```
Contents
                                                                                                                     return Long.parseLong(nextToken());
                                                            void e(Object o) {
  1. Code Templates
                                                                 System.err.println(o);
                                                                                                                   public String n() {
  1.1. Java Template
                                                                                                                     return nextToken();
  1.2. Python Template
                                                            public static void main(String[] args)
  1.3. C++ Template
                                                             throws Exception {
                                                                                                                   private BufferedReader r;
  1.4. Fast IO Java
                                                                 BufferedReader in = new BufferedReader
                                                                                                                   private String line;
  2. Data Structures
                                                                     (new InputStreamReader(System.in));
                                                                                                                   private StringTokenizer st;
  2.1. Binary Indexed Tree
                                                                 (new A()).solve(in);
                                                                                                                   private String token:
  2.2. Segment Tree
                                                                                                                   private String peekToken() {
  2.3. Lazy Segment Tree
                                                     2
                                                                                                                     if (token == null)
  2.4. Union Find
                                                     2
                                                                                                                       try {
  2.5. Monotone Queue
                                                        1.2. Python Template. A Python template
                                                                                                                         while (st == null || !st.hasMoreTokens()) {
  3. Graph Algorithms
                                                        import sys
                                                                                                                           line = r.readLine();
  3.1. Djikstras algorithm
                                                        line = sys.stdin.read()
                                                                                                                           if (line == null) return null;
  3.2. Bipartite Graphs
                                                                                                                           st = new StringTokenizer(line);
                                                        1.3. C++ Template. A C++ template
  3.3. Network Flow
                                                        #include<iostream>
  4. Dynamic Programming
                                                                                                                         token = st.nextToken();
                                                        #include<vector>
  4.1. Longest Increasing Subsequence
                                                                                                                       } catch (IOException e) { }
                                                        #include<queue>
  4.2. Knuuth Morris Pratt substring
                                                                                                                     return token;
                                                        #include<unordered_set>
  5. Etc
  5.1. System of Equations
                                                        using namespace std;
                                                                                                                   private String nextToken() {
  5.2. Convex Hull
                                                        int main() {
                                                                                                                     String ans = peekToken();
                                                          vector<string> in;
  6. NP tricks
                                                                                                                     token = null;
                                                          string line;
  6.1. MaxClique
                                                                                                                     return ans;
                                                           while(getline(cin, line)) in.push_back(line);
                                                                                                                 }
                                                        1.4. Fast IO Java. Kattio with easier names
                                                        import java.util.StringTokenizer;
                 1. Code Templates
                                                                                                                                  2. Data Structures
                                                        import java.io.*;
                                                                                                                 2.1. Binary Indexed Tree. Also called a fenwick tree.
1.1. Java Template. A Java template.
                                                        class Sc {
                                                                                                                 Builds in \mathcal{O}(n \log n) from an array. Querry sum from 0 to
import iava.util.*:
                                                          public Sc(InputStream i) {
                                                                                                                 i in \mathcal{O}(\log n) and updates an element in \mathcal{O}(\log n).
                                                             r = new BufferedReader(new InputStreamReader(i));
import java.io.*;
public class A {
                                                                                                                 private static class BIT {
    void solve(BufferedReader in) throws Exception {
                                                           public boolean hasM() {
                                                                                                                   long[] data;
                                                             return peekToken() != null;
                                                                                                                   public BIT(int size) {
                                                                                                                     data = new long[size+1];
    int toInt(String s) {return Integer.parseInt(s);}
                                                          public int nI() {
                                                                                                                   public void update(int i, int delta) {
    int[] toInts(String s) {
                                                             return Integer.parseInt(nextToken());
        String[] a = s.split(" ");
                                                                                                                     while(i< data.length) {</pre>
                                                           public double nD() {
        int[] o = new int[a.length];
                                                                                                                       data[i] += delta;
        for(int i = 0; i<a.length; i++)
                                                             return Double.parseDouble(nextToken());
                                                                                                                       i += i&-i; // Integer.lowestOneBit(i);
            o[i] = toInt(a[i]);
        return o;
                                                           public long nL() {
```

```
