

Algebra of Functions

If you can find things like $f(3)$ and $f(-5)$ then you can do this!!

Take a look at these two functions

$$f(x) = x + 2 \text{ and } g(x) = x^2 + 2$$

Let's find the following:

$$f(3) = (3) + 2 = 5$$

$$\underline{f(3) = 5}$$

$$g(3) = (3)^2 + 2 = 9 + 2 = 11$$

$$\underline{g(3) = 11}$$

$$f(3) + g(3) = 5 + 11 = 16$$

$$f(3) - g(3) = 5 - 11 = -6$$

$$f(3) * g(3) = 5 \times 11 = 55$$

$$f(3) / g(3) = \frac{5}{11}$$

You Try

$$f(x) = x + 1 \text{ and } g(x) = \sqrt{x + 3}$$

$$(f+g)(x) = f(x) + g(x) =$$

$$= x + 1 + \sqrt{x + 3}$$

$$= x + 1 + \sqrt{x + 3}$$

$$\begin{aligned}
 (f+g)(6) &= f(6) + g(6) = \\
 &= 7 + 3 \\
 &= 10
 \end{aligned}$$

SIDE NOTE

$$\begin{aligned}
 * f(6) &= x+1 \\
 &= 6+1 = 7 \\
 * g(6) &= \sqrt{x+3} \\
 &= \sqrt{6+3} \\
 &= \sqrt{9} = 3
 \end{aligned}$$

$$\begin{aligned}
 (f-g)(-4) &= f(-4) - g(-4) = \\
 &= -3 - i
 \end{aligned}$$

SIDE NOTE

$$\begin{aligned}
 f(-4) &= x+1 \\
 &= -4+1 = -3 \\
 g(-4) &= \sqrt{x+3} \\
 &= \sqrt{-4+3} \\
 &= \sqrt{-1} = i
 \end{aligned}$$

* Recall *

$$i = \sqrt{-1}$$

$$i^2 = i \cdot i = \sqrt{-1} \sqrt{-1} = -1$$

$$i^3 = i^2 \cdot i = -1 \cdot i = -i$$

$$i^4 = i^2 \cdot i^2 = -1 \cdot -1 = 1$$