



3D Face Reconstruction from a Single Image Using a Single Reference Face Shape

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Naïve model

Assumptions:

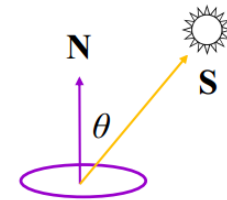
- 1.a Lambertian object
- 2.a set of images from the same view of the same object with known light directions.

Known: source vectors S_j and pixel values $I_j(x,y)$

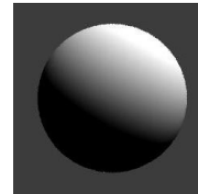
Unknown: surface normal $N(x,y)$ and albedo $\rho(x,y)$

$$B = \rho(\mathbf{N} \cdot \mathbf{S})$$

Diffuse reflection: Lambert's law



$$B = \rho(\mathbf{N} \cdot \mathbf{S})$$
$$= \rho \|\mathbf{S}\| \cos \theta$$



B : radiosity (total power leaving the surface per unit area)
 ρ : albedo (反射率 fraction of incident irradiance reflected by the surface)
 N : unit normal
 S : source vector (magnitude proportional to intensity of the source)

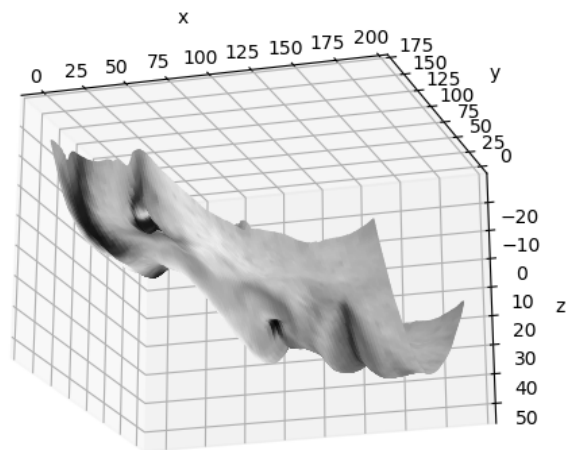
(from lecutre04 light)

Naïve model

Known: source vectors S_j and pixel values $I_j(x,y)$

Unknown: surface normal $N(x,y)$ and albedo $\rho(x,y)$

$$\begin{aligned} I_j(x,y) &= k \rho(x,y) (\mathbf{N}(x,y) \cdot \mathbf{S}_j) \\ &= (\rho(x,y) \mathbf{N}(x,y)) \cdot (k \mathbf{S}_j) \\ &= \mathbf{g}(x,y) \cdot \mathbf{V}_j \end{aligned}$$



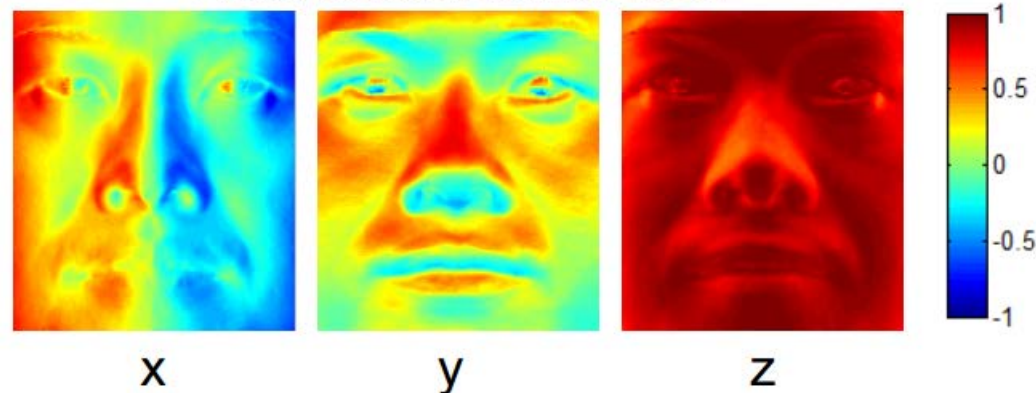
“integrability”
有限差分近似微分

For each pixel, set up a linear system:

$$\begin{bmatrix} I_1(x,y) \\ I_2(x,y) \\ \vdots \\ I_n(x,y) \end{bmatrix} = \begin{bmatrix} \mathbf{V}_1^T \\ \mathbf{V}_2^T \\ \vdots \\ \mathbf{V}_n^T \end{bmatrix} \mathbf{g}(x,y)$$

