

Question 5: Consider the following languages:

$$L_1 = \{a^{(n+m)} b^n a^m \mid n, m \geq 0\}$$

$$L_2 = \{a^{(n+m)} b^{(n+m)} a^{(n+m)} \mid n, m \geq 0\}$$

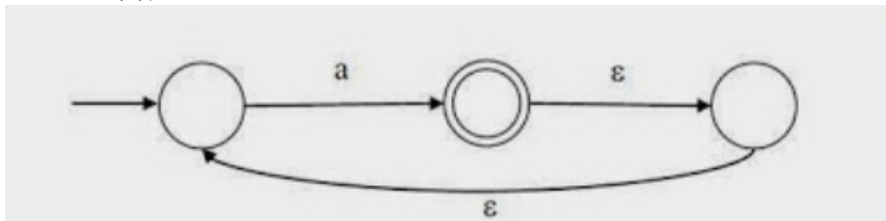
Which of the following is correct?

- A. Only L_1 is context-free language
- B. Only L_2 is context-free language
- C. Both L_1 and L_2 are context free languages
- D. Both L_1 and L_2 are not context free languages

Question 6: Regular expression $x(x+y)$ denotes the set

- A. $\{xx, xy\}$
- B. $\{x, y, xx, xy\}$
- C. $\{x, y\}$
- D. $\{x, y, xy\}$

Question 7: Which of the following languages is the complement of language L recognizable by the following NFA (L is a language over $\Sigma = \{a\}$):



- A) ϵ
- B) $\{a^n \mid n \geq 0\}$
- C) \emptyset
- D) $\{a\} \cup \{\epsilon\}$

Question 8: Which of the following regular expressions denotes a finite language?

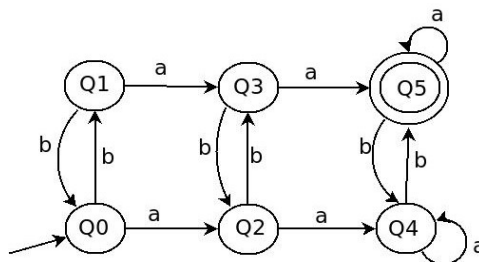
- A. $(bb + aba + bba)^*$
- B. $(aaa + bbb)^*$
- C. $((a + b)(a + b)(a + b))^*$
- D. $(aaa + ab + a) + (bbb + bb + a) + \epsilon^*$

Question 9: Which of the following instances of PCP does not have a match?

- A. $[a, aa], [bb, b], [a, bb]$
- B. $[a, aaa], [aab, b], [abaa, ab]$
- C. $[b, ba], [aa, b], [bab, aa], [ab, ba]$
- D. $[aa, aab], [bb, ba], [abb, b]$

Question 10 :

Which of the following strings is accepted by DFA M below?



- A. abbaaab
- B. aaabba
- C. bbaabaa
- D. baabbbb

Question 11: Parentheses consist of opening and closing parentheses $(, \{, [,]$ and an expression has balanced parentheses if:

- Expression between a matching opening and closing parentheses is a balanced parentheses.
 - There is no unmatched parentheses that is for every opening bracket, there is a closing bracket and vice versa
- Which of the following grammars generates the language of all balanced parenthesis expressions?

- A. $S \rightarrow (S) \mid () \mid [S] \mid [] \mid \{S\} \mid \{\}$
- B. $S \rightarrow (S \mid S) \mid [S \mid S] \mid \{S \mid S\} \mid (\mid) \mid [\mid] \mid \{ \mid \}$

- C. $S \rightarrow SS \mid (S) \mid \{S\} \mid [S] \mid \epsilon$
- D. None of these

Question 12: Given a context free grammar with set of variables $\{S, A, B\}$, set of terminal symbols $\{a, b\}$, and set of production rules: $\{S \rightarrow AB, A \rightarrow AB \mid a, B \rightarrow BA \mid b\}$. Which of the following derivations does not derive string abab?

