# FINAL EXAM CS372 FORMAL LANGUAGES & THE THEORY OF COMPUTATION

Student ID:
Name:

## PART 1 (Close book -60 minutes)

#### A. Yes/No questions (10 points total)

Decide for each statement whether it is True or False. Write T to the answer sheet if the statement is necessarily true; write F if it it is not necessarily true.

- 1. The set of all lanuguages over a finite alphabet  $\Sigma$  is uncountable.
- 2. Grammar  $G = \{ \{ a, b \}, \{ S,T \}, S, P >, \text{ with } P = \{ S \rightarrow S \mid T, T \rightarrow \varepsilon \} \text{ is ambiguous } \}$
- 3. Let  $\Sigma = \{a, b, c, d\}$  and  $L = \{a^i b^j c^k d^l \mid i+k=j+l\}$ . L is not regular.
- 4.  $x^+$  and  $x^+x^{*+}$  represent the same language.
- 5. Power of deterministic automata is equivalent to power of non-deterministic automata.
- 6. If a regular language is infinite, then every state diagram of DFA that recognizes it contains cycles
- 7. If a language L is context-free then L is generated by a context free grammar in CNF.
- 8. The difference between the PCP problem and the MPCP problem is that a solution of the MPCP problem must begin with the first pattern.
- 9. The language  $A_{TM} = (M, w)$  where M accept w is TM decidable.
- 10. NP  $\neq$  P.

### ANSWER SHEET

QUESTION	ANSWER
1	
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## **B.Multiple choice questions (30 points total)**

Read the questions carefully and check one option

**Question 1:** If language  $L=\{0,1\}^*$ , then the reversed language  $L^R=$ 

$$\begin{array}{ccc} A. & A.\{0,1\}^* & & B.\{\epsilon\} \\ & C.\{0\}^* & & D.\{1\}^* \end{array}$$

**Question 2:** Number of substrings in of acbab is

A. 11 B. 12 C. 13 D.None of these

**Question 3:** Two finite state machines are said to be equivalent if they:

- A. Have the same number of edges
- B. Have the same number of states
- C. Recognize the same set of tokens
- D. Have the same number of states and edges

**Question 4:** While applying Pumping lemma over a regular language, we consider a string w that belong to L and fragment it into \_\_\_\_\_\_ parts.

A.	2	B. 5	C. 3	D. 6

**Question 5:** Consider the following languages:

- $L_1 = \{a^{(n+m)} b^n a^m \mid n,m \ge 0\}$
- $L_2 = \{a^{(n+m)} b^{(n+m)} a^{(n+m)} | n,m \ge 0\}$

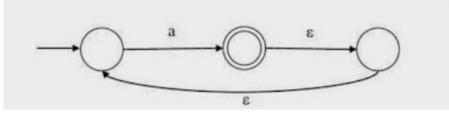
Which of the following is correct?

- A. Only L<sub>1</sub> is context-free language
- B. Only L<sub>2</sub> is context-free language
- C. Both L<sub>1</sub> and L<sub>2</sub> are context free languages
- D. Both  $L_1$  and  $L_2$  are not context free languagesx

**Question 6:** Regular expression x(x+y) denotes the set

- A.  $\{xx, xy\}$
- B.  $\{x, y, xx, xy\}$
- C.  $\{x,y\}$
- D.  $\{x,y,xy\}$

**Question 7:** Which of the following languages is the complement of language L recognizable by the following NFA (L is a language over  $\Sigma = \{a\}$ ):



- Α) ε
- C) Ø

- B)  $\{a^n \mid n \ge 0\}$
- D)  $\{a\} \cup \{\epsilon\}$

**Question 8:** Which of the following regular expressions denotes a finite language?

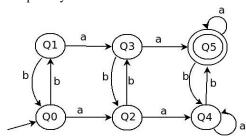
- A. (bb + aba + bba)\*
- B. (aaa + bbb)\*
- C. ((a+b)(a+b)(a+b))\*
- D.  $(aaa + ab + a) + (bbb + bb + a) + \epsilon^*$

Question 9: Which of the following instances of PCP does not have a match?

- A. [a, aa], [bb, b], [a, bb]
- B. [a, aaa], [aab, b], [abaa, ab]
- C. [b, ba], [aa, b], [bab, aa], [ab, ba]
- D. [aa, aab], [bb,ba][abb,b]

#### Question 10:

Which of the following strings is accepted by DFA M below?



