

Задорожний Антон 219/5

Правило Лопиталя

$$1) \lim_{x \rightarrow 1} \frac{3x^2 - 2x + 1}{x^2 + x + 2} = \frac{2}{0}$$

пример не подходит

$$2) \lim_{x \rightarrow 0} \frac{x \cos 3x}{1} = \lim_{x \rightarrow 0} x = \frac{0}{0}$$

$$\lim_{x \rightarrow a} \frac{f'(x)}{g'(x)}$$

$$f(x) = x \quad g(x) = \cos 3x$$

$$f'(x) = 1 \quad g'(x) = -3 \sin(3x)$$

$$\lim_{x \rightarrow 0} \frac{1}{-3 \sin(3x)} = \frac{1}{0}$$

$$3) \lim_{x \rightarrow 3} \left(\frac{6}{x-x^2} - \frac{1}{x+5} \right) = \lim_{x \rightarrow 3} \frac{6-3+x}{x-x^2} = \lim_{x \rightarrow 3} \frac{3+x}{x-x^2} =$$

$$\lim_{x \rightarrow -3.5} \frac{1}{5-x} = \frac{1}{8}$$

$$\lim_{x \rightarrow a} \frac{f'(x)}{g'(x)}$$

$$f(x) = 1$$

$$g(x) = 3-x$$

$$f'(x) = 0$$

$$g'(x) = -1$$

$$\lim_{x \rightarrow 3} \frac{0}{-1} = 0$$

$$4) \lim_{x \rightarrow 1} x^{\frac{1}{1-x}}$$

$$\lim_{x \rightarrow 1} \frac{\ln(x)}{-x+1} = \frac{0}{0}$$

$$\lim_{x \rightarrow a} \frac{f(x)}{g(x)}$$

$$\lim_{x \rightarrow 1}$$

$$5) \lim_{x \rightarrow 2} \frac{1}{x-2}$$

$$\lim_{x \rightarrow 2} \frac{1}{x-2}$$

$$\lim_{x \rightarrow 2} \frac{1}{x-2}$$

$$6) \lim_{x \rightarrow 0}$$

$$\frac{1}{x}$$

$$f(x)$$

$$f'(x)$$

$$\lim_{x \rightarrow 0}$$

$$1) y$$

$$\lim_{x \rightarrow a} \frac{f'(x)}{g'(x)} \quad f(x) = \ln x \quad g(x) = -x + 1$$

$$f'(x) = \frac{1}{x} \quad g'(x) = -1$$

$$\lim_{x \rightarrow 1} \frac{\frac{1}{x}}{-1} = \frac{1}{-1} = -1$$

$$5) \lim_{x \rightarrow \frac{\pi}{2}} \frac{f(x)}{g(x)} \quad f(x) = \ln(\tan x) \quad g(x) = \frac{1}{\cos x}$$

$$f'(x) = \frac{1}{\tan x} \cdot \sec^2 x \quad g'(x) = \frac{\sin x}{\cos^2 x}$$

$$\lim_{x \rightarrow \frac{\pi}{2}} \frac{\frac{\sec^2 x}{\tan x}}{\frac{\sin x}{\cos^2 x}} = \frac{\sec^2(\frac{\pi}{2}) + \frac{1}{\tan(\frac{\pi}{2})}}{\frac{\sin(\frac{\pi}{2})}{\cos^2(\frac{\pi}{2})}} = \frac{\cos(1) + 1 \cdot \tan(\frac{1}{2}) + \frac{1}{\tan(\frac{1}{2})}}{\sin(\frac{1}{2})}$$

$$6) \lim_{x \rightarrow 0} x^{\frac{1}{2} \ln x} = \lim_{x \rightarrow 0} \frac{\ln x}{-\frac{1}{2x}} = \frac{\infty}{-\infty} = \frac{\infty}{\infty}$$

$$\lim_{x \rightarrow a} \frac{f'(x)}{g'(x)}$$

$$f(x) = \ln x$$

$$f'(x) = \frac{1}{x}$$

$$\lim_{x \rightarrow 0} \frac{\frac{1}{x}}{\frac{1}{2x}} = \frac{\infty}{\infty}$$

