

NOTE: Answers must be hand-written, capture the image and post below before Monday 24th March 2025.

Tutorial 1 (Nurul Fariza , A194778)

1. a) Find $\gcd(85, 34)$ by tracing the :

i. Euclid algorithm

$\gcd(85, 34)$

i) Euclid Algorithm

Step	m	n	$m \bmod n$	r	new (a,b)
1	85	34	$85 \bmod 34$	17	(34, 17)
2	34	17	$34 \bmod 17$	0	(17, 0)

$\therefore \gcd(85, 34) = 17$

ii. Consecutive integer checking algorithm

b) Consecutive integer

step	q	$85 \bmod q$	$34 \bmod q$
1	34	$85 \bmod 34 = 17$	$34 \bmod 34 = 0$
2	33	$85 \bmod 33 = 19$	$34 \bmod 33 = 1$
3	32	$85 \bmod 32 = 21$	$34 \bmod 32 = 2$
4	31	$85 \bmod 31 = 23$	$34 \bmod 31 = 3$
5	30	$85 \bmod 30 = 25$	$34 \bmod 30 = 4$
6	29	$85 \bmod 29 = 27$	$34 \bmod 29 = 5$
7	28	$85 \bmod 28 = 1$	$34 \bmod 28 = 6$
8	27	$85 \bmod 27 = 4$	$34 \bmod 27 = 7$
9	26	$85 \bmod 26 = 7$	$34 \bmod 26 = 8$
10	25	$85 \bmod 25 = 10$	$34 \bmod 25 = 9$
11	24	$85 \bmod 24 = 13$	$34 \bmod 24 = 10$
12	23	$85 \bmod 23 = 16$	$34 \bmod 23 = 11$
13	22	$85 \bmod 22 = 19$	$34 \bmod 22 = 12$
14	21	$85 \bmod 21 = 1$	$34 \bmod 21 = 13$
15	20	$85 \bmod 20 = 5$	$34 \bmod 20 = 14$
16	19	$85 \bmod 19 = 9$	$34 \bmod 19 = 15$
17	18	$85 \bmod 18 = 13$	$34 \bmod 18 = 16$
18	17	$85 \bmod 17 = 0$	$34 \bmod 17 = 0$

$\therefore \gcd(85, 34) = 17$

*use the algorithms from the lecture slide

b. Compare the number of steps taken for both algorithms

b) Euclidean Algorithm has 2 steps taken while consecutive integer checking algorithm has 18 steps taken.

(5 marks)

2. Discuss the importance of sorting in your daily life by giving an example.

2) Sorting helps to organize information efficiently and make tasks easier and saving times. Example, Shopee uses sorting to help user find product efficiently and can sort result by price (low to high or high to low), popularity, rating or newest arrivals.

3. Consider the algorithm for the sorting problem that sorts an array by counting, for each of its elements, the number of smaller elements and then uses this information to put the element in its appropriate position in the sorted array:

ALGORITHM ComparisonCountingSort($A[0..n - 1]$)

//Sorts an array by comparison counting

//Input: Array $A[0..n - 1]$ of orderable values

//Output: Array $S[0..n - 1]$ of A 's elements sorted

// in nondecreasing order

for $i \leftarrow 0$ to $n - 1$ do

$\text{Count}[i] \leftarrow 0$

for $i \leftarrow 0$ to $n - 2$ do

 for $j \leftarrow i + 1$ to $n - 1$ do

 if $A[i] < A[j]$

$\text{Count}[j] \leftarrow \text{Count}[j] + 1$

 else $\text{Count}[i] \leftarrow \text{Count}[i] + 1$

for $i \leftarrow 0$ to $n - 1$ do

$S[\text{Count}[i]] \leftarrow A[i]$

return S

Apply this algorithm to sort the list 52, 16, 81, 98, 41, 74.

3) $A = [52, 16, 81, 98, 41, 74]$
 $count = [0, 0, 0, 0, 0, 0]$

i	j	A[i]	A[j]	comparision	count
0	1	52	16	$52 > 16$	$count[0] += 1$
0	2	52	81	$52 < 81$	$count[2] += 1$
0	3	52	98	$52 < 98$	$count[3] += 1$
0	4	52	41	$52 > 41$	$count[0] += 1$
0	5	52	74	$52 < 74$	$count[5] += 1$
1	2	16	81	$16 < 81$	$count[2] += 1$
1	3	16	98	$16 < 98$	$count[3] += 1$
1	4	16	41	$16 < 41$	$count[4] += 1$
1	5	16	74	$16 < 74$	$count[5] += 1$
2	3	81	98	$81 < 98$	$count[3] += 1$
2	4	81	41	$81 > 41$	$count[2] += 1$
2	5	81	74	$81 > 74$	$count[2] += 1$
3	4	98	41	$98 > 41$	$count[3] += 1$
3	5	98	74	$98 > 74$	$count[3] += 1$
4	5	41	74	$41 < 74$	$count[5] += 1$

$count = [2, 0, 4, 1, 5, 3]$

A[i]	count[i]	Position in S
52	2	$S[2] = 52$
16	0	$S[0] = 16$
81	4	$S[4] = 81$
98	5	$S[5] = 98$
41	1	$S[1] = 41$
74	3	$S[3] = 74$

sorted array S :

$S = [16, 41, 52, 74, 81, 98]$