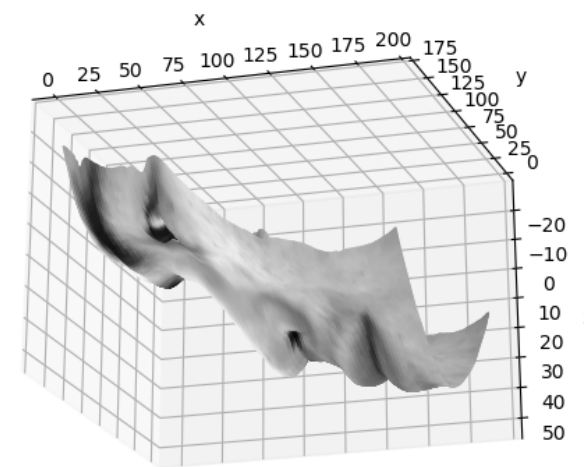
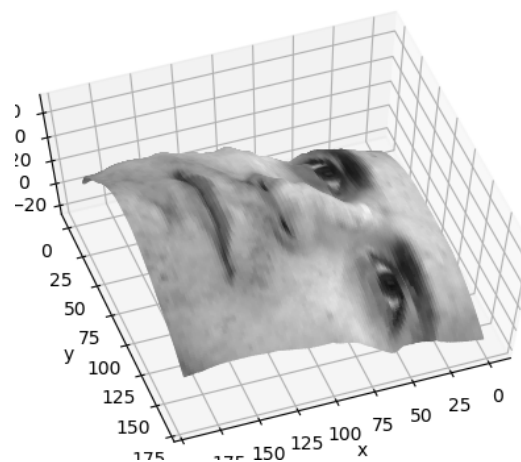
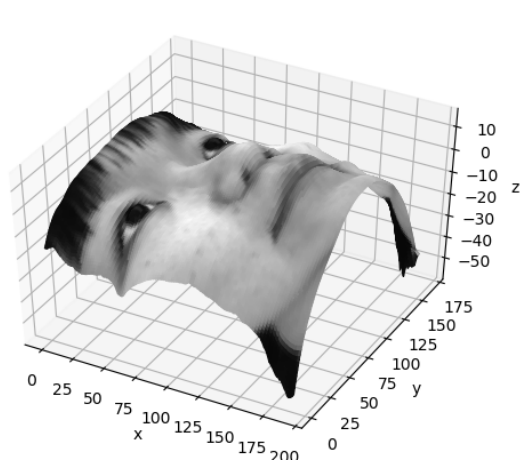
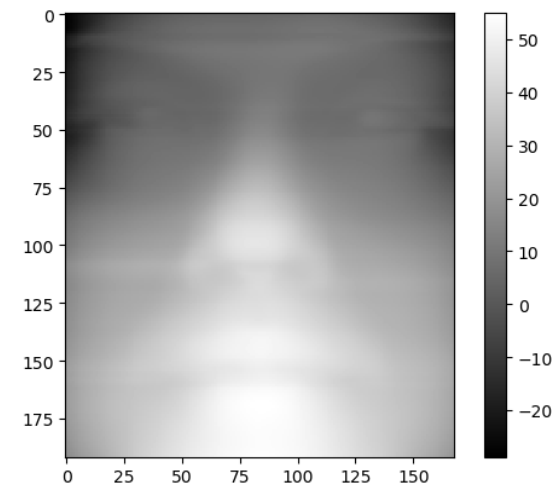
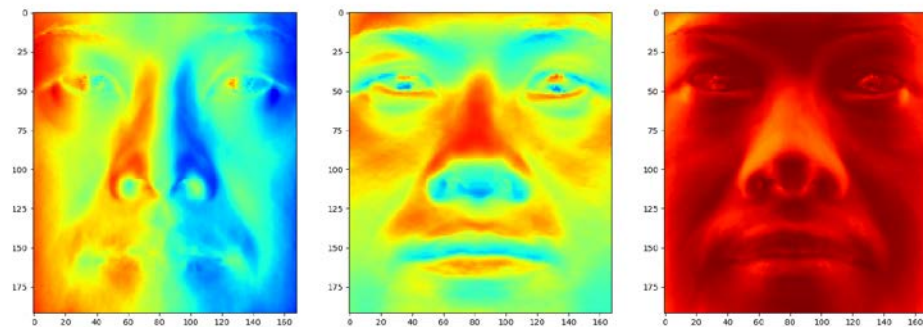
$(n \times 1)$ known $(n \times 3)$ known (3×1) unknown

Recovered normal field



partly quoted from lecutre04 light

Experiments result



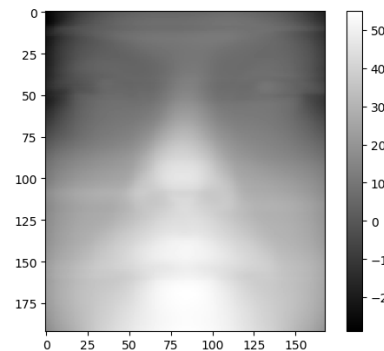
Research base on YaleB chopped database

Advanced model



Assumptions:

1. A single picture of a nearly frontal face
2. a reference 3-D face model with norms, albedo, depth.
3. No cast shadow, interreflection



✓



Fig. 2. The generic face model obtained by taking the mean shape over the entire USF database.