$$g(x) = -\frac{\ln x}{2} + \frac{1}{4}$$

$$g'(x) = -\frac{1}{2x}$$

- unbestimmt

l'Hôpital'sche Regel

anwenden

$$1) y = 3x^2 + 5x + 9$$

$\Delta y = ?$

$$x_1 = 3$$

$$\Delta y = y_2 - y_1$$

$$x_2 = 3,001$$

$$\Delta y_1 = 3 \cdot 3^2 + 5 \cdot 3 + 1 = 27 + 15 + 1 = 43$$

$$y_2 = 3 \cdot (3,001)^2 + 5 \cdot 3,001 + 1 = 3 \cdot 9,00601 + 15,005 =$$

$$27,01803 + 15,005 + 1 = 43,02303$$

$$\Delta y = 43,02303 - 43 = \underline{0,02303}$$

$$2) y = x^3 - 4x^2 - 6x + 3 \quad x = 1,03$$

$$y = 1,092727 - 4 \cdot 1,0609 + 6,18 + 3 =$$

$$10,272727 - 4,2436 = \underline{10,029127}$$

Задача 215/5

ПР 2.

$$2. y = \frac{1}{3}x^3 + 2x^2 - \frac{1}{3}$$

$$y' = \left(\frac{1}{3}x^3 + 2x^2 - \frac{1}{3}\right)' = y' = \left(\frac{1}{3}x^3\right)' + (2x^2)' - \left(\frac{1}{3}\right)' =$$

$$y' = \frac{1}{3} \cdot 3x^2 + 2 \cdot 2x - 0$$

$$y' = x^2 + 4x$$

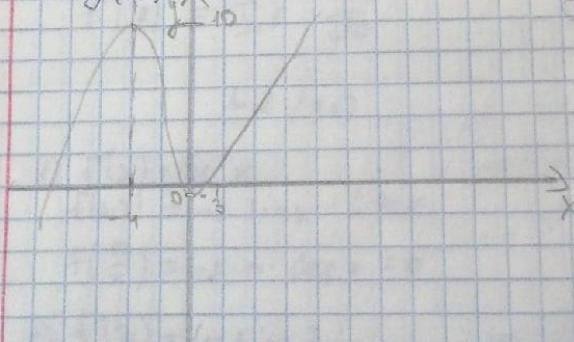
$$x^2 + 4x = 0$$

$$x(x+4) = 0$$

$$x_1 = 0 \quad x_2 = -4$$

$$\max 1) y(-4) = \frac{1}{3}(-4)^3 + 2(-4)^2 - \frac{1}{3} = -\frac{64}{3} + 32 - \frac{1}{3} = \frac{32}{3} - \frac{1}{3} = \frac{31}{3}$$

$$\min 2) y(0) = 0 + 0 - \frac{1}{3} = -\frac{1}{3}$$



$$3. S = -t^3 + 6t^2 + 24t - 5$$

$$(V)' = \frac{(S(t))'}{(t)'} = -3t^2 + 12t + 24$$

Найдем t_{\max} и t_{\min} $V = \max$

$$V'(t) =$$

Условие

$$t = 1$$

Числ. Точ

V_{\max}

$$2. y = \frac{1}{3}$$

$$y' =$$

$$y' =$$

$$2x$$

$$x$$

$$1) y$$

$$2) y$$

$$V'(t) = -6t + 12 \quad -6t + 12 = 0 \quad t = 2$$

Проверим $V'(t)$ на экстрем. значения

$$t = 1 < 2 \quad V'(1) = 6 > 0 \quad t = 3 > 2 \quad V'(3) = -6 < 0$$

След. точка $t = 2$ есть точка макс.