public long sum(int i) {
                                                                                                                   public void inc(int a, int b, int v) {
    long sum = 0;
                                                        static int update(ST root, int i, int val) {
                                                                                                                     inc(1, a, b, v);
    while(i>0) {
                                                          int diff = 0:
      sum += data[i];
                                                          if(root.li==root.ri && i == root.li) {
                                                                                                                   private void inc(int i, int a, int b, int v) {
      i -= i&-i;
                                                            diff = val-root.sum; //max/min
                                                                                                                     if(b < lo[i] || a > hi[i]) return;
                                                            root.sum=val; //max/min
                                                                                                                     if(a <= lo[i] && hi[i] <= b) {
                                                            return diff; //root.max
                                                                                                                       delta[i] += v;
    return sum;
                                                                                                                       return;
                                                          int mid = (root.li + root.ri) / 2:
                                                          if (i <= mid) diff = update(root.lN, i, val);</pre>
                                                                                                                     prop(i);
2.2. Segment Tree. More general than a fenwick tree. Can
                                                          else diff = update(root.rN, i, val);
                                                                                                                     inc(2*i, a, b, v);
adapt other operations than sum, e.g. min and max.
                                                          root.sum+=diff; //ask other child
                                                                                                                     inc(2*i+1, a, b, v);
                                                          return diff: //and compute max/min
                                                                                                                     update(i):
private static class ST {
 int li, ri;
 int sum; //change to max/min
                                                        2.3. Lazy Segment Tree. More general implementation of
                                                                                                                   private void init() {
 ST lN:
                                                        a segment tree where its possible to increase whole segments
                                                                                                                    init(1, 0, n-1, new int[n]);
 ST rN;
                                                        by some diff, with lazy propagation. Implemented with arrays
                                                        instead of nodes, which probably has less overhead to write
static ST makeSgmTree(int[] A, int l, int r) {
                                                                                                                   private void init(int i, int a, int b, int[] v) {
                                                        during a competition.
                                                                                                                    lo[i] = a;
 if(l == r) {
                                                                                                                    hi[i] = b;
    ST node = new ST();
                                                        class LazySegmentTree {
                                                                                                                     if(a == b) {
    node.li = l:
                                                          private int n:
                                                                                                                       sum[i] = v[a];
    node.ri = r;
                                                          private int[] lo, hi, sum, delta;
                                                                                                                       return;
    node.sum = A[l]; //max/min
                                                          public LazySegmentTree(int n) {
    return node;
                                                            this.n = n;
                                                            lo = new int[4*n + 1];
                                                                                                                     int m = (a+b)/2;
                                                                                                                     init(2*i, a, m, v);
  int mid = (l+r)/2;
                                                            hi = new int[4*n + 1];
                                                            sum = new int[4*n + 1];
                                                                                                                    init(2*i+1, m+1, b, v);
  ST lN = makeSgmTree(A,l,mid);
                                                            delta = new int[4*n + 1];
                                                                                                                     update(i);
 ST rN = makeSgmTree(A,mid+1,r);
 ST root = new ST();
                                                            init();
                                                                                                                   private void update(int i) {
  root.li = lN.li;
                                                                                                                     sum[i] = sum(2*i) + sum(2*i+1);
  root.ri = rN.ri:
                                                          public int sum(int a, int b) {
  root.sum = lN.sum + rN.sum; //max/min
                                                            return sum(1, a, b);
                                                                                                                   private int range(int i) {
  root.lN = lN;
  root.rN = rN;
                                                          private int sum(int i, int a, int b) {
                                                                                                                     return hi[i] - lo[i] + 1;
  return root:
                                                            if(b < lo[i] || a > hi[i]) return 0:
                                                                                                                   private int sum(int i) {
                                                            if(a <= lo[i] && hi[i] <= b) return sum(i);</pre>
                                                            prop(i);
                                                                                                                     return sum[i] + range(i)*delta[i];
static int getSum(ST root, int l, int r) {//max/min
 if(root.li>=l && root.ri<=r)</pre>
                                                            int l = sum(2*i, a, b);
                                                                                                                   private void prop(int i) {
    return root.sum; //max/min
                                                            int r = sum(2*i+1, a, b);
                                                                                                                     delta[2*i] += delta[i];
  if(root.ri<l || root.li > r)
                                                            update(i);
                                                                                                                     delta[2*i+1] += delta[i];
    return 0; //minInt/maxInt
                                                            return l + r;
                                                                                                                     delta[i] = 0;
  else //max/min
    return getSum(root.lN,l,r) + getSum(root.rN,l,r); }
```

```
}
}
```

