

Group Homework 3

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1. 604.124_8 to base 12 = $\boxed{284.1B7_{12}}$

$$= 6 \times 8^2 + 0 \times 8^1 + 4 \times 8^0 + 1 \times 8^{-1} + 2 \times 8^{-2} + 4 \times 8^{-3} = 388.1340625_{10}$$

$$\begin{array}{l|l} \begin{array}{l} n \geq 3\log_{12}8 \\ n = 3 \end{array} & \begin{array}{l} 388 \div 12 = 32 \quad R4 \\ 32 \div 12 = 2 \quad R8 \\ 2 \div 12 = 0 \quad R2 \end{array} \end{array} \quad \begin{array}{l} 12 \times .1640625 = 1 + .96875 \\ 12 \times .96875 = 11 + .6142 \\ 12 \times .6142 = 7 + .3704 \quad \text{round up} \end{array}$$

2. 374.24_{13} to base 8 = $\boxed{1132.133_8}$

$$= 3 \times 13^2 + 7 \times 13^1 + 4 \times 13^0 + 2 \times 13^{-1} + 4 \times 13^{-2} = 602.177514792_{10}$$

$$\begin{array}{l|l} \begin{array}{l} n \geq 2\log_8 13 \\ n = 3 \end{array} & \begin{array}{l} 602 \div 8 = 75 \quad R2 \\ 75 \div 8 = 9 \quad R3 \\ 9 \div 8 = 1 \quad R1 \\ 1 \div 8 = 0 \quad R1 \end{array} \end{array} \quad \begin{array}{l} 8 \times .177514792 = 1 + .420118336 \\ 8 \times .420118336 = 3 + .360946688 \\ 8 \times .360946688 = 2 + .887573504 \quad \text{round up} \end{array}$$

3. $3A4.24_{16}$ to base 5 = $\boxed{12212.0323_5}$

$$= 3 \times 16^2 + 10 \times 16^1 + 4 \times 16^0 + 2 \times 16^{-1} + 4 \times 16^{-2} = 932.140625_{10}$$

$$\begin{array}{l|l} \begin{array}{l} n \geq 2\log_5 16 \\ n = 4 \end{array} & \begin{array}{l} 932 \div 5 = 186 \quad R2 \\ 186 \div 5 = 37 \quad R1 \\ 37 \div 5 = 7 \quad R2 \\ 7 \div 5 = 1 \quad R2 \\ 1 \div 5 = 0 \quad R1 \end{array} \end{array} \quad \begin{array}{l} 5 \times .140625 = 0 + .703125 \\ 5 \times .703125 = 3 + .515625 \\ 5 \times .515625 = 2 + .578125 \\ 5 \times .578125 = 2 + .890625 \quad \text{round up} \end{array}$$

4. $427.2B_{14}$ to base 6 = $\boxed{3443.111_6}$

$$= 4 \times 14^2 + 2 \times 14^1 + 7 \times 14^0 + 2 \times 14^{-1} + 11 \times 14^{-2} = 819.198979591_{10}$$

$$\begin{array}{l|l} n \geq 2\log_6 14 & \begin{array}{l} 819 \div 6 = 136 \quad R3 \\ 136 \div 6 = 22 \quad R4 \\ 22 \div 6 = 3 \quad R4 \\ 3 \div 6 = 0 \quad R3 \end{array} \\ n = 3 & \end{array} \quad \begin{array}{l} 6 \times .198979591 = 1 + .193877551 \\ 6 \times .193877551 = 1 + .163265306 \\ 6 \times .163265306 = 0 + .9795991836 \quad \text{round up} \end{array}$$

5. 344.12_5 to base 20 = $\boxed{4J.A8_{20}}$

$$= 3 \times 5^2 + 4 \times 5^1 + 4 \times 5^0 + 1 \times 5^{-1} + 2 \times 5^{-2} = 99.52_{10}$$

$$\begin{array}{l|l} n \geq 2\log_{20} 5 & \begin{array}{l} 99 \div 20 = 4 \quad R19 \\ 4 \div 20 = 0 \quad R4 \end{array} \\ n = 2 & \end{array} \quad \begin{array}{l} 20 \times .52 = 10 + .4 \\ 20 \times .4 = 8 + 0.0 \quad \text{round down} \end{array}$$

6. $3B74.2C4_{18}$ to base 9 = $\boxed{32054.1304_9}$

$$= 3 \times 18^3 + 11 \times 18^2 + 7 \times 18^1 + 4 \times 18^0 + 2 \times 18^{-1} + 12 \times 18^{-2} + 4 \times 18^{-3}$$

$$= 21190.148834019_{10}$$

$$\begin{array}{l|l} n \geq 3\log_9 18 & \begin{array}{l} 21190 \div 9 = 2354 \quad R4 \\ 2354 \div 9 = 261 \quad R5 \\ 261 \div 9 = 29 \quad R0 \\ 29 \div 9 = 3 \quad R2 \\ 3 \div 9 = 0 \quad R3 \end{array} \\ n = 4 & \end{array} \quad \begin{array}{l} 9 \times .148834019 = 1 + .339506171 \\ 9 \times .339506171 = 3 + .055555539 \\ 9 \times .055555539 = 0 + .499999851 \\ 9 \times .499999851 = 4 + .499998659 \quad \text{round down} \end{array}$$

7. 120221_3 to base 9 = $\boxed{527_9}$

8. 322.14_8 to base 4

$$= 011010010.001100_2$$

$$= \boxed{3102.030_4}$$

9. 374.24_9 to base 27

$$= 102111.021100_3$$

$$= \boxed{BD.79_{27}}$$

10. 3112.22_4 to base 16 = $\boxed{D6.A_{16}}$