×



3D Face Reconstruction from a Single Image Using a Single Reference Face Shape

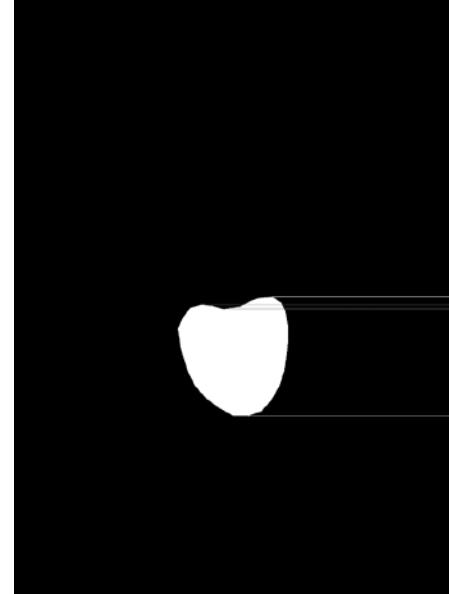
Ira Kemelmacher-Shlizerman, *Member, IEEE*, and Ronen Basri, *Senior Member, IEEE*



Region estimate

steps:

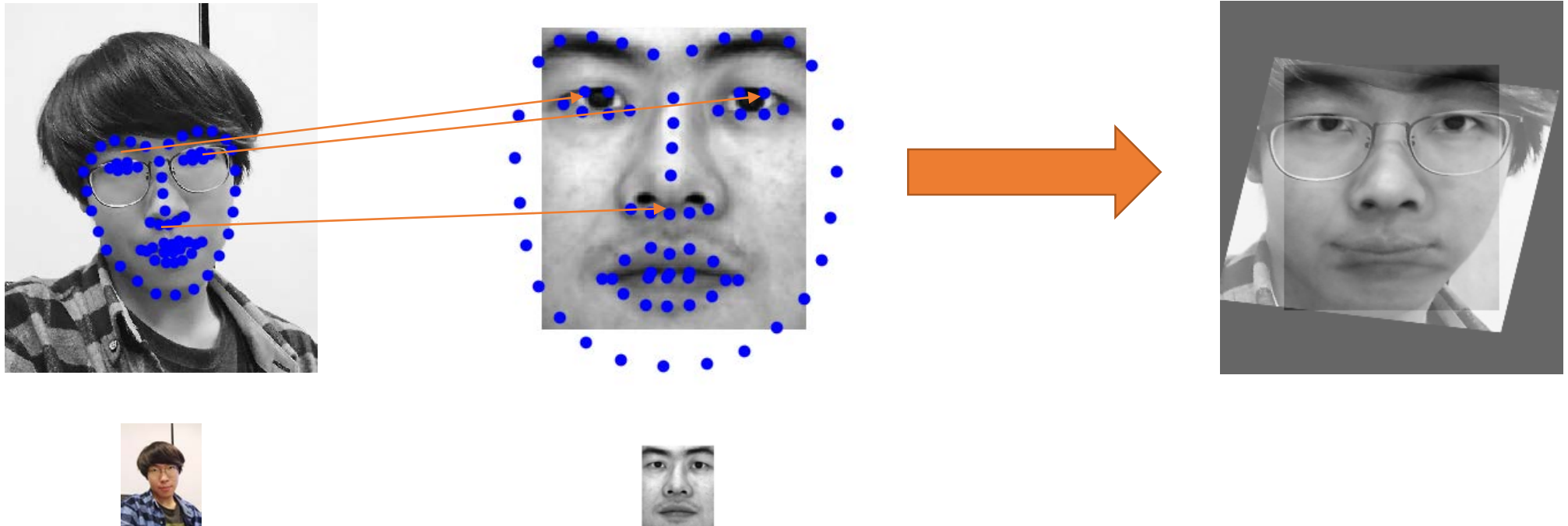
- 1.extract key points from faces(pretrained)
- 2.take the closed region of the rounding key points