2.4. Union Find. This data structure is used in varoius algorithms, for example Kruskals algorithm for finding a Minimal Spanning Tree in a weighted graph. Also it can be used for backward simulation of dividing a set.

```
private class Node {
 Node parent;
 int h:
  public Node() {
    parent = this;
    h = 0:
  public Node find() {
    if(parent != this) parent = parent.find();
    return parent;
}
static void union(Node x, Node y) {
 Node xR = x.find(), yR = y.find();
 if(xR == yR) return;
 if(xR.h > yR.h)
    yR.parent = xR;
  else {
    if(yR.h == xR.h) yR.h++;
    xR.parent = yR;
 }
```

2.5. Monotone Queue. Used in sliding window algorithms where one would like to find the minimum in each interval of a given length. Amortized  $\mathcal{O}(n)$  to find min in each of these intervals in an array of length n. Can easily be used to find the maximum as well.

```
private static class MinMonOue {
    LinkedList<Integer> que = new LinkedList<>();
    public void add(int i) {
        while(!que.isEmpty() && que.getFirst() > i)
            que.removeFirst();
        que.addFirst(i);
    public int last() {
        return que.getLast();
```

```
public void remove(int i) {
    if(que.getLast() == i) que.removeLast();
```

3. Graph Algorithms 3.1. Djikstras algorithm. Finds the shortest distance be-

tween two Nodes in a weighted graph in  $\mathcal{O}(|E|\log|V|)$  time.

```
//Requires java.util.LinkedList and java.util.TreeSet
  LinkedList<Edge> edges = new LinkedList<>();
  int w;
  int id:
  public Node(int id) {
   w = Integer.MAX_VALUE;
    this.id = id;
  public int compareTo(Node n) {
   if(w != n.w) return w - n.w;
    return id - n.id:
  //Asumes all nodes have weight MAXINT.
  public int djikstra(Node x) {
    this.w = 0:
   TreeSet<Node> set = new TreeSet<>();
    set.add(this);
    while(!set.isEmpty()) {
      Node curr = set.pollFirst();
      if(x == curr) return x.w;
      for(Edge e: curr.edges) {
       Node other = e.u == curr? e.v : e.u;
        if(other.w > e.cost + curr.w) {
          set.remove(other);
          other.w = e.cost + curr.w:
          set.add(other);
     }
    return -1;
```

private static class Edge {

```
Node u,v;
  int cost:
  public Edge(Node u, Node v, int c) {
    this.u = u; this.v = v;
    cost = c;
}
```

