

SINTEF Energy Research

Address:

P.O. Box 4761 Sluppen NO-7465 Trondheim

NORWAY

Telephone: +47 73597200 Telefax: +47 73597250

Documentation of the binary-XY code in thermopack

energy.research@sintef.no www.sintef.no Enterprise / VAT no.: NO 939 350 675 MVA

PERSON RESPONSIBLE / AUTHOR

Morten Hammer

Memo

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Contents

1	Introduction	2
2	Governing equations 2.1 Changing the specification	2 2 2
3	Results	3
4	Further improvements	3
Α	Jacobian	3



1 Introduction

The equations required to describe an binary Txy or Pxy plot.

2 Governing equations

The equation system F(X) = 0, is defined by equation (1) to (8).

$$f_i = \ln K_i + \ln \hat{\varphi}_i(\mathbf{y}) - \ln \hat{\varphi}_i(\mathbf{x}) = 0, \quad i = 1, 2$$
 (1)

$$f_{i+2} = y_i - K_i x_i = 0, \quad i = 1, 2$$
 (2)

$$f_5 = x_1 + x_2 - 1 = 0 (3)$$

$$f_6 = y_1 + y_2 - 1 = 0 (4)$$

$$f_7 = S - S_{\text{spec}} = 0 \tag{5}$$

(6)

$$\mathbf{F} = \begin{pmatrix} f_1 \\ \vdots \\ f_7 \end{pmatrix} \tag{7}$$

The last variable will be $\ln T$ or $\ln P$, for simplicity the equations are written out for a Txy binary plot. The temperature is therefore constant. The last variable is therefore $\ln P$. The Pxy problem can be developed in the same manner.

$$\mathbf{X} = \begin{pmatrix} \ln \mathbf{K} \\ \mathbf{x} \\ \mathbf{y} \\ \ln P \end{pmatrix} \tag{8}$$

2.1 Changing the specification

Differentiating, we get:

$$\frac{d\mathbf{F}(\mathbf{X})}{d\mathbf{X}}\frac{d\mathbf{X}}{dS_{\text{spec}}} + \frac{d\mathbf{F}(\mathbf{X})}{dS_{\text{spec}}} = \mathbf{0}$$
(9)

$$\frac{\mathrm{d}\mathbf{F}(\mathbf{X})}{\mathrm{d}\mathbf{X}}\frac{\mathrm{d}\mathbf{X}}{\mathrm{d}S_{\mathrm{spec}}} = \begin{pmatrix} \mathbf{0} \\ 1 \end{pmatrix} \tag{10}$$

We are therefore able to produce new initial guesses when we change the specification, $S_{\rm spec}$.

2.2 Termination

The binaryXY routine need to terminate when one of the following situations occur:

- 1. One of the components become zero.
- 2. Critical point or azeotrope is reached. (x = y)
- 3. User given maximum in pressure or minimum in temperature is reached.



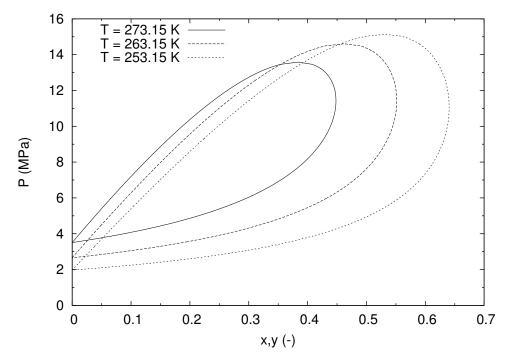


Figure 1: Mole fraction of NO in anCO₂-NO mixture with SRK and $k_{ij} = 0$.

3 Results

Have tested the mixture CO_2 -NO with SRK and PR. Both have been tested with the binary interaction parameters $k_{ij}=0$ and $k_{ij}=-0.105$. The plots have been initialised at the CO_2 bubble point.

See Figure 1, 2, 3 and 4.

4 Further improvements

Currently only the basic functions are implemented in order to produce the Txy-plot for CO₂-NO. There is remaining work related to the initiation and termination of the binary plots.

- 1. Extend to include a search for two liquid phases.
- 2. Automate initiation and search direction.
- 3. Extend to Pxy plot.
- 4. Do testing of difficult systems.

A Jacobian

The Jacobian required for a Newton solver of the equation system in section 2.



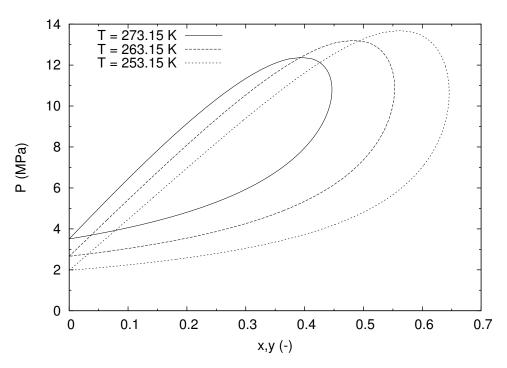


Figure 2: Mole fraction of NO in anCO₂-NO mixture with SRK and $k_{ij} = -0.119$.

