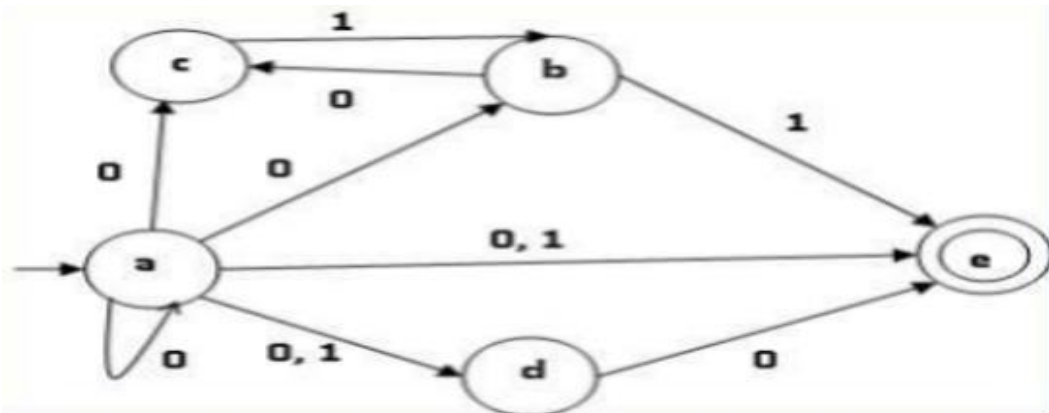


ASSIGNMENT 2

Q. Minimize the given DFA:



Q. Convert the given Moore machine into Mealy machine. Draw state transition diagram of Mealy machine.

Present State	Next State		Output
	0	1	
$\rightarrow p_0$	r	q ₀	ϵ
p ₁	r	q ₀	1
q ₀	p ₁	s ₀	0
q ₁	p ₁	s ₀	1
r	q ₁	p ₁	0
s ₀	s ₁	r	0
s ₁	s ₁	r	1

Q. Write Regular Expressions corresponding to each of the following subsets of $\{0,1\}^*$

- (i) The language of all strings in $\{0,1\}^*$ that containing at least two 0's.
- (ii) The language of all strings containing both 101 and 010 as substrings.
- (iii) The language of all strings that do not end w

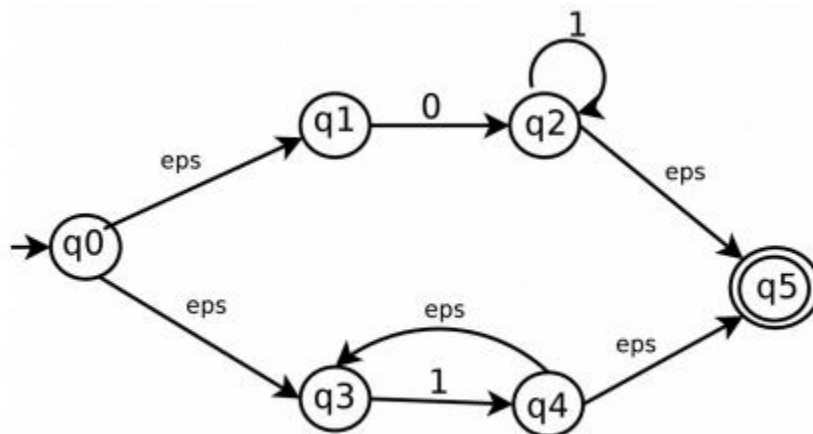
Q. Draw a FA for following regular language.

- (i) $(11+110)^* 0$ (ii) $(0+1)^*(10$

Q. Design an NFA with no more than five states for set $\{abab^n | n \geq 0\} \cup \{aba^n | n \geq 0\}$

Q. Design an NFA for all strings containing at least two a's or exactly two b's.

Q. Convert epsilon NFA to DFA



Q. Suppose that language A_1 has a context-free grammar $G_1 = (V_1, \Sigma, R_1, S_1)$, and language A_2 has a context-free grammar $G_2 = (V_2, \Sigma, R_2, S_2)$, where, for $i = 1, 2$, V_i is the set of variables, R_i is the set of rules, and S_i is the start variable for CFG G_i . The CFGs have the same set of terminals Σ . Assume that $V_1 \cap V_2 = \emptyset$. Define another CFG $G_3 = (V_3, \Sigma, R_3, S_3)$ with $V_3 = V_1 \cup V_2 \cup \{S_3\}$, where $S_3 \in V_1 \cup V_2$, and $R_3 = R_1 \cup R_2 \cup \{S_3 \rightarrow S_1, S_3 \rightarrow S_2\}$. Argue that G_3 generates the language $A_1 \cup A_2$. Thus, conclude that the class of context-free languages is closed under union

Q. Define derivation, types of derivation, Derivation tree & ambiguous grammar. Give example for each.

Q. Using pumping lemma for CFL prove that below languages are not context free $\{p \mid p \text{ is a prime}\}$

Q. Given the Context Free Grammar G, find a CFG G' in Chomsky Normal Form generating $L(G) - \{ \}$

$$S \rightarrow aY \mid Ybb \mid Y$$

$$X \rightarrow \wedge \mid a$$

$$Y \rightarrow aXY \mid bb \mid XX$$

Q. Describe the Chomsky hierarchy of languages.

Q. Show that the CFG with productions

$$S \rightarrow a \mid Sa \mid bSS \mid SSb \mid SbS \text{ is ambiguous.}$$

Q. Prove that There are CFLs L_1 and L_2 so that $L_1 \cap L_2$ is not a CFL, and there is a CFL L so that L' is not a CFL.

Q. For the language $L = \{ xc x^R \mid x \in \{a,b\}^* \}$ design a PDA(Push Down Automata)

Q. Write PDA for following languages: $\{ a^i b^j c^k \mid i, j, k \geq 0 \text{ and } j = i \text{ or } j = k \}$

Q. $L = \{ 0^n 1^m \mid n \geq 1, m \geq 1, m > n + 2 \}$. Construct a PDA for the language L.

Q. Give transition tables for deterministic PDA recognizing following language:

$$L = \{ x \in \{a, b\}^* \mid n_a(x) \neq n_b(x) \}$$

Trace it for the string abbaababbb

Q. Convert PDA to CFG. PDA is given by $P = (\{p,q\}, \{0,1\}, \{X,Z\}, \delta, q, Z)$, Transition function δ is defined by

$$\delta(q, 1, Z) = \{(q, XZ)\}$$

$$\delta(q, 1, X) = \{(q, XX)\}$$

$$\delta(q, H, X) = \{(q, H)\}$$

$$\delta(q, 0, X) = \{(p, X)\}$$

$$\delta(p, 1, X) = \{(p, H)\}$$