Rough alignment

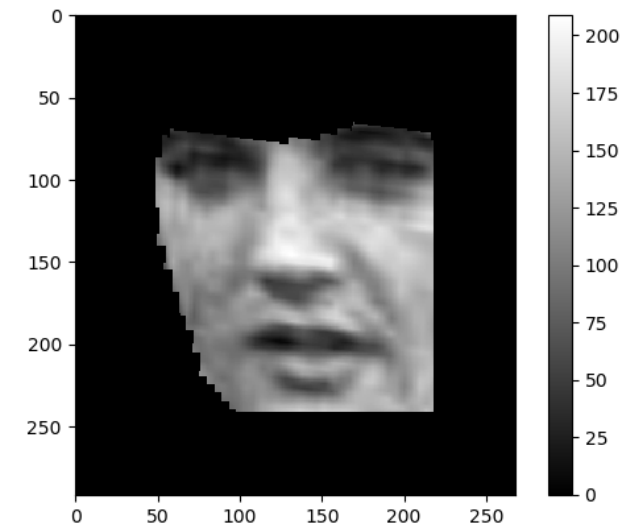
steps:

- 1.extract key points from faces(pretrained)
- 2.apply rigid transformation with three key points (two eyes and nose)
- 3.derive the intersection of obj. face and ref. face



Rough alignment

The assignment of region Ω : intersection of obj face region and ref face region



Ω



Light coefficient (general Idea)

Nth order of spherical harmonic approximation, the light reflected by a Lambertian surface:

$$R(x, y) \approx \sum_{n=0}^N \sum_{m=-n}^n l_{nm} \alpha_n Y_{nm}(x, y),$$

2th order of approximation:

$$R(\vec{n}(x, y); \rho(x, y), \vec{l}) \approx \vec{l}^T \vec{Y}(\vec{n}(x, y)), \quad \vec{Y}(\vec{n}) = (1, \boxed{n_x, n_y, n_z}, n_x n_y, n_x n_z, n_y n_z, n_x^2 - n_y^2, 3n_z^2 - 1)^T, \quad I(x, y) = \rho(x, y) R(x, y).$$

Loss function:

$$\min_{\vec{l}} \sum_{(x, y) \in \Omega} (I(x, y) - \rho_{\text{ref}}(x, y) \vec{l}^T \vec{n}_{\text{ref}}(x, y))^2.$$



Depth recovery(general Idea)

Data term:

$$I(x, y) = \rho(x, y)R(x, y). \quad R(\vec{n}(x, y); \rho(x, y), \vec{l}) \approx \vec{l}^T \vec{Y}(\vec{n}(x, y)),$$

$$\vec{Y}(\vec{n}) = \left(1, \frac{1}{N}p, \frac{1}{N}q, \frac{-1}{N}, \frac{1}{N^2}pq, \frac{-1}{N^2}p, \frac{-1}{N^2}q, \right. \\ \left. \frac{1}{N^2}(p^2 - q^2), \frac{3}{N^2} - 1 \right)^T, \quad N(x, y) = \sqrt{p^2 + q^2 + 1}$$



$$I = \rho_{\text{ref}} l_0 + \frac{\rho_{\text{ref}}}{N_{\text{ref}}} (l_1 z(x+1, y) - l_1 z(x, y) \\ + l_2 z(x, y+1) - l_2 z(x, y) - l_3,$$

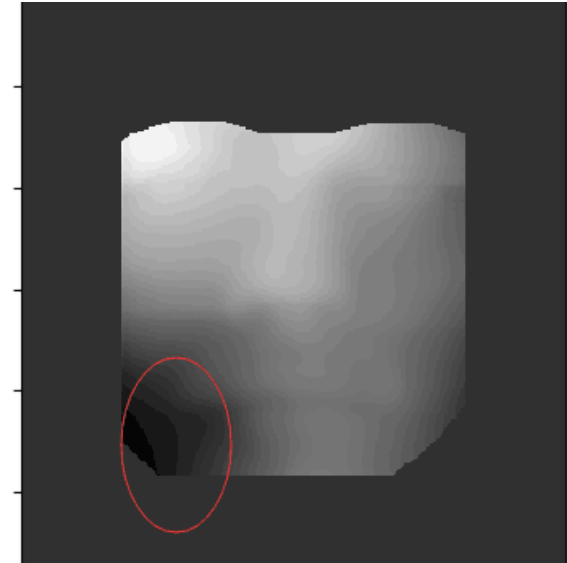
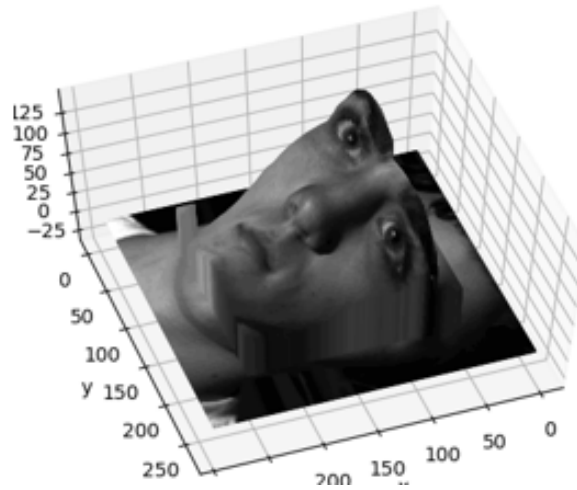
$$p = z(x+1, y) - z(x, y).$$