A. abbaaab

- B. aaabba
- C. bbaabaa
- D. baabbbb

**Question 11:** Parentheses consist of opening and closing parentheses (,),{,},[,] and an expression has balanced parentheses if:

- Expression between a matching opening and closing parentheses is a balanced parentheses.
- There is no unmatched parentheses that is for every opening bracket, there is a closing bracket and vice versa Which of the following grammars generates the language of all balanced parenthesis expressions?
- A.  $S \to (S) | () | [S] | [] | \{S\} | \{\}$
- B.  $S \to (S | S) | [S | S] | \{S | S\} | (||) | [||] | \{||\}|$

- C.  $S \rightarrow SS \mid (S) \mid \{S\} \mid [S] \mid \varepsilon$
- D. None of these

**Question12:** Given a context free grammar with set of variables  $\{S,A,B\}$ , set of terminal symbols  $\{a,b\}$ , and set of production rules:  $\{S \to AB, A \to AB \mid a, B \to BA \mid b\}$ . Which of the following derivations does not derive string abab?

- A.  $S \Rightarrow AB \Rightarrow Ab \Rightarrow ABb \Rightarrow ABAb \Rightarrow AbAb \Rightarrow Abab \Rightarrow abab$
- B.  $S \Rightarrow AB \Rightarrow ABB \Rightarrow ABAB \Rightarrow aBaB \Rightarrow abab$
- C.  $S \Rightarrow AB \Rightarrow ABA \Rightarrow ABAB \Rightarrow ABAb \Rightarrow AbAb \Rightarrow Abab \Rightarrow abab$
- D.  $S \Rightarrow AB \Rightarrow aB \Rightarrow aBA \Rightarrow abAB \Rightarrow abaB \Rightarrow abab$

#### Question 13: The problem that is decidable is

- A. Emptiness problem for TM's
- B. Membership problem for CFG's
- C. Equivalence problem for TMs
- D. Acceptance problem for TM's

**Question 14:** The worst-case efficiency of solving the searching problem (with an unsorted list L[n] and key k) is? Here p represents a polynomial function.

- A. O(p(n))
- B.  $O(p(n \log n))$
- C.  $O(p(n^2))$
- D.  $O(p(m \log n))$

**Question 15:** The language described by the regular expression 0\*00(0+1)\* over the alphabet  $\{0\ 1\}$  is the set of

- A. all strings beginning with at least two 0's
- B. all strings ending with at least two 0's
- C. All strings that begin and end with either 0's or 1's
- D. All strings containing the substring 00

**Question 16:** If 
$$L_1 = \{a^n \mid n \ge 0\}$$
,  $L_2 = \{a^n b^m \mid n \ge 0, m \ge 1\}$  then  $L_1 \cup L_2$  is:

$$\begin{array}{lll} A.\{a^nb^m \mid \ n \geq 0, \ m \geq 1\} & B.\{a^nb^m \mid \ n \geq 0, \ m \geq 0\} \\ C.\{a^nb^m \mid \ n \geq 1, \ m \geq 0\} & D,\{a^nb^m \mid \ n \geq 1, \ m \geq 1\} \end{array}$$

**Question 17:**Which of the following statements is false?

- A. A context sensitive language is also a regular language
- B. A context free language is also a context sensitive language
- C. A context free language is also recursive enumerable language
- D. A regular languageis also a context free language

**Question 18:** Which of the following problems is NP complete?

- A. Emptiness of a regular languag
- B. Halting Problem
- C. Satisfiability
- D. Modified Post's Correspondence Problem

**Question 19:** We have decision problems  $P_1$  and  $P_2$  as described below:

P<sub>1</sub>: Does a given Turing machine accept a given string?

P<sub>2</sub>: Does a given context-free grammar generate an infinite number of strings?

The statement that holds true for  $P_1$  and  $P_2$  is

- A. Only P<sub>2</sub> is decidable
- B. Only P<sub>1</sub> is decidable
- C. Neither  $P_1$  nor  $P_2$  are decidable
- D. Both P<sub>1</sub> and P<sub>2</sub> are decidable

**Question 20:** is the class of decision problems that can be solved by non-deterministic polynomial algorithms?

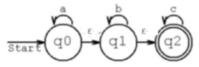
- A. NP
- B. Non P
- C. NP Hard
- D. Complete

# ANSWER SHEET

QUESTION	ANSWER	QUESTION	ANSWER
1		11	
2		12	
3		13	
4		14	
5		15	
6		16	
7		17	
8		18	
9		19	
10		20	

# PART I1 (Open book – 60 minutes)

1/(15 points) Give a DFA that accepts the language accepted by the following NFA:

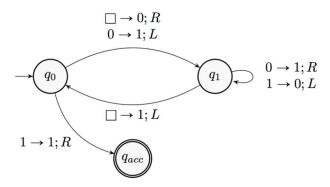


2/(5 points)Prove that the following instance of PCP does not have a match: [0, 111], [10111, 101], [10, 01], [01, 11]

3/(15 points) Convert the following grammar to equivalent grammar in Chomsky normal form:

$$S \rightarrow aXbX,\, X \rightarrow aY \mid bY \mid c,\, Y \rightarrow aXa \mid c$$

5/(10 points) Given the encoding of the following Turing machine, here  $\square$  represents blank symbol.



5/ (15 points) Consider the following Push down automaton M. Give the sequence of configurations that M accepts input strings abcc