- A. $S \Rightarrow AB \Rightarrow Ab \Rightarrow ABb \Rightarrow ABAb \Rightarrow AbAb \Rightarrow Abab \Rightarrow abab$
- B. $S \Rightarrow AB \Rightarrow ABB \Rightarrow ABAB \Rightarrow aBaB \Rightarrow abab$
- C. $S \Rightarrow AB \Rightarrow ABA \Rightarrow ABAB \Rightarrow ABAb \Rightarrow AbAb \Rightarrow Abab \Rightarrow abab$
- D. $S \Rightarrow AB \Rightarrow aB \Rightarrow aBA \Rightarrow abA \Rightarrow abAB \Rightarrow abaB \Rightarrow abab$

Question 13: The problem that is decidable is

- A. Emptiness problem for TM's
- B. Membership problem for CFG's
- C. Equivalence problem for TMs
- D. Acceptance problem for TM's

Question 14: The worst-case efficiency of solving the searching problem (with an unsorted list $L[n]$ and key k) is? Here p represents a polynomial function.

- A. $O(p(n))$
- B. $O(p(n \log n))$
- C. $O(p(n^2))$
- D. $O(p(m \log n))$

Question 15: The language described by the regular expression $0^*00(0+1)^*$ over the alphabet $\{0, 1\}$ is the set of

- A. all strings beginning with at least two 0's
- B. all strings ending with at least two 0's
- C. All strings that begin and end with either 0's or 1's
- D. All strings containing the substring 00

Question 16: If $L_1 = \{a^n \mid n \geq 0\}$, $L_2 = \{a^n b^m \mid n \geq 0, m \geq 1\}$ then $L_1 \cup L_2$ is:

- A. $\{a^n b^m \mid n \geq 0, m \geq 1\}$
- B. $\{a^n b^m \mid n \geq 0, m \geq 0\}$
- C. $\{a^n b^m \mid n \geq 1, m \geq 0\}$
- D. $\{a^n b^m \mid n \geq 1, m \geq 1\}$

Question 17: Which of the following statements is false?

- A. A context sensitive language is also a regular language
- B. A context free language is also a context sensitive language
- C. A context free language is also recursive enumerable language
- D. A regular language is also a context free language

Question 18: Which of the following problems is NP complete?

- A. Emptiness of a regular language
- B. Halting Problem
- C. Satisfiability
- D. Modified Post's Correspondence Problem

Question 19: We have decision problems P_1 and P_2 as described below:

P_1 : Does a given Turing machine accept a given string?

P_2 : Does a given context-free grammar generate an infinite number of strings?

The statement that holds true for P_1 and P_2 is

- A. Only P_2 is decidable
- B. Only P_1 is decidable
- C. Neither P_1 nor P_2 are decidable
- D. Both P_1 and P_2 are decidable

Question 20: _____ is the class of decision problems that can be solved by non-deterministic polynomial algorithms?

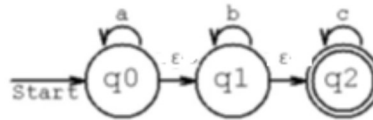
- A. NP
- B. Non P
- C. NP Hard
- D. Complete

ANSWER SHEET

QUESTION	ANSWER	QUESTION	ANSWER
1		11	
2		12	
3		13	
4		14	
5		15	
6		16	
7		17	
8		18	
9		19	
10		20	

PART II (Open book – 60 minutes)

1/(15 points) Give a DFA that accepts the language accepted by the following NFA:

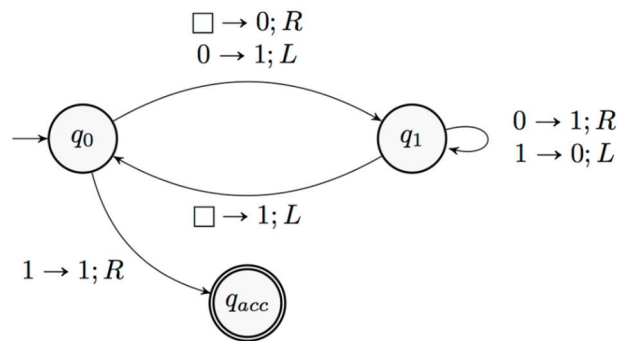


2/(5 points) Prove that the following instance of PCP does not have a match: $[0, 111]$, $[10111, 101]$, $[10, 01]$, $[01, 11]$

3/(15 points) Convert the following grammar to equivalent grammar in Chomsky normal form:

$$S \rightarrow aXbX, X \rightarrow aY \mid bY \mid c, Y \rightarrow aXa \mid c$$

5/ (10 points) Given the encoding of the following Turing machine, here \square represents blank symbol.



5/ (15 points) Consider the following Push down automaton M. Give the sequence of configurations that M accepts input strings abcc