$$q = z(x, y+1) - z(x, y).$$

Regularization term:

$$\lambda_1(z(x, y) - G * z(x, y)) = \lambda_1(z_{\text{ref}}(x, y) - G * z_{\text{ref}}(x, y)).$$

Experiments result ☹️



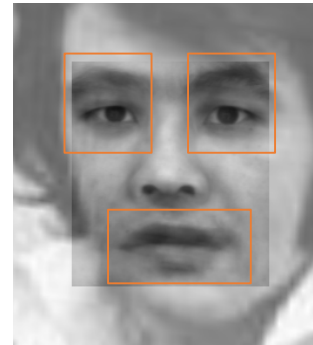


Causes

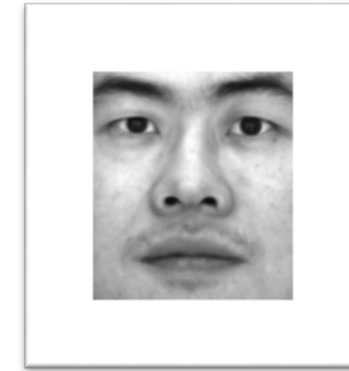
1. the reference model is not “mean” enough
2. Is the lighting coefficient estimating method effective? *
3. Is the depth assumption too rigid?
4. Ambiguous boundary conditions

Observations from lightening coefficients

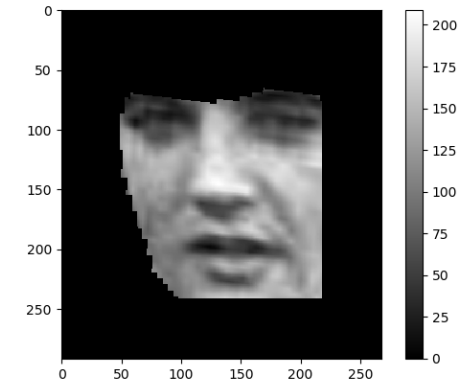
- Unrobustness lightning evaluation (why?)



huge difference
between
reference model
and actual image
at eyes at some
regions



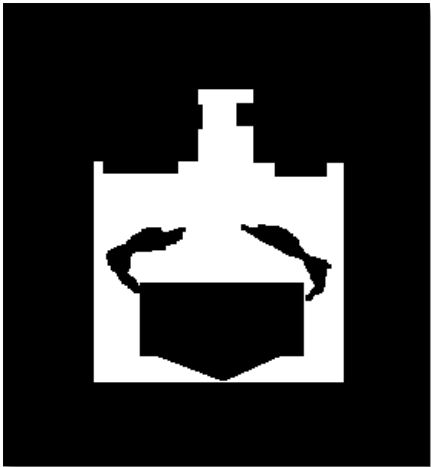
scaled reference
model albedo



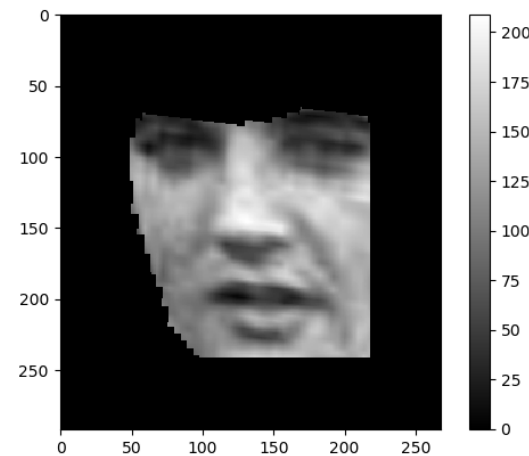
Intersection
region Ω

A more robust way

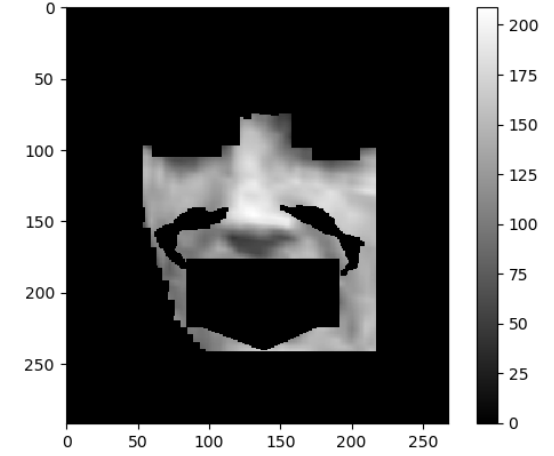
- only estimate the robust regions(manually assigned), the dark region is excluded from estimation.(i.e: to guarantee facial expression invariant)