3.2. Bipartite Graphs. The Hopcroft-Karp algorithm finds the maximal matching in a bipartite graph. Also, this matching can together with Könings theorem be used to construct a private static class Node implements Comparable<Node>{ minimal vertex-cover, which as we all know is the complement of a maximum independent set. Runs in  $\mathcal{O}(|E|\sqrt{|V|})$ .

```
import java.util.*;
class Node {
  int id:
 LinkedList<Node> ch = new LinkedList<>();
  public Node(int id) {
    this.id = id;
 }
public class BiGraph {
  private static int INF = Integer.MAX_VALUE;
 LinkedList<Node> L, R;
  int N, M;
 Node[] U;
  int[] Pair, Dist;
  int nild;
  public BiGraph(LinkedList<Node> L, LinkedList<Node> R){
    N = L.size(); M = R.size();
    this.L = L; this.R = R;
    U = new Node[N+M]:
    for(Node n: L) U[n.id] = n;
    for(Node n: R) U[n.id] = n;
  private boolean bfs() {
    LinkedList<Node> Q = new LinkedList<>();
    for(Node n: L)
      if(Pair[n.id] == -1) {
        Dist[n.id] = 0;
        Q.add(n);
      }else
        Dist[n.id] = INF;
```

```
nild = INF;
  while(!Q.isEmpty()) {
    Node u = Q.removeFirst();
    if(Dist[u.id] < nild)</pre>
      for(Node v: u.ch) if(distp(v) == INF){
       if(Pair[v.id] == -1)
          nild = Dist[u.id] + 1;
        else {
         Dist[Pair[v.id]] = Dist[u.id] + 1:
          Q.addLast(U[Pair[v.id]]);
     }
  return nild != INF;
private int distp(Node v) {
  if(Pair[v.id] == -1) return nild;
  return Dist[Pair[v.id]];
private boolean dfs(Node u) {
  for(Node v: u.ch) if(distp(v) == Dist[u.id] + 1) {
    if(Pair[v.id] == -1 || dfs(U[Pair[v.id]])) {
      Pair[v.id] = u.id:
      Pair[u.id] = v.id;
      return true;
   }
  Dist[u.id] = INF;
  return false;
public HashMap<Integer, Integer> maxMatch() {
  Pair = new int[M+N];
  Dist = new int[M+N]:
  for(int i = 0; i < M+N; i++) {
    Pair[i] = -1;
    Dist[i] = INF;
  HashMap<Integer, Integer> out = new HashMap<>();
  while(bfs()) {
    for(Node n: L) if(Pair[n.id] == -1)
      dfs(n):
  for(Node n: L) if(Pair[n.id] != -1)
    out.put(n.id, Pair[n.id]);
```

```
return out;
public HashSet<Integer> minVTC() {
 HashMap<Integer, Integer> Lm = maxMatch();
 HashMap<Integer, Integer> Rm = new HashMap<>();
  for(int x: Lm.keySet()) Rm.put(Lm.get(x), x);
  boolean[] Z = new boolean[M+N];
 LinkedList<Node> bfs = new LinkedList<>();
  for(Node n: L) {
   if(!Lm.containsKey(n.id)) {
      Z[n.id] = true;
      bfs.add(n);
  while(!bfs.isEmpty()) {
    Node x = bfs.removeFirst();
    int nono = -1:
    if(Lm.containsKey(x.id))
      nono = Lm.qet(x.id);
    for(Node y: x.ch) {
      if(y.id == nono || Z[y.id]) continue;
      Z[v.id] = true;
      if(Rm.containsKey(y.id)){
        int xx = Rm.get(y.id);
        if(!Z[xx]) {
          Z[xx] = true;
          bfs.addLast(U[xx1):
        }
     }
   }
  HashSet<Integer> K = new HashSet<>();
  for(Node n: L) if(!Z[n.id]) K.add(n.id);
  for(Node n: R) if(Z[n.id]) K.add(n.id);
  return K;
}
```