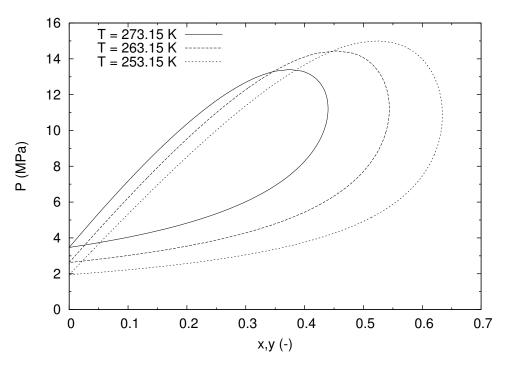


Figure 3: Mole fraction of NO in anCO₂-NO mixture with PR and $k_{ij} = 0$.



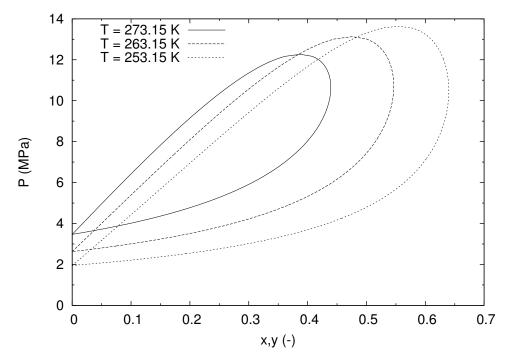


Figure 4: Mole fraction of NO in anCO₂-NO mixture with PR and $k_{ij} = -0.105$.

$$\frac{\partial f_1}{\partial \ln K_1} = 1 \tag{11}$$

$$\frac{\partial f_1}{\partial \ln K_2} = 0 \tag{12}$$

$$\frac{\partial f_1}{\partial x_i} = -\frac{\partial \ln \hat{\varphi}_1(\mathbf{x})}{\partial x_i}, \quad i = 1, 2$$
(13)

$$\frac{\partial f_1}{\partial y_i} = \frac{\partial \ln \hat{\varphi}_1(\mathbf{y})}{\partial y_i}, \quad i = 1, 2$$
(14)

$$\frac{\partial f_1}{\partial \ln P} = P \left(\frac{\partial \ln \hat{\varphi}_1(\mathbf{y})}{\partial P} - \frac{\partial \ln \hat{\varphi}_1(\mathbf{x})}{\partial P} \right)$$
(15)

$$\frac{\partial f_2}{\partial \ln K_1} = 0 \tag{16}$$

$$\frac{\partial f_2}{\partial \ln K_2} = 1 \tag{17}$$

$$\frac{\partial f_2}{\partial x_i} = -\frac{\partial \ln \hat{\varphi}_2(\mathbf{x})}{\partial x_i}, \quad i = 1, 2$$
(18)

$$\frac{\partial f_2}{\partial y_i} = \frac{\partial \ln \hat{\varphi}_2(\mathbf{y})}{\partial y_i}, \quad i = 1, 2$$
 (19)

$$\frac{\partial f_2}{\partial \ln P} = P \left(\frac{\partial \ln \hat{\varphi}_2(\mathbf{y})}{\partial P} - \frac{\partial \ln \hat{\varphi}_2(\mathbf{x})}{\partial P} \right)$$
 (20)



$$\frac{\partial f_3}{\partial \ln K_1} = -K_1 x_1 \tag{21}$$

$$\frac{\partial f_3}{\partial \ln K_2} = 0 \tag{22}$$

$$\frac{\partial f_3}{\partial x_1} = -K_1 \tag{23}$$

$$\frac{\partial f_3}{\partial x_2} = 0 \tag{24}$$

$$\frac{\partial f_3}{\partial y_1} = 1 \tag{25}$$

$$\frac{\partial f_3}{\partial y_2} = 0 \tag{26}$$

$$\frac{\partial f_3}{\partial \ln P} = 0 \tag{27}$$

$$\frac{\partial f_4}{\partial \ln K_1} = 0 \tag{28}$$

$$\frac{\partial f_4}{\partial \ln K_2} = -K_2 x_2 \tag{29}$$

$$\frac{\partial f_4}{\partial x_1} = 0 \tag{30}$$

$$\frac{\partial f_4}{\partial x_2} = -K_2 \tag{31}$$

$$\frac{\partial f_4}{\partial y_1} = 0 \tag{32}$$

$$\frac{\partial f_4}{\partial y_2} = 1 \tag{33}$$

$$\frac{\partial f_4}{\partial \ln P} = 0 \tag{34}$$

$$\frac{\partial f_5}{\partial X_i} = 0 \quad i = 1, 2, 5, 6, 7$$
 (35)

$$\frac{\partial f_5}{\partial x_i} = 1 \quad i = 3, 4 \tag{36}$$

$$\frac{\partial f_6}{\partial X_i} = 0 \quad i = 1, 2, 3, 4, 7$$
 (37)

$$\frac{\partial f_6}{\partial y_i} = 1 \quad i = 5, 6 \tag{38}$$

$$\frac{\partial f_7}{\partial X_i} = \begin{cases} 1 & i = i_{\text{spec}} \\ 0 & \text{otherwise} \end{cases}$$
 (39)