mask



Intersection
region Ω

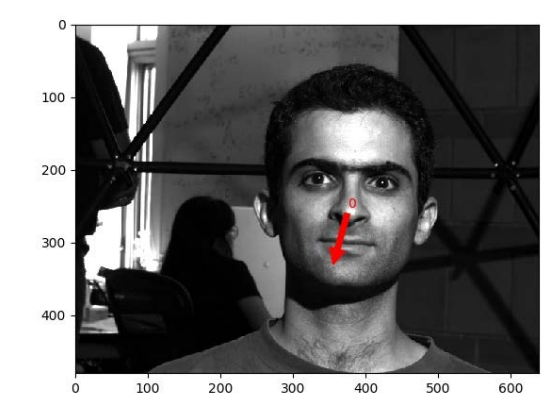
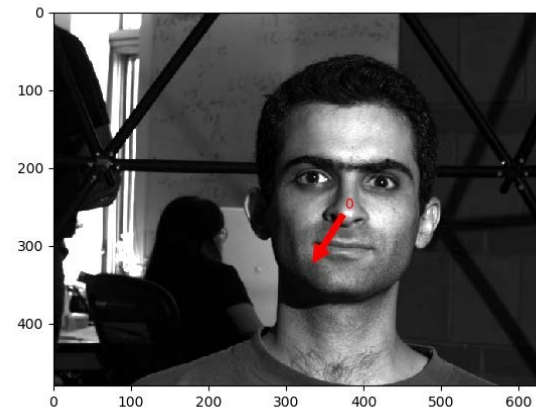
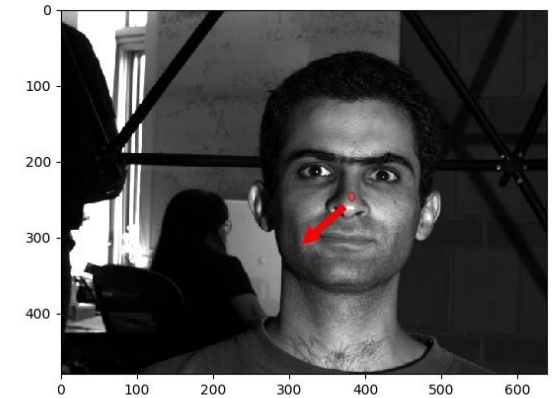
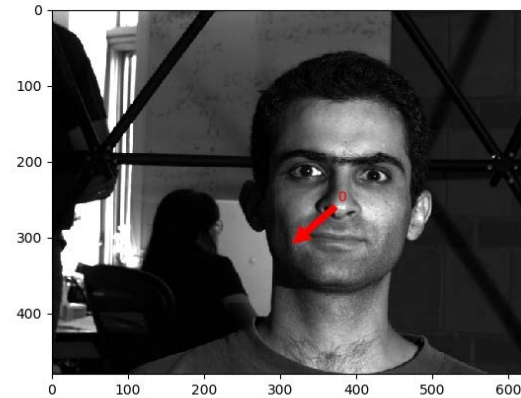
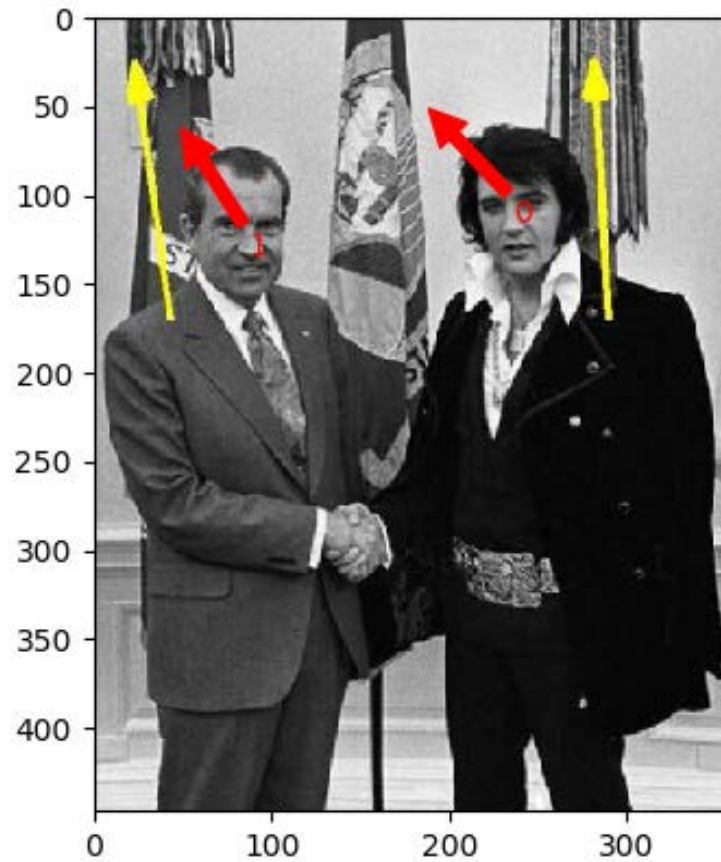


