (-1+4i) \cdot (4-3i)$$

$$-4+3i+16i-12i^2$$

$$-4+12+3i+16i$$

$$\underline{8+19i}$$

$$3 \cdot (2-i)(-3+2i)$$

$$-6+4i+3i-2i^2$$

$$-6+2+4i+3i$$

$$-9+7i$$

$$4 \cdot (4+4i)(-2-5i)$$

$$-8-20i-8i-20i^2$$

$$-8+20-20i-8i$$

$$12-28i$$

$$\bullet (-4+4i)(3+2i)$$
$$-12 - 8i + 12i + 8i^2$$
$$-12 - 8 - 8i + 12i$$
$$-20 + 4i$$

$$\bullet (-2-3i)(-5-2i)$$
$$+10 + 4i + 15i + 6i^2$$
$$10 - 6 + 4i + 15i$$
$$4 + 19i$$

$$\bullet (1+2i)(1-4i)$$
$$1 - 4i + 2i - 8i^2$$
$$1 + 8 - 4i + 2i$$
$$9 - 2i$$

$$(-3-i)(3+i)$$
$$-9 - 3i - 3i - i^2$$
$$-9 + 1 - 3 - 3i$$
$$-8 - 6i$$

Add and Subtract complex nr

1  $(10 - 22i) + (22i)$

10

2  $(-13 + 16i) - (-3 + 4i)$

$-13 + 16i - 3 - 4i$

$-16 + 12i$

3  $(-30i) + (52 - 30i)$

$-30i + 52 - 30i$

$52 - 60i$

4  $(3 + 4i) - (6 - 10i)$

$3 + 4i - 6 + 10i$

$-3 + 14i$

$$(18 + 4i) + (-11 + 23i)$$

$$18 + 4i - 11 + 23i$$

$$7 + 27i$$

$$(-7 - 10i) - (3 + 30i)$$

$$-4 - 40i$$

$$(4) + (14 - 4i)$$

$$18 - 4i$$

$$(-19 + 7i) - (29 + 32i)$$

$$-48 - 25i$$

$$-82$$

$$+ 11$$

$$-83$$

$$-40$$

$$\textcircled{*} \quad f'(x) = 4f(x) \quad f(0) = 10$$

$f'(x) = kf(x)$   
 $f(x) = C \cdot e^{kx}$

$$f(0) = k \cdot C^{4 \cdot 0}$$

$$10 = k \cdot C^{4 \cdot 0}$$

$$\underline{k = 10}$$

$$\underbrace{f'(x)}_{= 10C^{4x}} = 10C^{4x}$$

$$\textcircled{*} \quad \frac{dy}{dt} = y \quad y = 1 \quad t = 4$$

$$\underline{k = 1}$$

$$y = C \cdot e^{1 \cdot t}$$

$$1 = C \cdot e^t$$

$$e^{-t} = C$$

$$y = e^{t-4}$$

$$\frac{dy}{dt} = ky$$

$$y = C \cdot e^{kt}$$

$$\bullet \frac{dy}{dx} = 3y \quad y=2 \quad x=1 \quad \text{differential equations}$$

$$\int \frac{1}{y} dy = \int 3 dx$$

$$e^{\ln|y|} = e^{3x + k}$$

$$y = e^{-3x+k} = y = k e^{-3x} \quad 2 = k e^{-3 \cdot 1} \\ k = 2 e^{-3}$$

$$y = 2 e^{-3x} \cdot e^{-3x}$$

$$y = 2 e^{-3x-3}$$

$$\bullet \frac{dy}{dx} = 3y \quad y=2 \quad x=1$$

$$\int \frac{1}{y} dy = \int 3 dx$$

$$\ln|y| = e^{3x+k}$$

$$y = k e^{3x} = 2 = k e^{3 \cdot 1} = 2 e^3 = k$$

$$y = 2 e^3 \cdot e^{3x} = y = 2 e^{3x+3}$$

$$\textcircled{1} \frac{dy}{dx} = 7y \quad y=1 \quad x=0$$

$$\int \frac{1}{y} dy = \int 7 dx$$

$$|\ln|y|| = 7x + k$$

$$y = ke^{7x}$$

$$1 = ke^{7 \cdot 0} \\ k = 1$$

$$\underline{y = 1 \cdot e^{7x}}$$

$$\underline{y = e^{7x}}$$

$$\textcircled{2} \frac{dy}{dx} = -4y \quad y=3 \quad x=2$$

$$\int \frac{1}{y} dy = \int -4 dx$$

$$|\ln|y|| = -4x + k$$

$$y = ke^{-4x} = 3 = ke^{-4 \cdot 2} = \underline{k = 3e^8}$$

$$y = 3e^8 \cdot e^{-4x} = \underline{y = 3e^{8-4x}}$$

$$\textcircled{3} \frac{dy}{dt} = 2y \quad y=8 \quad t=0$$

$$\int \frac{1}{y} dy = \int 2 dt$$

$$|\ln|y|| = 2t + k$$

$$y = ke^{2t}$$

$$8 = ke^{2 \cdot 0} \quad \underline{k=8}$$

$$\underline{y = 8e^{2t}}$$

$$\textcircled{a} \quad g'(x) = 8g(x) \quad g(2) = 7$$

$$g(x) = k e^{kx} \quad k=8$$

$$7 = k e^{8 \cdot 2} = k = 7 e^{-16}$$

$$\underline{\underline{g(x) = 7 e^{8x-16}}}$$

$$\textcircled{b} \quad \frac{dy}{dt} = -7y \quad y=3 \quad t=0$$

$$\int \frac{1}{y} dy = -7 dt$$

$$e^{\ln|y|} = e^{-7t+k}$$

$$y = k e^{-7t} \quad 3 = k e^{-7 \cdot 0} \quad k = 3 e^7$$

$$y = 3 e^{-7t}$$

$$\textcircled{c} \quad h'(x) = 6h(x) \quad h(1) = 5$$

$$h(x) = k e^{kx} \quad k=6$$

$$5 = k e^{6 \cdot 1} = k = 5 e^6$$

$$\underline{\underline{h(x) = 5 e^{6x-6}}}$$

$$\bullet h'(x) = -h(x) \quad h(0) = 12$$

$$h(x) = ke^{kx} \quad k = -1$$

$$12 = ke^{-1 \cdot 0} \quad k = 12$$

$$h(x) = 12e^{-1x}$$

$$\bullet f'(x) = -6f(x) \quad f(2) = 1$$

$$f(x) = ke^{kx} \quad k = -6$$

$$1 = ke^{-6 \cdot 2} \quad k = e^{12}$$

$$h(x) = e^{12-6x}$$