3.3. **Network Flow.** The Floyd Warshall algorithm for determining the maximum flow through a graph can be used for a lot of unexpected problems. Given a problem that can be formulated as a graph, where no ideas are found trying, it might help trying to apply network flow. The running time is  $\mathcal{O}(C \cdot m)$  where C is the maximum flow and m is the amount

of edges in the graph. If C is very large we can change the running time to  $\mathcal{O}(\log Cm^2)$  by only studying edges with a large enough capacity in the beginning.

```
import java.util.*;
class Node {
  LinkedList<Edge> edges = new LinkedList<>();
  int id:
  boolean visited = false:
  Edge last = null;
  public Node(int id) {
    this.id = id:
  public void append(Edge e) {
    edges.add(e);
 }
class Edge {
  Node source, sink;
  int cap;
  int id;
  Edge redge:
  public Edge(Node u, Node v, int w, int id){
    source = u; sink = v;
    cap = w;
    this.id = id:
}
class FlowNetwork {
  Node[] adi:
  int edgec = 0;
  HashMap<Integer.Integer> flow = new HashMap<>():
  ArrayList<Edge> real = new ArrayList<Edge>();
  public FlowNetwork(int size) {
    adj = new Node[size];
    for(int i = 0: i<size: i++) {</pre>
      adj[i] = new Node(i);
    }
  void add_edge(int u, int v, int w, int id){
    Node Nu = adi[u], Nv = adi[v];
    Edge edge = new Edge(Nu, Nv, w, edgec++);
    Edge redge = new Edge(Nv, Nu, 0, edgec++);
    edge.redge = redge:
```

```
redge.redge = edge;
  real.add(edge);
  adj[u].append(edge);
  adj[v].append(redge);
  flow.put(edge.id, 0);
  flow.put(redge.id, 0);
void reset() {
  for(int i = 0; i<adj.length; i++) {
    adj[i].visited = false; adj[i].last = null;
  }
}
LinkedList<Edge> find_path(Node s, Node t,
        List<Edge> path){
  reset():
  LinkedList<Node> active = new LinkedList<>();
  active.add(s);
  while(!active.isEmpty() && !t.visited) {
    Node now = active.pollFirst();
    for(Edge e: now.edges) {
      int residual = e.cap - flow.get(e.id);
      if(residual>0 && !e.sink.visited) {
        e.sink.visited = true;
        e.sink.last = e;
        active.addLast(e.sink):
      }
    }
  if(t.visited) {
    LinkedList<Edge> res = new LinkedList<>();
    Node curr = t:
    while(curr != s) {
      res.addFirst(curr.last);
      curr = curr.last.sink;
    return res:
  } else return null;
}
int max_flow(int s, int t) {
  Node source = adi[s];
  Node sink = adj[t];
```

```
LinkedList<Edge> path = find_path(source, sink,
          new LinkedList<Edge>());
 while (path != null) {
   int min = Integer.MAX_VALUE;
   for(Edge e : path) {
     min = Math.min(min, e.cap - flow.get(e.id));
    for (Edge e : path) {
     flow.put(e.id, flow.get(e.id) + min);
     Edge r = e.redge;
     flow.put(r.id, flow.get(r.id) - min);
   path = find_path(source, sink,
            new LinkedList<Edge>());
 int sum = 0:
 for(Edge e: source.edges) {
   sum += flow.get(e.id);
 return sum;
LinkedList<Edge> min_cut(int s, int t) {
 HashSet<Node> A = new HashSet<>();
 LinkedList<Node> bfs = new LinkedList<>();
 bfs.add(adi[s]);
 A.add(adj[s]);
 while(!bfs.isEmpty()) {
   Node i = bfs.removeFirst();
   for(Edge e: i.edges) {
     int c = e.cap - flow.get(e.id);
     if(c > 0 \& \& !A.contains(e.sink)) {
       bfs.add(e.sink);
       A.add(e.sink);
       if(e.sink.id == t) return null;
     }
 LinkedList<Edge> out = new LinkedList<>();
 for(Node n: A) for(Edge e: n.edges)
     if(!A.contains(e.sink) && e.cap != 0)
          out.add(e);
 return out;
```