Intersection
region Ω^+

Experiment results



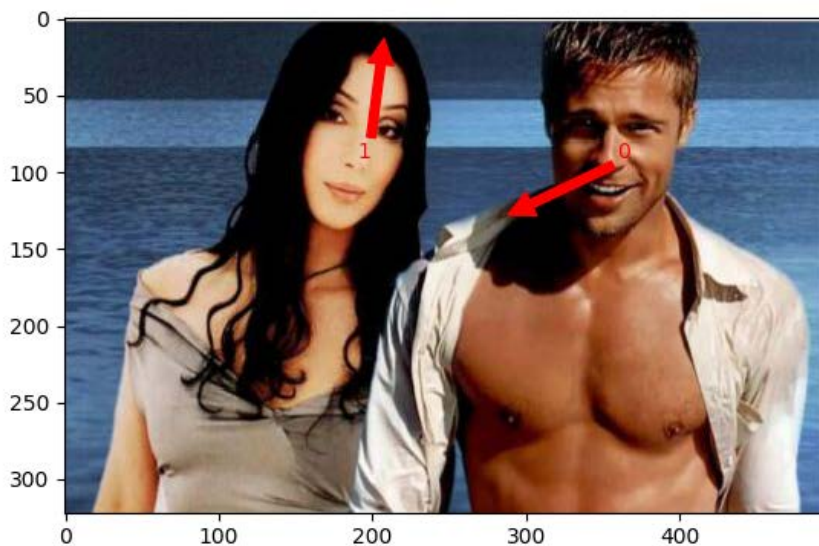
Images from extended yaleB database
detailed information will be in report



direction estimated from 1nd
approximation term

Application scenario1

detecting composite photos



fake photo



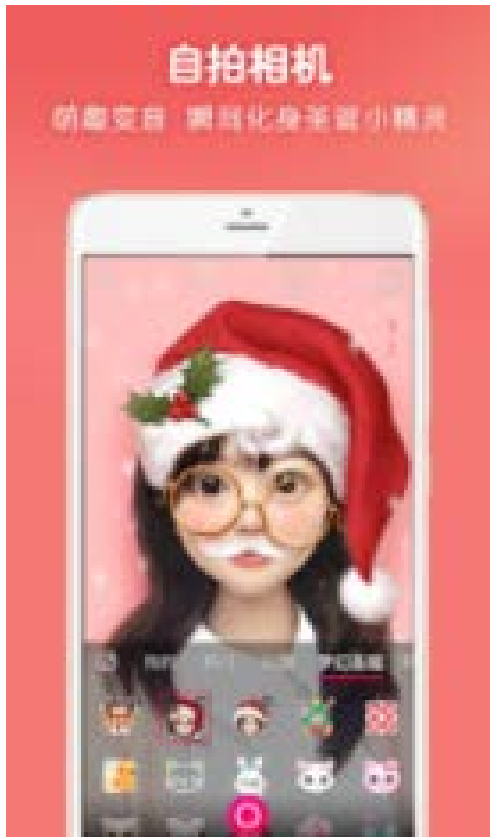
real photo

M. K. Johnson and H. Farid, [Exposing Digital Forgeries by Detecting Inconsistencies in Lighting](#),
ACM Multimedia and Security Workshop, 2005.