$$V_{\max} = -3 \cdot 4 + 12 \cdot 2 + 24 = 36$$

$$y = \frac{2}{3}x^3 + 4x^2 - 10$$

$$y' = \left(\frac{2}{3}x^3\right)' + (4x^2)' - (10)' = y' = \frac{2}{3} \cdot 3x^2 + 4 \cdot 2x - 0$$

$$y' = 2x^2 + 8x$$

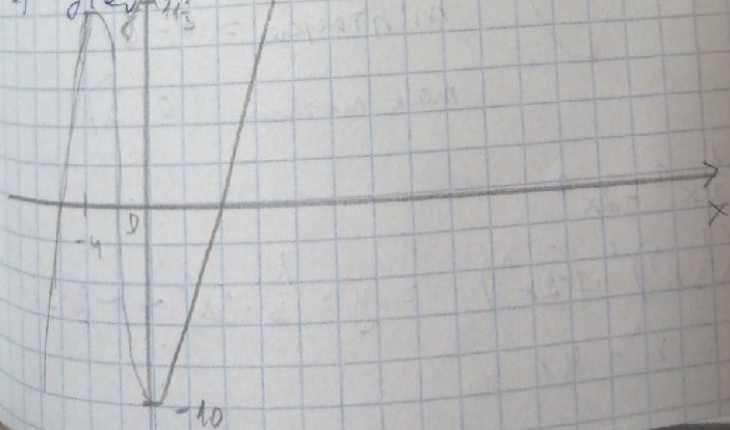
$$2x^2 + 8x = 0$$

$$x(2x + 8) = 0$$

$$x_1 = 0 \quad x_2 = -4$$

$$1) \quad y(-4) = \frac{2}{3}(-4)^3 + 4(-4)^2 - 10 = -\frac{128}{3} + 64 - 10 = 11\frac{1}{3} \text{ max}$$

$$2) \quad y(0) = 0 + 0 - 10 = -10 \text{ min}$$



$$3. S = -t^3 + 5t^2 - 24t + 3$$

$$(V)' = -3t^2 + 10t - 24$$

Найдем t_{max} и при V_{max}

$$(V)' = -6t + 18 = 0$$

$$t = 3$$

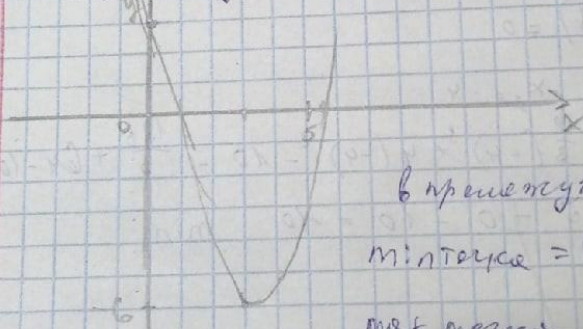
$$V_{max} = -3 \cdot 3^2 + 18 \cdot 3 - 24 = -27 + 54 - 24 = 3$$

$$2. y = x^2 - 6x + 9$$

Найдем мин. значение функции, $x = \frac{-b}{2a} = 3$

$$y = 3^2 - 6 \cdot 3 + 9 = 9 - 18 + 9 = 0$$

$$\text{пересечение } y = 0^2 - 6 \cdot 0 + 9 = 9$$



В промежутке от 0 до 3

$$\text{минимум} = (3; 0)$$

$$\text{максимум} = (0; 9)$$

$$3. y = \frac{1}{3}x^3 - 2x^2$$

$$y' = \left(\frac{1}{3}x^3\right)' - (2x^2)' = y' = \frac{1}{3} \cdot 3x^2 - 2 \cdot 2x$$

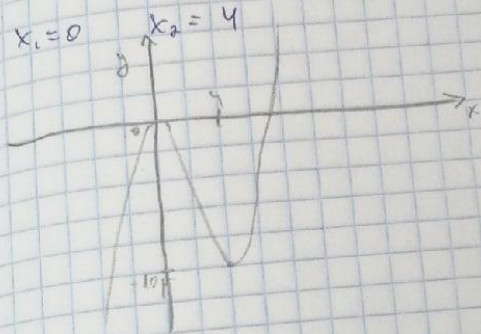
$$y' = x^2 - 4x$$

$$x^2 - 4x = 0$$

$$x(x-4) = 0$$

$$x_1 = 0$$

$$x_2 = 4$$



$$1) y(4) = \frac{1}{3}(4)^3 - 2(4)^2 = \frac{64}{3} - 32 = -10 \frac{2}{3}$$

$$2) y(0) = 0$$

$$y(4) = 6 + -4 = 2$$