## 4. Dynamic Programming

}

}

4.1. Longest Increasing Subsequence. Finds the longest increasing subsequence in an array in  $\mathcal{O}(n \log n)$  time. Can easility be transformed to longest decreasing/nondecreasing/nonincreasing subsequence.

```
public static int lis(int[] X) {
 int n = X.length;
 int P[] = new int[n];
 int M[] = new int[n+1]:
  int L = 0;
  for(int i = 0; i < n; i++) {
   int lo = 1:
   int hi = L:
    while(lo<=hi) {</pre>
      int mid = lo + (hi - lo + 1)/2:
      if(X[M[mid]]<X[i])</pre>
        lo = mid+1:
      else
        hi = mid-1:
    int newL = lo;
    P[i] = M[newL-1];
    M[newL] = i:
    if (newL > L)
      L = newL;
  int[] S = new int[L];
  int k = M[L]:
 for (int i = L-1; i >= 0; i--) {
   S[i] = k; //or X[k]
   k = P[k];
  return L; // or S
```

4.2. Knuuth Morris Pratt substring. Finds if w is a sub-array to s in linear time.

```
//assumes s.length>=w.length
public static boolean kmp(int [] w, int [] s) {
  int T[] = new int[w.length];
```

```
T[0] = -1; T[1] = 0;
int m = 0, i = 2;
while(i<w.length) {</pre>
  if(w[i-1] == w[m]) {
    T[i] = ++m;
    i++;
  } else if (m>0) {
    m = T[m];
  } else {
   T[i] = 0;
    i++;
  }
m = 0; i = 0;
while(m+i<s.length){</pre>
  if(w[i] == s[m+i]) {
    if(i == w.length - 1)
      return true; //m
    i++;
  } else {
    if(T[i] > -1) {
      m = m + i - T[i];
      i = T[i];
    } else {
     i = 0;
      m = m+1:
    }}}
return false;
                      5. ETC
```

Ax = b by Gaussian elimination. This can for example be used to determine the expected value of each node in a markov chain. Runns in  $\mathcal{O}(N^3)$ .

```
//Computes A^{-1} * b
static double[] solve(double[][] A, double[] b) {
 int N = b.length:
 // Gaussian elimination with partial pivoting
 for (int i = 0; i < N; i++) {
   // find pivot row and swap
   int max = i:
```

```
for (int j = i + 1; j < N; j++)
    if (Math.abs(A[j][i]) > Math.abs(A[max][i]))
      max = j;
  double[] tmp = A[i];
  A[i] = A[max];
  A[max] = tmp;
  double tmp2 = b[i];
  b[i] = b[max];
  b[max] = tmp2:
  // A doesn't have full rank
  if (Math.abs(A[i][i])<0.00001) return null;</pre>
  // pivot within b
  for (int j = i + 1; j < N; j++)
   b[j] = b[i] * A[j][i] / A[i][i];
  // pivot within A
  for (int j = i + 1; j < N; j++) {
    double m = A[j][i] / A[i][i];
    for (int k = i+1; k < N; k++)
      A[i][k] -= A[i][k] * m;
    A[j][i] = 0.0;
 }
// back substitution
double[] x = new double[N];
for (int j = N - 1; j >= 0; j --) {
  double t = 0.0;
  for (int k = j + 1; k < N; k++)
   t += A[j][k] * x[k];
  x[j] = (b[j] - t) / A[j][j];
return x;
```

5.1. System of Equations. Solves the system of equations 5.2. Convex Hull. From a collection of points in the plane the convex hull is often used to compute the largest distance or the area covered, or the length of a rope that encloses the points. It can be found in  $\mathcal{O}(N \log N)$  time by sorting the points on angle and the sweeping over all of them.