Pictures from the internet

Application scenario2

more natural compositing photos



- ✓ with known surface norm information
- ✓ with known albedo
- ✓ with known light direction

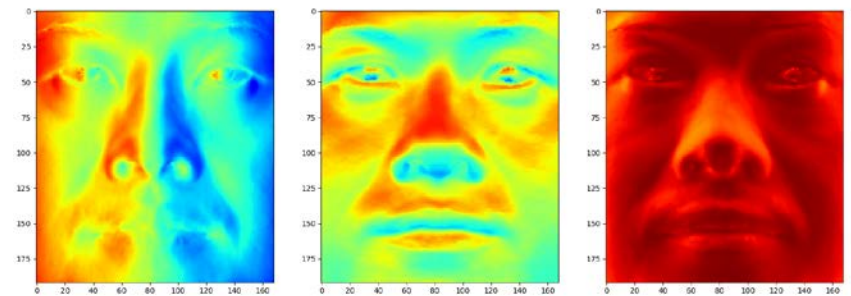
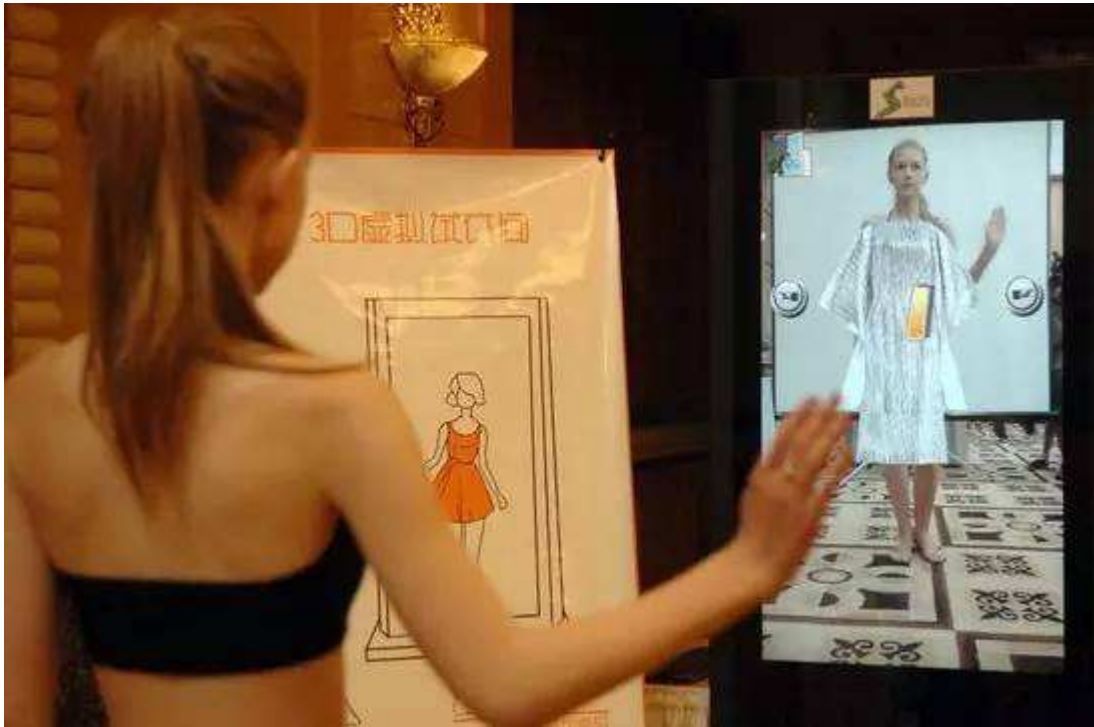
Application scenario2

more natural compositing videos



can apply lightning information to
any 3-D model with known norms
and albedo

We only have ..

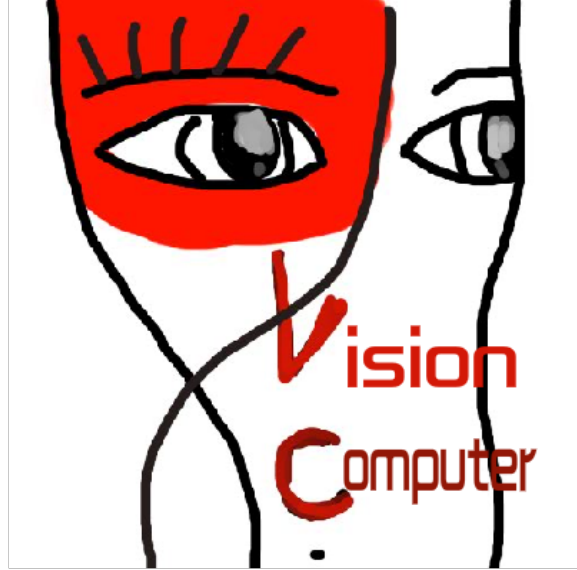


Application scenario2

more natural compositing photos



estimated from 2nd order spherical
harmonic approximation



Q?&A!