

Radical Rules

$$\sqrt[m]{a^m} = |a| \quad m = \text{odd } \#$$

Root and exponent cancel each other out

$$\sqrt[3]{\boxed{a}} = |\boxed{a}|$$

$$\sqrt[m]{a^m} = a \quad m = \text{even } \#$$

Root and exponent cancel each other out

$$\sqrt{\boxed{a}} = \boxed{a}$$

$$\sqrt[m]{a} \times \sqrt[n]{b} = \sqrt[mn]{a \times b}$$

$$\text{Ex) } \sqrt{3} \times \sqrt{x} = \sqrt{3x}$$

When roots match put them under one root

$$\sqrt{\boxed{a}} \times \sqrt{\boxed{b}} = \sqrt{\boxed{a} \times \boxed{b}}$$

$$\sqrt[m]{\frac{a}{b}} = \frac{\sqrt[m]{a}}{\sqrt[m]{b}}$$

$$\text{Ex) } \sqrt[3]{\frac{z}{y}} = \frac{\sqrt[3]{z}}{\sqrt[3]{y}}$$

break it - root numerator
root denominator

$$\sqrt{\frac{\boxed{a}}{\boxed{b}}} = \frac{\sqrt{\boxed{a}}}{\sqrt{\boxed{b}}}$$

$$\sqrt[n]{a^m} = (\sqrt[n]{a})^m = a^{m/n}$$

$$\text{Ex} \quad \sqrt[3]{x^2} = (\sqrt[3]{x})^2 = x^{2/3}$$

root and inside exponent

root becomes $1/\text{index}$, exponent becomes numerator.

$$\sqrt[m]{\frac{a}{b}} = \left(\sqrt[m]{a}\right)^{\frac{1}{m}} = \frac{a^{\frac{1}{m}}}{b^{\frac{1}{m}}}$$

Rational Properties

$$a^{-\frac{m}{n}} = \frac{1}{a^{m/n}}$$

$$\text{Ex} \quad x^{-\frac{2}{3}} = \frac{1}{x^{2/3}}$$

Cannot have negative exponents

$$\frac{1}{a^{-\frac{m}{n}}} = \frac{1}{\frac{1}{a^{m/n}}} = a^{m/n}$$

$$\frac{1}{a^{-m}} = a^m$$

$$\text{Ex} \quad \frac{1}{2^{-x}} = 2^x$$

Cannot have negative exponents

$$\frac{1}{a^{-\frac{m}{n}}} = a^{\frac{m}{n}}$$