}

```
import iava.util.*:
public class ConvexHull {
  static class Point implements Comparable<Point> {
    static Point xmin;
   int x, y;
    public Point(int x, int y) {
```

```
this.x = x; this.y = y;
 public int compareTo(Point p) {
    int c = cross(this, xmin, p);
   if(c!=0) return c;
    double d = dist(this,xmin) - dist(p,xmin);
    return (int) Math.signum(d);
static double dist(Point p1, Point p2) {
  return Math.hypot(p1.x - p2.x, p1.y - p2.y);
static int cross(Point a, Point b, Point c) {
 int dx1 = b.x - a.x;
 int dy1 = b.y - a.y;
 int dx2 = c.x - b.x;
 int dy2 = c.y - b.y;
 return dx1*dy2 - dx2*dy1;
Point[] convexHull(Point[] S) {
 // find a point on th econvex hull.
 int N = S.length;
 Point xmin = S[0]:
 int id = 0;
 for(int i = 0; i < N; i++) {
    Point p = S[i];
   if(xmin.x > p.x | |
      xmin.x == p.x \&\& xmin.y > p.y) {
      xmin = p;
      id = i;
   }
 }
 S[id] = S[N-1];
 S[N-1] = xmin;
 Point.xmin = xmin;
 // Sort on angle of xmin.
 Arrays.sort(S, 0, N-1);
 Point[] H = new Point[N+1];
 H[0] = S[N-2];
 H[1] = xmin;
 for(int i = 0; i < N-1; i++)
   H[i+2] = S[i];
 int M = 1;
 for(int i = 2; i \le N; i++) {
```

ok = false;

maxc[i] = Integer.bitCount(i);
max = Math.max(max, maxc[i]);

if(ok) {

```
while(cross(H[M-1],H[M],H[i]) <= 0) {
       if(M>1)
         M--;
        else if (i == N)
          break;
        else
          i += 1;
      }
      M+=1:
      Point tmp = H[M];
      H[M] = H[i];
      H[i] = tmp;
    Point[] Hull = new Point[M];
    for(int i = 0; i < M; i++)
      Hull[i] = H[i];
    return Hull;
}
```

## 6. NP Tricks

6.1. MaxClique. The max clique problem is one of Karp's 21 NP-complete problems. The problem is to find the lagest subset of an undirected graph that forms a clique - a complete graph. There is an obvious algorithm that just inspects every subset of the graph and determines if this subset is a clique. This algorithm runns in  $\mathcal{O}(n^22^n)$ . However one can use the meet in the middle trick (one step divide and conqurer) and reduce the complexity to  $\mathcal{O}(n^22^{\frac{n}{2}})$ .

```
static int max_clique(int n, int[][] adj) {
   int fst = n/2;
   int snd = n - fst;
   int[] maxc = new int[1<<fst];
   int max = 1;
   for(int i = 0; i<(1<<fst); i++) {
      for(int a = 0; a<fst; a++) {
        if((i&1<<a) != 0)
            maxc[i] = Math.max(maxc[i], maxc[i^(1<<a)]);
      }
   boolean ok = true;
   for(int a = 0; a<fst; a++) if((i&1<<a) != 0) {
      for(int b = a+1; b<fst; b++) {
        if((i&1<<b) != 0 && adj[a][b] == 0)</pre>
```

```
for(int i = 0; i < (1 << snd); i++) {
 boolean ok = true;
 for(int a = 0; a<snd; a++) if((i&1<<a) != 0) {
    for(int b = a+1; b<snd; b++) {</pre>
     if((i\&1 << b) != 0)
        if(adj[a+fst][b+fst] == 0)
          ok = false;
   }
 if(!ok) continue;
  int mask = 0;
  for(int a = 0; a<fst; a++) {</pre>
   ok = true;
    for(int b = 0; b < snd; b++) {
     if((i&1<<b) != 0) {
        if(adj[a][b+fst] == 0) ok = false;
      }
   if(ok) mask |= (1<<a);
 max = Math.max(Integer.bitCount(i) + maxc[mask],
          max);
return max;
```